List Recursion: Practice & Examples		 One-Slid Writing recursive fur recursive data struct are standard approx list?, member, sum are all important re- operate on lists. You and how to write th DrScheme can trace recursive function to understand. 	de Summary nctions that operate on tures takes practice. There aches to such problems. list, intsto, map and filter cursive functions that u should know what they do em. the execution of a o make it easier to
Ou • Review: Procedure Pr • Review: list, cons, ca • list? • member • sumlist • intsto • map • filter • Tracing	tline oblem Solving r, cdr $\underbrace{\texttt{Watchfire Bobby}}_{\texttt{int} the scan has finished stopping.}$	 Book PS2 Partners Posted Meet during lab hour PS1 Written Grades Posted Holding Fee Pick them up Feynman Point? Read the book! 	kkeeping rs? We have a new computer system Our service will be slower than usual
 How To Write A Procedure Find out what it is supposed to do. What are the inputs? What types of values? What is the output? A number? Procedure? List? Think about some example inputs and outputs Define your procedure More on this next slide Test your procedure Test your procedure Office UNIT FOR THIS DEVICE. 		 Defining Be optimistic! Base case: Think of problem that you kn For number inputs, th For list inputs, this i Recursive step: Thi the problem in term part of the work now call to handle the residue of the second to handle the re	A Procedure the simplest input to the now the answer to. this is often zero. s often the empty list (null). nk of how you would solve as of a smaller input. Do w, then make a recursive est. sually involves subtracting 1.

<pre>Procedure Skeleton • The vast majority of recursive functions look like this: (define (my-procedure my-input) (if (is-base-case? my-input) (handle-base-case my-input) (combine (first-part-of my-input) (my-procedure (rest-of my-input)))))</pre>	Pairs and Lists cons makes a pair of two things (cons 1 2)> (1 . 2) (pair? (cons 1 2))> #t car and cdr get the first and second part (car (cons "a" "b"))> "a" (cdr (cons "y" "z"))> "z" A list is <i>either</i> null <i>or</i> a pair where the second element is also a list (cons 1 (cons 2 (cons 3 null)))> (1 2 3) (list 1 2 3)> (1 2 3) (null? (list 1 2))> #f (append (list 1 2) (list 3 4)) -> (1 2 3 4)
More Power Needed!	list?
<image/> <image/>	 The list? function takes a single argument and returns #t if that argument is a list, #f otherwise. Recall: a list is either null or a pair where the second element is a list (list? null)> #t (pair? (cons 1 2))> #t (list? for 1 null))> #f (list? (cons 1 2))> #f Write it now on paper. Base case? Recursion? #10
list? Hint	Definition of list?
 Here's a hint: (define (list? something) (if (null? something) #t)) 	<pre>• Here it is: (define (list? something) (if (null? something) #t (if (pair? something) (list? (cdr something)) #f)))</pre>

Liberal Arts Trivia: Economics • This 1930 Tariff Act raised US tariffs on imported goods to record levels. Over 1000 US Economists signed a petition against it, and after it passed many other contributed increased their tariffs in retribution. US exports and imports dropped by half and many view this Act as a major catalyst for the Great Depression.	Liberal Arts Trivia: German Lit • This tragic closet play is considered by many to be one of the greatest works of German literature. It centers on a man who makes a pact with the Devil in exchange for knowledge in his quest to discover the essence of life ("was die Welt im Innersten zusammenhält") The man's name officially means "Lucky" in Latin, but now has negative connotations.
 Write a function member that takes two arguments: an element and a list. It returns #f if the list does not contain the element. Otherwise it returns the sublist starting with that element. (member 2 (list 1 2 3)) -> (2 3) (member 5 (list 1 2 3)) -> #f (member 1 (list 1 2 3)) -> (1 2 3) (member 3 (list 1 2 3)) -> (3) (eq? 3 5) -> #f (eq? 2 2) -> #t 	Definition of member (define (member elt lst) (if (null? lst) #f ;; empty list contains nothing (if (eq? elt (car lst)) lst ;; we found it! (member elt (cdr lst))))) ;; keep looking • Where is the base case? Where is the inductive step?
 sumlist Write a procedure sumlist that takes as input a list of numbers. It returns the sum (addition) of all of the elements of the list. It returns 0 for the empty list. (sumlist (list 1 2 3)) -> 6 (sumlist null) -> 0 	Definition of sumlist • And here it is (define (sumlist lst) (if (null? lst) 0 ;; base case (+ (car lst) ;; else add current element (sumlist (cdr lst))))) ;; to rest of list

intsto	Definition of intsto?	
 The function intsto takes a single non-negative integer as an argument. It produces a list of all of the integers between 1 and its argument. (intsto 3) -> (1 2 3) (intsto 7) -> (1 2 3 4 5 6 7) (intsto 0) -> null 	(define (intsto x) (if (< x 1) null ;; base case (cons ;; else make a list x ;; list contains x (intsto (- x 1))))) ;; and recursive result	
	• What's wrong?	
#19	#20	
Correct Definition of intsto	Higher-Order Functions: map	
<pre>(define (intsto x) (if (< x 1) null ;; base case (append ;; else make a list (intsto (- x 1)) ;; recursive result (list x)))) ;; followed by x</pre>	 The map function takes two arguments: a work function and a list. It applies the work function to every element of the list in order and returns a list of the result. (map sqrt (list 9 16 36)) -> (3 4 6) (map square (list 1 2 3)) -> (1 4 9) (map abs (list 2 -3 4)) -> (2 3 4) (map string-length (list "I" "Claudius")) -> (1 8) (map sqrt null) -> null 	
• Huzzah!		
 Mission Impossible: Write map You can do it! (map square (list 1 2 3)) -> (1 4 9) (map abs (list 2 -3 4)) -> (2 3 4) (map sqrt null) -> null 	<pre>Definition of map • Let's look in detail: (define (map work-fun lst) (if (null? lst) null ;; base case (cons ;; else make a list (work-fun (car lst)) ;; first part of result (map work-fun (cdr lst))))) ;; rest o'result</pre>	

Liberal Arts Trivia: Philosophy • This branch of philosophy deals with the theory, nature and scope of knowledge. Key questions include "what is knowledge?", "how is knowledge acquired?", "what do people know?", "how do we know what we know?", "what is the relationship between truth and belief?".	Liberal Arts Trivia: Norse Myth • In Norse Mythology, this god is associated with light and beauty. His mother made every object on earth vow never to harm him, but she did not ask mistletoe. The other gods made a new pastime of hurling objects at him and watching them bounce off. The trickster Loki heard of this, fashioned a spear from mistletoe and had it thrown a him, with fatal results.
#25	#26
Liberal Arts Trivia: Music • This musical instrument of the brass family produces sound when the player's vibrating lips cause the air column inside the instrument to vibrate. It is usually characterized by a telescopic slide with which the player varies the length of the tube to change the pitch. Glenn Miller, famous for his "big band" and songs like <i>In the Mood</i> and <i>Chattanooga Choo</i> <i>Choo</i> , played this instrument.	<pre>Using map to get iteration . In C or Java: for (x=1 ; x <= 5 ; x=x+1) { display(x*x); // output: 1 4 9 16 25 . Recall that we have intsto: (intsto 3) -> (1 2 3) (intsto 7) -> (1 2 3 4 5 6 7) . How can map and intsto to simulate for?</pre>
<pre>Using map to get iteration • In C or Java: for (x=1 ; x <= 5 ; x=x+1) { display(x*x); } // output: 1 4 9 16 25 • Recall that we have intsto: - (intsto 3) -> (1 2 3) • Then we can do: (map (lambda (x) (display (square x))) (intsto 5)) Expect me on tests or extra credit later #29</pre>	 Filter The filter function takes two arguments: a predicate and a list. A predicate is a function that returns true or false. Filter returns the sublist consisting of those elements that satisfy the predicate. (filter is-odd? (list 1 2 3 4)) -> (1 3) (filter null? (list 1 null null "hi")) -> (null null) (filter (lambda (x) (< x 5)) (list 1 9 2 0)) -> (1 2 0) (filter null? (list "susan" "b" "anthony")) -> null (filter is-odd? null) -> null



#35