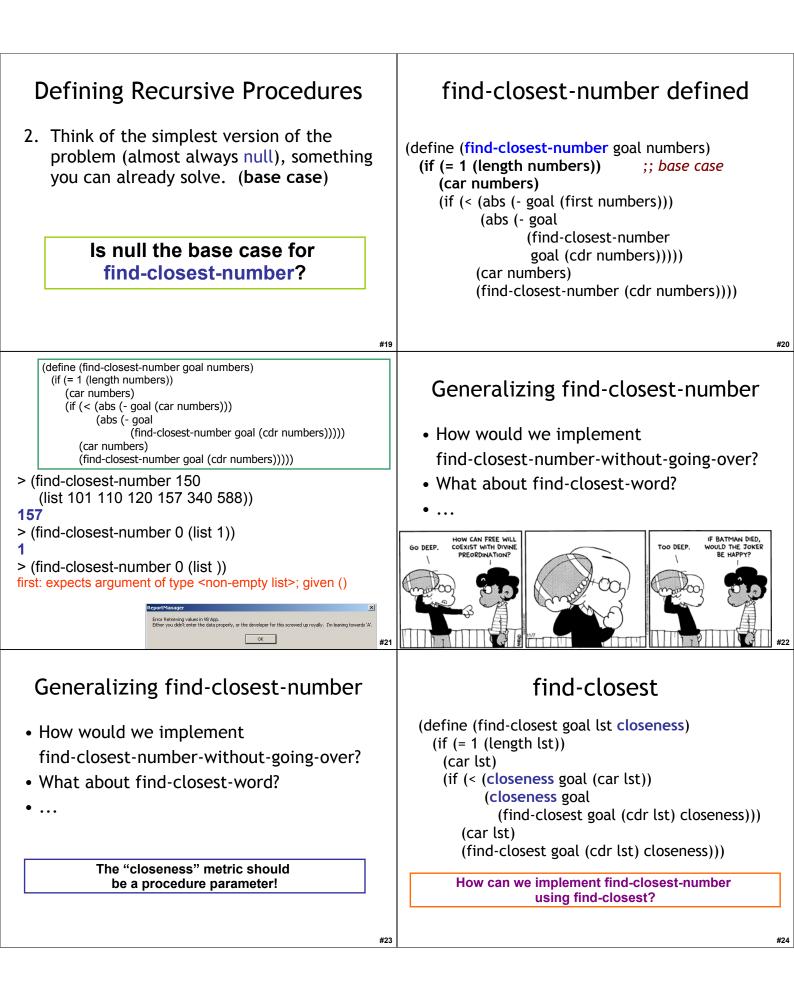
<section-header><section-header></section-header></section-header>	 One-Slide Summary Recursive functions that operate on lists have a similar structure. list-cruncher is a higher-order function that can be used to implement many others. Decisions in a function can be abstracted out by adding a function argument. For example, find-closest-number is just find-closest plus a function defining what a close-number is. The Fibonacci numbers are a recursively-defined sequence. Almost all music uses a stack structure: starts on the tonic, repeats similar patterns in a structured way, ends on the tonic.
Outline	Anonymous Course Feedback
 Your Comments list-cruncher find-closest-number Reminder: procedure definition strategy! find-closest Fibonacci numbers Recursive Transition Networks vs. Backus-Naur Form Grammars Musical Harmony 	 Too Fast v. Too Slow? No CS experience? Jargon in "base lecture"? "I really do appreciate that he tries to read people's facial expressions and ensure that we understand before we move on." vs. "The hand-raising is too frequent." "I wish the TAs would get around to more people in lab." vs. "I asked a TA a question about why one of my procedures wasn't working, and thoroughly explained why, and after he was done asked if his explanation made sense to make sure that I understood everything." "Wes does try to involve everyone, but it seems like students are punished for wanting to participate more than once." vs. "I think there are too many questions directed towards the class."
Similarities and Differences	Similarities and Differences
(define (map f p) (define (sumlist p) (if (null? p) (if (null? p) null 0 (cons (f (car p)) (+ (car p) (map f (cdr p))))) (sumlist (cdr p)))))	(define (map f p) (define (sumlist p) (if (null? p) (if (null? p) null 0 (cons (f (car p)) (+ (car p) (map f (cdr p))))) (sumlist (cdr p)))))
(define (list-cruncher lst) (if (null? lst) base result (combiner (car lst) (recursive-call (cdr lst))))	(define (list-cruncher ? ? lst) (if (null? lst) base result (combiner (car lst) (recursive-call (cdr lst))))
#9	#6

How could this work? • I want to crunch all lists. How would I get started?	<pre>One Ring To Rule Them All? (define (list-cruncher base proc combiner lst) (if (null? lst) base (combiner (proc (car lst)) (list-cruncher base proc combiner (cdr lst)))) (define (sumlist p) (list-cruncher 0 (lambda (x) x) + p)) (define (map f p) (list-cruncher null f cons p))</pre>
Crunchy Center (define (list-cruncher base proc combiner lst) (if (null? lst) base (combiner (proc (car lst)) (list-cruncher base proc combiner (cdr lst))))) • How would you define length using list-cruncher? (define (length lst) (if (null? lst) 0 (+ 1 (length (cdr lst)))))	<pre>list-cruncher crunches length (define (list-cruncher base proc combiner lst) (if (null? lst) base (combiner (proc (car lst))</pre>
#9 Crunchy Center 2 (define (list-cruncher base proc combiner lst) (if (null? lst) base (combiner (proc (car lst)) (list-cruncher base proc combiner (cdr lst))))) • How would you define filter using list-cruncher? (define (filter predicate lst) (if (null? lst) null (append (if (predicate (car lst)) (list (car lst)) null) (filter predicate (cdr lst)))))	#10 List-cruncher crunches filters (define (list-cruncher base proc combiner lst) (if (null? lst) base (combiner (proc (car lst)) (list-cruncher base proc combiner (cdr lst))))) (define (filter predicate lst) (if (null? lst) null (append (if (predicate (car lst)) (list (car lst)) null) (filter predicate (cdr lst))))) (define (filter pred lst) (list-cruncher null (lambda (carlst) (if (pred carlst) (list carlst) null)) append lst))

Liberal Arts Trivia: Drama • In this 1948 play by Samuel Beckett has been called "the most significant English-language play of the 20 th century". The minimal setting calls to mind "the idea of the 'lieu vague', a location which should not be particularised", and the play features two characters who never meet the title character.	Liberal Arts Trivia: History • At the height of its power, in the 16 th and 17 th century, this political organization spanned three continents. It controlled much of Southeastern Europe, the Middle East and North Africa, and contained 29 provinces and multiple vassal states. Noted cultural achievements include architecture (vast inner spaces confined by seemingly weightless yet massive domes, harmony between inner and outer spaces, articulated light and shadow, etc.), classical music, and cuisine.
<pre>find-closest-number find-closest-number takes two arguments. The first is a single number called the goal. The second is a non-empty list of numbers. It returns the number in the input list that is closest to the goal number. (find-closest-number 150 (list 101 110 120 157 340 588)) 157 (find-closest-number 12 (list 4 11 23)) 11 (find-closest-number 12 (list 95)) We'll do this one together! </pre>	<section-header><section-header><section-header><section-header><section-header><text><text><text></text></text></text></section-header></section-header></section-header></section-header></section-header>
find-closest-number hint One Approach for the Recursive Case: You have two possible answers: the current car of the list and the result of the recursive call. Compare them both against the goal number, and return the one that is closer.	Optimistic Function (define (find-closest goal numbers) ;; base case missing for now (if (< (abs (- goal (car numbers))) (abs (- goal (find-closest-number goal (cdr numbers))))) (car numbers) (find-closest-number goal (cdr numbers)))))

#18



Using find-closest	find-closest
(define (find-closest-number goal numbers) (find-closest goal numbers (lambda (a b) (abs (- a b)))))	(define (find-closest goal lst closeness) (if (= 1 (length lst)) (car lst) (if (< (closeness goal (car lst)) (closeness goal
(define (find-closest-below goal numbers) (find-closest goal numbers (lambda (a b) (if (>= a b) (- a b) 99999))))	(find-closest goal (cdr lst) closeness))) (car lst) (find-closest goal (cdr lst) closeness))) How can we avoid
#25	evaluating find-closest twice?
find-closest	Seen Anything Like This?
<pre>(define (find-closest goal lst closeness) (if (= 1 (length lst)) (car lst) (pick-closest closeness goal (car lst)</pre>	(define (find-best-match sample tiles color-comparator) (if (= (length tiles) 1) (car tiles) (pick-better-match sample (car tiles) (find-best-match sample (cdr tiles) color-comparator) (if (color-comparator sample (tile-color tile1) (tile-color tile2)) tile1 tile2)) tile1 tile2)) (find-best-match sample (cdr tiles) color-comparator) color-comparator)))))
Liberal Arts Trivia: Philosophy. • This branch of philosophy, which Aristotle called "First Philosophy", investigates principles of reality transcending those of any particular science. It is concerned with explaining the ultimate nature of being and the world (e.g., determinism and free will, mind and matter, space and time). Its modern name comes from the fact that Aristotle's chapters about it were placed "beyond" his chapters on matter and force.	Liberal Arts Trivia: Film Studies • Born in 1965 to Muslim parents, this Indian actor has starred in flims such as <i>Kuch Kuch</i> <i>Hota Hai, Kal Ho Naa Ho, Veer-Zaara,</i> and <i>Devdas.</i> In 2008, <i>Newsweek</i> named him one of the 50 most powerful people in the world. He has replaced Amitabh "Big B" Bachchan as the host of Kaun Banega Crorepti, and has won India's Padma Shri, a life-sized wax statue at Madame Tussaud's, and the French government's Ordre des Arts et des Lettres.

Liberal Arts Trivia: Painting

 Name this 1930 oilon-beaverboard painting by Grant Wood. It is one of the most familiar images of 20th century American art and has achieved an iconic status.



Fibonacci's Problem

Filius Bonacci, 1202 in Pisa:

Suppose a newly-born pair of rabbits, one male, one female, are put in a field. Rabbits mate at the age of one month so that at the end of its second month a female can produce another pair of rabbits.

Suppose that our rabbits **never die** and that the female **always** produces one new pair (one male, one female) **every month** from the second month on.

Fibonacci Numbers

These numbers are best defined

FIBO(1) = FIBO(2) = 1

recursively by the pair of formulas

Can we turn this into a Scheme procedure?

FIBO (n) = FIBO (n - 1) + FIBO (n - 2)

for n > 2

for n <= 2

How many pairs will there be in one year?

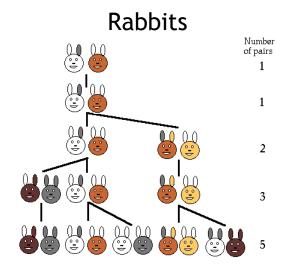
GEB p. 136:

Music Harmony Stacks and Recursion Theology Language Structure Number Sequences Chaos Fractals (PS3 out today. Start early. Why?) Quantum Electrodynamics (later lecture) DNA (later lecture)

Consider the optional reading!

- Sameness-in-differentness
- Game-playing algorithms (later lecture)

#32



GEB Chapter V

You could spend the rest of your life just studying things in this chapter (25 pages)!

From http://www.mcs.surrey.ac.uk/Personal/R.Knott/Fibonacci/fibnat.html #34

Defining FIBO

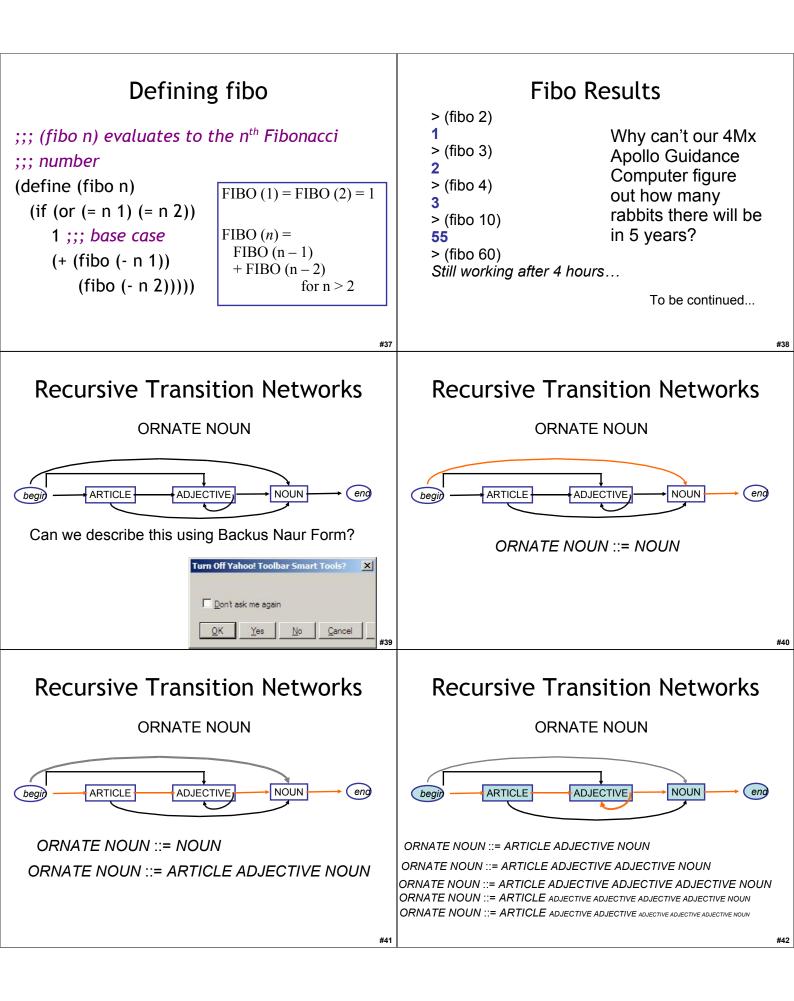
- Be optimistic assume you can solve it, if you could, how would you solve a bigger problem.
- 2. Think of the simplest version of the problem, something you can already solve.
- 3. Combine them to solve the problem.

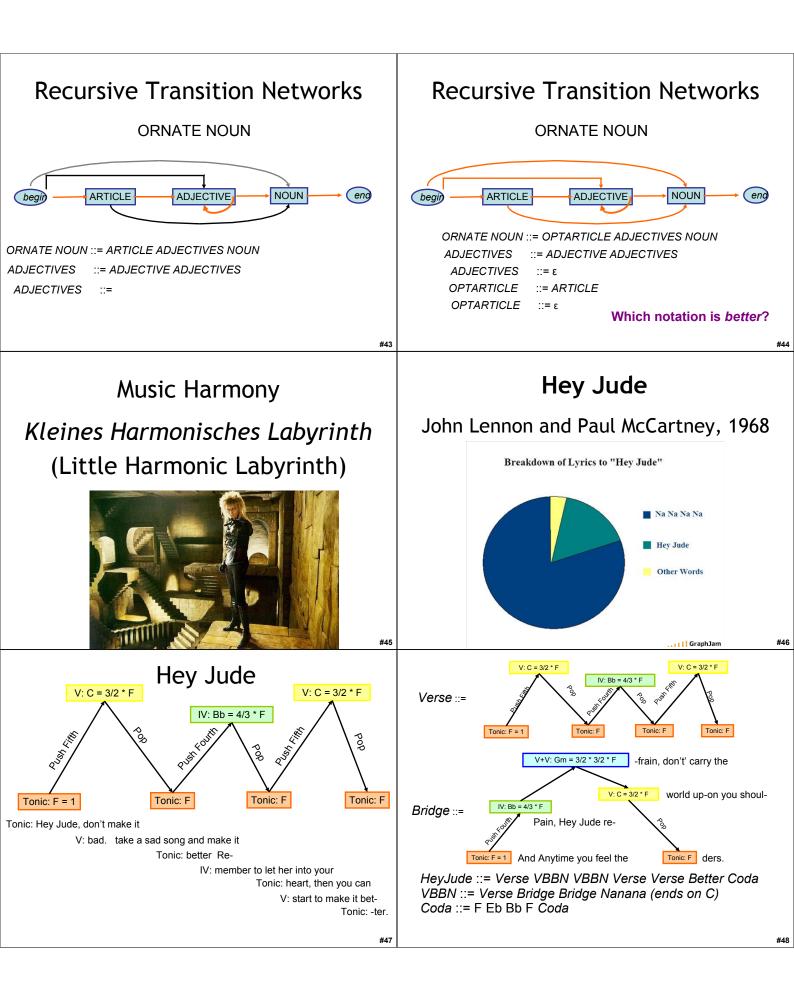
These numbers are best defined recursively by the pair of formulas FIBO (n) =FIBO (n-1)+ FIBO (n-2)for n > 2FIBO (1) = FIBO (2) = 1

#35

#33

#36





	Charge
 Music Almost All Music Is Like This Pushes and pops the listener's stack, but doesn't go too far away from it Repeats similar patterns in structured way Keeps coming back to Tonic, and Ends on the Tonic Any famous Beatles song that doesn't end on Tonic? 	 Challenge: Try to find a "pop" song with a 3-level deep harmonic stack PS3: due in Wed Feb 17. Be optimistic! You know everything you need to finish it now, and it is longer than PS2, so get started now! Beatles: "A Day in the Life" (starts on G, ends on E)
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