EECS 583 – Class 2
Control Flow Analysis

University of Michigan

August 30, 2023

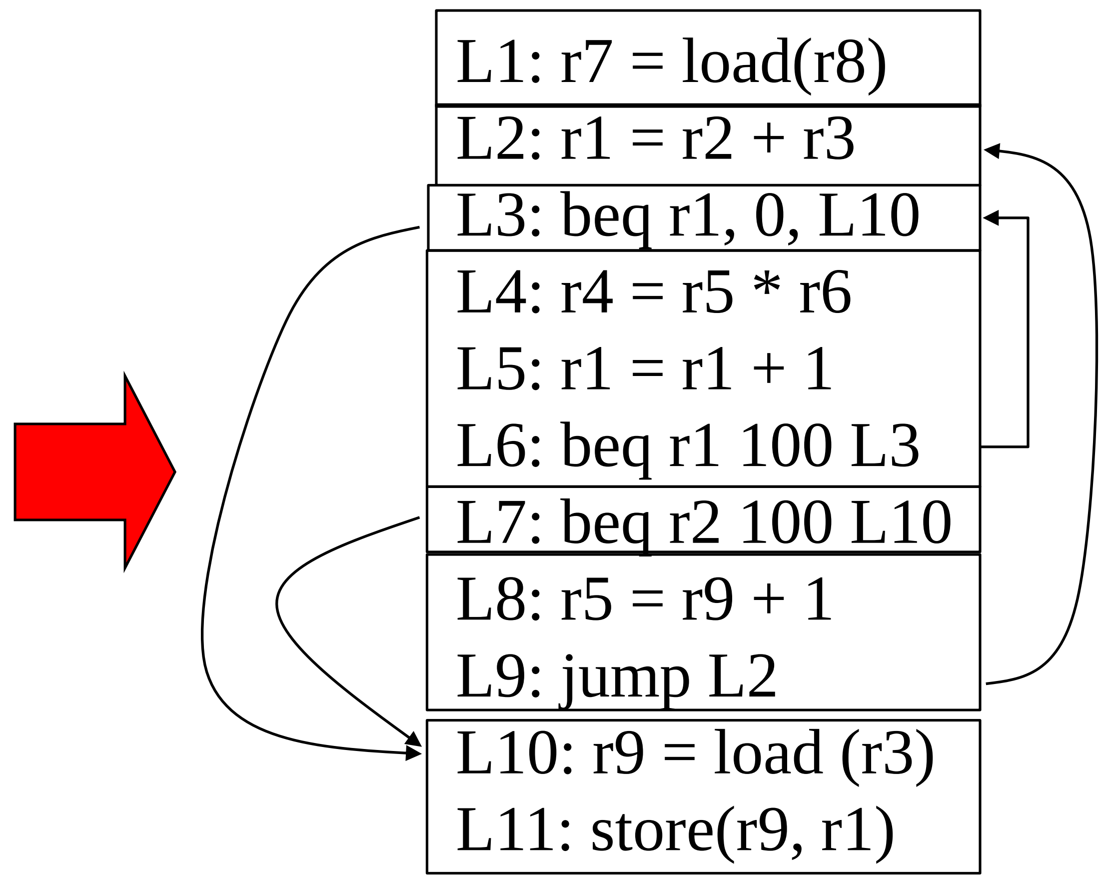
https://web.eecs.umich.edu/~mahlke/courses/583f23

Announcements & Reading Material

- eecs583a,eecs583b.eecs.umich.edu servers are ready
  - Everyone has home directory and login
- HW 0 – Due Next Monday, but nothing to turn in
  - Please get this done ASAP, talk to Aditya/Tarun if you have problems
  - Needed for HW 1 which goes out next Friday
  - Go to http://llvm.org
  - Detailed instructions on piazza, see Aditya's post
- Reading
  - Today's class
    - Ch 9.4, 10.4 (6.6, 9.6) from Compilers: Principles, Techniques Tools Ed 1 (Ed 2)
  - Next class
    - "Trace Selection for Compiling Large C Applications to Microcode", Chang and Hwu, MICRO-21, 1988.
    - "The Superblock: An Effective Technique for VLIW and Superscalar Compilation", Hwu et al., Journal of Supercomputing, 1993

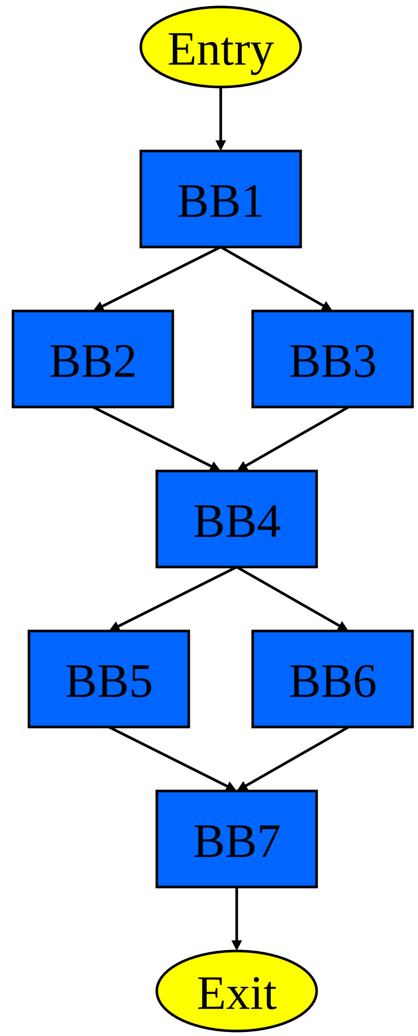
From Last Time: Identifying BBs - Answer

L1: r7 = load(r8)
L2: r1 = r2 + r3
L3: beq r1, 0, L10
L4: r4 = r5 * r6
L5: r1 = r1 + 1
L6: beq r1 100 L3
L7: beq r2 100 L10
L8: r5 = r9 + 1
L9: jump L2
L10: r9 = load (r3)
L11: store(r9, r1)



From Last Time: Control Flow Graph (CFG)

- Defn Control Flow Graph – Directed graph, G = (V,E) where each vertex V is a basic block and there is an edge E, v1 (BB1) → v2 (BB2) if BB2 can immediately follow BB1 in some execution sequence
  - A BB has an edge to all blocks it can branch to
  - Standard representation used by many compilers
  - Often have 2 pseudo vertices
    - entry node
    - exit node

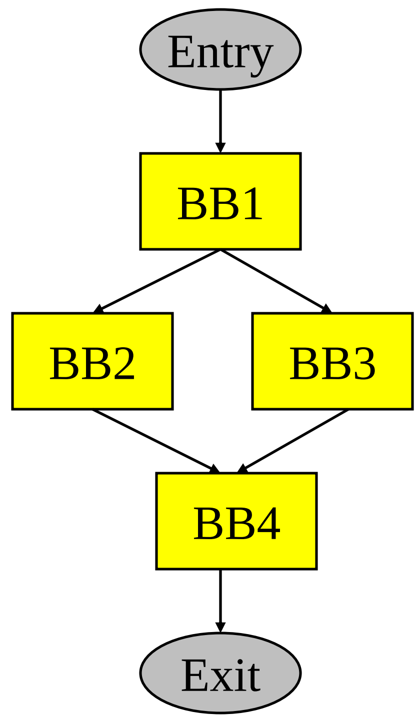


Property of CFGs: Dominator (DOM)

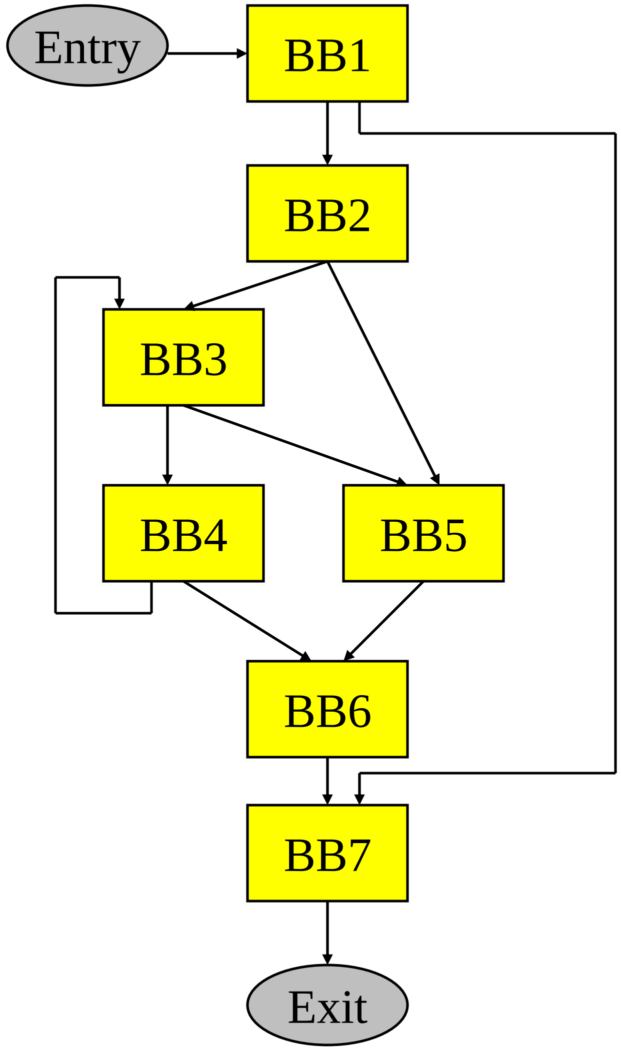
- Defn: Dominator – Given a CFG(V, E, Entry, Exit), a node x dominates a node y, if every path from the Entry block to y contains x
- 3 properties of dominators
  - Each BB dominates itself
  - If x dominates y, and y dominates z, then x dominates z
  - If x dominates z and y dominates z, then either x dominates y or y dominates x
- Intuition
  - Given some BB, which blocks are guaranteed to have executed prior to executing the BB

Dominator Example 1

Compute Dom(BBi) = set of blocks that dominate BBi



Dominator Example 2

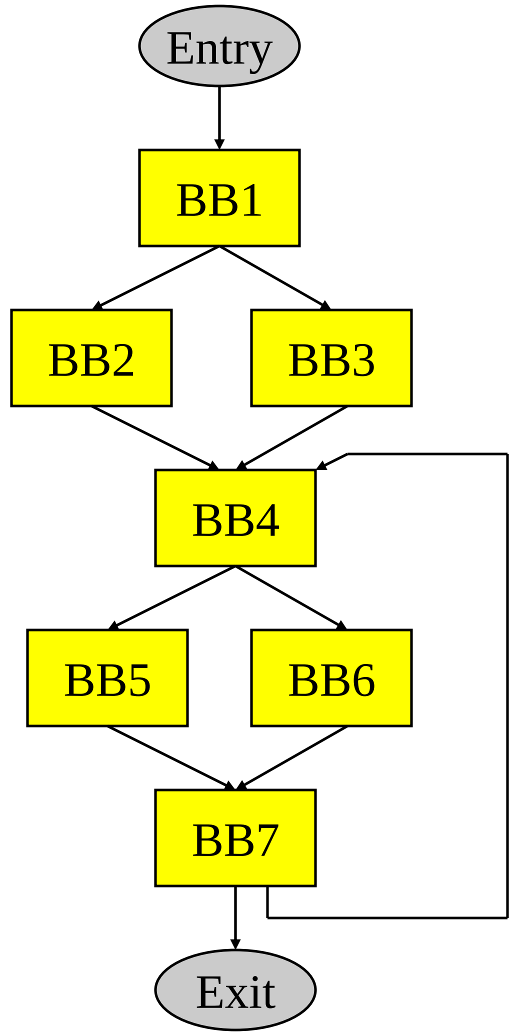


Dominator Analysis

- Compute dom(BBi) = set of BBs that dominate BBi
- Initialization
  - Dom(entry) = entry
  - Dom(everything else) = all nodes
- Iterative computation
  - while change, do
    - change = false
    - for each BB (except the entry BB)
      - tmp(BB) = BB + {intersect of Dom of all predecessor BB's}
      - if (tmp(BB) != dom(BB))

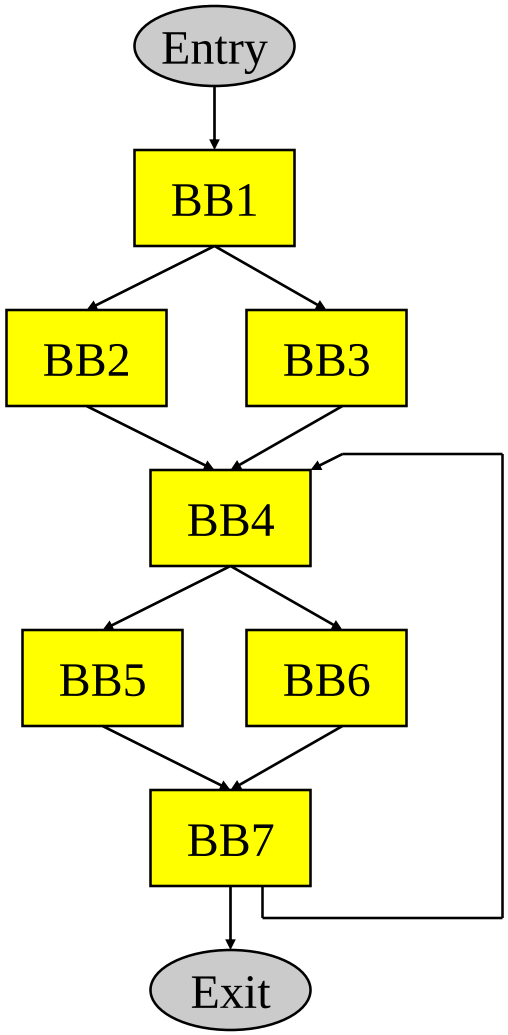
        dom(BB) = tmp(BB)

        change = true



Immediate Dominator

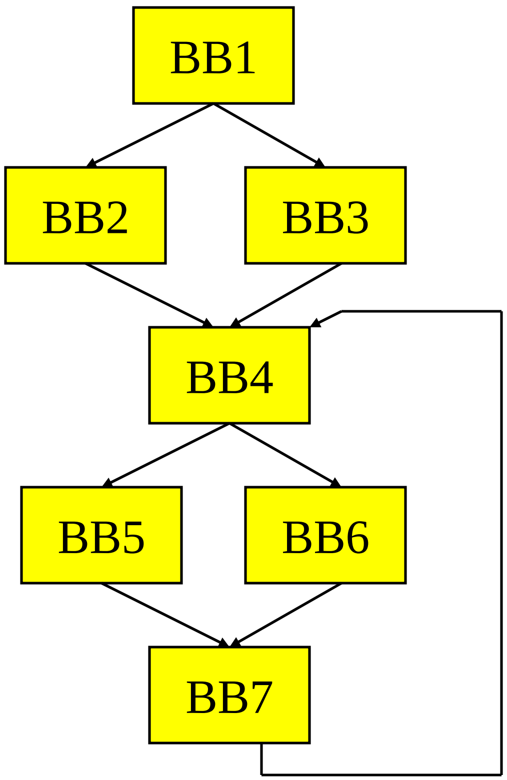
- Defn: Immediate dominator (idom) – Each node n has a unique immediate dominator m that is the last dominator of n on any path from the initial node to n
  - Closest node that dominates

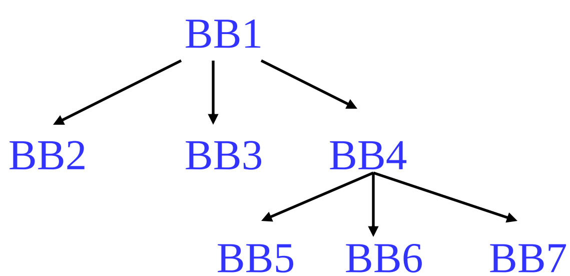


Dominator Tree

First BB is the root node, each node dominates all of its descendants

BB	DOM	BB	DOM
1	1	5	1,4,5
2	1,2	6	1,4,6
3	1,3	7	1,4,7
4	1,4		



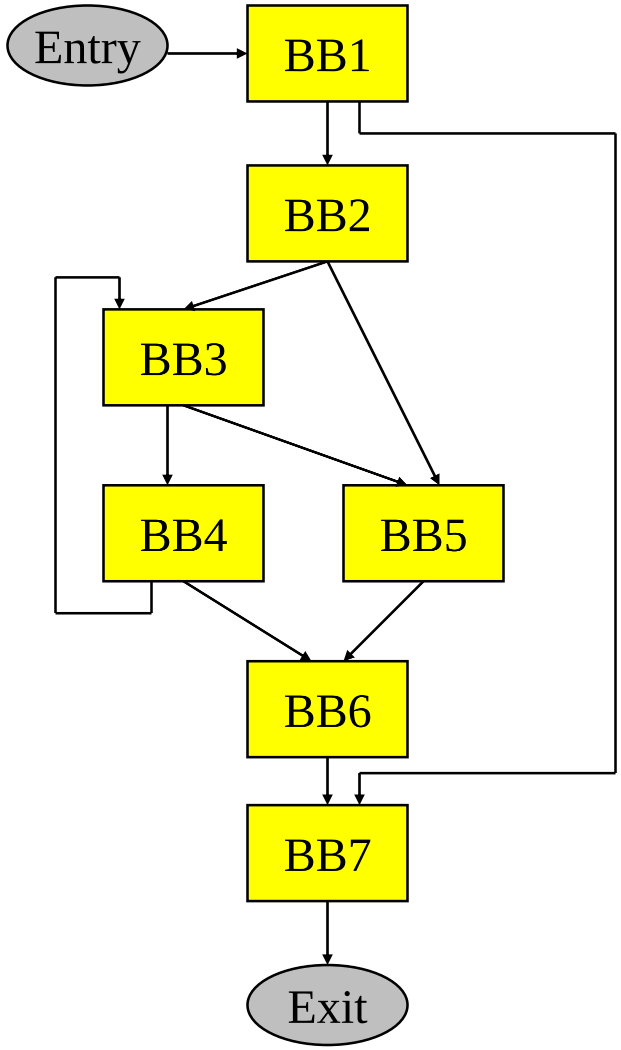


Dom tree

Dominator Tree Example

Draw the dominator tree

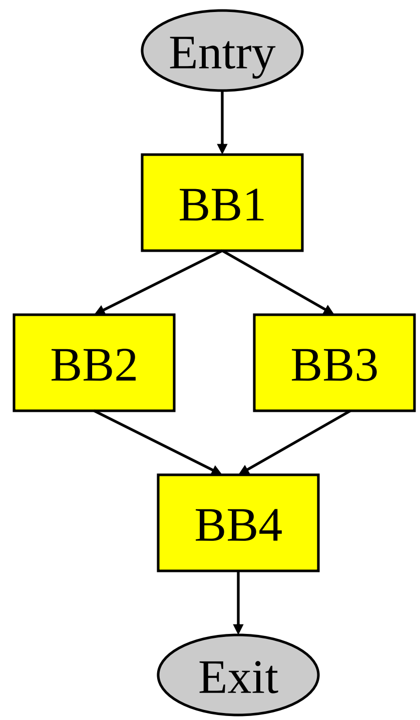
BB	DOM
1	E,1
2	E,1,2
3	E,1,2,3
4	E,1,2,3,4
5	E,1,2,5
6	E,1,2,6
7	E,1,7



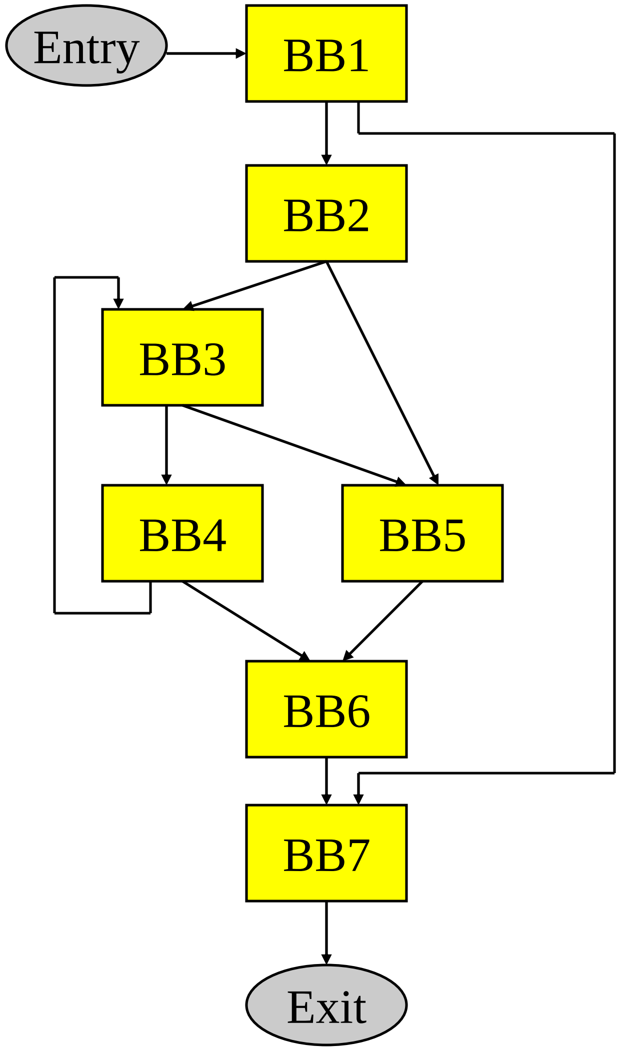
Post Dominator (PDOM)

- Reverse of dominator
- Defn: Post Dominator – Given a CFG(V, E, Entry, Exit), a node x post dominates a node y, if every path from y to the Exit contains x
- Intuition
  - Given some BB, which blocks are guaranteed to have executed after executing the BB
- pdom(BBi) = set of BBs that post dominate BBi
- Initialization
  - Pdom(exit) = exit
  - Pdom(everything else) = all nodes
- Iterative computation
  - while change, do
    - change = false
    - for each BB (except the exit BB)
      - tmp(BB) = BB + {intersect of pdom of all successor BB's}
      - if (tmp(BB) != pdom(BB))
pdom(BB) = tmp(BB)
change = true

Post Dominator Example 1

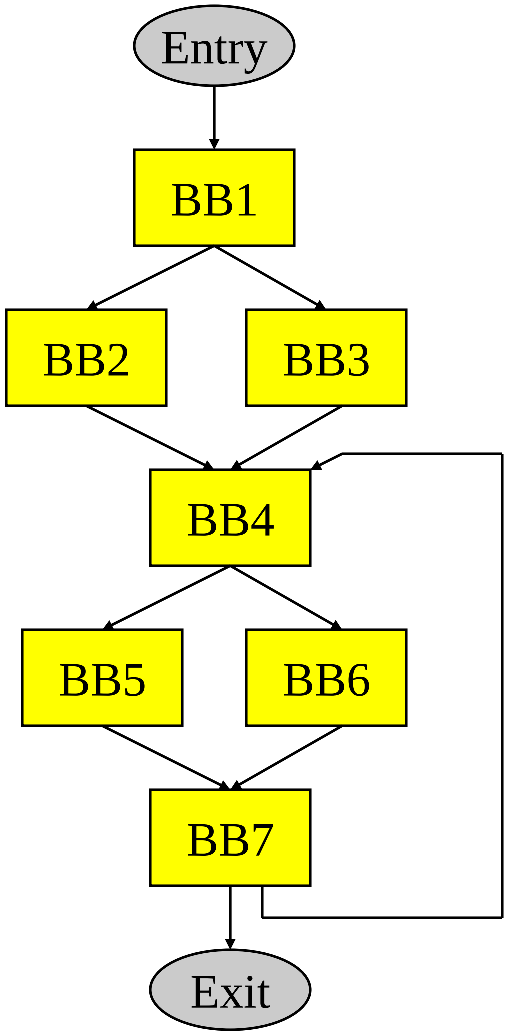


Post Dominator Example 2



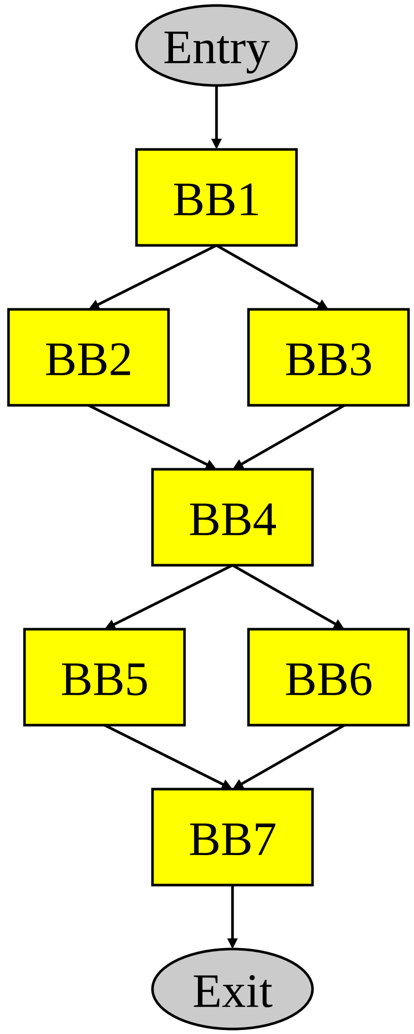
Immediate Post Dominator

- Defn: Immediate post dominator (ipdom) – Each node n has a unique immediate post dominator m that is the first post dominator of n on any path from n to the Exit
  - » Closest node that post dominates
  - » First breadth-first successor that post dominates a node



Why Do We Care About Dominators?

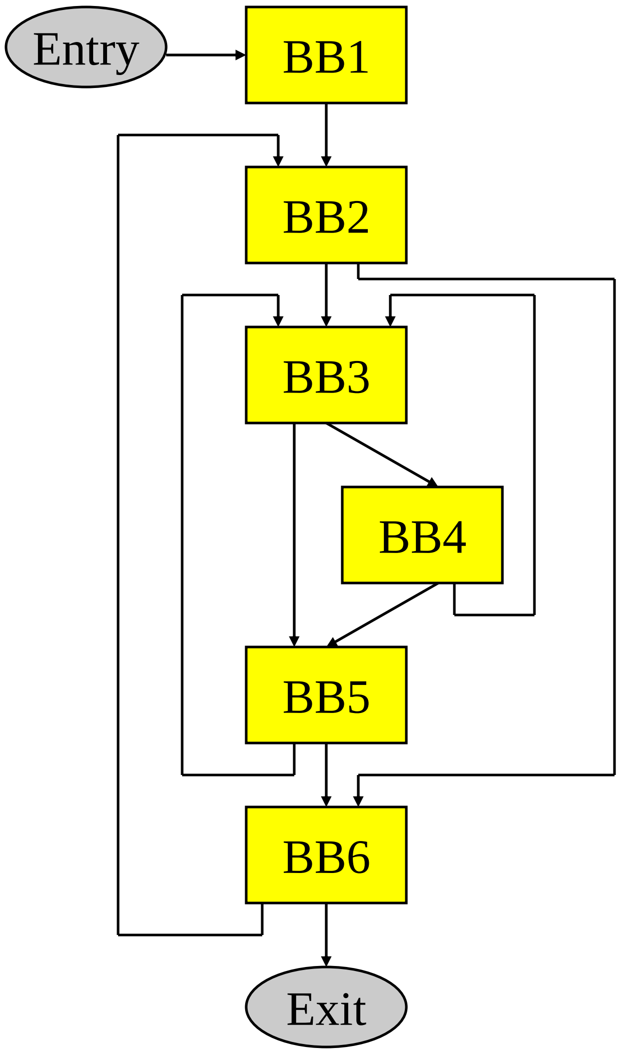
- Loop detection – next subject
- Dominator
  - Guaranteed to execute before
  - Redundant computation – an op is redundant if it is computed in a dominating BB
  - Most global optimizations use dominance info
- Post dominator
  - Guaranteed to execute after
  - Make a guess (ie 2 pointers do not point to the same locn)
  - Check they really do not point to one another in the post dominating BB



Natural Loops

- Cycle suitable for optimization
  - Discuss optimizations later
- 2 properties
  - Single entry point called the header
    - Header dominates all blocks in the loop
  - Must be one way to iterate the loop (ie at least 1 path back to the header from within the loop) called a backedge
- Backedge detection
  - Edge, x→ y where the target (y) dominates the source (x)

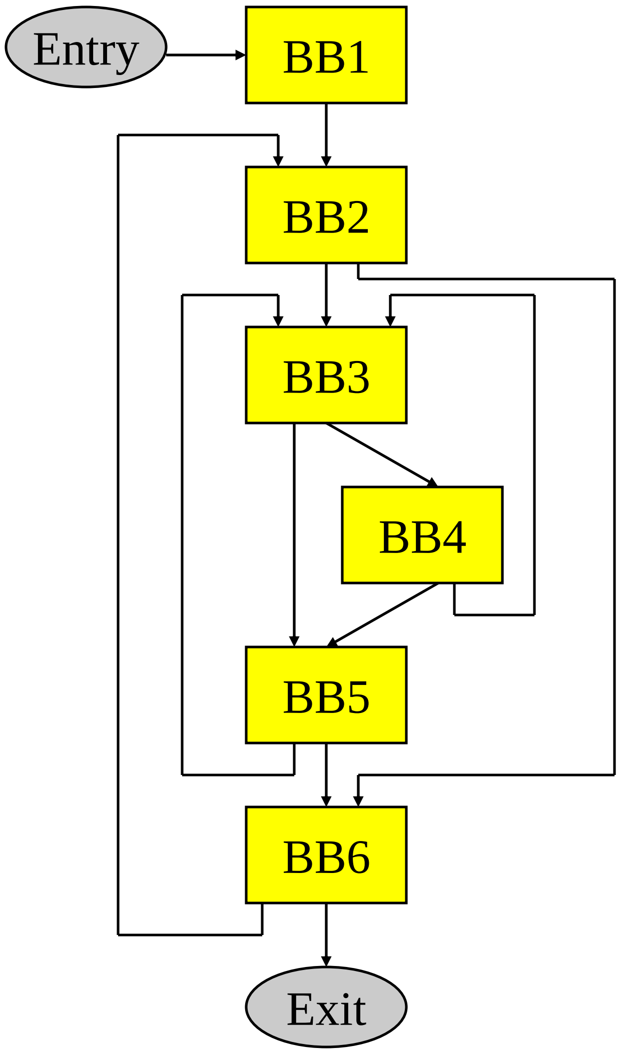
Backedge Example



Loop Detection

- Identify all backedges using Dom info
- Each backedge (x → y) defines a loop
  - Loop header is the backedge target (y)
  - Loop BB – basic blocks that comprise the loop
    - All predecessor blocks of x for which control can reach x without going through y are in the loop
- Merge loops with the same header
  - I.e., a loop with 2 continues
  - LoopBackedge = LoopBackedge1 + LoopBackedge2
  - LoopBB = LoopBB1 + LoopBB2
- Important property
  - Header dominates all LoopBB

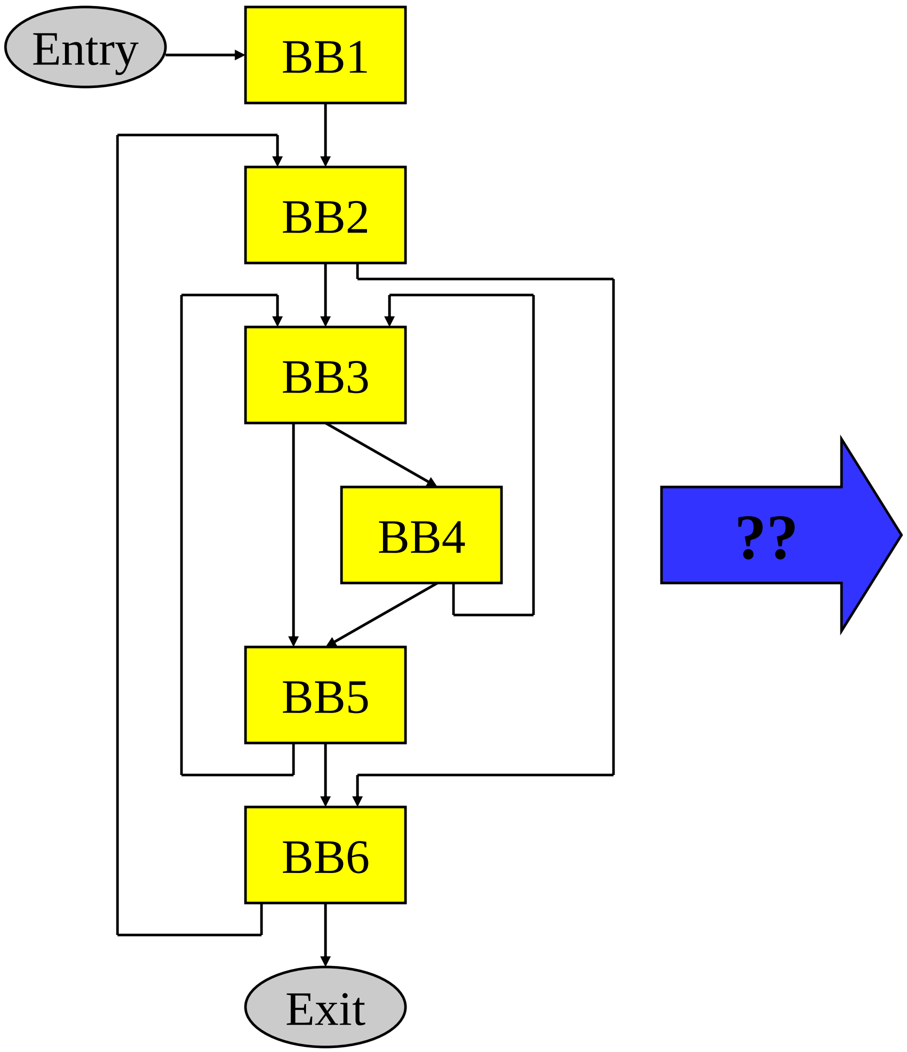
Loop Detection Example



Important Parts of a Loop

- Header, LoopBB
- Backedges, BackedgeBB
- Exitedges, ExitBB
  - For each LoopBB, examine each outgoing edge
  - If the edge is to a BB not in LoopBB, then its an exit
- Preheader (Preloop)
  - New block before the header (falls through to header)
  - Whenever you invoke the loop, preheader executed
  - Whenever you iterate the loop, preheader NOT executed
  - All edges entering header
    - Backedges – no change
    - All others, retarget to preheader
- Postheader (Postloop) - analogous

Find the Preheaders for each Loop

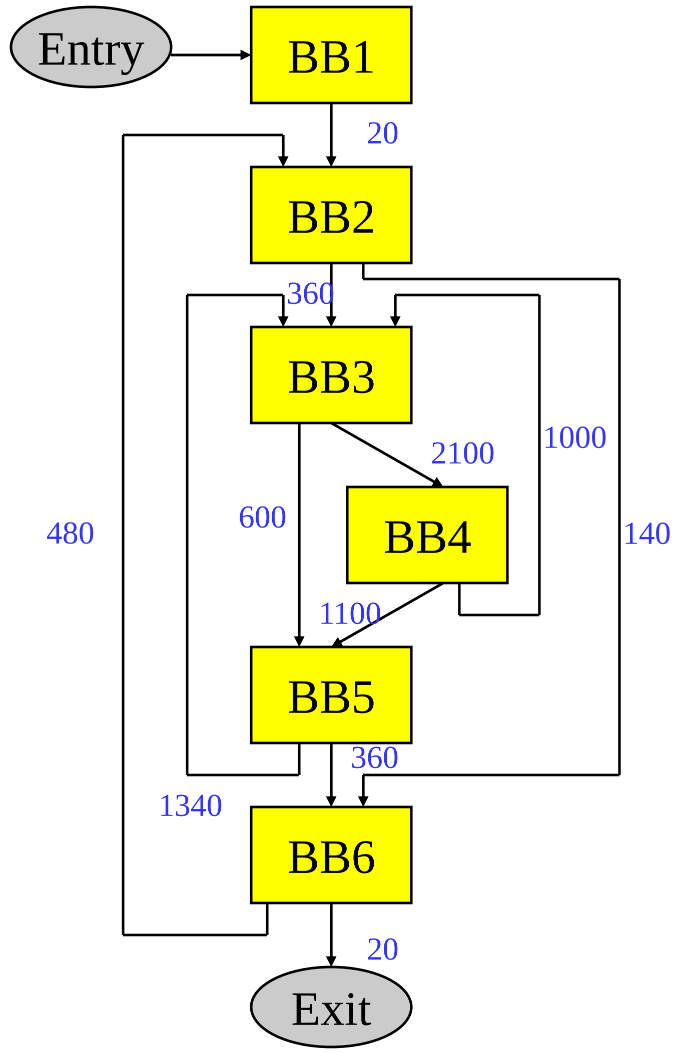


Characteristics of a Loop

- Nesting (generally within a function scope)
  - Inner loop – Loop with no loops contained within it
  - Outer loop – Loop contained within no other loops
  - Nesting depth
    - depth(outer loop) = 1
    - depth = depth(parent or containing loop) + 1
- Trip count (average trip count)
  - How many times (on average) does the loop iterate
  - for (I=0; I<100; I++) → trip count = 100
  - With profile info:
    - Ave trip count = weight(header) / weight(preheader)

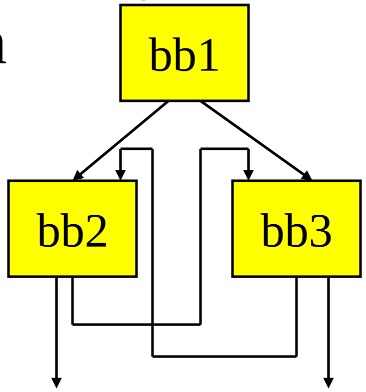
Trip Count Calculation Example

Calculate the trip counts for all the loops in the graph



Reducible Flow Graphs

- A flow graph is reducible if and only if we can partition the edges into 2 disjoint groups often called forward and back edges with the following properties
  - » The forward edges form an acyclic graph in which every node can be reached from the Entry
  - » The back edges consist only of edges whose destinations dominate their sources
- More simply – Take a CFG, remove all the backedges (x→ y where y dominates x), you should have a connected, acyclic graph



Non-reducible!