

1 4F-1 Bookkeeping

- 0 pts Correct

2F-2

$VC(\text{let } x = e \text{ in } c, B) = VC([e/x] c, B)$. The original rule does not properly handle shadowing, and behaves as assignment.

2F-3

$$\begin{aligned} c &= (\text{let } x = 1 \text{ in skip}) \\ B &= (x = 1) \\ \sigma &= [x := 0] \end{aligned}$$

This verification condition is valid:

$$\begin{aligned} VC(\text{let } x = 1 \text{ in skip}, x = 1) &= [e/x]VC(\text{skip}, x = 1) \\ &= VC(\text{skip}, 1 = 1) \\ &= 1 = 1 \\ &= \text{true} \end{aligned}$$

But Using the evaluation rule for let:

$$\frac{\langle e, \sigma \rangle \Downarrow v \quad \langle c, \sigma[x := v] \rangle \Downarrow \sigma'}{\langle \text{let } x = e \text{ in } c, \sigma \rangle \Downarrow \sigma'[x := \sigma(x)]}$$

This evaluates to the state $\sigma' = [x := 0]$:

$$\frac{\langle 1, [x := 0] \rangle \Downarrow 1 \quad \langle \text{skip}, \sigma[x := 1] \rangle \Downarrow [x := 1]}{\langle \text{let } x = 1 \text{ in skip}, [x := 0] \rangle \Downarrow [x := 0]}$$

which does not satisfy $B (x = 1)$ because $x = 0$ under σ' .

2F-4

$$\frac{\vdash \{A\}c\{B\} \quad \vdash \{B \wedge b\}c\{B\}}{\vdash \{A\}\text{do } c \text{ while } b\{B \wedge \neg b\}}$$

2 4F-2 VCGen for Let

- 0 pts Correct

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3 4F-3 VCGen Mistakes

- 0 pts Correct

2F-2

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4 4F-4 Axiomatic Do-While

- 0 pts Correct