



# EECS 487: Interactive Computer Graphics

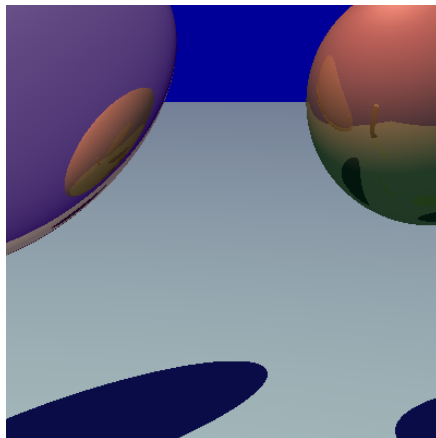
Lecture 29:

- Distributed Ray Tracing

## Why Does Ray Tracing Look Obviously Computer Generated?

Crisp images . . . too “perfect”:

- surfaces are **perfectly** shiny
- glass is **perfectly** clear
- everything in **perfect** focus
- every object is **completely** still
- even the shadows have **perfect** silhouettes
- but . . . up close, edges are jagged



## Ray Tracing

Introduction and context

- ray casting

Recursive ray tracing

- shadows
- reflection
- refraction

Distributed Ray Tracing

- anti-aliasing
- motion blur
- depth-of-field
- glossy surface
- translucency
- soft-shadows

Ray tracing implementation

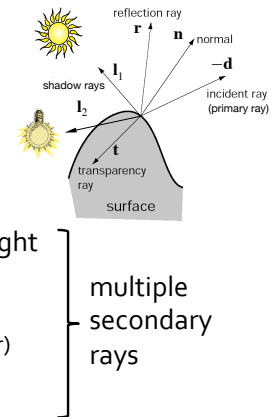
## “Distributed” Ray Tracing

Replace each single ray with a **distribution** of multiple rays  $\Rightarrow$  a.k.a. *distribution* ray tracing

- average results together

Multiple rays everywhere:

- multiple primary rays through a pixel:
  - **supersampling**: distribute rays spatially
  - **motion blur**: distribute rays temporally
  - **depth of field**: distribute rays through a lens
- multiple shadow rays to sample an area light
  - **soft shadows**
- multiple reflection rays
  - **glossy surfaces** (blurry reflection, rough specular)
- multiple refraction rays
  - **translucency**



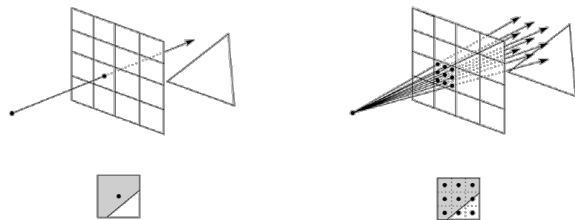
multiple secondary rays

# Supersampling

Instead of point sampling the color of a pixel with a ray, we cast multiple rays from eye (primary rays) through different parts of one pixel and average down the results

- for example, cast  $n \times n$  sub-pixel rays, and average the results together:

$$c_{pixel} = \frac{1}{n^2} \sum_{i=0}^{n-1} \sum_{j=0}^{n-1} c_{subpixel(i,j)}$$



Curlesso8

# Non-fixed Sampling Patterns

Super-sampling **doesn't eliminate aliasing**, it simply pushes it to **higher frequencies**

- supersampling captures more high frequencies, but frequencies above the supersampling rate are still aliased
- fundamentally, problem is that the signal is not bandlimited  $\Rightarrow$  aliasing happens

Other than regular, fixed sampling pattern, sampling can also be stochastic (a.k.a., random, probabilistic, or Monte Carlo)

Durando8

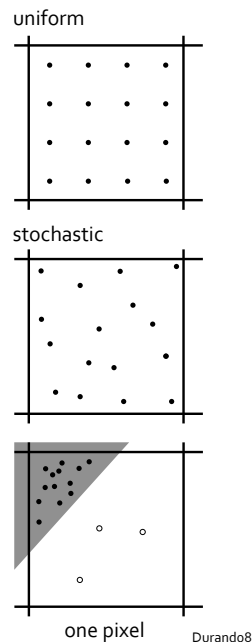
# Stochastic Supersampling

Samples taken at non-uniformly spaced random offsets

Replaces low-frequency aliasing pattern by **noise**, which is less objectionable to humans

However, with random sampling, we could get unlucky, e.g., all samples in one corner

- over 80% of the samples are black while the pixel should be light grey



Durando8

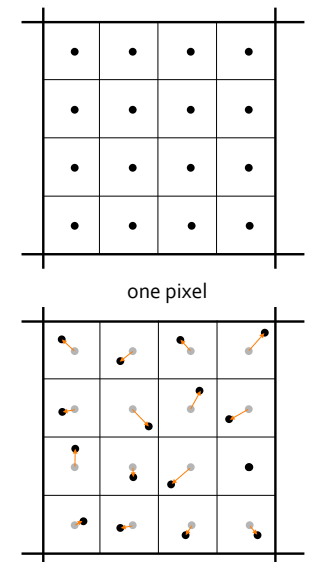
# Stratified Sampling

To prevent clustering of the random samples, divide domain (pixel) into non-overlapping regions (sub-pixels) called **strata**

Take one random sample per stratum

**Jittered sampling** is stratified sampling with per-stratum sample taken at an offset from the center of each stratum:

- one sample per stratum
- randomly perturb the sample location
- size of perturbation vector limited by the subpixel distance
- patented by Pixar!

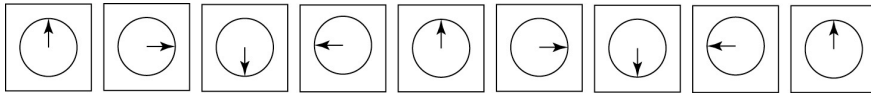


Durand

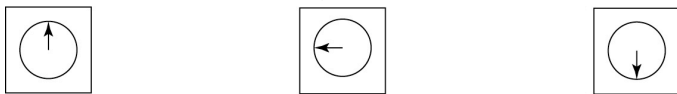
# Temporal Aliasing: Motion Blur

Aliasing happens in time as well as in space

- the sampling rate is the frame rate:  
30Hz (NTSC), 25Hz (PAL), 24Hz (film)
- if we point-sample time, objects have a jerky, strobed look, e.g., sampling at  $\frac{1}{4}$  rotation



- or move backward, e.g., sampled at  $\frac{3}{4}$  rotation



- see [http://www.michaelbach.de/ot/mot\\_wagonWheel/index.html](http://www.michaelbach.de/ot/mot_wagonWheel/index.html)
- fast moving objects move large distances between frames
- be careful when doing collision detection!

Curless, Hanrahan

# Temporal Aliasing: Motion Blur

Film automatically does temporal anti-aliasing

- photographic film integrates over the exposure time
- this shows up as **motion blur** in the photographs



Hodginso6, London et al.

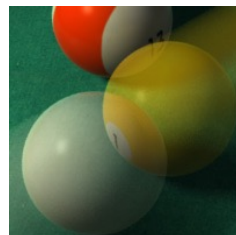
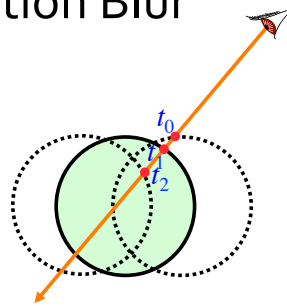
# Temporal Aliasing: Motion Blur

To avoid temporal aliasing we need to average over time also

Sample objects temporally

- cast multiple rays from eye through the same point in each pixel
- each of these rays intersects the scene at a different time:  $\mathbf{r}(\mathbf{e}, \mathbf{d}, t)$
- average out results

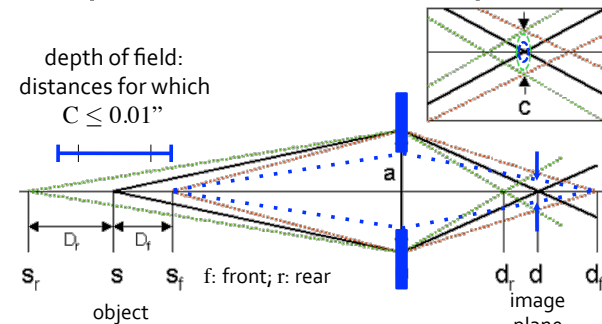
The result is still-frame motion blur and smooth animation



Hodginso6, Durando8, Merrello8

# Depth of Field and Aperture

depth of field:  
distances for which  
 $C \leq 0.01''$

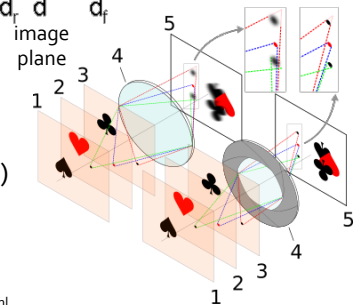


Thin lens equation  
 $1/s + 1/d = 1/f$   
where  $f$  is lens  
focal length

$a$  = aperture  
 $C$  = circle of  
confusion

Object is **considered in focus** if on an  $8 \times 10$  print viewed at a distance of  $10''$ , diameter of  $C \leq 0.01''$  (1930's standard!)

Later human study shows that  $C$  should be  $\leq 0.003''$



normankoren.com/Tutorials/MTF6.html

# Depth of Field

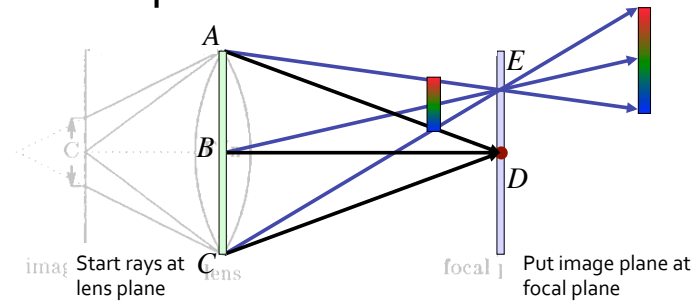
- Real cameras have lenses with focal lengths
- only one plane is truly in focus
  - points away from the focus project as "circle of confusion"
  - the further away from the focus the larger the circle

The range of distances that appear in focus is the **depth of field**

- smaller apertures (larger f-numbers) result in greater depth of field

Depth of field can be simulated by distributing primary rays through different parts of a lens assembly

# DoF: Implementation



## Standard ray tracing:

- all rays emanate from  $B$
- pixel  $D$  uses ray  $BD$
- pixel  $E$ , for object behind (or in front of) the focal plane, uses ray  $BE$

## Distributed ray tracing:

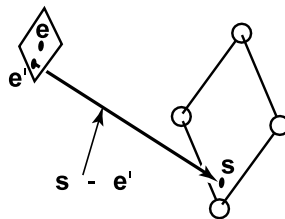
- rays emanate from lens plane
- pixel  $D$  uses rays  $AD, BD, CD$
- pixel  $E$  averages rays  $AE, BE, CE$
- to simulate more accurately, first refract primary rays through lens

Harto8

Harto8

# DoF: Implementation

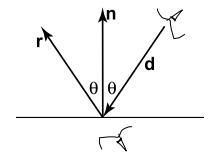
Or simply select eye positions randomly from a square region



/Shirley02

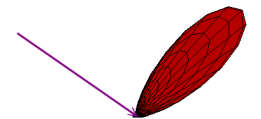
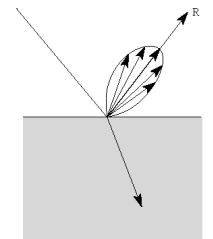
# Glossy Surfaces

Ray tracing simulates perfect specular reflection, true only for perfect mirrors and chrome surfaces



Most surfaces are imperfect specular reflectors:

- surface microfacets perturb direction of reflected rays
- reflect rays in a cone around perfect reflection direction
- Phong specular lighting tries to fake this with the  $m_{shi}$  exponent

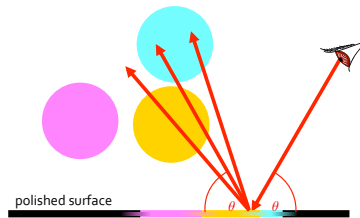
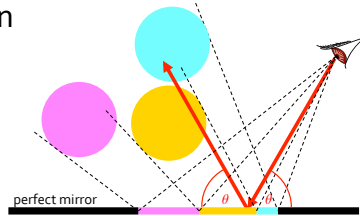


KIK,TP3

# Glossy Reflections: Implementation

For each ray-object intersection

- instead of shooting one ray in the perfect specular reflection (mirror) direction,
- stochastically sample **multiple rays within the cone** about the specular angle
- strength of reflection drops off rapidly away from the specular angle,
- probability of sampling that direction should fall off similarly

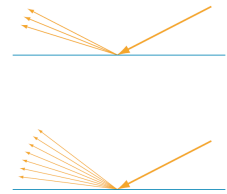


Harto8, Yuo8, Durando8

# Glossy Reflections

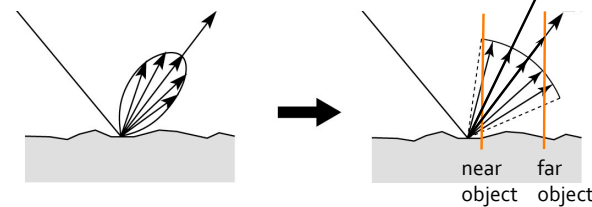
Instead of mirror images:

- highlights can be soft
- blurred reflections of objects

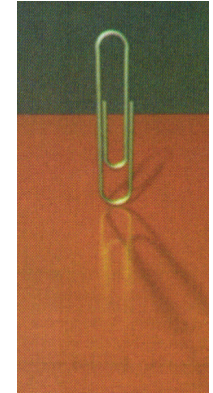


Nearby objects reflect more clearly because distribution still narrow

Farther objects reflect more blurry because distribution has spread



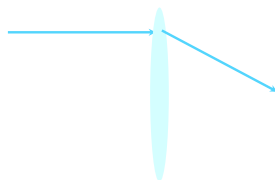
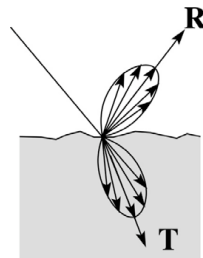
RTR, Curlessog, Harto8



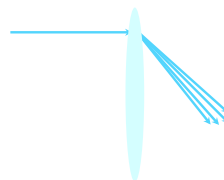
# Translucency

Similar, but for refraction

- instead of distributing rays around the reflection ray, distribute them around the refracted ray



Transparent

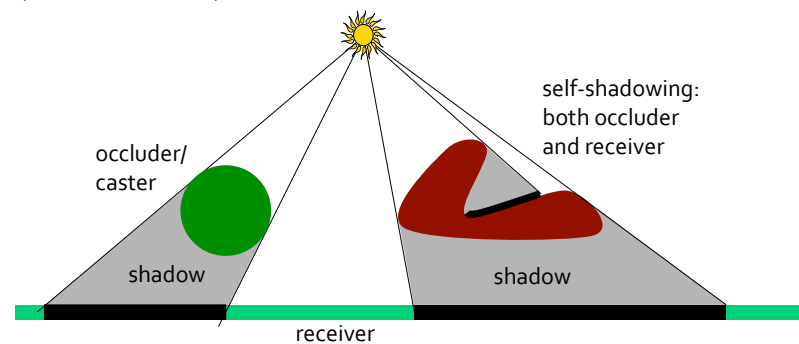


Translucent

Merello8, Curlesso8

# Shadows

Darkness caused when part or all of the illumination from a light source is blocked by an occluder (shadow caster)



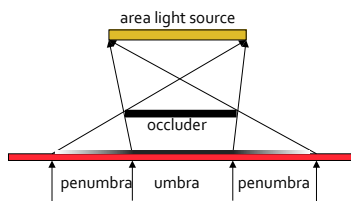
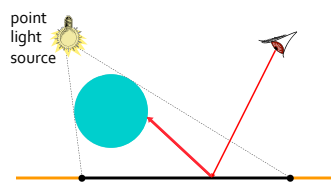
Akenine-...

# Hard and Soft Shadows

Point light sources give unrealistic hard shadows

Light sources that extend over an area (area light sources) cast soft-edged shadows

- some points see all the light: fully illuminated
- some points see none of the light source: the umbra
- some points see part of the light source: the penumbra

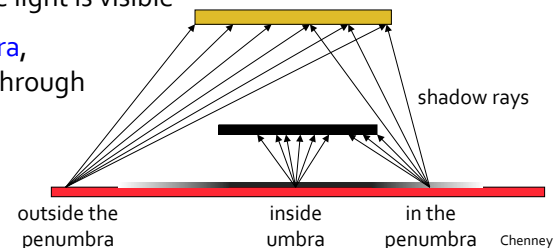


Durand,Chenney

# Ray Tracing Area Light Source to Create Soft Shadows

Cast multiple shadow rays from surface, distributed across the surface of the light: each ray to a different point on the light source

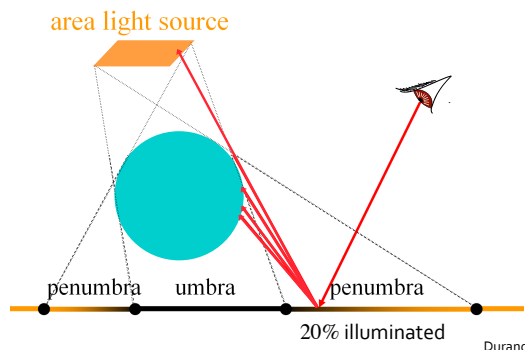
- inside the umbra, no shadow rays get through to light
- inside the penumbra, some shadow rays get through and some parts of the are light is visible
- outside the penumbra, all shadow rays get through



Chenney

# Ray Tracing Area Light Source to Create Soft Shadows

At each point, sum the contributions of shadow rays from that point to find the strength of shadow: hits/rays = % illuminated

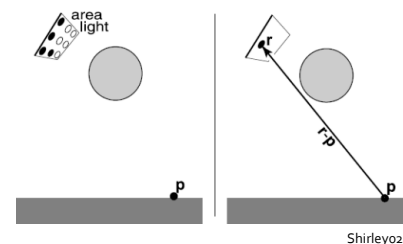


Durand

# Sampling Area Light

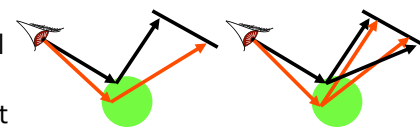
Anti-aliasing:

- break a pixel into a grid of sub-pixels and distribute rays over the sub-pixels



Soft-shadows:

- break an area light into a grid of  $N = n \times n$  point lights, each with  $1/N$ -th the intensity of the base light
- sample the light, not the pixel
- each primary ray generates multiple shadow rays per light



# Classic Recursive Ray Tracing

```
render() {
  for each pixel {
    generate primary/viewing ray
    pixel_color = trace(primary_ray)
  }
}
```

```
trace(ray) {
  (point, normal) = ray.intersect(scene);
  return shade(point, normal)
}

shade(pt, normal) {
  color = 0
  for each light source {
    if(!intersect(shadow_ray, scene))
      color += direct_illumination
  }
  if(specular)
    color += F * trace(reflected_ray)
  // also add transmitted color...
  return color
}
```

# Distributed Area-Light Sampling

```
render() {
  for each pixel {
    generate primary/viewing ray
    pixel_color = trace(primary_ray)
  }
}
```

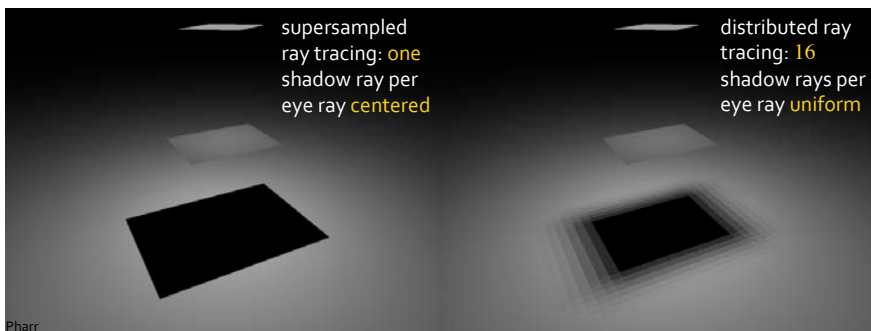
```
trace(ray) {
  (point, normal) = ray.intersect(scene);
  return shade(point, normal)
}

shade(pt, normal) {
  color = 0
  for each light source {
    generate N random shadow rays
    foreach (shadow ray) {
      if(!intersect(shadow_ray, scene))
        color += direct_illumination*1/N
    }
  }
  if(specular)
    color += F * trace(reflected_ray)
  // also add transmitted color...
  return color
}
```

## Sample Distribution?

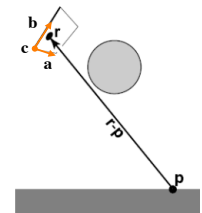
Uniform distribution gives rise to sharp transitions/patterns inside penumbra

4 eye rays per pixel in both cases:

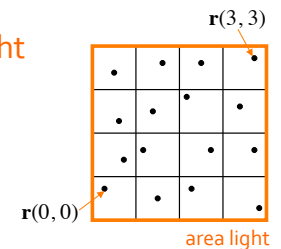


## Stochastic Sampling of Area Light

Area light represented as a rectangle in 3D, each ray-object intersection samples the area-light at random:  $\mathbf{r} = \mathbf{c} + \xi_1 \mathbf{a} + \xi_2 \mathbf{b}$ , where  $\xi_1$  and  $\xi_2$  are random variables



Stratified sampling of the area light with samples spaced uniformly plus a small perturbation  $\{ \mathbf{r}(i, j), 0 \leq i, j \leq n-1 \}$



# Sampling Rate

As with stochastic super-sampling for anti-aliasing, light sampling rate must be high, otherwise high-frequency noise becomes visible

