



## **Supervised Segmentation**



### Contributions



- 1. First deep end-to-end non-parametric segmentation
- 2. First deep unsupervised semantic segmentation
- 3. Interpretability from retrieved segments

# SegSort: Unified Metric Learning Framework for Segmentation



- von-Mises Fisher distribution:
- Single MLE objective:
- Optimize in a two-stage EM:

### **Pixel Sorting: Partition Each Image**

- Update  $\mathcal{Z}$ :  $p(z_i)$ • Update  $\Theta: \hat{\mu}_c =$



SegSort: Segmentation by Discriminative Sorting of Segments Jyh-Jing Hwang, Stella X. Yu, Jianbo Shi, Maxwell D. Collins, Tien-Ju Yang, Xiao Zhang, Liang-Chieh Chen

segment sorting loss

• Basic idea: Assuming independent normal distributions for individual segments, we seek a maximum likelihood estimation of the feature mapping  $\mathcal{V}$ , so that the feature induced partitioning  $\mathcal{Z}$  in the image and  $\Theta$ clustering across images provide maximum discrimination among segments.

$$f(\boldsymbol{v} \mid \boldsymbol{\mu}, \kappa) = C_d(\kappa) \exp(\kappa \boldsymbol{\mu}^\top \boldsymbol{v})$$
  
$$\min_{\phi, \mathcal{Z}, \Theta} - \log P(\mathcal{V}, \mathcal{Z} \mid \Theta) = \min_{\phi, \mathcal{Z}, \Theta} - \sum_i \log f_{z_i}(\boldsymbol{v}_i \mid \theta_{z_i})$$
  
$$[\mathcal{Z} \heartsuit \Theta] \diamondsuit \mathcal{V}$$

• EM for K-mean clustering based on  $\mathcal{V}$  for each image • Unsupervised vMF Loss:

$$= s | \boldsymbol{v}_i, \Theta) = \frac{f_s(\boldsymbol{v}_i \mid \Theta)}{\sum_{l=1}^k f_l(\boldsymbol{v}_l \mid \Theta)}$$
$$= \frac{\sum_i \boldsymbol{v}_i p(z_i = c \mid \boldsymbol{v}_i, \Theta)}{||\sum_i \boldsymbol{v}_i p(z_i = c \mid \boldsymbol{v}_i, \Theta)||} = \frac{\sum_{i \in \mathcal{R}_c} \boldsymbol{v}_i}{||\sum_{i \in \mathcal{R}_c} \boldsymbol{v}_i||}$$

• Alternative for unsupervised semantic segmentation:

#### Segment Sorting: Organize All Segments

- > Maximize discrimination among segments.

$$L_{\text{vMF}}^{i} = -\log p_{\phi}(c \mid \boldsymbol{v}_{i}, \Theta) = -\log \frac{\exp(\kappa \boldsymbol{\mu}_{c}^{\top} \boldsymbol{v}_{i})}{\sum_{l=1}^{k} \exp(\kappa \boldsymbol{\mu}_{l}^{\top} \boldsymbol{v}_{i})}$$

- Supervised vMF-NCA Loss:
- > Maximize discrimination between *different-class* segments.

$$L_{ ext{vMF-N}}^{i} = -\log \sum_{s \in C_{i}^{+}} p_{\phi}'(z_{i} = s \mid \boldsymbol{v}_{i}, \Theta) = -\log rac{\sum_{s \in C_{i}^{+}} p_{\phi}'(z_{i} = s \mid \boldsymbol{v}_{i}, \Theta)}{\sum_{l \in C_{i}^{+}} p_{\phi}'(z_{l} = s \mid \boldsymbol{v}_{l}, \Theta)} = -\log rac{\sum_{s \in C_{i}^{+}} p_{\phi}'(z_{i} = s \mid \boldsymbol{v}_{i}, \Theta)}{\sum_{l \in C_{i}^{+}} p_{\phi}'(z_{l} = s \mid \boldsymbol{v}_{i}, \Theta)} = -\log rac{\sum_{s \in C_{i}^{+}} p_{\phi}'(z_{i} = s \mid \boldsymbol{v}_{i}, \Theta)}{\sum_{l \in C_{i}^{+}} p_{\phi}'(z_{i} = s \mid \boldsymbol{v}_{i}, \Theta)} = -\log rac{\sum_{s \in C_{i}^{+}} p_{\phi}'(z_{i} = s \mid \boldsymbol{v}_{i}, \Theta)}{\sum_{s \in C_{i}^{+}} p_{\phi}'(z_{i} = s \mid \boldsymbol{v}_{i}, \Theta)} = -\log rac{\sum_{s \in C_{i}^{+}} p_{\phi}'(z_{i} = s \mid \boldsymbol{v}_{i}, \Theta)}{\sum_{s \in C_{i}^{+}} p_{\phi}'(z_{i} = s \mid \boldsymbol{v}_{i}, \Theta)} = -\log rac{\sum_{s \in C_{i}^{+}} p_{\phi}'(z_{i} = s \mid \boldsymbol{v}_{i}, \Theta)}{\sum_{s \in C_{i}^{+}} p_{\phi}'(z_{i} = s \mid \boldsymbol{v}_{i}, \Theta)} = -\log rac{\sum_{s \in C_{i}^{+}} p_{\phi}'(z_{i} = s \mid \boldsymbol{v}_{i}, \Theta)}{\sum_{s \in C_{i}^{+}} p_{\phi}'(z_{i} = s \mid \boldsymbol{v}_{i}, \Theta)} = -\log rac{\sum_{s \in C_{i}^{+}} p_{\phi}'(z_{i} = s \mid \boldsymbol{v}_{i}, \Theta)}{\sum_{s \in C_{i}^{+}} p_{\phi}'(z_{i} = s \mid \boldsymbol{v}_{i}, \Theta)} = -\log \frac{\sum_{s \in C_{i}^{+}} p_{\phi}'(z_{i} = s \mid \boldsymbol{v}_{i}, \Theta)}{\sum_{s \in C_{i}^{+}} p_{\phi}'(z_{i} = s \mid \boldsymbol{v}_{i}, \Theta)} = -\log \frac{\sum_{s \in C_{i}^{+}} p_{\phi}'(z_{i} = s \mid \boldsymbol{v}_{i}, \Theta)}{\sum_{s \in C_{i}^{+}} p_{\phi}'(z_{i} = s \mid \boldsymbol{v}_{i}, \Theta)} = -\log \frac{\sum_{s \in C_{i}^{+}} p_{\phi}'(z_{i} = s \mid \boldsymbol{v}_{i}, \Theta)}{\sum_{s \in C_{i}^{+}} p_{\phi}'(z_{i} = s \mid \boldsymbol{v}_{i}, \Theta)}$$

• Memory bank caching segment prototypes across batches.

# Penn :

#### **Unsupervised Segmentation**

clustering

predictions

V 2 AV \* S

 $\sum_{i \in C_i^+} \exp(\kappa oldsymbol{\mu}_s^+ oldsymbol{v}_i)$  $\boldsymbol{u}_{l \neq c} \exp(\kappa \boldsymbol{\mu}_l^\top \boldsymbol{v}_i)$