

EECS 498-004: Introduction to Natural Language Processing

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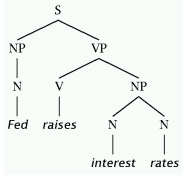
Two views of linguistic structure:  
 1. Constituency (phrase structure)

- Phrase structure organizes words into nested constituents.
  - Fed raises interest rates

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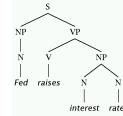
- Phrase structure organizes words into nested constituents.



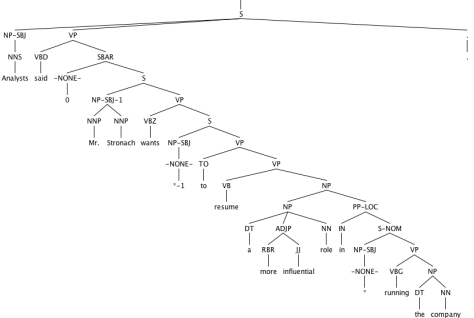
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Two views of linguistic structure:  
 1. Constituency (phrase structure)

- Phrase structure organizes words into nested constituents.
- How do we know what is a **constituent**? (Not that linguists don't argue about some cases.)
  - Distribution: a constituent behaves as a unit that can appear in different places:
    - John talked [to the children] [about drugs].
    - John talked [about drugs] [to the children].
    - \*John talked drugs to the children about
  - Substitution/expansion/pronoun:
    - I sat [on the box/right on top of the box/there].



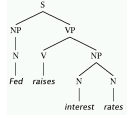
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Headed phrase structure

- Context-free grammar
- VP → ... VB\* ...
- NP → ... NN\* ...
- ADJP → ... JJ\* ...
- ADVP → ... RB\* ...
- S → ... NP VP ...
- Plus minor phrase types:
  - QP (quantifier phrase in NP: *some people*), CONJP (multi word constructions: *as well as*), INTJ (interjections: *aha*), etc.



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Two views of linguistic structure:  
 2. Dependency structure

- Dependency structure shows which words depend on (modify or are arguments of) which other words.

*The boy put the tortoise on the rug*

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Two views of linguistic structure:  
 2. Dependency structure

- Dependency structure shows which words depend on (modify or are arguments of) which other words.

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Outline

- Phrase Chunking
- (Probabilistic) Context-Free Grammars
- Chomsky Normal Form
- CKY Parsing

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Phrase Chunking

- Find all non-recursive noun phrases (NPs) and verb phrases (VPs) in a sentence.
- [NP I] [VP ate] [NP the spaghetti] [PP with] [NP meatballs].
- [NP He] [VP reckons] [NP the current account deficit] [VP will narrow] [PP to] [NP only 1.8 billion] [PP in] [NP September].

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Phrase Chunking as Sequence Labeling

- Tag individual words with one of 3 tags
  - B (Begin) word starts new target phrase
  - I (Inside) word is part of target phrase but not the first word
  - O (Other) word is not part of target phrase
- Sample for NP chunking
  - He reckons the current account deficit will narrow to only 1.8 Billion in September.

Begin    Inside    Other

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Evaluating Chunking

Per token accuracy does not evaluate finding correct full chunks.  
 Instead use:

Precision =  $\frac{\text{Number of correct chunks found}}{\text{Total number of chunks found}}$

Recall =  $\frac{\text{Number of correct chunks found}}{\text{Total number of actual chunks}}$

F measure:  $F_1 = \frac{1}{(\frac{1}{P} + \frac{1}{R})/2} = \frac{2PR}{P+R}$

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### Current Chunking Results

- Best system for NP chunking:  $F_1=96\%$
- Typical results for finding range of chunk types (CoNLL 2000 shared task: NP, VP, PP, ADV, SBAR, ADJP) is  $F_1=92-94\%$

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### Outline

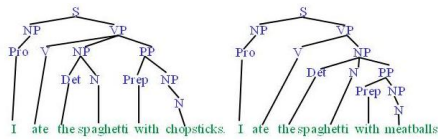
- Phrase Chunking
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### Syntactic Parsing

- Produce the correct syntactic parse tree for a sentence.



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### Annotated data: The Penn Treebank

[Marcus et al. 1993, Computational Linguistics]

```
(S
  (NP-SBJ (DT The) (NN move))
  (VP (VBD followed)
    (NP
      (NP (DT a) (NN round))
      (PP (IN of)
        (NP
          (NP (JJ similar) (NNS increases))
          (PP (IN by)
            (NP (JJ other) (NNS lenders)))
          (PP (IN against)
            (NP (NNP Arizona) (JJ real) (NN estate) (NNS loans))))))
      (.))
    (S-ADV
      (NP-SBJ (-NONE- *))
      (VP (VBG reflecting)
        (NP
          (NP (DT a) (VBG continuing) (NN decline))
          (PP-LOC (IN in)
            (NP (DT that) (NN market))))))
      (.)))
```

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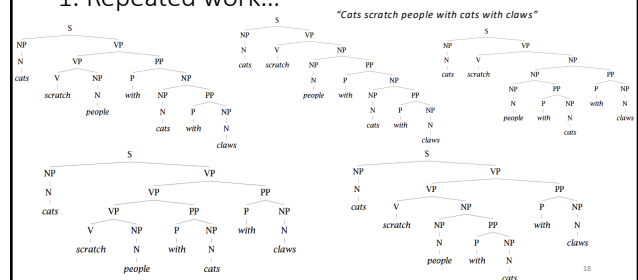
### The rise of annotated data

- Starting off, building a treebank seems a lot slower and less useful than building a grammar
- But a treebank gives us many things
  - Reusability of the labor
    - Many parsers, POS taggers, etc.
    - Valuable resource for linguistics
  - Broad coverage
  - Frequencies and distributional information
  - A way to evaluate systems

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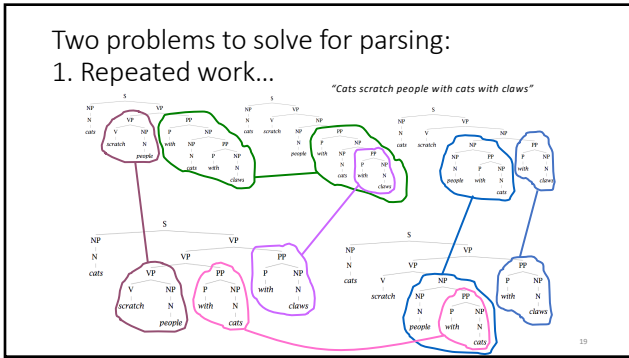
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### Two problems to solve for parsing: 1. Repeated work...



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- Two problems to solve for parsing:  
2. Choosing the correct parse
- How do we work out the correct attachment:
    - She saw the man with a telescope
  - Words are good predictors of attachment, even absent full understanding
    - Moscow **sent** more than 100,000 soldiers **into** Afghanistan ...
    - Sydney Water breached an **agreement with** NSW Health ...
  - Our statistical parsers will try to exploit such statistics.

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- Statistical parsing applications
- Statistical parsers are now robust and widely used in larger NLP applications:
- High precision question answering [Pasca and Harabagiu SIGIR 2001]
  - Improving biological named entity finding [Finkel et al. JNLPBA 2004]
  - Syntactically based sentence compression [Lin and Wilbur 2007]
  - Extracting opinions about products [Bloom et al. NAACL 2007]
  - Improved interaction in computer games [Gorniak and Roy 2005]
  - Helping linguists find data [Resnik et al. BLS 2005]
  - Source sentence analysis for machine translation [Xu et al. 2009]
  - Relation extraction systems [Fundel et al. Bioinformatics 2006]

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- (Probabilistic) Context-Free Grammars
- CFG
  - PCFG

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- Phrase structure grammars  
= context-free grammars (CFGs)
- $G = (T, N, S, R)$ 
    - T is a set of terminal symbols
    - N is a set of nonterminal symbols
    - S is the start symbol ( $S \in N$ )
    - R is a set of rules/productions of the form  $X \rightarrow \gamma$ 
      - $X \in N$  and  $\gamma \in (N \cup T)^*$

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- A phrase structure grammar
- |                          |                                 |
|--------------------------|---------------------------------|
| $S \rightarrow NP VP$    | $N \rightarrow \textit{people}$ |
| $VP \rightarrow V NP$    | $N \rightarrow \textit{fish}$   |
| $VP \rightarrow V NP PP$ | $N \rightarrow \textit{tanks}$  |
| $NP \rightarrow NP NP$   | $N \rightarrow \textit{rods}$   |
| $NP \rightarrow NP PP$   | $V \rightarrow \textit{people}$ |
| $NP \rightarrow N$       | $V \rightarrow \textit{fish}$   |
| $NP \rightarrow e$       | $V \rightarrow \textit{tanks}$  |
| $PP \rightarrow P NP$    | $P \rightarrow \textit{with}$   |
- people fish tanks*  
*people fish with rods*

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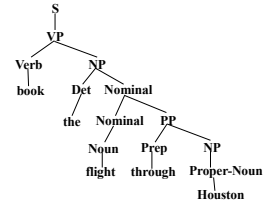
### Phrase structure grammars = context-free grammars (CFGs)

- $G = (T, N, S, R)$ 
  - T is a set of terminal symbols
  - N is a set of nonterminal symbols
  - S is the start symbol ( $S \in N$ )
  - R is a set of rules/productions of the form  $X \rightarrow \gamma$ 
    - $X \in N$  and  $\gamma \in (N \cup T)^*$
- A grammar G generates a language L.

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### Sentence Generation

- Sentences are generated by recursively rewriting the start symbol using the productions until only terminal symbols remain.



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### Phrase structure grammars in NLP

- $G = (T, C, N, S, L, R)$ 
  - T is a set of terminal symbols
  - C is a set of preterminal symbols
  - N is a set of nonterminal symbols
  - S is the start symbol ( $S \in N$ )
  - L is the lexicon, a set of items of the form  $X \rightarrow x$ 
    - $X \in C$  and  $x \in T$
  - R is the grammar, a set of items of the form  $X \rightarrow \gamma$ 
    - $X \in N$  and  $\gamma \in (N \cup C)^*$
- By usual convention, S is the start symbol, but in statistical NLP, we usually have an extra node at the top (ROOT, TOP)
- We usually write  $e$  for an empty sequence, rather than nothing

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### A phrase structure grammar

- |                          |                        |
|--------------------------|------------------------|
| $S \rightarrow NP VP$    | $N \rightarrow people$ |
| $VP \rightarrow V NP$    | $N \rightarrow fish$   |
| $VP \rightarrow V NP PP$ | $N \rightarrow tanks$  |
| $NP \rightarrow NP NP$   | $N \rightarrow rods$   |
| $NP \rightarrow NP PP$   | $V \rightarrow people$ |
| $NP \rightarrow N$       | $V \rightarrow fish$   |
| $NP \rightarrow e$       | $V \rightarrow tanks$  |
| $PP \rightarrow P NP$    | $P \rightarrow with$   |
- people fish tanks*  
*people fish with rods*

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### Probabilistic – or stochastic – context-free grammars (PCFGs)

- $G = (T, N, S, R, P)$ 
  - T is a set of terminal symbols
  - N is a set of nonterminal symbols
  - S is the start symbol ( $S \in N$ )
  - R is a set of rules/productions of the form  $X \rightarrow \gamma$
  - P is a probability function
    - $P: R \rightarrow [0,1]$
    - $\forall X \in N, \sum_{\gamma \in R} P(X \rightarrow \gamma) = 1$
- A grammar G generates a language model L.

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### A PCFG

- |                          |     |                        |     |
|--------------------------|-----|------------------------|-----|
| $S \rightarrow NP VP$    | 1.0 | $N \rightarrow people$ | 0.5 |
| $VP \rightarrow V NP$    | 0.6 | $N \rightarrow fish$   | 0.2 |
| $VP \rightarrow V NP PP$ | 0.4 | $N \rightarrow tanks$  | 0.2 |
| $NP \rightarrow NP NP$   | 0.1 | $N \rightarrow rods$   | 0.1 |
| $NP \rightarrow NP PP$   | 0.2 | $V \rightarrow people$ | 0.1 |
| $NP \rightarrow N$       | 0.7 | $V \rightarrow fish$   | 0.6 |
| $PP \rightarrow P NP$    | 1.0 | $V \rightarrow tanks$  | 0.3 |
|                          |     | $P \rightarrow with$   | 1.0 |

[With empty NP removed so less ambiguous]

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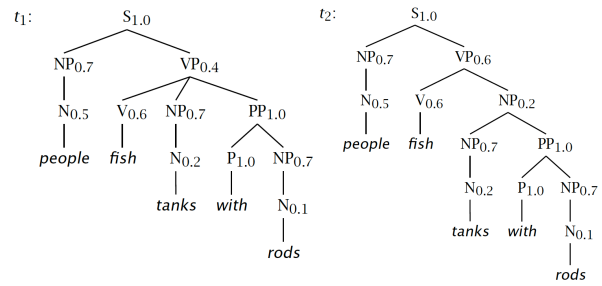
### The probability of trees and strings

- $P(t)$  – The probability of a tree  $t$  is the product of the probabilities of the rules used to generate it.
- $P(s)$  – The probability of the string  $s$  is the sum of the probabilities of the trees which have that string as their yield

$$P(s) = \sum_t P(s, t) \text{ where } t \text{ is a parse of } s$$

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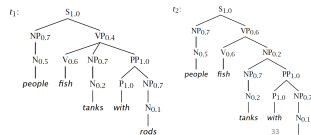


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### Tree and String Probabilities

- $s = \text{people fish tanks with rods}$
- $P(t_1) = 1.0 \times 0.7 \times 0.4 \times 0.5 \times 0.6 \times 0.7 \times 1.0 \times 0.2 \times 1.0 \times 0.7 \times 0.1 = 0.0008232$  **Verb attach**
- $P(t_2) = 1.0 \times 0.7 \times 0.6 \times 0.5 \times 0.6 \times 0.2 \times 0.7 \times 1.0 \times 0.2 \times 1.0 \times 0.7 \times 0.1 = 0.00024696$  **Noun attach**
- $P(s) = P(t_1) + P(t_2) = 0.0008232 + 0.00024696 = 0.00107016$



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### Outline

- Phrase Chunking
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### Chomsky Normal Form

- All rules are of the form  $X \rightarrow YZ$  or  $X \rightarrow w$ 
  - $X, Y, Z \in N$  and  $w \in T$
- A transformation to this form doesn't change the generative capacity of a CFG
  - That is, it recognizes the **same language**
    - But maybe with **different trees**
- Empties and unaries are removed recursively
- n-ary rules are divided by introducing new nonterminals ( $n > 2$ )

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### A phrase structure grammar

- |                          |                               |
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| $PP \rightarrow P NP$    | $P \rightarrow \text{with}$   |

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### Chomsky Normal Form steps

S → NP VP	
S → VP	N → <i>people</i>
VP → V NP	N → <i>fish</i>
VP → V	N → <i>tanks</i>
VP → V NP PP	N → <i>rods</i>
VP → V PP	V → <i>people</i>
NP → NP NP	V → <i>fish</i>
NP → NP	V → <i>tanks</i>
NP → NP PP	P → <i>with</i>
NP → PP	
NP → N	
PP → P NP	
PP → P	

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### Chomsky Normal Form steps

S → NP VP	N → <i>people</i>
VP → V NP	N → <i>fish</i>
S → V NP	N → <i>tanks</i>
VP → V	N → <i>rods</i>
S → V NP PP	V → <i>people</i>
VP → V PP	V → <i>fish</i>
S → V PP	V → <i>tanks</i>
NP → NP NP	P → <i>with</i>
NP → NP	
NP → NP PP	
NP → PP	
NP → N	
PP → P NP	
PP → P	

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### Chomsky Normal Form steps

S → NP VP	N → <i>people</i>
VP → V NP	N → <i>fish</i>
S → V NP	N → <i>tanks</i>
VP → V	N → <i>rods</i>
VP → V NP PP	V → <i>people</i>
S → V NP PP	S → <i>people</i>
VP → V PP	V → <i>fish</i>
S → V PP	V → <i>fish</i>
NP → NP NP	S → <i>fish</i>
NP → NP	V → <i>tanks</i>
NP → NP PP	V → <i>tanks</i>
NP → PP	S → <i>tanks</i>
NP → N	P → <i>with</i>
PP → P NP	
PP → P	

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### Chomsky Normal Form steps

S → NP VP	N → <i>people</i>
VP → V NP	N → <i>fish</i>
S → V NP	N → <i>tanks</i>
VP → V NP PP	N → <i>rods</i>
S → V NP PP	V → <i>people</i>
VP → V PP	S → <i>people</i>
S → V PP	VP → <i>people</i>
NP → NP NP	V → <i>fish</i>
NP → NP	S → <i>fish</i>
NP → NP PP	VP → <i>fish</i>
NP → PP	V → <i>tanks</i>
NP → N	S → <i>tanks</i>
PP → P NP	VP → <i>tanks</i>
PP → P	P → <i>with</i>

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### Chomsky Normal Form steps

S → NP VP	NP → <i>people</i>
VP → V NP	NP → <i>fish</i>
S → V NP	NP → <i>tanks</i>
VP → V	NP → <i>rods</i>
VP → V NP PP	V → <i>people</i>
S → V NP PP	S → <i>people</i>
VP → V PP	VP → <i>people</i>
S → V PP	V → <i>fish</i>
NP → NP NP	S → <i>fish</i>
NP → NP	VP → <i>fish</i>
NP → NP PP	V → <i>tanks</i>
NP → P NP	S → <i>tanks</i>
PP → P NP	VP → <i>tanks</i>
	P → <i>with</i>
	PP → <i>with</i>

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### Chomsky Normal Form steps

S → NP VP	NP → <i>people</i>
VP → V NP	NP → <i>fish</i>
S → V NP	NP → <i>tanks</i>
VP → V @VP_V	NP → <i>rods</i>
@VP_V → NP PP	V → <i>people</i>
S → V @S_V	S → <i>people</i>
@S_V → NP PP	VP → <i>people</i>
VP → V PP	V → <i>fish</i>
S → V PP	S → <i>fish</i>
NP → NP NP	VP → <i>fish</i>
NP → NP PP	V → <i>tanks</i>
NP → P NP	S → <i>tanks</i>
PP → P NP	VP → <i>tanks</i>
	P → <i>with</i>
	PP → <i>with</i>

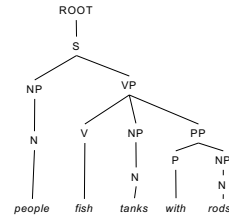
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### Chomsky Normal Form

- You should think of this as a transformation for efficient parsing
- **Binarization** is crucial for cubic time CFG parsing
- The rest isn't necessary; it just makes the algorithms cleaner and a bit quicker

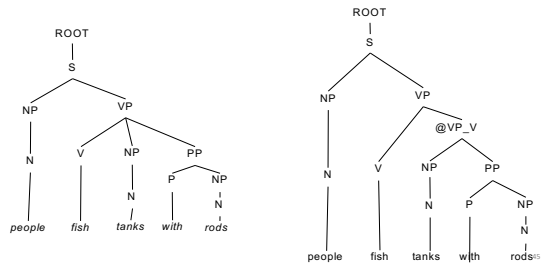
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### An example: before binarization...



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### Before and After binarization on VP



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### Outline

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- ➔ • CKY Parsing

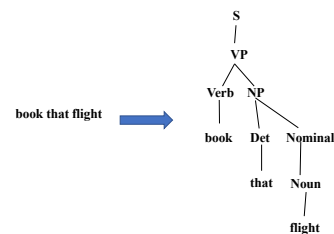
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### Parsing

- Given a string of terminals (e.g. sentences) and a CFG, determine if the string can be generated by the CFG.
  - Also return a parse tree for the string
  - Also return all possible parse trees for the string
- Must search space of derivations for one that derives the given string.
  - **Top-Down Parsing:** Start searching space of derivations for the start symbol.
  - **Bottom-up Parsing:** Start search space of reverse derivations from the terminal symbols in the string.

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### Parsing Example



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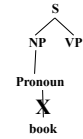
Top Down Parsing



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Top Down Parsing



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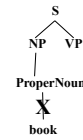
Top Down Parsing



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Top Down Parsing



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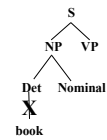
Top Down Parsing



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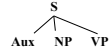
Top Down Parsing



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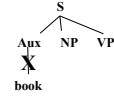
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Top Down Parsing



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Top Down Parsing



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Top Down Parsing



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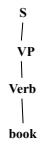
Top Down Parsing



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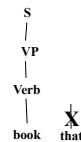
Top Down Parsing



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Top Down Parsing



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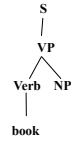
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Top Down Parsing



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Top Down Parsing

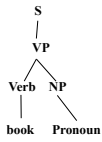


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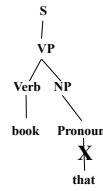
Top Down Parsing



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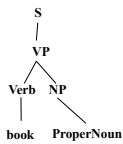
Top Down Parsing



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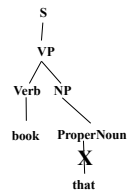
Top Down Parsing



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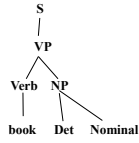
Top Down Parsing



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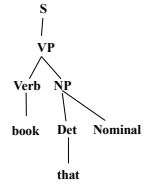
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Top Down Parsing



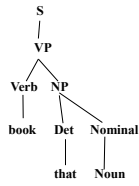
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Top Down Parsing



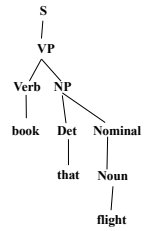
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Top Down Parsing



69

Top Down Parsing



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Bottom Up Parsing

book that flight

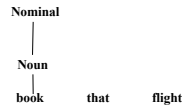
71

Bottom Up Parsing

Noun  
book that flight

72

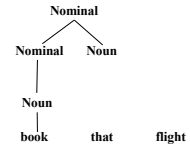
Bottom Up Parsing



73

73

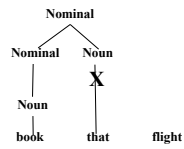
Bottom Up Parsing



74

74

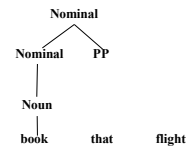
Bottom Up Parsing



75

75

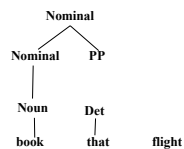
Bottom Up Parsing



76

76

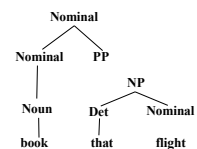
Bottom Up Parsing



77

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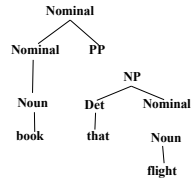
Bottom Up Parsing



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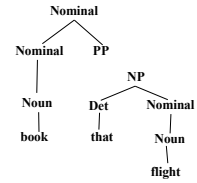
Bottom Up Parsing



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79

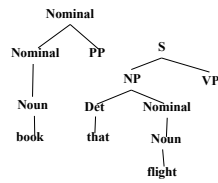
Bottom Up Parsing



80

80

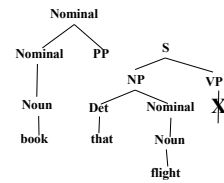
Bottom Up Parsing



81

81

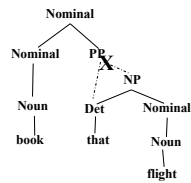
Bottom Up Parsing



82

82

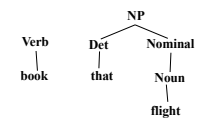
Bottom Up Parsing



83

83

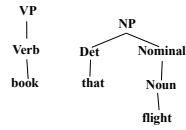
Bottom Up Parsing



84

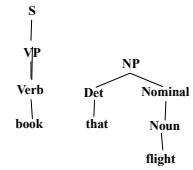
84

Bottom Up Parsing



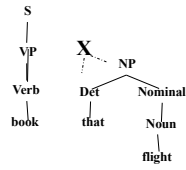
85

Bottom Up Parsing



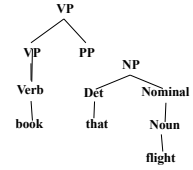
86

Bottom Up Parsing



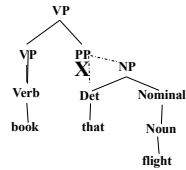
87

Bottom Up Parsing



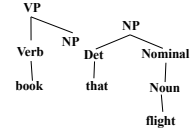
88

Bottom Up Parsing

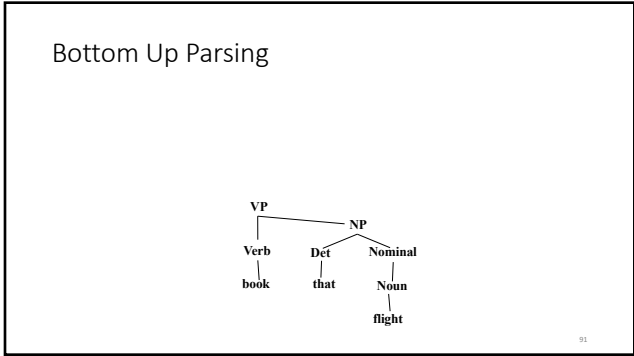


89

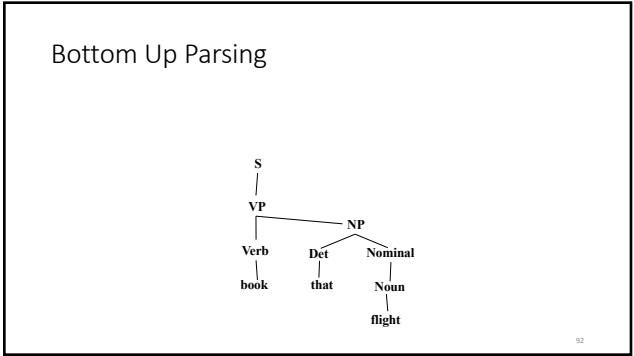
Bottom Up Parsing



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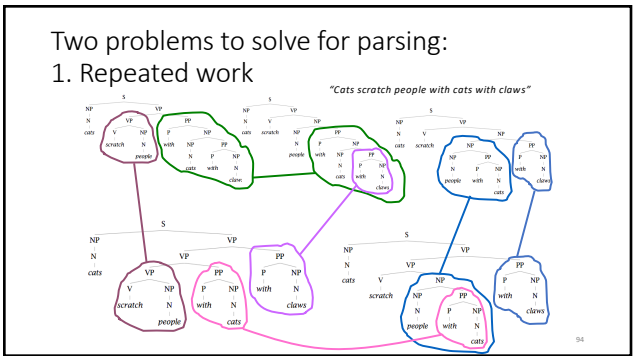
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- ### Top Down vs. Bottom Up
- Top down never explores options that will not lead to a full parse, but can explore many options that never connect to the actual sentence.
  - Bottom up never explores options that do not connect to the actual sentence but can explore options that can never lead to a full parse.
  - Relative amounts of wasted search depend on how much the grammar branches in each direction.

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- ### Dynamic Programming Parsing
- To avoid extensive repeated work, must cache intermediate results, i.e. completed phrases.
  - Caching (memorizing) is critical to obtaining a polynomial time parsing (recognition) algorithm for CFGs.

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### (Probabilistic) CKY Parsing

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### Constituency Parsing

Input: a PCFG, and a sentence

fish people fish tanks

PCFG		
Rule	Prob	$\theta_i$
$S \rightarrow NP VP$		$\theta_0$
$NP \rightarrow NP NP$		$\theta_1$
...		
$N \rightarrow fish$		$\theta_{k2}$
$N \rightarrow people$		$\theta_{k3}$
$V \rightarrow fish$		$\theta_{k4}$
...		

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### Constituency Parsing

Output: a parsing tree

PCFG		
Rule	Prob	$\theta_i$
$S \rightarrow NP VP$		$\theta_0$
$NP \rightarrow NP NP$		$\theta_1$
...		
$N \rightarrow fish$		$\theta_{k2}$
$N \rightarrow people$		$\theta_{k3}$
$V \rightarrow fish$		$\theta_{k4}$
...		

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### Cocke-Kasami-Younger (CKY) Constituency Parsing

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### Reusing local decisions

$NP \rightarrow people$	0.35
$V \rightarrow people$	0.1
$N \rightarrow people$	0.5
$VP \rightarrow fish$	0.06
$V \rightarrow fish$	0.6
$N \rightarrow fish$	0.2
$S \rightarrow NP VP$	0.9
$S \rightarrow VP$	0.1
$VP \rightarrow V NP$	0.5
$NP \rightarrow NP NP$	0.1
$NP \rightarrow NP PP$	0.2
$PP \rightarrow P NP$	1.0

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### Reusing local decisions

$NP \rightarrow people$	0.35
$V \rightarrow people$	0.1
$N \rightarrow people$	0.5
$VP \rightarrow fish$	0.06
$V \rightarrow fish$	0.6
$N \rightarrow fish$	0.2
$S \rightarrow NP VP$	0.9
$S \rightarrow VP$	0.1
$VP \rightarrow V NP$	0.5
$NP \rightarrow NP NP$	0.1
$NP \rightarrow NP PP$	0.2
$PP \rightarrow P NP$	1.0

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### Reusing local decisions

$NP \rightarrow people$	0.35
$V \rightarrow people$	0.1
$N \rightarrow people$	0.5
$VP \rightarrow fish$	0.06
$V \rightarrow fish$	0.6
$N \rightarrow fish$	0.2
$S \rightarrow NP VP$	0.9
$S \rightarrow VP$	0.1
$VP \rightarrow V NP$	0.5
$NP \rightarrow NP NP$	0.1
$NP \rightarrow NP PP$	0.2
$PP \rightarrow P NP$	1.0

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### The CKY algorithm (1960/1965) ... extended to unaries

```
function CKY(words, grammar) returns [most_probable_parse, prob]
score = new double[#(words)+1][#(words)+1][#(nonterms)]
back = new Pair[#(words)+1][#(words)+1][#(nonterms)]
for i=0; i<#(words); i++
  for A in nonterms
    if A -> words[i] in grammar
      score[i][i+1][A] = P(A -> words[i])
//handle unaries
boolean added = true
while added
  added = false
  for A, B in nonterms
    if score[i][i+1][B] > 0 && A->B in grammar
      prob = P(A->B)*score[i][i+1][B]
      if prob > score[i][i+1][A]
        score[i][i+1][A] = prob
        back[i][i+1][A] = B
        added = true
```

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### The CKY algorithm (1960/1965) ... extended to unaries

```
for span = 2 to #(words)
  for begin = 0 to #(words) - span
    end = begin + span
    for split = begin+1 to end-1
      for A, B, C in nonterms
        prob = score[begin][split][B]*score[split][end][C]*P(A->BC)
        if prob > score[begin][end][A]
          score[begin][end][A] = prob
          back[begin][end][A] = new Triple(split, B, C)
//handle unaries
boolean added = true
while added
  added = false
  for A, B in nonterms
    prob = P(A->B)*score[begin][end][B];
    if prob > score[begin][end][A]
      score[begin][end][A] = prob
      back[begin][end][A] = B
      added = true
return buildTree(score, back)
```

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