Glue, Photons, P=NP? **One-Slide Summary** • The lambda calculus is a universal, fundamental model of computation. You can view it as "the essence of Scheme". It contains terms and rules describing variables, function abstraction, and function application. • It is possible to encode programming concepts, such as true, false, if, numbers, lists, etc., in the lambda calculus. Lambda calculus can simulate Turing machines. Quantum computers and non-determinsitic Turing machines can try many options at once. They are not more powerful than normal Turing machines. • The Complexity Class P contains tractable problems that can be solved in polynomial time. The Complexity Class NP contains problems for which solutions can be verified in odel of the Tink polynomial time. er Museum, Bosto DNA Helix Photomosaic from cover of • Does P = NP? We don't know! \$1+ million if you know. Nature, 15 Feb 2001 (made by Eric Lander) #2 Final Exam Office Hours • Vote! Sunday 1pm - My Apologies • Option A: All students must complete the • Evan Davis Today, 5pm - 9pm, Stacks take-home final exam. The final exam will be Vote: Yes/No worth 15-50% of your grade, as per the - Evan Davis Tomorrow, 5pm-9pm, Stacks syllabus. Individuals may still opt for the Pick At Most One Time and one Modality: comprehensive oral exam. - Yang He, Today, 6:00-7:00pm • Option B: There will be no final exam; no - Yang He, Tomorrow, any time except Noon-4pm student may complete the final exam. - Yang He, Wednesday, any time before 5pm Individuals may still opt for the - Pick One: Office Hour or aim/gchat channel comprehensive oral exam. #3 What is 42? Lambda Calculus is a Universal Computer? z z z z z z z z z z z Ζ Ζ z z z z 42 Read/Write Infinite Tape), X, L --), #, R **Mutable Lists** forty-two • Finite State Machine **Numbers** Processing XT, TT Way to make decisions (if) Finite State Machine

cuarenta y dos

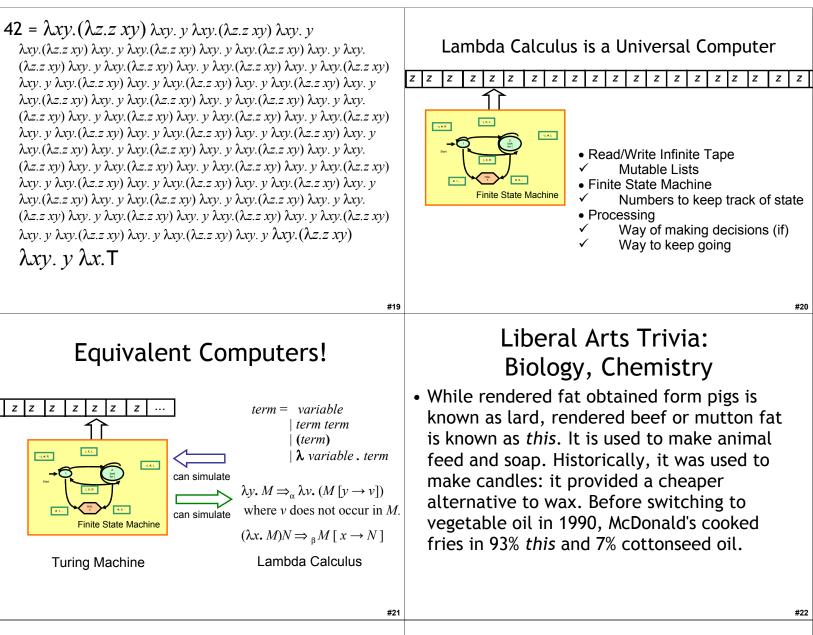
#6

#5

Way to keep going

 <i>beaning of Numbers</i> "42-ness" is something who's successor is "43-ness" "42-ness" is something who's predecessor is "41-ness" "Zero" is special. It has a successor "one-ness", but no predecessor. 	Meaning of Numbers pred (succ N) $\rightarrow N$ succ (pred N) $\rightarrow N$ succ (pred (succ N)) \rightarrow succ N zero? zero \rightarrow T zero? (succ zero) \rightarrow F
Is this enough? Can we define add with pred, succ, zero? and zero? add = λxy .if (zero? x) y (add (pred x) (succ y))	Can we define lambda terms that behave like zero, zero?, pred and succ? Hint: what if we had cons, car and cdr?
Mumbers are Lists zero? = null? pred = cdr succ = $\lambda x \cdot cons F x$ The length of the list corresponds to the number value.	Liberal Arts Trivia: Religious Studies • In Sunni Islam, the Five Pillars of Islam are five duties incumbent on Muslims. They include the Profession of Faith, Formal Prayers, and Giving Alms. Name the remaining two pillars.

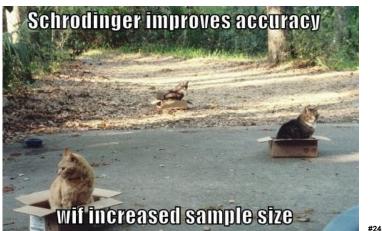
<pre>Making Pairs (define (make-pair x y) (lambda (selector) (if selector x y))) (define (car-of-pair p) (p #t)) (define (cdr-of-pair p) (p #f)) A pair is just an if statement that chooses between the car (then) and the cdr (else).</pre>	$\begin{array}{c} \textbf{cons and car} \\ \textbf{cons} \equiv \lambda x. \lambda y. \lambda z. zxy \\ \textbf{Example: cons M N} = (\lambda x. \lambda y. \lambda z. zxy) M N \\ \rightarrow_{\beta} (\lambda y. \lambda z. zMy) N \\ \rightarrow_{\beta} \lambda z. zMN \\ \textbf{Car} \equiv \lambda p. p T \qquad \textbf{T} \equiv \lambda xy. x \\ \textbf{Example: car (cons M N)} \equiv car (\lambda z. zMN) \equiv (\lambda p. p T) \\ (\lambda z. zMN) \rightarrow_{\beta} (\lambda z. zMN) T \rightarrow_{\beta} TMN \\ \rightarrow_{\beta} (\lambda y. x) MN \\ \rightarrow_{\beta} (\lambda y. M)N \\ \rightarrow_{\beta} M \end{array}$
cdr too!	Null and null?
$cons \equiv \lambda xyz.zxy$	
$car \equiv \lambda p.p T$	$null \equiv \lambda x.T$
$\mathbf{cdr} \equiv \lambda p.p \ \mathbf{F}$	null? $\equiv \lambda x.(x \lambda y.\lambda z.\mathbf{F})$
Example: cdr (cons $M N$) cdr $\lambda z.zMN = (\lambda p.p F) \lambda z.zMN$ $\rightarrow_{\beta} (\lambda z.zMN) F$ $\rightarrow_{\beta} FMN$ $\rightarrow_{\beta} N$	Example: null? null $\rightarrow \lambda x.(x \ \lambda y. \lambda z. F) \ (\lambda x. T)$ $\rightarrow_{\beta} (\lambda x. T) (\lambda y. \lambda z. F)$ $\rightarrow_{\beta} T$ s
Null and null?	Counting
null $\equiv \lambda x.\mathbf{T}$	0 ≡ null
null? $\equiv \lambda x.(x \lambda y.\lambda z.F)$	$0 \equiv 1000$ $1 \equiv cons F 0$
	$2 \equiv \cos F 1$
	$3 \equiv \cos F 2$
null? (cons M N) $\rightarrow \lambda x.(x \lambda y.\lambda z.F) \lambda z.zMN$	
$\rightarrow_{\beta} (\lambda z. z \text{ MN})(\lambda y. \lambda z. F)$	$\mathbf{succ} \equiv \lambda x.\mathbf{cons} \mathbf{F} x$
$\rightarrow_{\beta}(\lambda y.\lambda z.F)$ MN	$\mathbf{pred} \equiv \lambda x.\mathbf{cdr} x$
$\rightarrow_{\beta}\mathbf{F}$	
#	7 #18



Universal Computer

- Lambda Calculus can simulate a Turing Machine
 - Everything a Turing Machine can compute, Lambda Calculus can compute also
- Turing Machine can simulate Lambda Calculus (we didn't prove this)
 - Everything Lambda Calculus can compute, a Turing Machine can compute also
- Church-Turing Thesis: this is true for *any* other mechanical computer also

What about "non-mechanical" computers?



Quantum Physics for Dummies

- Light behaves like both a wave and a particle at the same time
- A single photon is in many states at once
- Can't observe its state without forcing it into one state
- Schrödinger's Cat
 - Put a live cat in a box with cyanide vial that opens depending on quantum state
 - Cat is both dead and alive at the same time until you open the box







#2F

#27

Quantum Computing

- Feynman, 1982
- Quantum particles are in all possible states
- Can try lots of possible computations at once with the same particles
- In theory, can test all possible factorizations/keys/paths/etc. and get the right one!
- In practice, very hard to keep states entangled: once disturbed, must be in just one possible state

Qubit

- Regular bit: either a 0 or a 1
- Quantum bit: 0, 1 or in betwee - p% probability it is a 1
- A single qubit is in 2 possible states at once
- If you have 7 bits, you can represent any one of 27 different states
- If you have 7 qubits, you have 2⁷ different states (at once!)

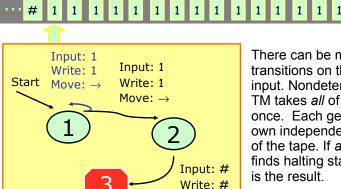
Quantum Computers Today

- Several quantum algorithms - Shor's algorithm: factoring using a guantum computer
- Actual guantum computers
 - 5-qubit computer built by IBM (2001)
 - Implemented Shor's algorithm to factor:
 - "World's most complex quantum computation" **15** (= 5 * 3)
 - D-Wave 16-gubit guantum computer (2007) Solves Sudoku puzzles
- To exceed practical normal computing need > 50 aubits
 - Adding another qubit is more than twice as hard

#28

Nondeterministic Computing

Move: \rightarrow



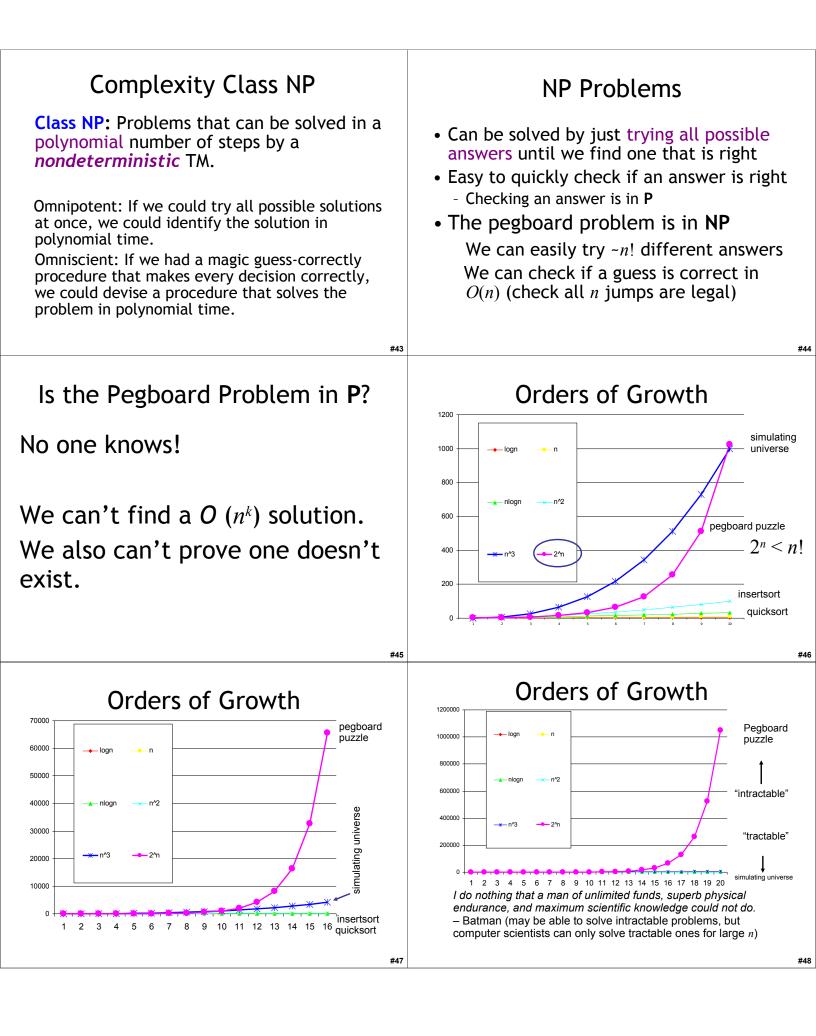
There can be multiple transitions on the same input. Nondeterministic TM takes all of them at once. Each gets its own independent copy of the tape. If any path finds halting state, that

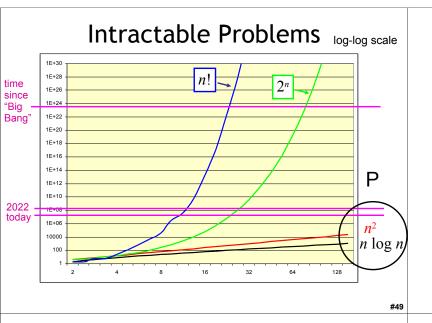
Two Ways of Thinking about Nondeterminstic Computing

- Omniscient (all-knowing): machine always guesses right (the right guess is the one that eventually leads to a halting state)
- Omnipotent (all-powerful): machine can split in two every step, all resulting machines execute on each step, if one of the machines halts its tape is the output

Computability Is a nondeterministic TM more powerful than a deterministic TM?	Liberal Arts Trivia: Geography • This second-longest river in the United States flows form Lake Itasca in Minnesota to the Gulf of Mexico. Forty percent of North America's ducks, geese, swan and wading bird species use it as a migration corridor. It serves as the shared border for ten states, contains over 29 locks and dams, and generates more than a billion dollars a year in revenue from recreational uses, including over 600 water-oriented sites.
Computability	*32 Speed
ls a nondeterministic TM more powerful than a deterministic TM?	Is a nondeterministic TM faster than a deterministic TM?
No! We can simulate a nondeterminstic TM with a regular TM.	
#33	#34
Speed	Pegboard Problem
Is a nondeterministic TM faster than a deterministic TM?	UMP ALL BT DE SARES"
open problem in CS.	LEAR DAY ONLY ONC - WOIRS USING LEAR TO AND OURS AUST FLAM DUMN LEAR THREE AND OURS AUST FLAM DUMN LEAR THREE AND OURS AUST FLAM DUMN LEAR THREE AND OURS AUST FLAM DUMN THREE AND OURS AUST FLAM DUMN THREE AND OURS AUST FLAM DUMN THREE AUST AUST AUST AUST AUST AUST AUST AUST

 Pegboard Problem Input: a configuration of <i>n</i> pegs on a cracker barrel style pegboard Output: if there is a sequence of jumps that leaves a single peg, output that sequence of jumps. Otherwise, output false. How hard is the Pegboard Problem? 	 Problems and Procedures To know a <i>O</i>(<i>f</i>) bound for a problem, we need to find a Θ(<i>f</i>) procedure that solves it The sorting problem is <i>O</i>(<i>n</i> log <i>n</i>) since we know a procedure that solves it in Θ(<i>n</i> log <i>n</i>) To know a Ω(<i>f</i>) bound for a problem, we need to prove that there is no procedure faster than Θ(<i>f</i>) that solves it We could prove sorting is Ω(<i>n</i> log <i>n</i>) by reasoning about the number of decisions needed
#37	#38
 How much work is the Pegboard Problem? Upper bound: (<i>O</i>) <i>O</i>(<i>n</i>!) Try all possible permutations Lower bound: (Ω) Ω(<i>n</i>) Must at least look at every peg Tight bound: (Θ) What do you think? 	 How much work is the Pegboard Problem? Upper bound: (<i>O</i>) <i>O</i>(<i>n</i>!) Try all possible permutations Lower bound: (Ω) Ω(<i>n</i>) Must at least look at every peg Tight bound: (Θ) No one knows!
#39	#40
Complexity Class P "Tractable" Class P: problems that can be solved in a polynomial (O(n ^k) for some constant k) number of steps by a deterministic TM.	 Liberal Arts Trivia: Astronomy This space telescope was launched into orbit by the Space Shuttle Discovery in 1990. After having its incorrectly-ground main mirror replaced in 1993, it has helped to make
Easy problems like sorting, making a photomosaic using duplicate tiles, and simulating the universe are all in P .	breakthroughs in astrophysics. Notable are its Ultra Deep Field image, which details the universe's most distant objects, and its help in determining the ultimate expansion of the universe (the eponymous constant).





Complexity Classes

Class P: problems that can be solved in polynomial time by deterministic TM

Easy problems like simulating the universe are all in **P**.

Class NP: problems that can be solved in polynomial time by a nondeterministic TM.

Includes all problems in **P** and some problems possibly outside **P** like the Pegboard puzzle.

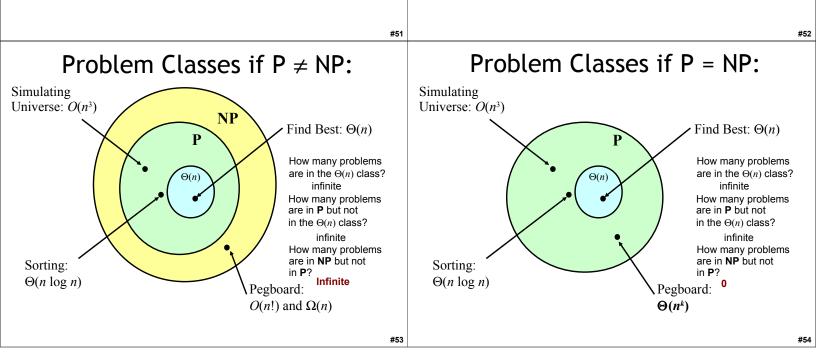
Moore's Law Doesn't Help

- If the fastest procedure to solve a problem is Θ(2ⁿ) or worse, Moore's Law doesn't help much.
- Every *doubling* in computing power only increases the solvable problem size by **1**.

Liberal Arts Trivia: Psychology

#50

• This Swiss philosopher and natural scientist is known as "the great pioneer of the constructivist theory of knowing." His four stages of development include infancy, preschool, childhood and adolescence. Each stage corresponds to the child's understanding of reality (e.g., conservation, abstract reasoning) during that period.



 P = NP? Is P different from NP: is there a problem in NP that is not also in P If there is one, there are infinitely many Is the "hardest" problem in NP also in P If it is, then every problem in NP is also in P If it is, then every problem in NP is also in P Listed first on Millennium Prize Problems \$1M + an automatic A+ in this course (and probably all CS courses at UVA) 	 NP-Complete: is the class of problems that are the <i>hardest</i> problems in NP Cook and Levin proved that 3SAT was NP-Complete (1971) If 3SAT can be transformed into a different problem in polynomial time, than that problem must also be NP-complete. Pegboard ⇔ 3SAT Either all NP-complete problems are tractable (in P) or none of them are!
 NP-Complete Problems Easy way to solve by trying all possible guesses If given the "yes" answer, quick (in P) way to check if it is right If given the "no" answer, no quick way to check if it is right No solution (can't tell there isn't one) No way (can't tell there isn't one) This part is hard to prove: requires showing you could use a solution to the problem to solve a known NP-Complete problem. 	Most Important Science/Technology Races 1930-40s:Decryption Nazis vs. British Winner: British Reason: Bletchley Park had computers (and Alan Turing), Nazi's didn't 1940s: Atomic Bomb Nazis vs. US Winner: US Reason: Heisenberg miscalculated, US had better physicists, computers, resources 1960s: Moon Landing Soviet Union vs. US Winner: US Reason: Many, better computing was a big one

Human Genome Race



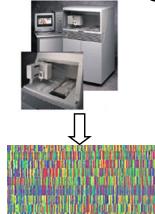
- UVa CLAS 1970
- Yale PhD
- Tenured Professor at U. Michigan



Craig Venter (President of Celera Genomics)

- San Mateo College
- Almost court-martialed
- Denied tenure at SUNY Buffalo

Reading the Genome



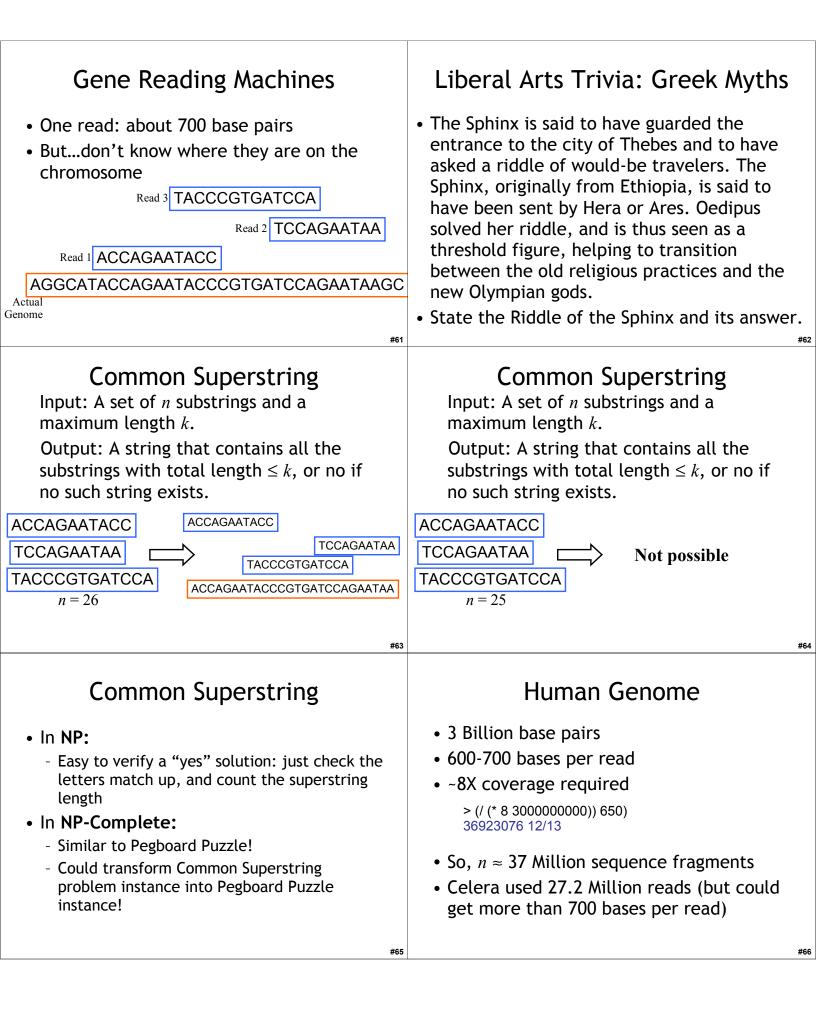
1990s-2001: Sequencing Human Genome



#58

#60

Whitehead Institute, MIT



Give up?

No way to solve an NP-Complete problem (best known solutions being $O(2^n)$ for $n \approx 20$ Million)



Result: Draw?



President Clinton announces Human Genome Sequence essentially complete, June 26, 2000

CS 1120

- Language: Formal Systems, Rules of Eval
- Recursive Definitions
- Programming with Lists
- Programming with Mutation and Objects
- Interpreters, Lazy Eval, Type Checking
- Programming for the Internet
- Measuring Complexity
- Computability
- Models of Computation

Approaches

- Human Genome Project (Collins)
 - Change problem: Start by producing a genome map (using biology, chemistry, etc) to have a framework for knowing where the fragments should go
- Celera Solution (Venter)
 - **Approximate:** we can't guarantee finding the shortest possible, but we can develop clever algorithms that get close most of the time in $O(n \log n)$

"Biology 2.0"

• The past few weeks have seen an announcement that may, in retrospect, turn out to have been as portentous as the sequencing of the human genome: Dr Venter's construction of an organism with a completely synthetic genome. The ability to write new genomes in this way brings true biological engineering—as opposed to the tinkering that passes for biotechnology at the moment—a step closer. (The Economist, July 2010)

Homework

- PS 9 Presentation Requests due Today
- This Wednesday, Here, 5pm-...
 - Presentations
 - Extra Credit on PS9 for attending
- Tuesday December 14
 - Final Project Reports Due

#67

#69

#72

#68

Liberal Arts Trivia: Bias

• Weimer recommends that you take classes on philosophy until you've covered epistemology, free will, logic, the philosophy of science, and "what it is like to be a bat". Take cognitive psychology classes until you've covered perception and the Flynn effect. Take speech or rhetoric classes until you've covered persuasion. Take anthropology as well as gender studies classes until you've covered Mead and Freeman and you have a better feel for which behaviors are socially constructed and which may be essential. Take classes in statistics until you can avoid being fooled. Take classes in religion or ethics until you've covered the relationship between unhappiness and unrealized desires. Take classes in physics until you can explain how a microphone, radio and speaker all work. Take classes on government until you have an opinion about the feasibility of legislating morality. Take classes on history until you are not condemned to repeat the mistakes of the past.