EECS 498-004: Introduction to Natural Language Processing

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Thanks for your hard work and feedbacks on homework!

- We will strive for clarity!
- Things that I want to stress:

 - This course will not rely on automated grading. Several considerations:

 Oding flexibility: Results may vary due to different choices of tools, e.g. sentence segmenters, tokenizers, etc (we're happy to make recommendations, but will not put constraints on the choice).

 Results may also differ among submissions due to different machines (and configurations) used

 Personalized comments: IAs will run your code and grade based on logics, and comment accordingly.

 - Readings are required (i.e. not optional).

 Some notations are different in 3rd edition of the textbook, but shouldn't affect understanding.

Quick polls on programming assignments

- 1. HW2: Currently we have two programming questions in HW2 (one for HMM with Viterbi implementation, the other for feedforward neural networks using existing tools). Q: moving the neural network question to next homework (i.e. HW3)?
- 2. HW 3&4: **Q**: reducing programming assignments (less questions) in the future homeworks?

Outline

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- Logistic Regression
 - Feedforward Neural Networks
 - Recurrent Neural Networks

[Some slides are borrowed from Dan Jurafsky, Hugo Larochelle, and Chris Manning]

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Logistic Regression (LogReg)

- Generative and Discriminative Classifiers
- Classification in LogReg (test)
- An example with sentiment analysis
- Learning in LogReg (training)

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Generative and Discriminative Classifiers

• Naïve Bayes is a generative classifier

by contrast:

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· Logistic regression is a discriminative classifier

Generative and Discriminative Classifiers

Suppose we're distinguishing cat from dog images





Generative Classifier:

- Build a model of what's in a cat image
 - Knows about whiskers, ears, eyes
 Assigns a probability to any image
 - Assigns a probability to any image:
 how cat-y is this image?



Also build a model for dog images

Now given a new image:

Run both models and see which one fits better

Discriminative Classifier

Just try to distinguish dogs from cats





Oh look, dogs have collars! Let's ignore everything else

Finding the correct class c from a document d in Generative vs Discriminative Classifiers

• Naive Bayes

 $\hat{c} = \underset{c}{\operatorname{argmax}} \quad \overbrace{P(d|c)}^{\text{likelihood prior}} \quad \overbrace{P(c)}^{\text{prior}}$

• Logistic Regression

posterior

$$\hat{c} = \underset{c \in C}{\operatorname{argmax}} P(c|d)$$

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Components of a probabilistic machine learning classifier

Given m input/output pairs $(x^{(i)}, y^{(i)})$:

- 1. A **feature representation** of the input. For each input observation x(i), a vector of features $[x_1, x_2, ..., x_n]$. Feature i for input $x^{(j)}$ is x_i , or sometimes $f_i(x)$.
- 2. A classification function that computes y, the estimated class, via $\rho(y|x)$, like the sigmoid or softmax functions.
- 3. An objective function for learning, like cross-entropy loss.
- An algorithm for optimizing the objective function: stochastic gradient descent.

The two phases of Logistic Regression

- \bullet $\mathbf{Training}:$ we learn weights w and b using $\mathbf{stochastic}$ $\mathbf{gradient}$ descent and cross-entropy loss.
- **Test**: Given a test example x we compute p(y|x) using learned weights (or parameters), and return whichever label (y = 1 or y = 0)is higher probability

Logistic Regression (LogReg)

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Binary Classification in Logistic Regression

- Given a series of input/output pairs:
 - (x⁽ⁱ⁾, y⁽ⁱ⁾)
- For each observation x⁽ⁱ⁾
 - We represent $x^{(i)}$ by a **feature vector** $[x_1, x_2,..., x_n]$
 - We compute an output: a predicted class $\hat{\mathbf{v}}^{(i)} \in$ {0,1}

Features in logistic regression

- For feature x_i, weight w_i tells "how important is x_i"
 - x_i ="review contains 'awesome'": w_i = +10 x_j ="review contains 'abysma1'": w_j = -10

 - xk ="review contains 'mediocre'": wk = -2

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Logistic Regression for one observation x

- Input observation: vector $x = [x_1, x_2, ..., x_n]$
- Weights: one per feature: $W = [w_1, w_2, ..., w_n]$
 - \bullet Sometimes we call the weights θ
- Output: a predicted class $\hat{y} \in \{0,1\}$

How to do classification

- For each feature x_i, weight w_i tells us the importance of
- Plus we'll have a bias b
- We'll sum up all the weighted features and the bias

$$z = \left(\sum_{i=1}^{n} w_i x_i\right) + b$$

 $\Longrightarrow z = w \cdot x + b$

• If this sum is high, we say y=1; if low, then y=0

But we want a probabilistic classifier

- We need to formalize "sum is high".
- We'd like a principled classifier that gives us a probability, just like Naive Bayes did
- Concretely, we want a model that can tell us: p(y=1|x) p(y=0|x)

The problem: z isn't a probability, it's just a number!

$$z = w \cdot x + b$$

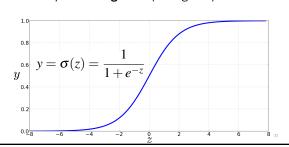
• Solution: use a function of z that goes from 0 to 1

$$y = \sigma(z) = \frac{1}{1 + e^{-z}} = \frac{1}{1 + \exp(-z)}$$

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The very useful **sigmoid** (or logistic) function



Idea of logistic regression

- We'll compute $w \cdot x + b$
- And then we'll pass it through the sigmoid function: $\sigma(w\cdot x+b)$
- And we'll just treat it as a probability

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Making probabilities with sigmoids

$$P(y=1) = \sigma(w \cdot x + b)$$

$$= \frac{1}{1 + \exp(-(w \cdot x + b))}$$

$$P(y=0) = 1 - \sigma(w \cdot x + b)$$

$$= 1 - \frac{1}{1 + \exp(-(w \cdot x + b))}$$

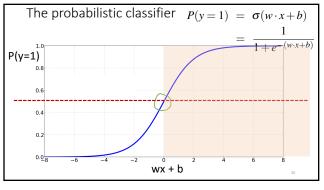
$$= \frac{\exp(-(w \cdot x + b))}{1 + \exp(-(w \cdot x + b))}$$

Turning a probability into a classifier

$$\hat{y} = \begin{cases} 1 & \text{if } P(y=1|x) > 0.5\\ 0 & \text{otherwise} \end{cases}$$

0.5 here is called the decision boundary

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Turning a probability into a classifier

$$\hat{y} = \begin{cases} 1 & \text{if } P(y=1|x) > 0.5 & \text{if } \mathbf{w} \cdot \mathbf{x} + \mathbf{b} > 0 \\ 0 & \text{otherwise} & \text{if } \mathbf{w} \cdot \mathbf{x} + \mathbf{b} \le 0 \end{cases}$$

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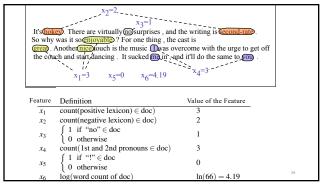
Logistic Regression (LogReg)

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Sentiment example: does y=1 or y=0?

•It's hokey . There are virtually no surprises , and the writing is second-rate . So why was it so enjoyable ? For one thing , the cast is great . Another nice touch is the music . I was overcome with the urge to get off the couch and start dancing . It sucked me in , and it'll do the same to you .

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Classifying sentiment for input x Feature Definition Value of the Feature $count(positive lexicon) \in doc)$ x_1 $count(negative\ lexicon) \in doc)$ 2 ∫ 1 if "no" ∈ doc 1 0 otherwise $count(1st \text{ and } 2nd \text{ pronouns} \in doc)$ 3 x_4 ∫ 1 if "!" ∈ doc x_5 0 otherwise log(word count of doc) ln(66) = 4.19Suppose w = [2.5, -5.0, -1.2, 0.5, 2.0, 0.7] b = 0.1

Classifying sentiment for input x

Suppose w = [2.5, -5.0, -1.2, 0.5, 2.0, 0.7] b = 0.1
$$p(+|x) = P(Y = 1|x) = \sigma(w \cdot x + b)$$
$$= \sigma([2.5, -5.0, -1.2, 0.5, 2.0, 0.7] \cdot [3, 2, 1, 3, 0, 4.19] + 0.1)$$
$$= \sigma(.833)$$
$$= 0.70$$
$$p(-|x|) = P(Y = 0|x) = 1 - \sigma(w \cdot x + b)$$
$$= 0.30$$

Classification in (binary) logistic regression: summary

- Given:
 - a set of classes: (+ sentiment,- sentiment)
- a vector ${\boldsymbol x}$ of features [${\boldsymbol x}_1$, ${\boldsymbol x}_2$, ..., ${\boldsymbol x}_n$]
 - x₁= count("awesome")
 - x₂ = log(number of words in review)
- A vector \mathbf{w} of weights $[w_1, w_2, ..., w_n]$
 - w_i for each feature f_i

$$P(y=1) = \sigma(w \cdot x + b)$$
$$= \frac{1}{1 + e^{-(w \cdot x + b)}}$$

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Wait, where did the W's come from?

- Supervised classification: we know the correct label y (either 0 or 1) for each x.
- What the system produces is an estimate, \hat{y}
- We want to set w and b to minimize the **distance** between our estimate $\hat{y}^{(i)}$ and the true $y^{(i)}$.

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Wait, where did the W's come from?

- Supervised classification: we know the correct label y (either 0 or 1) for each x.
- What the system produces is an estimate, \hat{y}
- We want to set w and b to minimize the **distance** between our estimate $\hat{y}^{(i)}$ and the true $y^{(i)}$.
 - We need a distance estimator: a loss function or a cost function
 - ullet We need an optimization algorithm to update w and b to minimize the loss.

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Learning components

- A loss function:
 - cross-entropy loss
- An optimization algorithm:
 - stochastic gradient descent (not covered in the lecture)

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The distance between \hat{y} and y

We want to know how far is the classifier output:

$$\hat{y} = \sigma(w \cdot x + b)$$

from the true output:

We'll call this difference:

 $L(\hat{y}, y) = \text{how much } \hat{y} \text{ differs from the true } y$

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Deriving cross-entropy loss for a single observation x

- Goal: maximize probability of the correct label p(y|x)
- Since there are only 2 discrete outcomes (0 or 1) we can express the probability p(y|x) from our classifier (the thing we want to maximize) as

$$p(y|x) = \hat{y}^y (1-\hat{y})^{1-y}$$

- if the gold-standard label y=1, this simplifies to \hat{y} (the predicted probability for x having a label of 1)
- if the gold-standard label y=0, this simplifies to 1– \hat{y}

Deriving cross-entropy loss for a single observation x

• We choose the parameters w,b that maximize the probability

of the true y labels in the training data given the observations

Goal: maximize probability of the correct label p(y|x)

Cross-entropy loss

Maximize:

$$p(y|x) = \hat{y}^y (1-\hat{y})^{1-y}$$

• Now take the log of both sides (mathematically handy)

Maximize

$$\log p(y|x) = \log [\hat{y}^{y} (1 - \hat{y})^{1 - y}]$$

= $y \log \hat{y} + (1 - y) \log (1 - \hat{y})$

• Whatever values maximize log p(y|x) will also maximize p(y|x)

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Deriving cross-entropy loss for a single observation x

Goal: maximize probability of the correct label p(y|x)

Maximize:
$$\log p(y|x) = \log [\hat{y}^y (1-\hat{y})^{1-y}]$$

= $y \log \hat{y} + (1-y) \log (1-\hat{y})$

• Now flip sign to turn this into a loss: something to minimize Cross-entropy loss

$$L_{\text{CE}}(\hat{y}, y) = -\log p(y|x) = -[y \log \hat{y} + (1-y) \log(1-\hat{y})]$$

• Or, plugging in definition of \hat{y} :

$$L_{CE}(\hat{y}, y) = -[y \log \sigma(w \cdot x + b) + (1 - y) \log (1 - \sigma(w \cdot x + b))]$$

Let's see if this works for our sentiment example

• We want loss to be:

smaller if the model's prediction is close to the correct label bigger if model is confused

• Let's first suppose the true label of this is y=1 (positive)

It's hokey . There are virtually no surprises , and the writing is second-rate . So why was it so enjoyable ? For one thing , the cast is great . Another nice touch is the music . I was overcome with the urge to get off the couch and start dancing . It sucked me in , and it'll do the same to you .

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Let's see if this works for our sentiment example

• True value is y=1. How well is our model doing?

$$\begin{array}{ll} p(+|x) = P(Y=1|x) &=& \sigma(w \cdot x + b) \\ &=& \sigma([2.5, -5.0, -1.2, 0.5, 2.0, 0.7] \cdot [3, 2, 1, 3, 0, 4.19] + 0.1) \\ &=& \sigma(.833) \\ &=& 0.70 \end{array}$$

• Pretty well! What's the loss?

$$\begin{array}{ll} L_{\text{CE}}(\hat{\mathbf{y}}, \mathbf{y}) = & -[y \log \sigma(w \cdot x + b) + (1 - y) \log (1 - \sigma(w \cdot x + b))] \\ = & -[\log \sigma(w \cdot x + b)] \\ = & -\log(.70) \\ = & .36 \end{array}$$

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Let's see if this works for our sentiment example

• Suppose true value instead was y=0.

$$p(-|x) = P(Y = 0|x) = 1 - \sigma(w \cdot x + b)$$

= 0.30

• What's the loss?

$$\begin{split} L_{\text{CE}}(\hat{\mathbf{y}}, \mathbf{y}) &= & -[y \log \sigma(w \cdot x + b) + (1 - y) \log (1 - \sigma(w \cdot x + b))] \\ &= & -[\log (1 - \sigma(w \cdot x + b))] \\ &= & -\log (.30) \\ &= & 1.2 \end{split}$$

Let's see if this works for our sentiment example

• The loss when model was right (if true y=1)

$$\begin{aligned} L_{\text{CE}}(\hat{y}, y) &= & -[y \log \sigma(w \cdot x + b) + (1 - y) \log (1 - \sigma(w \cdot x + b))] \\ &= & -[\log \sigma(w \cdot x + b)] \\ &= & -\log(.70) \\ &= & 36 \end{aligned}$$

• Is lower than the loss when model was wrong (if true y=0):

$$\begin{array}{lll} L_{\text{CE}}(\hat{\mathbf{y}}, \mathbf{y}) = & & -[y \log \sigma(w \cdot x + b) + (1 - y) \log (1 - \sigma(w \cdot x + b))] \\ = & & -[\log (1 - \sigma(w \cdot x + b))] \\ = & & -\log (.30) \\ = & & 1.2 \end{array}$$

• Sure enough, loss was bigger when model was wrong!

Our goal: minimize the loss

- Let's make explicit that the loss function in parameterized by weights θ =(w,b)
- We want the weights that minimize the loss, averaged over all

$$\hat{\theta} = \underset{\theta}{\operatorname{argmin}} \frac{1}{m} \sum_{i=1}^{m} L_{CE}(f(x^{(i)}; \theta), y^{(i)})$$

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Problem of Overfitting

- A model that perfectly match the training data has a problem.
- It will also overfit to the data, e.g.,
 - A random word that perfectly predicts y (it happens to only occur in one class) will get a very high weight.
- Failing to generalize to a test set without this word.
- A good model should be able to generalize.

Problem of Overfitting

This movie drew me in, and it'll do the same to you.

I can't tell you how much I hated this movie. It sucked. Useful or harmless features

X1 = "this" X2 = "movie X3 = "hated" X4 = "drew me in"

4gram features that just "memorize" training set and might cause problems

X5 = "the same to you" X6 = "tell you how much"

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Problem of Overfitting

- 4-gram model on tiny data will just memorize the data • 100% accuracy on the training set
- But it will be surprised by the novel 4-grams in the test data • Low accuracy on test set
- Models that are too powerful can overfit the data
 - Fitting the details of the training data so exactly that the model doesn't generalize well to the test set
 - How to avoid overfitting?
 - · Regularization in logistic regression
 - Dropout in neural networks

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Regularization

- A solution for overfitting
- Add a regularization term $R(\theta)$ to the loss function (for now written as maximizing log probability rather than minimizing loss)

$$\hat{\theta} = \underset{\theta}{\operatorname{argmax}} \sum_{i=1}^{m} \log P(y^{(i)}|x^{(i)}) - \alpha R(\theta)$$

- Idea: choose an $R(\theta)$ that penalizes large weights
 - fitting the data well with lots of big weights not as good as fitting the data a little less well, with small weights

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L2 Regularization

- The sum of the squares of the weights: L2 norm $||\theta||_2$ • i.e., the square of the **Euclidean distance** of θ to the origin.
- L2 regularized objective function:

$$R(\theta) = ||\theta||_2^2 = \sum_{j=1}^n \theta_j^2$$

$$\hat{\theta} = \underset{\theta}{\operatorname{argmax}} \left[\sum_{i=1}^{m} \log P(y^{(i)}|x^{(i)}) \right] - \alpha \sum_{j=1}^{n} \theta_{j}^{2}$$

L1 Regularization

- The sum of the absolute value of the weights: L1 norm $\|\theta\|_1$
- L1 regularized objective function:

$$R(\theta) = ||\theta||_1 = \sum_{i=1}^{n} |\theta_i|$$

$$R(\theta) = ||\theta||_1 = \sum_{i=1}^n |\theta_i|$$

$$\hat{\theta} = \underset{\theta}{\operatorname{argmax}} \left[\sum_{1=i}^m \log P(y^{(i)}|x^{(i)}) \right] - \alpha \sum_{j=1}^n |\theta_j|$$

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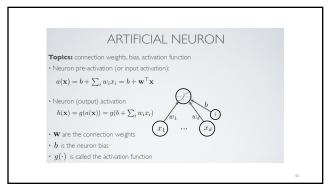
Outline

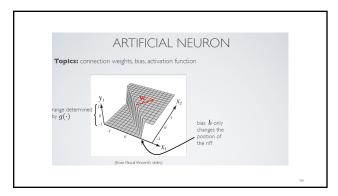
- Logistic Regression
- Feedforward Neural Networks
 - Recurrent Neural Networks

Neural Network Learning

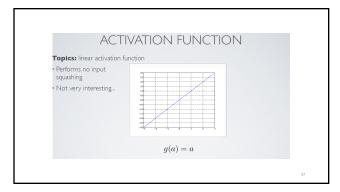
- Learning approach based on modeling adaptation in biological neural
- Perceptron: Initial algorithm for learning simple neural networks (single layer) developed in the 1950's.
- Backpropagation: More complex algorithm for learning multi-layer neural networks developed in the 1980's. (not required for this class)

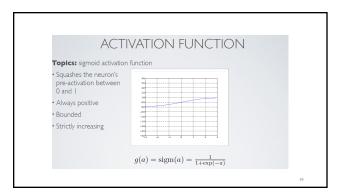
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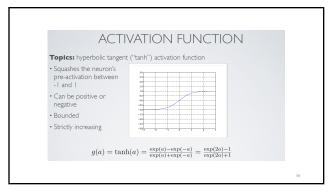


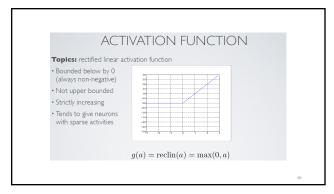
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class Neuron(object):
 # ...
def forward(inputs):
 """ assume inputs and weights are 1-D numpy arrays and bias is a number """
 cell_body_sum = np.sum(inputs * self.weights) + self.bias
 firing_rate = 1.0 / (1.0 + math.exp(-cell_body_sum)) # sigmoid activation function
 return firing_rate

Linear Separator

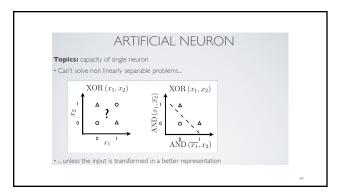
• Since one-layer neuron (aka perceptron) uses linear threshold function, it is searching for a linear separator that discriminates the classes.

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ARTIFICIAL NEURON

Topics: capacity of single neuron
• Can solve linearly separable problems

OR (x_1, x_2) AND $(\overline{x_1}, x_2)$ AND $(x_1, \overline{x_2})$ $(x_1$

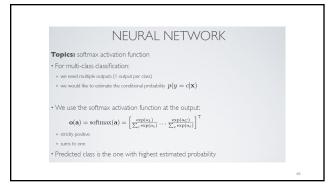


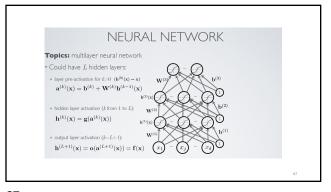
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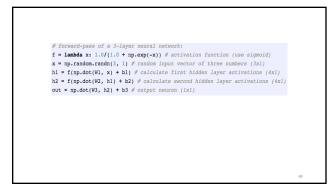
NEURAL NETWORK

Topics: single hidden layer neural network

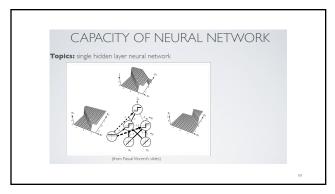
• Hidden layer pre-activation: $\mathbf{a}(\mathbf{x}) = \mathbf{b}^{(1)} + \mathbf{W}^{(1)}\mathbf{x}$ $(a(\mathbf{x})_1 + a(\mathbf{y})^{(1)} + \mathbf{y}_1 + b(\mathbf{y})^{(1)} + \mathbf{y}_2 + b(\mathbf{y})^{(1)} + b(\mathbf{y})$

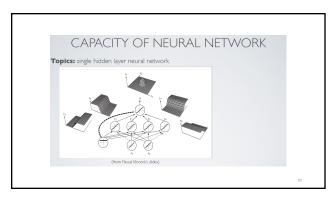




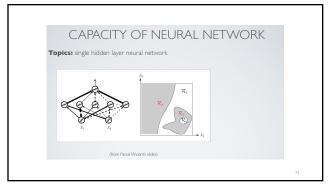


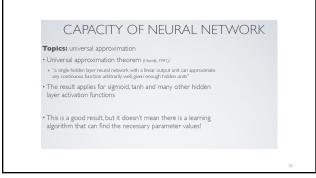
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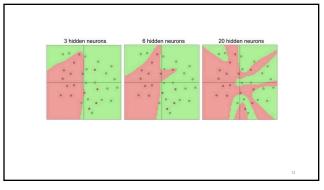
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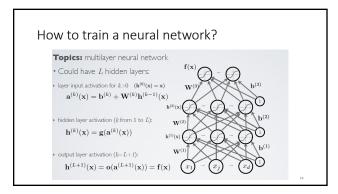




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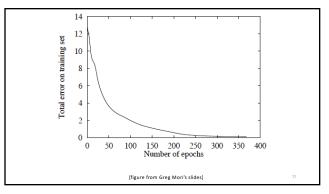


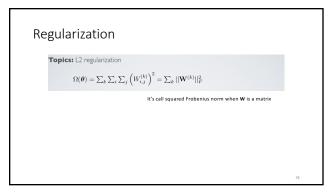


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Empirical Risk Minimization and Regularization $\begin{array}{l} \textbf{Toples:} \text{ empirical risk minimization, regularization} \\ \bullet \text{ Empirical risk minimization} \\ \bullet \text{ Empirical risk minimization} \\ \bullet \text{ framework to design learning algorithms} \\ & \underset{\boldsymbol{\theta}}{\arg\min} \frac{1}{T} \sum_{t} l(f(\mathbf{x}^{(t)}; \boldsymbol{\theta}), y^{(t)}) + \lambda \Omega(\boldsymbol{\theta}) \\ \bullet \text{ } l(f(\mathbf{x}^{(t)}; \boldsymbol{\theta}), y^{(t)}) \text{ is a loss function} \\ \bullet \Omega(\boldsymbol{\theta}) \text{ is a regularizer (penalizes certain values of } \boldsymbol{\theta}) \\ \bullet \text{ Learning is cast as optimization} \\ \bullet \text{ ideally, we'd optimize classification error, but it's not smooth} \\ \bullet \text{ loss function is a surrogate for what we truly should optimize (e.g. upper bound)} \\ \end{array}$

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 $\lambda = 0.001 \qquad \lambda = 0.1$ [http://cs231n.github.io/neural-networks-1/]

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Topics: initialization

For biases

• initialize all to 0

• For weights

• Can't initialize weights to 0 with tarh activation

• we can show that all guidents would then be 0 (addle point)

• Can't initialize all weights to 0 with tarh activation

• we can show that all guidents would then be 0 (addle point)

• Can't initialize all weights to the same value

• we can show that all hidden units in a layer will always behave the same

• need to break symmetry

• Recipice sample $W^{(4)}_{ab}$ from U[-b,b] where $b = \sqrt{b}$ • the idea is to sample around 0 but break symmetry

• the idea is to sample around 0 but break symmetry

• other values of b could work well find an exact science) (see Caront & Bergio, 2016)

Learning the Parameters (weights and bias)

• Backpropagation (BP) algorithm (not required for this course)

• Further reading on BP:

• https://towardsdatascience.com/understanding-backpropagation-algorithm-77b53aa2f95fd

https://mattmazur.com/2015/03/17/a-step-by-step-backpropagation-example/

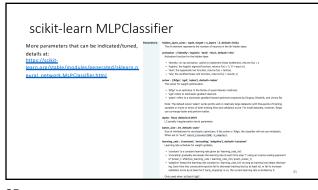
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Popular Tools

- scikit-learn: https://scikit-learn.org/
- PyTorch: https://pytorch.org/
- Tensorflow: https://www.tensorflow.org/

scikit-learn MLPClassifier

>>> from sklearn.neural_network import MLPClassifier
>>> X = [[0., e]., [1., 1.]]
>>> y = [0., 1]
>>> (tf = MLPClassifier(solver='lbfgs', alpha=le=5,
hidden_layer_size=(5, 2), random_state=1)
>>> clt.fst(X, y)
MLPClassifier(alpha=le=05, hidden_layer_sizes=(5, 2), random_state=1, solver='lbfgs')



Outline

• Logistic Regression

• Feedforward Neural Networks

• Recurrent Neural Networks

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Long Distance Dependencies

It is very difficult to train NNs to retain information over many time steps
This makes it very difficult to handle long-distance dependencies, such as subject-verb agreement.

E.g. Jane walked into the room. John walked in too. It was late in the day. Jane said hi to _?_

Recurrent Neural Networks (RNN)

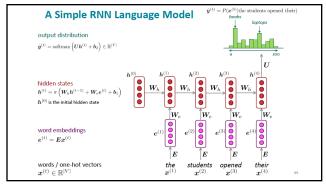
• Core idea: Apply the same weights W repeatedly

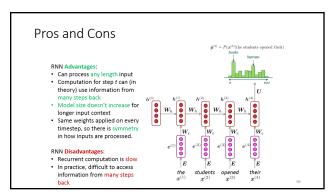
outputs (optional) { $\hat{y}^{(1)}$ $\hat{y}^{(2)}$ $\hat{y}^{(3)}$ $\hat{y}^{(4)}$...

hidden states { $\hat{y}^{(1)}$ $\hat{y}^{(2)}$ $\hat{y}^{(3)}$ $\hat{y}^{(4)}$...

input sequence (any length) { $\hat{x}^{(1)}$ $\hat{x}^{(2)}$ $\hat{x}^{(3)}$ $\hat{x}^{(4)}$...

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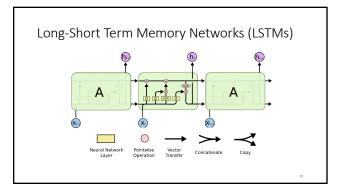




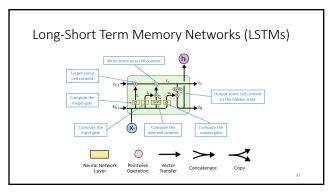
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Long-Short Term Memory Networks (LSTMs)

• A type of RNN proposed by Hochreiter and Schmidhuber in 1997



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Sequence to Sequence

• Encoder/Decoder framework maps one sequence to a "deep vector" then another LSTM maps this vector to an output sequence.

This is my cat C'est mon chat

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Successful Applications of LSTMs

- Speech recognition: Language and acoustic modeling
- Sequence labeling
 - POS Tagging
 - NER
 - Phrase Chunking
- Neural syntactic and semantic parsing
- Image captioning
- Sequence to Sequence
 - Machine Translation (Sustkever, Vinyals, & Le, 2014)
 - Summarization
 - Video Captioning (input sequence of CNN frame outputs)