

# EECS 583 – Class 10

## ILP Optimization and Intro. to Code Generation

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*University of Michigan*

*February 8, 2023*

# Announcements & Reading Material

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- ❖ Reminder: HW 2
  - » Due next Wednes, You should have started by now
  - » Talk to Aditya if you are stuck
- ❖ Class project
  - » Project team formation and general topic area
- ❖ Today's class
  - » “Machine Description Driven Compilers for EPIC Processors”, B. Rau, V. Kathail, and S. Aditya, HP Technical Report, HPL-98-40, 1998. (long paper but informative)
- ❖ Next class
  - » “The Importance of Prepass Code Scheduling for Superscalar and Superpipelined Processors,” P. Chang et al., IEEE Transactions on Computers, 1995, pp. 353-370.

# Class Problem From Last Time – Readable Solution

Assume:  $+$  = 1,  $*$  = 3

operand	0	0	0	1	2	0
arrival times	r1	r2	r3	r4	r5	r6

1.  $r10 = r1 * r2$
2.  $r11 = r10 + r3$
3.  $r12 = r11 + r4$
4.  $r13 = r12 - r5$
5.  $r14 = r13 + r6$

Back substitute

Re-express in tree-height reduced form

Account for latency and arrival times

Expression after back substitution

$$r14 = r1 * r2 + r3 + r4 - r5 + r6$$

Want to perform operations on r1,r2,r3,r6 first due to operand arrival times

$$t1 = r1 * r2$$

$$t2 = r3 + r6$$

The multiply will take 3 cycles, so combine t2 with r4 and then r5, and then finally t1

$$t3 = t2 + r4$$

$$t4 = t3 - r5$$

$$r14 = t1 + t4$$

Equivalently, the fully parenthesized expression  
 $r14 = ((r1 * r2) + (((r3 + r6) + r4) - r5))$

# From Last Time: Loop Unrolling

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```
for (i=x; i< 100; i++) {  
    sum += a[i]*b[i];  
}
```

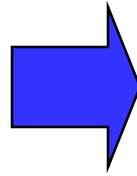


```
loop:  r1 = load(r2)  
       r3 = load(r4)  
       r5 = r1 * r3  
       r6 = r6 + r5  
       r2 = r2 + 4  
       r4 = r4 + 4  
       if (r4 < 400) goto loop
```

Unroll = replicate loop body  
n-1 times.

Hope to enable overlap of  
operation execution from  
different iterations

unroll 3 times



```
loop:  r1 = load(r2)  
       r3 = load(r4)
```

```
       r5 = r1 * r3  
       r6 = r6 + r5
```

```
iter1  r2 = r2 + 4  
       r4 = r4 + 4
```

```
       if (r4 >= 400) goto exit
```

```
       r1 = load(r2)  
       r3 = load(r4)
```

```
iter2  r5 = r1 * r3  
       r6 = r6 + r5
```

```
       r2 = r2 + 4  
       r4 = r4 + 4
```

```
       if (r4 >= 400) goto exit
```

```
       r1 = load(r2)  
       r3 = load(r4)
```

```
iter3  r5 = r1 * r3  
       r6 = r6 + r5
```

```
       r2 = r2 + 4  
       r4 = r4 + 4
```

```
       if (r4 < 400) goto loop
```

```
exit:
```

# Smarter Loop Unrolling with Known Trip Count

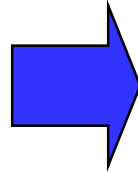
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Want to remove early exit branches

Trip count =  $400/4 = 100$

```
    r4 = 0
loop: r1 = load(r2)
      r3 = load(r4)
      r5 = r1 * r3
      r6 = r6 + r5
      r2 = r2 + 4
      r4 = r4 + 4
      if (r4 < 400) goto loop
```

unroll multiple  
of trip count



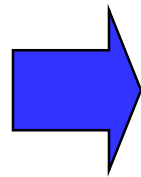
```
loop: r1 = load(r2)
      r3 = load(r4)
      r5 = r1 * r3
      r6 = r6 + r5
      r2 = r2 + 4
      r4 = r4 + 4
-----
      r1 = load(r2)
      r3 = load(r4)
      r5 = r1 * r3
      r6 = r6 + r5
      r2 = r2 + 4
      r4 = r4 + 4
-----
      r1 = load(r2)
      r3 = load(r4)
      r5 = r1 * r3
      r6 = r6 + r5
      r2 = r2 + 4
      r4 = r4 + 4
-----
      r1 = load(r2)
      r3 = load(r4)
      r5 = r1 * r3
      r6 = r6 + r5
      r2 = r2 + 4
      r4 = r4 + 4
      if (r4 < 400) goto loop
exit:
```

# What if the Trip Count is not Statically Known?

---

```
loop:  r4 = ??  
      r1 = load(r2)  
      r3 = load(r4)  
      r5 = r1 * r3  
      r6 = r6 + r5  
      r2 = r2 + 4  
      r4 = r4 + 4  
      if (r4 < 400) goto loop
```

Create a preloop to  
ensure trip count of  
unrolled loop is a multiple  
of the unroll factor

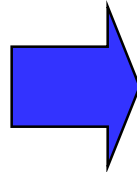


```
preloop  for (i=0; i< ((400-r4)/4)%3; i++) {  
          sum += a[i]*b[i];  
        }  
  
loop:    r1 = load(r2)  
        r3 = load(r4)  
iter1    r5 = r1 * r3  
        r6 = r6 + r5  
        r2 = r2 + 4  
        r4 = r4 + 4  
        -----  
        r1 = load(r2)  
        r3 = load(r4)  
iter2    r5 = r1 * r3  
        r6 = r6 + r5  
        r2 = r2 + 4  
        r4 = r4 + 4  
        -----  
        r1 = load(r2)  
        r3 = load(r4)  
iter3    r5 = r1 * r3  
        r6 = r6 + r5  
        r2 = r2 + 4  
        r4 = r4 + 4  
        if (r4 < 400) goto loop  
  
exit:
```

# Unrolling Not Enough for Overlapping Iterations: Register Renaming

---

```
loop: r1 = load(r2)
      r3 = load(r4)
      r5 = r1 * r3
iter1  r6 = r6 + r5
      r2 = r2 + 4
      r4 = r4 + 4
-----
      r1 = load(r2)
      r3 = load(r4)
      r5 = r1 * r3
iter2  r6 = r6 + r5
      r2 = r2 + 4
      r4 = r4 + 4
-----
      r1 = load(r2)
      r3 = load(r4)
      r5 = r1 * r3
iter3  r6 = r6 + r5
      r2 = r2 + 4
      r4 = r4 + 4
      if (r4 < 400) goto loop
```



```
loop: r1 = load(r2)
      r3 = load(r4)
      r5 = r1 * r3
iter1  r6 = r6 + r5
      r2 = r2 + 4
      r4 = r4 + 4
-----
      r11 = load(r2)
      r13 = load(r4)
      r15 = r11 * r13
iter2  r6 = r6 + r15
      r2 = r2 + 4
      r4 = r4 + 4
-----
      r21 = load(r2)
      r23 = load(r4)
      r25 = r21 * r23
iter3  r6 = r6 + r25
      r2 = r2 + 4
      r4 = r4 + 4
      if (r4 < 400) goto loop
```

# Register Renaming is Not Enough!

---

```
loop: r1 = load(r2)
      r3 = load(r4)
      r5 = r1 * r3
iter1  r6 = r6 + r5
      r2 = r2 + 4
      r4 = r4 + 4
-----
      r11 = load(r2)
      r13 = load(r4)
      r15 = r11 * r13
iter2  r6 = r6 + r15
      r2 = r2 + 4
      r4 = r4 + 4
-----
      r21 = load(r2)
      r23 = load(r4)
      r25 = r21 * r23
iter3  r6 = r6 + r25
      r2 = r2 + 4
      r4 = r4 + 4
      if (r4 < 400) goto loop
```

- ❖ Still not much overlap possible
- ❖ Problems
  - » r2, r4, r6 sequentialize the iterations
  - » Need to rename these
- ❖ 2 specialized renaming optis
  - » Accumulator variable expansion (r6)
  - » Induction variable expansion (r2, r4)



# Accumulator Variable Expansion

---

```

    r16 = r26 = 0
loop: r1 = load(r2)
        r3 = load(r4)
        r5 = r1 * r3
iter1  r6 = r6 + r5
        r2 = r2 + 4
        r4 = r4 + 4
        -----
        r11 = load(r2)
        r13 = load(r4)
        r15 = r11 * r13
iter2  r16 = r16 + r15
        r2 = r2 + 4
        r4 = r4 + 4
        -----
        r21 = load(r2)
        r23 = load(r4)
        r25 = r21 * r23
iter3  r26 = r26 + r25
        r2 = r2 + 4
        r4 = r4 + 4
        if (r4 < 400) goto loop
    r6 = r6 + r16 + r26
```

- ❖ Accumulator variable
  - »  $x = x + y$  or  $x = x - y$
  - » where  $y$  is loop variant!!
- ❖ Create  $n-1$  temporary accumulators
- ❖ Each iteration targets a different accumulator
- ❖ Sum up the accumulator variables at the end
- ❖ May not be safe for floating-point values

# Induction Variable Expansion

---

```
    r12 = r2 + 4, r22 = r2 + 8
    r14 = r4 + 4, r24 = r4 + 8
    r16 = r26 = 0
loop: r1 = load(r2)
      r3 = load(r4)
      r5 = r1 * r3
iter1  r6 = r6 + r5
      r2 = r2 + 12
      r4 = r4 + 12
      -----
      r11 = load(r12)
      r13 = load(r14)
iter2  r15 = r11 * r13
      r16 = r16 + r15
      r12 = r12 + 12
      r14 = r14 + 12
      -----
      r21 = load(r22)
      r23 = load(r24)
iter3  r25 = r21 * r23
      r26 = r26 + r25
      r22 = r22 + 12
      r24 = r24 + 12
      if (r4 < 400) goto loop
```

---

r6 = r6 + r16 + r26

- ❖ Induction variable
  - »  $x = x + y$  or  $x = x - y$
  - » where  $y$  is loop invariant!!
- ❖ Create  $n-1$  additional induction variables
- ❖ Each iteration uses and modifies a different induction variable
- ❖ Initialize induction variables to  $\text{init}$ ,  $\text{init} + \text{step}$ ,  $\text{init} + 2 * \text{step}$ , etc.
- ❖ Step increased to  $n * \text{original step}$
- ❖ Now iterations are completely independent !!

# Better Induction Variable Expansion

---

```
    r16 = r26 = 0
loop: r1 = load(r2)
      r3 = load(r4)
      r5 = r1 * r3
iter1  r6 = r6 + r5

-----
      r11 = load(r2+4)
      r13 = load(r4+4)
iter2  r15 = r11 * r13
      r16 = r16 + r15

-----
      r21 = load(r2+8)
      r23 = load(r4+8)
iter3  r25 = r21 * r23
      r26 = r26 + r25
      r2 = r2 + 12
      r4 = r4 + 12
      if (r4 < 400) goto loop
      r6 = r6 + r16 + r26
```

- ❖ With base+displacement addressing, often don't need additional induction variables
  - » Just change offsets in each iterations to reflect step
  - » Change final increments to n \* original step

# Homework Problem

---

**loop:**

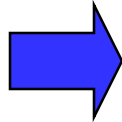
**r1 = load(r2)**

**r5 = r6 + 3**

**r6 = r5 + r1**

**r2 = r2 + 4**

**if (r2 < 400) goto loop**



**loop:**

**r1 = load(r2)**

**r5 = r6 + 3**

**r6 = r5 + r1**

**r2 = r2 + 4**

**r1 = load(r2)**

**r5 = r6 + 3**

**r6 = r5 + r1**

**r2 = r2 + 4**

**r1 = load(r2)**

**r5 = r6 + 3**

**r6 = r5 + r1**

**r2 = r2 + 4**

**if (r2 < 400) goto loop**

Optimize the unrolled  
loop

Renaming

Tree height reduction

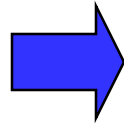
Ind/Acc expansion

# Homework Problem - Answer

---

loop:

```
r1 = load(r2)
r5 = r6 + 3
r6 = r5 + r1
r2 = r2 + 4
if (r2 < 400) goto loop
```



loop:

```
r1 = load(r2)
r5 = r6 + 3
r6 = r5 + r1
r2 = r2 + 4
r1 = load(r2)
r5 = r6 + 3
r6 = r5 + r1
r2 = r2 + 4
r1 = load(r2)
r5 = r6 + 3
r6 = r5 + r1
r2 = r2 + 4
if (r2 < 400)
    goto loop
```

loop:

```
r1 = load(r2)
r5 = r1 + 3
r6 = r6 + r5
r2 = r2 + 4
r11 = load(r2)
r15 = r11 + 3
r6 = r6 + r15
r2 = r2 + 4
r21 = load(r2)
r25 = r21 + 3
r6 = r6 + r25
r2 = r2 + 4
if (r2 < 400)
    goto loop
```

r16 = r26 = 0

loop:

```
r1 = load(r2)
r5 = r1 + 3
r6 = r6 + r5
r11 = load(r2+4)
r15 = r11 + 3
r16 = r16 + r15
r21 = load(r2+8)
r25 = r21 + 3
r26 = r26 + r25
r2 = r2 + 12
if (r2 < 400)
    goto loop
r6 = r6 + r16
r6 = r6 + r26
```

Optimize the unrolled  
loop

Renaming  
Tree height reduction  
Ind/Acc expansion

after renaming and  
tree height reduction

after acc and  
ind expansion

# Code Generation

---

- ❖ Map optimized “machine-independent” assembly to final assembly code
- ❖ Input code
  - » Classical optimizations
  - » ILP optimizations
  - » Formed regions (sbs, hbs), applied if-conversion (if appropriate)
- ❖ Virtual → physical binding
  - » 2 big steps
  - » 1. Scheduling
    - Determine when every operation executions
    - Create MultiOps (for VLIW) or reorder instructions (for superscalar)
  - » 2. Register allocation
    - Map virtual → physical registers
    - Spill to memory if necessary

# Scheduling Operations

---

- ❖ Need information about the processor
  - » Number of resources, latencies, encoding limitations
  - » For example:
    - 2 issue slots, 1 memory port, 1 adder/multiplier
    - load = 2 cycles, add = 1 cycle, mpy = 3 cycles; all fully pipelined
    - Each operand can be register or 6 bit signed literal
- ❖ Need ordering constraints amongst operations
  - » What order defines correct program execution?
- ❖ Given multiple operations that can be scheduled, how do you pick the best one?
  - » Is there a best one? Does it matter?
  - » Are decisions final?, or is this an iterative process?
- ❖ How do we keep track of resources that are busy/free
  - » Reservation table: Resources x time

# Schedule Before or After Register Allocation?

---

virtual registers

```
r1 = load(r10)  
r2 = load(r11)  
r3 = r1 + 4  
r4 = r1 - r12  
r5 = r2 + r4  
r6 = r5 + r3  
r7 = load(r13)  
r8 = r7 * 23  
store (r8, r6)
```

physical registers

```
R1 = load(R1)  
R2 = load(R2)  
R5 = R1 + 4  
R1 = R1 - R3  
R2 = R2 + R1  
R2 = R2 + R5  
R5 = load(R4)  
R5 = R5 * 23  
store (R5, R2)
```

Too many artificial ordering constraints if schedule after allocation!!!!

But, need to schedule after allocation to bind spill code

**Solution, do both! Prepass schedule, register allocation, postpass schedule**

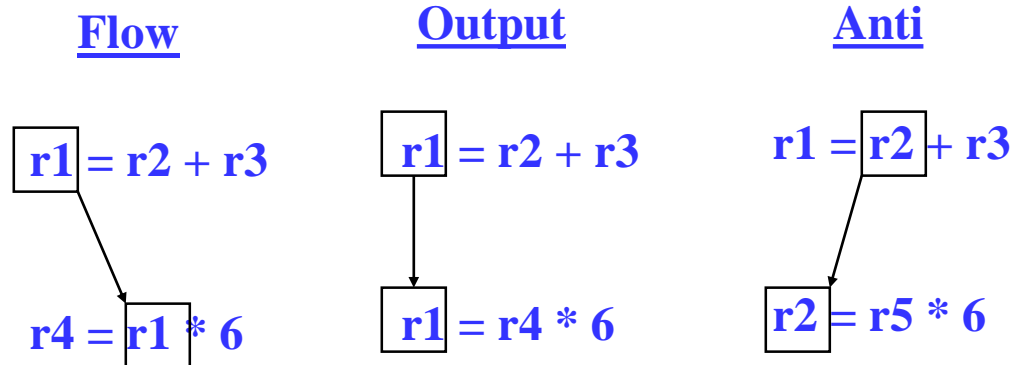


# Data Dependences

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## ❖ Data dependences

- » If 2 operations access the same register, they are dependent
- » However, only keep dependences to most recent producer/consumer as other edges are transitively redundant
- » Types of data dependences



# More Dependences

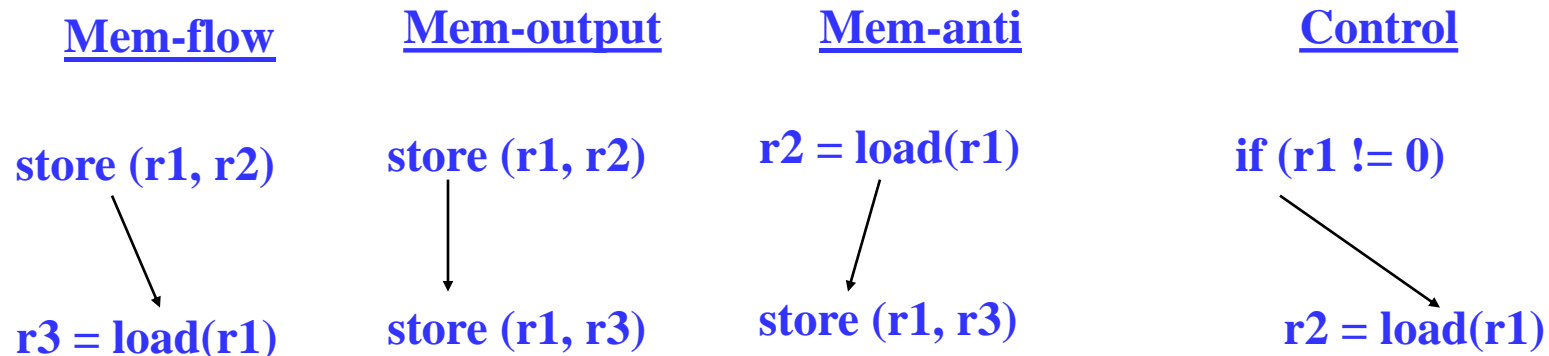
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## ❖ Memory dependences

- » Similar as register, but through memory
- » Memory dependences may be certain or maybe

## ❖ Control dependences

- » We discussed this earlier
- » Branch determines whether an operation is executed or not
- » Operation must execute after/before a branch



# Dependence Graph

---

- ❖ Represent dependences between operations in a block via a DAG

- » Nodes = operations/instructions
- » Edges = dependences

- ❖ Single-pass traversal required to insert dependences

- ❖ Example

**1: r1 = load(r2)**

**2: r2 = r1 + r4**

**3: store (r4, r2)**

**4: p1 = cmpp (r2 < 0)**

**5: branch if p1 to BB3**

**6: store (r1, r2)**

BB3:

①

②

③

④

⑤

⑥

# Dependence Graph - Solution

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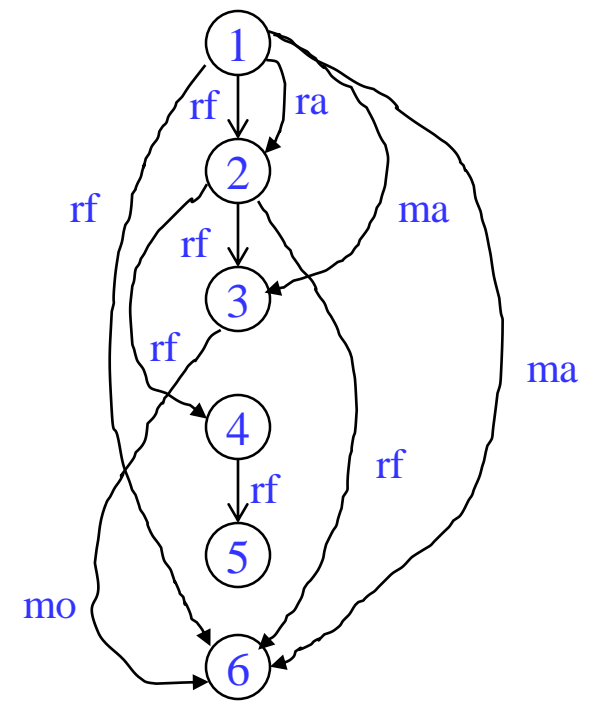
## ❖ Example

1: **r1 = load(r2)**  
2: **r2 = r1 + r4**  
3: **store (r4, r2)**  
4: **p1 = cmpp (r2 < 0)**  
5: **branch if p1 to BB3**  
6: **store (r1, r2)**

BB3:

Instructions 1-4 have  
control dependence to instruction 5

5 → 6 control dependence



# Dependence Edge Latencies

---

- ❖ Edge latency = minimum number of cycles necessary between initiation of the predecessor and successor in order to satisfy the dependence
- ❖ Register flow dependence,  $a = b + c \rightarrow d = a + 1$ 
  - » Latency of producer instruction for most processors
- ❖ Register anti dependence,  $a = b + c \rightarrow b = d + e$ 
  - » 0 cycles for most processors
- ❖ Register output dependence,  $a = b + c \rightarrow a = d + e$ 
  - » 1 cycle for most processors
- ❖ Is negative latency possible?
  - » Yes, means successor can start before predecessor
  - » We will only deal with latency  $\geq 0$

# Dependence Edge Latencies (2)

---

## ❖ Memory dependences

- » Store → load (memory flow)
- » Load → Store (memory anti)
- » Store → Store (memory output)
- » All 1 cycle for most processors

## ❖ Control dependences

- » branch → b
  - Instructions inside then/else paths dependent on branch
  - 1 cycle for most processors
- » a → branch
  - Op a must be issued before the branch completes
  - 0 cycles for most processors

# Class Problem – Add Latencies to Dependence Edges

---

latencies

add: 1  
cmpp: 1  
load: 2  
store: 1



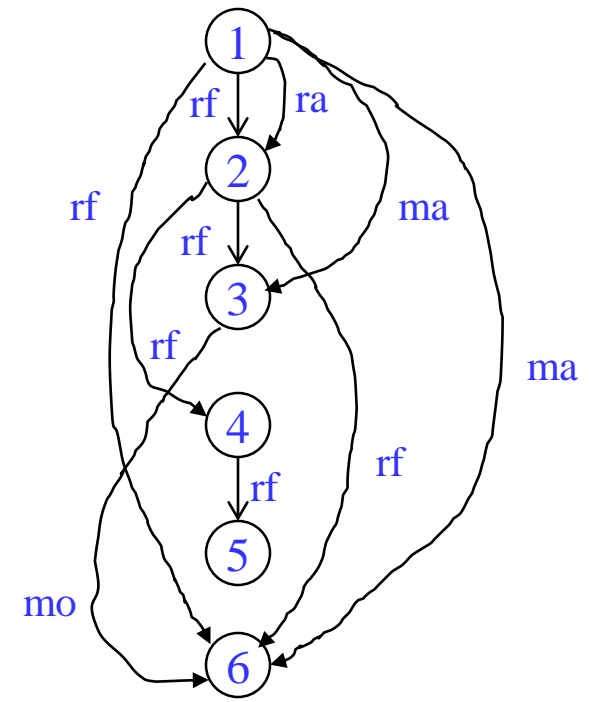
Example

**1: r1 = load(r2)**  
**2: r2 = r1 + r4**  
**3: store (r4, r2)**  
**4: p1 = cmpp (r2 < 0)**  
**5: branch if p1 to BB3**  
**6: store (r1, r2)**

BB3:

Instructions 1-4 have control dependence to instruction 5

5→6 control dependence



# Homework Problem 1 – Answer Next Time

---

machine model

latencies

add: 1  
mpy: 3  
load: 2  
store: 1

1. Draw dependence graph
2. Label edges with type and latencies

1.  $r1 = \text{load}(r2)$
2.  $r2 = r2 + 1$
3.  $\text{store}(r8, r2)$
4.  $r3 = \text{load}(r2)$
5.  $r4 = r1 * r3$
6.  $r5 = r5 + r4$
7.  $r2 = r6 + 4$
8.  $\text{store}(r2, r5)$

①

②

③

④

⑤

⑥

⑦

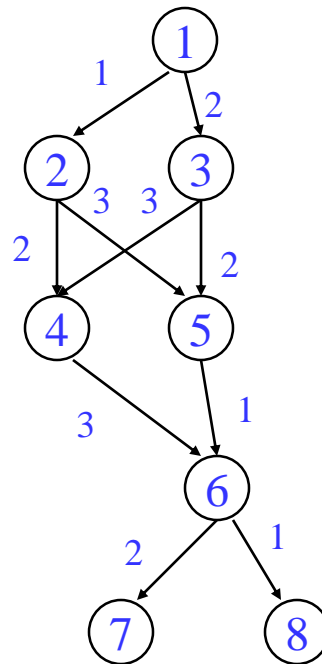
⑧



# Dependence Graph Properties - Estart

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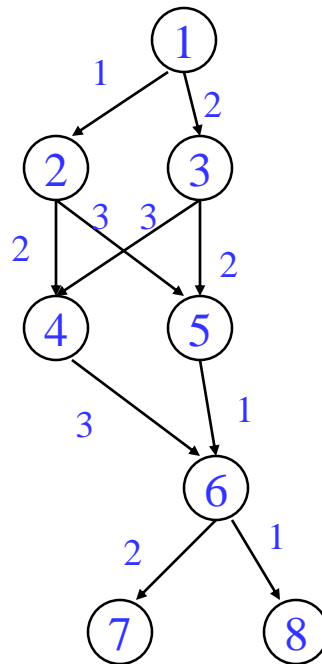
- ❖ Estart = earliest start time, (as soon as possible - ASAP)
  - » Schedule length with infinite resources (dependence height)
  - » Estart = 0 if node has no predecessors
  - » Estart = MAX(Estart(pred) + latency) for each predecessor node
  - » Example



# Lstart

---

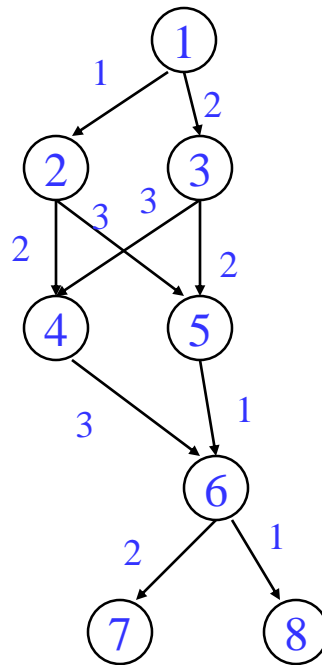
- ❖ Lstart = latest start time, ALAP
  - » Latest time a node can be scheduled s.t. sched length not increased beyond infinite resource schedule length
  - » Lstart = Estart if node has no successors
  - » Lstart = MIN(Lstart(succ) - latency) for each successor node
  - » Example



# Slack

---

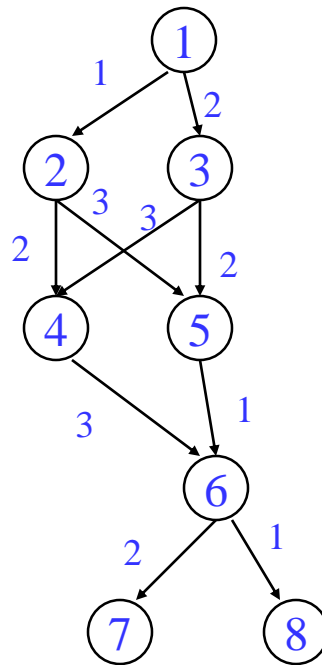
- ❖ Slack = measure of the scheduling freedom
  - »  $\text{Slack} = L_{\text{start}} - E_{\text{start}}$  for each node
  - » Larger slack means more mobility
  - » Example



# Critical Path

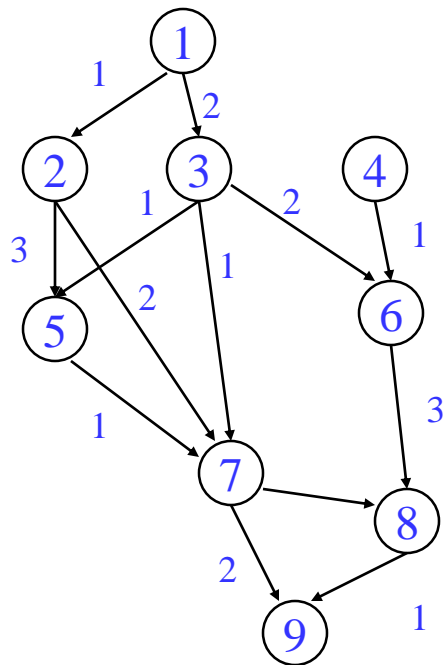
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- ❖ Critical operations = Operations with slack = 0
  - » No mobility, cannot be delayed without extending the schedule length of the block
  - » Critical path = sequence of critical operations from node with no predecessors to exit node, can be multiple crit paths



# Homework Problem 2 – Answer Next Time

---



Node	Estart	Lstart	Slack
------	--------	--------	-------

1			
---	--	--	--

2			
---	--	--	--

3			
---	--	--	--

4			
---	--	--	--

5			
---	--	--	--

6			
---	--	--	--

7			
---	--	--	--

8			
---	--	--	--

9			
---	--	--	--

Critical path(s) =