Lecture 19: Generative Models, Part 1

Justin Johnson

Lecture 19 - 1

Admin: Midterm grades

Many students did worse on midterm than homework; this is typical! Overall course will be curved if needed (but only to your benefit)



WI2022 Midterm Grade Distribution

Justin Johnson

Lecture 19 - 2

Admin: Midterm grades

WI2022 Midterm Grade Distribution

Many students did worse on midterm than homework; this is typical! Overall course will be curved if needed (but only to your benefit)



FA2020 Course Grade Cutoffs / Distribution

A+: 98% / 5.8% A: 90.5% / 58.7% A-: 88.5% / 11.6% B+: 86 / 11.6% B: 81 / 5.8%

Justin Johnson

Lecture 19 - 3

Admin: A4

Object Detection: FCOS, Faster R-CNN

Due Tuesday, 3/29/2022, 11:59pm ET

See Piazza for updates to Faster R-CNN:

- Small changes to improve mAP
- Hand-grading rubric



Recurrent networks, Transformers

Should be out tonight, due Monday April 11, 11:59pm ET



Lecture 19 - 5

Last Time: Vision Transformer (ViT)



Justin Johnson

Lecture 19 - 6

Today: Generative Models, Part 1

Justin Johnson

Lecture 19 - 7

Supervised Learning

Data: (x, y) x is data, y is label

Goal: Learn a *function* to map x -> y

Examples: Classification, regression, object detection, semantic segmentation, image captioning, etc.

Classification



Cat

March 28, 2022

Justin Johnson

Supervised Learning

Data: (x, y) x is data, y is label

Goal: Learn a *function* to map x -> y

Examples: Classification, regression, object detection, semantic segmentation, image captioning, etc.

Object Detection



DOG, DOG, CAT

This image is CC0 public domain

Justin Johnson

Lecture 19 - 9

Supervised Learning

Data: (x, y) x is data, y is label

Goal: Learn a *function* to map x -> y

Examples: Classification, regression, object detection, semantic segmentation, image captioning, etc.

Semantic Segmentation



GRASS, CAT, TREE, SKY

Justin Johnson

Lecture 19 - 10

Supervised Learning

Data: (x, y) x is data, y is label

Goal: Learn a *function* to map x -> y

Examples: Classification, regression, object detection, semantic segmentation, image captioning, etc.

Image captioning



A cat sitting on a suitcase on the floor

Caption generated using <u>neuraltalk2</u> Image is <u>CC0 Public domain</u>.

Justin Johnson

Lecture 19 - 11

Supervised Learning

Unsupervised Learning

Data: (x, y) x is data, y is label

Goal: Learn a *function* to map x -> y

Examples: Classification, regression, object detection, semantic segmentation, image captioning, etc.

Data: x Just data, no labels!

Goal: Learn some underlying hidden *structure* of the data

Examples: Clustering, dimensionality reduction, feature learning, density estimation, etc.

Justin Johnson



Unsupervised Learning

Data: x

Just data, no labels!

Goal: Learn some underlying hidden *structure* of the data

Examples: Clustering, dimensionality reduction, feature learning, density estimation, etc.

This image is CC0 public domain

Dimensionality Reduction (e.g. Principal Components Analysis)



Data: x

Lecture 19 - 14

Just data, no labels!

Unsupervised Learning

Goal: Learn some underlying hidden *structure* of the data

Examples: Clustering, dimensionality reduction, feature learning, density estimation, etc.

March 28, 2022

This image from Matthias Scholz is CC0 public domain

Justin Johnson

Feature Learning (e.g. autoencoders)



Data: x

Just data, no labels!

Unsupervised Learning

Goal: Learn some underlying hidden *structure* of the data

Examples: Clustering, dimensionality reduction, feature learning, density estimation, etc.

Justin Johnson

Unsupervised Learning

Density Estimation



Justin Johnson



Data: x

Just data, no labels!

Goal: Learn some underlying hidden *structure* of the data

Examples: Clustering, dimensionality reduction, feature learning, density estimation, etc.

Images left and right are CC0 public domain



Supervised Learning

Unsupervised Learning

Data: (x, y) x is data, y is label

Goal: Learn a *function* to map x -> y

Examples: Classification, regression, object detection, semantic segmentation, image captioning, etc.

Data: x Just data, no labels!

Goal: Learn some underlying hidden *structure* of the data

Examples: Clustering, dimensionality reduction, feature learning, density estimation, etc.

Justin Johnson

Discriminative Model:

Learn a probability distribution p(y|x)

Generative Model: Learn a probability distribution p(x) Data: x



Conditional Generative Model: Learn p(x|y) Label: y Cat

Justin Johnson

Lecture 19 - 18

Discriminative Model:

Learn a probability distribution p(y|x)

Generative Model: Learn a probability distribution p(x)

Conditional Generative Model: Learn p(x|y) Data: x



Label: y Cat

Probability Recap:

Density Function

p(x) assigns a positivenumber to each possiblex; higher numbers meanx is more likely

Density functions are **normalized**:

 $\int_X p(x)dx = 1$

Different values of x **compete** for density

Justin Johnson

Lecture 19 - 19

Discriminative Model: Learn a probability distribution p(y|x)

Generative Model: Learn a probability distribution p(x)

Conditional Generative Model: Learn p(x|y)

Data: x





Density Function

p(x) assigns a positive number to each possible x; higher numbers mean x is more likely Density functions are **normalized**:

p(x)dx = 1

Different values of x **compete** for density

Justin Johnson

Lecture 19 - 20

Discriminative Model: Learn a probability distribution p(y|x)

Generative Model: Learn a probability distribution p(x)

Conditional Generative Model: Learn p(x|y)



Discriminative model: the possible labels for each input "compete" for probability mass. But no competition between **images**

Discriminative Model: Learn a probability distribution p(y|x)

Generative Model: Learn a probability distribution p(x)

Conditional Generative Model: Learn p(x|y)



Discriminative model: No way for the model to handle unreasonable inputs; it must give label distributions for all images

Justin Johnson

Discriminative Model: Learn a probability distribution p(y|x)

Generative Model: Learn a probability distribution p(x)

Conditional Generative Model: Learn p(x|y)



Discriminative model: No way for the model to handle unreasonable inputs; it must give label distributions for all images

March 28, 2022

Justin Johnson

Discriminative Model:

Learn a probability distribution p(y|x)

Generative Model: Learn a probability distribution p(x)

Conditional Generative Model: Learn p(x|y)



Generative model: All possible images compete with each other for probability mass

Discriminative Model:

Learn a probability distribution p(y|x)

Generative Model: Learn a probability distribution p(x)

Conditional Generative Model: Learn p(x|y)



Generative model: All possible images compete with each other for probability mass

Requires deep image understanding! Is a dog more likely to sit or stand? How about 3-legged dog vs 3-armed monkey?

Discriminative Model:

Learn a probability distribution p(y|x)

Generative Model: Learn a probability distribution p(x)

Conditional Generative Model: Learn p(x|y)



Generative model: All possible images compete with each other for probability mass

Model can "reject" unreasonable inputs by assigning them small values

Justin Johnson

Lecture 19 - 26

Discriminative Model:

Learn a probability distribution p(y|x)

Generative Model: Learn a probability distribution p(x)

Conditional Generative Model: Learn p(x|y)



Conditional Generative Model: Each possible label induces a competition among all images

Justin Johnson

Lecture 19 - 27

Discriminative Model:

Learn a probability distribution p(y|x)

Generative Model:

Learn a probability distribution p(x)

Conditional Generative Model: Learn p(x|y)

Recall Bayes' Rule:

$$P(x \mid y) = \frac{P(y \mid x)}{P(y)}P(x)$$

Justin Johnson

Lecture 19 - 28

Discriminative Model:

Learn a probability distribution p(y|x)

Generative Model:

Learn a probability distribution p(x)

Conditional Generative Model: Learn p(x|y)

Recall Bayes' Rule:



We can build a conditional generative model from other components!

Justin Johnson

What can we do with a discriminative model?

Discriminative Model:

Learn a probability distribution p(y|x)

Assign labels to data Feature learning (with labels)

Generative Model:

Learn a probability distribution p(x)

Conditional Generative Model: Learn p(x|y)

What can we do with a generative model?

Discriminative Model:

Learn a probability distribution p(y|x)

Generative Model: Learn a probability distribution p(x) Assign labels to data Feature learning (with labels)

Detect outliers

Feature learning (without labels)
Sample to generate new data

Conditional Generative Model: Learn p(x|y)

What can we do with a generative model?

Discriminative Model:

Learn a probability distribution p(y|x)

Generative Model: Learn a probability distribution p(x)

Conditional Generative _ **Model:** Learn p(x|y)

Assign labels to data Feature learning (with labels)

Detect outliers

Feature learning (without labels)
Sample to generate new data

Assign labels, while rejecting outliers! Generate new data conditioned on input labels

Generative models

Figure adapted from Ian Goodfellow, Tutorial on Generative Adversarial Networks, 2017.

Justin Johnson





Figure adapted from Ian Goodfellow, Tutorial on Generative Adversarial Networks, 2017.

Justin Johnson





Lecture 19 - 35

Can compute p(x)

- Autoregressive
- NADE / MADE
- NICE / RealNVP

Justin Johnson

- Glow
- Ffjord

Figure adapted from Ian Goodfellow, Tutorial on Generative Adversarial Networks, 2017.



Figure adapted from Ian Goodfellow, Tutorial on Generative Adversarial Networks, 2017.

Justin Johnson

Lecture 19 - 36
Taxonomy of Generative Models



Figure adapted from Ian Goodfellow, Tutorial on Generative Adversarial Networks, 2017.

March 28, 2022

Justin Johnson

Taxonomy of Generative Models



Figure adapted from Ian Goodfellow, Tutorial on Generative Adversarial Networks, 2017.

Justin Johnson

Lecture 19 - 38

Autoregressive models

Justin Johnson

Lecture 19 - 39

Goal: Write down an explicit function for p(x) = f(x, W)

Goal: Write down an explicit function for p(x) = f(x, W)

Given dataset $x^{(1)}$, $x^{(2)}$, ... $x^{(N)}$, train the model by solving:

$$W^* = \arg \max_{W} \prod_i p(x^{(i)})$$

Maximize probability of training data (Maximum likelihood estimation)

Justin Johnson

Goal: Write down an explicit function for p(x) = f(x, W)

Given dataset $x^{(1)}$, $x^{(2)}$, ... $x^{(N)}$, train the model by solving:

$$W^* = \arg \max_{W} \prod_i p(x^{(i)})$$

Maximize probability of training data (Maximum likelihood estimation)

$$= \arg \max_{W} \sum_{i} \log p(x^{(i)}) \qquad \square$$

Log trick to exchange product for sum

Goal: Write down an explicit function for p(x) = f(x, W)

Given dataset $x^{(1)}$, $x^{(2)}$, ... $x^{(N)}$, train the model by solving:

$$W^* = \arg \max_{W} \prod_i p(x^{(i)})$$

Maximize probability of training data (Maximum likelihood estimation)

$$= \arg \max_{W} \sum_{i} \log p(x^{(i)})$$

Log trick to exchange product for sum

$$= \arg \max_{W} \sum_{i} \log f(x^{(i)}, W)$$

This will be our loss function! Train with gradient descent

Goal: Write down an explicit function for p(x) = f(x, W)Assume x consists of multiple subparts: $x = (x_1, x_2, x_3, ..., x_T)$

Justin Johnson

Goal: Write down an explicit function for p(x) = f(x, W)

Assume x consists of multiple subparts:

Break down probability using the chain rule:

$$x = (x_1, x_2, x_3, \dots, x_T)$$

$$p(x) = p(x_1, x_2, x_3, \dots, x_T)$$

= $p(x_1)p(x_2 | x_1)p(x_3 | x_1, x_2) \dots$

Goal: Write down an explicit function for p(x) = f(x, W)

Assume x consists of multiple subparts:

Break down probability using the chain rule:

$$x = (x_1, x_2, x_3, \dots, x_T)$$

$$p(x) = p(x_1, x_2, x_3, \dots, x_T)$$

= $p(x_1)p(x_2 | x_1)p(x_3 | x_1, x_2) \dots$
= $\prod_{t=1}^{T} p(x_t | x_1, \dots, x_{t-1})$

Probability of the next subpart given all the previous subparts

Goal: Write down an explicit function for p(x) = f(x, W)

Assume x consists of multiple subparts:

Break down probability using the chain rule:

$$x = (x_1, x_2, x_3, \dots, x_T)$$

$$p(x) = p(x_1, x_2, x_3, ..., x_T)$$

= $p(x_1)p(x_2 | x_1)p(x_3 | x_1, x_2) ...$
= $\prod_{t=1}^{T} p(x_t | x_1, ..., x_{t-1})$
is! Probability of the next subpart

given all the previous subparts

Generate image pixels one at a time, starting at the upper left corner

Compute a hidden state for each pixel that depends on hidden states and RGB values from the left and from above (LSTM recurrence)

$$h_{x,y} = f(h_{x-1,y}, h_{x,y-1}, W)$$

At each pixel, predict red, then blue, then green: softmax over [0, 1, ..., 255]



Van den Oord et al, "Pixel Recurrent Neural Networks", ICML 2016

March 28, 2022

Generate image pixels one at a time, starting at the upper left corner

Compute a hidden state for each pixel that depends on hidden states and RGB values from the left and from above (LSTM recurrence)

$$h_{x,y} = f(h_{x-1,y}, h_{x,y-1}, W)$$

At each pixel, predict red, then blue, then green: softmax over [0, 1, ..., 255]



Van den Oord et al, "Pixel Recurrent Neural Networks", ICML 2016

March 28, 2022

Generate image pixels one at a time, starting at the upper left corner

Compute a hidden state for each pixel that depends on hidden states and RGB values from the left and from above (LSTM recurrence)

$$h_{x,y} = f(h_{x-1,y}, h_{x,y-1}, W)$$

At each pixel, predict red, then blue, then green: softmax over [0, 1, ..., 255]



Van den Oord et al, "Pixel Recurrent Neural Networks", ICML 2016

March 28, 2022

Generate image pixels one at a time, starting at the upper left corner

Compute a hidden state for each pixel that depends on hidden states and RGB values from the left and from above (LSTM recurrence)

$$h_{x,y} = f(h_{x-1,y}, h_{x,y-1}, W)$$

At each pixel, predict red, then blue, then green: softmax over [0, 1, ..., 255]



Van den Oord et al, "Pixel Recurrent Neural Networks", ICML 2016

March 28, 2022

Generate image pixels one at a time, starting at the upper left corner

Compute a hidden state for each pixel that depends on hidden states and RGB values from the left and from above (LSTM recurrence)

$$h_{x,y} = f(h_{x-1,y}, h_{x,y-1}, W)$$

At each pixel, predict red, then blue, then green: softmax over [0, 1, ..., 255]



Van den Oord et al, "Pixel Recurrent Neural Networks", ICML 2016

March 28, 2022

Generate image pixels one at a time, starting at the upper left corner

Compute a hidden state for each pixel that depends on hidden states and RGB values from the left and from above (LSTM recurrence)

$$h_{x,y} = f(h_{x-1,y}, h_{x,y-1}, W)$$

At each pixel, predict red, then blue, then green: softmax over [0, 1, ..., 255]



Van den Oord et al, "Pixel Recurrent Neural Networks", ICML 2016

March 28, 2022

Generate image pixels one at a time, starting at the upper left corner

Compute a hidden state for each pixel that depends on hidden states and RGB values from the left and from above (LSTM recurrence)

$$h_{x,y} = f(h_{x-1,y}, h_{x,y-1}, W)$$

At each pixel, predict red, then blue, then green: softmax over [0, 1, ..., 255]



Van den Oord et al, "Pixel Recurrent Neural Networks", ICML 2016

March 28, 2022

Generate image pixels one at a time, starting at the upper left corner

Compute a hidden state for each pixel that depends on hidden states and RGB values from the left and from above (LSTM recurrence)

$$h_{x,y} = f(h_{x-1,y}, h_{x,y-1}, W)$$

At each pixel, predict red, then blue, then green: softmax over [0, 1, ..., 255]

Each pixel depends **implicity** on all pixels above and to the left:



Van den Oord et al, "Pixel Recurrent Neural Networks", ICML 2016

March 28, 2022

Justin Johnson

Generate image pixels one at a time, starting at the upper left corner

Compute a hidden state for each pixel that depends on hidden states and RGB values from the left and from above (LSTM recurrence)

$$h_{x,y} = f(h_{x-1,y}, h_{x,y-1}, W)$$

At each pixel, predict red, then blue, then green: softmax over [0, 1, ..., 255]

Each pixel depends **implicity** on all pixels above and to the left:



Van den Oord et al, "Pixel Recurrent Neural Networks", ICML 2016

March 28, 2022

Justin Johnson

Generate image pixels one at a time, starting at the upper left corner

Compute a hidden state for each pixel that depends on hidden states and RGB values from the left and from above (LSTM recurrence)

 $h_{x,y} = f(h_{x-1,y}, h_{x,y-1}, W)$

At each pixel, predict red, then blue, then green: softmax over [0, 1, ..., 255]

Each pixel depends **implicity** on all pixels above and to the left:

Problem: Very slow during both training and testing; N x N image requires 2N-1 sequential steps



Van den Oord et al, "Pixel Recurrent Neural Networks", ICML 2016

March 28, 2022

Justin Johnson



Still generate image pixels starting from corner

Dependency on previous pixels now modeled using a CNN over context region



Van den Oord et al, "Conditional Image Generation with PixelCNN Decoders", NeurIPS 2016

March 28, 2022

Justin Johnson

PixelCNN

Still generate image pixels starting from corner

Dependency on previous pixels now modeled using a CNN over context region

Training: maximize likelihood of training images



$$p(x) = \prod_{i=1}^{n} p(x_i | x_1, \dots, x_{i-1})$$

Van den Oord et al, "Conditional Image Generation with PixelCNN Decoders", NeurIPS 2016

March 28, 2022

Justin Johnson

PixelCNN

Still generate image pixels starting from corner

Dependency on previous pixels now modeled using a CNN over context region

Training: maximize likelihood of training images

Training is faster than PixelRNN (can parallelize convolutions since context region values known from training images) Softmax loss

at each pixel

Generation must still proceed sequentially => still slow

Van den Oord et al, "Conditional Image Generation with PixelCNN Decoders", NeurIPS 2016

Justin Johnson

Lecture 19 - 60

PixelRNN: Generated Samples



32x32 CIFAR-10



32x32 ImageNet

Van den Oord et al, "Pixel Recurrent Neural Networks", ICML 2016

Justin Johnson

Lecture 19 - 61

Autoregressive Models: PixelRNN and PixelCNN

Pros:

- Can explicitly compute likelihood p(x)
- Explicit likelihood of training data gives good evaluation metric
- Good samples

Con:

- Sequential generation => slow

Improving PixelCNN performance

- Gated convolutional layers
- Short-cut connections
- Discretized logistic loss
- Multi-scale
- Training tricks
- Etc...

See

- Van der Oord et al. NIPS 2016
- Salimans et al. 2017 (PixelCNN++)

Justin Johnson

Variational Autoencoders

Justin Johnson

Lecture 19 - 63

Variational Autoencoders

PixelRNN / PixelCNN explicitly parameterizes density function with a neural network, so we can train to maximize likelihood of training data:

$$p_W(x) = \prod_{t=1}^T p_W(x_t \mid x_1, \dots, x_{t-1})$$

Variational Autoencoders (VAE) define an **intractable density** that we cannot explicitly compute or optimize

But we will be able to directly optimize a **lower bound** on the density

Variational <u>Autoencoders</u>

Justin Johnson

Lecture 19 - 65

Unsupervised method for learning feature vectors from raw data x, without any labels

Features should extract useful information (maybe object identities, properties, scene type, etc) that we can use for downstream tasks

Originally: Linear + nonlinearity (sigmoid) **Later**: Deep, fully-connected **Later**: ReLU CNN



Problem: How can we learn this feature transform from raw data?

Features should extract useful information (maybe object identities, properties, scene type, etc) that we can use for downstream tasks But we can't observe features!

Originally: Linear + nonlinearity (sigmoid) **Later**: Deep, fully-connected **Later**: ReLU CNN





Input Data

Justin Johnson

Lecture 19 - 67

Problem: How can we learn this feature transform from raw data?

Idea: Use the features to <u>reconstruct</u> the input data with a **decoder** "Autoencoding" = encoding itself



Justin Johnson

Lecture 19 - 68

Loss: L2 distance between input and reconstructed data.





Input Data

Justin Johnson

Lecture 19 - 69



Reconstructed data



Decoder: 4 tconv layers Encoder: 4 conv layers



Input Data

Justin Johnson

Lecture 19 - 70



Loss: L2 distance between input and reconstructed data.

Reconstructed data



Decoder: 4 tconv layers Encoder: 4 conv layers



Input Data

Justin Johnson

Lecture 19 - 71

After training, throw away decoder and use encoder for a downstream task



```
Justin Johnson
```
(Regular, non-variational) Autoencoders

After training, throw away decoder and use encoder for a downstream task



Justin Johnson

(Regular, non-variational) Autoencoders

Autoencoders learn **latent features** for data without any labels! Can use features to initialize a **supervised** model **Not probabilistic: No way to sample new data from learned model**



Justin Johnson



Kingma and Welling, Auto-Encoding Variational Beyes, ICLR 2014

Justin Johnson

Lecture 19 - 75

Probabilistic spin on autoencoders:

- 1. Learn latent features z from raw data
- 2. Sample from the model to generate new data

Probabilistic spin on autoencoders:

- 1. Learn latent features z from raw data
- 2. Sample from the model to generate new data

Assume training data $\{x^{(i)}\}_{i=1}^{N}$ is generated from unobserved (latent) representation **z**

Intuition: x is an image, **z** is latent factors used to generate **x**: attributes, orientation, etc.

Justin Johnson

Lecture 19 - 77

Probabilistic spin on autoencoders:

- 1. Learn latent features z from raw data
- 2. Sample from the model to generate new data

After training, sample new data like this:

Sample from
conditional \boldsymbol{x} $p_{\theta^*}(x \mid z^{(i)})$ \uparrow Sample z
from prior
 $p_{\theta^*}(z)$ \boldsymbol{z}

Assume training data $\{x^{(i)}\}_{i=1}^{N}$ is generated from unobserved (latent) representation **z**

Intuition: x is an image, z is latent factors used to generate x: attributes, orientation, etc.

Justin Johnson

Lecture 19 - 78

Probabilistic spin on autoencoders:

- 1. Learn latent features z from raw data
- 2. Sample from the model to generate new data

After training, sample new data like this:

Sample from
conditional \boldsymbol{x} $p_{\theta^*}(x \mid z^{(i)})$ \uparrow Sample z
from prior
 $p_{\theta^*}(z)$ \boldsymbol{z}

Assume training data $\{x^{(i)}\}_{i=1}^{N}$ is generated from unobserved (latent) representation **z**

Intuition: x is an image, z is latent factors used to generate x: attributes, orientation, etc.

Assume simple prior p(z), e.g. Gaussian

Justin Johnson

Lecture 19 - 79

Probabilistic spin on autoencoders:

- 1. Learn latent features z from raw data
- 2. Sample from the model to generate new data

After training, sample new data like this:

Sample from conditional $p_{\theta^*}(x \mid z^{(i)})$	x
Sample z from prior $p_{ heta^*}(z)$	z

Assume training data $\{x^{(i)}\}_{i=1}^{N}$ is generated from unobserved (latent) representation **z**

Intuition: x is an image, z is latent factors used to generate x: attributes, orientation, etc.

Assume simple prior p(z), e.g. Gaussian

Represent p(x|z) with a neural network (Similar to **decoder** from autencoder)

Justin Johnson

Decoder must be **probabilistic**: Decoder inputs z, outputs mean $\mu_{x|z}$ and (diagonal) covariance $\sum_{x|z}$

Sample x from Gaussian with mean $\mu_{x|z}$ and (diagonal) covariance $\sum_{x|z}$

Sample from conditional $p_{\theta^*}(x \mid z^{(i)})$ Sample z from prior $p_{\theta^*}(z)$ $\mu_x|z$ $\Sigma_x|z$ $\Sigma_x|z$ z Assume training data $\{x^{(i)}\}_{i=1}^{N}$ is generated from unobserved (latent) representation **z**

Intuition: x is an image, z is latent factors used to generate x: attributes, orientation, etc.

Assume simple prior p(z), e.g. Gaussian

Represent p(x|z) with a neural network (Similar to **decoder** from autencoder)

Justin Johnson

Decoder must be **probabilistic**: Decoder inputs z, outputs mean $\mu_{x|z}$ and (diagonal) covariance $\sum_{x|z}$

Sample x from Gaussian with mean $\mu_{x|z}$ and (diagonal) covariance $\sum_{x|z}$

Sample from conditional $p_{\theta^*}(x \mid z^{(i)})$ Sample z from prior $p_{\theta^*}(z)$ $\mu_x|z$ $\Sigma_x|z$ $\Sigma_x|z$ $\Sigma_x|z$ z Assume training data $\{x^{(i)}\}_{i=1}^{N}$ is generated from unobserved (latent) representation **z**

How to train this model?

Basic idea: maximize likelihood of data

If we could observe the z for each x, then could train a *conditional generative model* p(x|z)

Justin Johnson

Decoder must be **probabilistic**: Decoder inputs z, outputs mean $\mu_{x|z}$ and (diagonal) covariance $\sum_{x|z}$

Sample x from Gaussian with mean $\mu_{x|z}$ and (diagonal) covariance $\sum_{x|z}$

Assume training data $\{x^{(i)}\}_{i=1}^{N}$ is generated from unobserved (latent) representation **z**

How to train this model?

Basic idea: maximize likelihood of data

Sample from conditional $p_{\theta^*}(x \mid z^{(i)})$ Sample z from prior $p_{\theta^*}(z)$ $\mu_x|z$ $\Sigma_x|z$ $\Sigma_x|z$ z

We don't observe z, so need to marginalize:

$$p_{\theta}(x) = \int p_{\theta}(x, z) dz = \int p_{\theta}(x|z) p_{\theta}(z) dz$$

Justin Johnson

Lecture 19 - 83

Decoder must be **probabilistic**: Decoder inputs z, outputs mean $\mu_{x|z}$ and (diagonal) covariance $\sum_{x|z}$

Sample x from Gaussian with mean $\mu_{x|z}$ and (diagonal) covariance $\sum_{x|z}$

 $|\mu_{x|z}|$

Assume training data $\{x^{(i)}\}_{i=1}^{N}$ is generated from unobserved (latent) representation **z**

How to train this model?

Basic idea: maximize likelihood of data

We don't observe z, so need to marginalize:

$$p_{\theta}(x) = \int p_{\theta}(x, z) dz = \int p_{\theta}(x|z) p_{\theta}(z) dz$$

Ok, can compute this with decoder network

Justin Johnson

Sample from

 $p_{\theta^*}(x \mid z^{(i)})$

conditional

Sample z

from prior

 $p_{\theta^*}(z)$

Lecture 19 - 84

 $\sum_{x|z}$

z

Decoder must be **probabilistic**: Decoder inputs z, outputs mean $\mu_{x|z}$ and (diagonal) covariance $\sum_{x|z}$

Sample x from Gaussian with mean $\mu_{x|z}$ and (diagonal) covariance $\sum_{x|z}$

 $|\mu_{x|z}|$

Assume training data $\{x^{(i)}\}_{i=1}^{N}$ is generated from unobserved (latent) representation z

How to train this model?

Basic idea: maximize likelihood of data

 $\sum_{x|z}$ conditional $p_{\theta^*}(x \mid z^{(i)})$ Sample z ľ from prior z $p_{\theta^*}(z)$

We don't observe z, so need to marginalize:

$$p_{\theta}(x) = \int p_{\theta}(x, z) dz = \int p_{\theta}(x|z) p_{\theta}(z) dz$$

Ok, we assumed Gaussian prior for z

Justin Johnson

Sample from

Decoder must be **probabilistic**: Decoder inputs z, outputs mean $\mu_{x|z}$ and (diagonal) covariance $\sum_{x|z}$

Sample x from Gaussian with mean $\mu_{x|z}$ and (diagonal) covariance $\sum_{x|z}$

Assume training data $\{x^{(i)}\}_{i=1}^{N}$ is generated from unobserved (latent) representation **z**

How to train this model?

Basic idea: maximize likelihood of data

Sample from conditional $p_{\theta^*}(x \mid z^{(i)})$ Sample z from prior $p_{\theta^*}(z)$ $\mu_x|z$ $\Sigma_x|z$ $\Sigma_x|z$ z

We don't observe z, so need to marginalize: $p_{\theta}(x) = \int p_{\theta}(x, z) dz = \int p_{\theta}(x|z) p_{\theta}(z) dz$

Problem: Impossible to integrate over all z!

Justin Johnson

Lecture 19 - 86

Decoder must be **probabilistic**: Decoder inputs z, outputs mean $\mu_{x|z}$ and (diagonal) covariance $\sum_{x|z}$

Sample x from Gaussian with mean $\mu_{x|z}$ and (diagonal) covariance $\sum_{x|z}$

Sample from conditional $p_{\theta^*}(x \mid z^{(i)})$ Sample z from prior $p_{\theta^*}(z)$ $\mu_{x|z}$ $\Sigma_{x|z}$ $\Sigma_{x|z}$ $\Sigma_{x|z}$ $\Sigma_{x|z}$ Assume training data $\{x^{(i)}\}_{i=1}^{N}$ is generated from unobserved (latent) representation **z**

Recall $p(x,z) = p(x \mid z)p(z) = p(z \mid x)p(x)$

How to train this model?

Basic idea: maximize likelihood of data

Another idea: Try Bayes' Rule: $p_{\theta}(x) = \frac{p_{\theta}(x \mid z)p_{\theta}(z)}{p_{\theta}(z \mid x)}$

Justin Johnson

Decoder must be **probabilistic**: Decoder inputs z, outputs mean $\mu_{x|z}$ and (diagonal) covariance $\sum_{x|z}$

Sample x from Gaussian with mean $\mu_{x|z}$ and (diagonal) covariance $\sum_{x|z}$

Sample from conditional $p_{\theta^*}(x \mid z^{(i)})$ Sample z from prior $p_{\theta^*}(z)$ $\mu_x|z$ $\Sigma_x|z$ $\Sigma_x|z$ $\Sigma_x|z$ $\Sigma_x|z$ $\Sigma_x|z$ Assume training data $\{x^{(i)}\}_{i=1}^{N}$ is generated from unobserved (latent) representation **z**

Recall $p(x,z) = p(x \mid z)p(z) = p(z \mid x)p(x)$

How to train this model?

Basic idea: maximize likelihood of data

Another idea: Try Bayes' Rule
$$p_{\theta}(x) = \frac{p_{\theta}(x \mid z)p_{\theta}(z)}{p_{\theta}(z \mid x)} \quad \mathbf{o}$$

Ok, compute with decoder network

Justin Johnson

Lecture 19 - 88

.

Decoder must be **probabilistic**: Decoder inputs z, outputs mean $\mu_{x|z}$ and (diagonal) covariance $\sum_{x|z}$

Sample x from Gaussian with mean $\mu_{x|z}$ and (diagonal) covariance $\sum_{x|z}$

 $p_{ heta^*}(x \mid z^{(i)})$ Sample z from prior $p_{ heta^*}(z)$

Sample from

conditional



Recall $p(x,z) = p(x \mid z)p(z) = p(z \mid x)p(x)$

Assume training data $\{x^{(i)}\}_{i=1}^{N}$ is generated from unobserved (latent) representation **z**

How to train this model?

Basic idea: maximize likelihood of data

```
Another idea: Try Bayes' Rule:

p_{\theta}(x) = \frac{p_{\theta}(x \mid z)p_{\theta}(z)}{p_{\theta}(z \mid x)}
```

Ok, we assumed Gaussian prior

Justin Johnson

Lecture 19 - 89

Decoder must be **probabilistic**: Decoder inputs z, outputs mean $\mu_{x|z}$ and (diagonal) covariance $\sum_{x|z}$

Sample x from Gaussian with mean $\mu_{x|z}$ and (diagonal) covariance $\sum_{x|z}$

Sample from conditional $p_{\theta^*}(x \mid z^{(i)})$ Sample z from prior $p_{\theta^*}(z)$

Recall $p(x,z) = p(x \mid z)p(z) = p(z \mid x)p(x)$

Assume training data $\{x^{(i)}\}_{i=1}^{N}$ is generated from unobserved (latent) representation **z**

How to train this model?

Basic idea: maximize likelihood of data

Another idea: Try Bayes' Rule: $p_{\theta}(x) = \frac{p_{\theta}(x \mid z)p_{\theta}(z)}{p_{\theta}(z \mid x)} \quad \text{Produce}$ to

Problem: No way to compute this!

Justin Johnson

Lecture 19 - 90

Decoder must be **probabilistic**: Decoder inputs z, outputs mean $\mu_{x|z}$ and (diagonal) covariance $\sum_{x|z}$

Sample x from Gaussian with mean $\mu_{x|z}$ and (diagonal) covariance $\sum_{x|z}$

Sample from conditional $p_{\theta^*}(x \mid z^{(i)})$ Sample z from prior $p_{\theta^*}(z)$

Justin Johnson



Lecture 19 - 91

Recall $p(x,z) = p(x \mid z)p(z) = p(z \mid x)p(x)$

Assume training data $\{x^{(i)}\}_{i=1}^{N}$ is generated from unobserved (latent) representation **z**

How to train this model?

Basic idea: maximize likelihood of data

Another idea: Try Bayes' Rule: $n_0(x \mid z)n_0(z)$

 $p_{\theta}(x) = \frac{p_{\theta}(x \mid z)p_{\theta}(z)}{p_{\theta}(z \mid x)}$ Solution: Train another network (encoder) that learns $q_{\phi}(z \mid x) \approx p_{\theta}(z \mid x)$

Decoder must be **probabilistic**: Decoder inputs z, outputs mean $\mu_{x|z}$ and (diagonal) covariance $\sum_{x|z}$

Sample x from Gaussian with mean $\mu_{x|z}$ and (diagonal) covariance $\sum_{x|z}$

Sample from conditional $p_{\theta^*}(x \mid z^{(i)})$ Sample z from prior $p_{\theta^*}(z)$ $\mu_x \mid z$ $\sum_{x \mid z}$ $\sum_{x \mid z}$

Justin Johnson

Recall $p(x,z) = p(x \mid z)p(z) = p(z \mid x)p(x)$

Assume training data $\{x^{(i)}\}_{i=1}^{N}$ is generated from unobserved (latent) representation **z**

How to train this model?

Basic idea: maximize likelihood of data

Another idea: Try Bayes' Rule: $p_{\theta}(x) = \frac{p_{\theta}(x \mid z)p_{\theta}(z)}{p_{\theta}(z \mid x)} \approx \frac{p_{\theta}(x \mid z)p_{\theta}(z)}{q_{\phi}(z \mid x)}$ Use encoder to compute $q_{\phi}(z \mid x) \approx p_{\theta}(z \mid x)$ Lecture 19 - 92 March 28, 2022

Decoder network inputs latent code z, gives distribution over data x

Encoder network inputs

data x, gives distribution over latent codes z

If we can ensure that $q_{\phi}(z \mid x) \approx p_{\theta}(z \mid x)$,

$$p_{\theta}(x \mid z) = N(\mu_{x\mid z}, \Sigma_{x\mid z}) \quad q_{\phi}(z \mid x) = N(\mu_{z\mid x}, \Sigma_{z\mid x}) \quad \text{then we can approximate}$$

$$\frac{\mu_{x\mid z}}{p_{\theta}(x)} \sum_{x\mid z} \frac{p_{\theta}(x \mid z)p(z)}{q_{\phi}(z \mid x)} \quad p_{\theta}(x) \approx \frac{p_{\theta}(x \mid z)p(z)}{q_{\phi}(z \mid x)}$$

$$\frac{1}{2} \sum_{x\mid z} \sum_{x\mid z} \frac{p_{\theta}(x \mid z)p(z)}{q_{\phi}(z \mid x)} \quad p_{\theta}(x) \approx \frac{p_{\theta}(x \mid z)p(z)}{q_{\phi}(z \mid x)}$$

$$\log p_{\theta}(x) = \log \frac{p_{\theta}(x \mid z)p(z)}{p_{\theta}(z \mid x)}$$

Bayes' Rule

Justin Johnson

Lecture 19 - 94

$$\log p_{\theta}(x) = \log \frac{p_{\theta}(x \mid z)p(z)}{p_{\theta}(z \mid x)} = \log \frac{p_{\theta}(x \mid z)p(z)q_{\phi}(z \mid x)}{p_{\theta}(z \mid x)q_{\phi}(z \mid x)}$$

Multiply top and bottom by $q_{\Phi}(z|x)$

Justin Johnson

Lecture 19 - 95

$$\log p_{\theta}(x) = \log \frac{p_{\theta}(x \mid z)p(z)}{p_{\theta}(z \mid x)} = \log \frac{p_{\theta}(x \mid z)p(z)q_{\phi}(z \mid x)}{p_{\theta}(z \mid x)q_{\phi}(z \mid x)}$$

$$= \log p_{\theta}(x|z) - \log \frac{q_{\phi}(z|x)}{p(z)} + \log \frac{q_{\phi}(z|x)}{p_{\theta}(z|x)}$$

Split up using rules for logarithms

$$\log p_{\theta}(x) = \log \frac{p_{\theta}(x \mid z)p(z)}{p_{\theta}(z \mid x)} = \log \frac{p_{\theta}(x \mid z)p(z)q_{\phi}(z \mid x)}{p_{\theta}(z \mid x)q_{\phi}(z \mid x)}$$



Split up using rules for logarithms

Justin Johnson

Lecture 19 - 97

$$\log p_{\theta}(x) = \log \frac{p_{\theta}(x \mid z)p(z)}{p_{\theta}(z \mid x)} = \log \frac{p_{\theta}(x \mid z)p(z)q_{\phi}(z \mid x)}{p_{\theta}(z \mid x)q_{\phi}(z \mid x)}$$

$$= \log p_{\theta}(x|z) - \log \frac{q_{\phi}(z|x)}{p(z)} + \log \frac{q_{\phi}(z|x)}{p_{\theta}(z|x)}$$

We can wrap in an expectation since it doesn't depend on z

$$\log p_{\theta}(x) = E_{z \sim q_{\phi}(z|x)}[\log p_{\theta}(x)]$$

Justin Johnson

 $\log p_{\theta}(x) = E_{z \sim q_{\phi}(z|x)}[\log p_{\theta}(x)]$

$$\log p_{\theta}(x) = \log \frac{p_{\theta}(x \mid z)p(z)}{p_{\theta}(z \mid x)} = \log \frac{p_{\theta}(x \mid z)p(z)q_{\phi}(z \mid x)}{p_{\theta}(z \mid x)q_{\phi}(z \mid x)}$$

$$= E_z[\log p_\theta(x|z)] - E_z\left[\log \frac{q_\phi(z|x)}{p(z)}\right] + E_z\left[\log \frac{q_\phi(z|x)}{p_\theta(z|x)}\right]$$

We can wrap in an expectation since it doesn't depend on z

$$\log p_{\theta}(x) = \log \frac{p_{\theta}(x \mid z)p(z)}{p_{\theta}(z \mid x)} = \log \frac{p_{\theta}(x \mid z)p(z)q_{\phi}(z \mid x)}{p_{\theta}(z \mid x)q_{\phi}(z \mid x)}$$

$$= E_z[\log p_\theta(x|z)] - E_z\left[\log \frac{q_\phi(z|x)}{p(z)}\right] + E_z\left[\log \frac{q_\phi(z|x)}{p_\theta(z|x)}\right]$$

 $= E_{z \sim q_{\phi}(z|x)}[\log p_{\theta}(x|z)] - D_{KL}(q_{\phi}(z|x), p(z)) + D_{KL}(q_{\phi}(z|x), p_{\theta}(z|x))$ Data reconstruction

Justin Johnson

$$\log p_{\theta}(x) = \log \frac{p_{\theta}(x \mid z)p(z)}{p_{\theta}(z \mid x)} = \log \frac{p_{\theta}(x \mid z)p(z)q_{\phi}(z \mid x)}{p_{\theta}(z \mid x)q_{\phi}(z \mid x)}$$

$$= E_z[\log p_\theta(x|z)] - E_z\left[\log \frac{q_\phi(z|x)}{p(z)}\right] + E_z\left[\log \frac{q_\phi(z|x)}{p_\theta(z|x)}\right]$$

 $= E_{z \sim q_{\phi}(z|x)}[\log p_{\theta}(x|z)] - D_{KL}(q_{\phi}(z|x), p(z)) + D_{KL}(q_{\phi}(z|x), p_{\theta}(z|x))$

KL divergence between prior, and samples from the encoder network

Justin Johnson

$$\log p_{\theta}(x) = \log \frac{p_{\theta}(x \mid z)p(z)}{p_{\theta}(z \mid x)} = \log \frac{p_{\theta}(x \mid z)p(z)q_{\phi}(z \mid x)}{p_{\theta}(z \mid x)q_{\phi}(z \mid x)}$$

$$= E_z[\log p_\theta(x|z)] - E_z\left[\log \frac{q_\phi(z|x)}{p(z)}\right] + E_z\left[\log \frac{q_\phi(z|x)}{p_\theta(z|x)}\right]$$

 $= E_{z \sim q_{\phi}(z|x)}[\log p_{\theta}(x|z)] - D_{KL}(q_{\phi}(z|x), p(z)) + D_{KL}(q_{\phi}(z|x), p_{\theta}(z|x))$

KL divergence between encoder and posterior of decoder

Lecture 19 - 102

Justin Johnson

$$\log p_{\theta}(x) = \log \frac{p_{\theta}(x \mid z)p(z)}{p_{\theta}(z \mid x)} = \log \frac{p_{\theta}(x \mid z)p(z)q_{\phi}(z \mid x)}{p_{\theta}(z \mid x)q_{\phi}(z \mid x)}$$

$$= E_z[\log p_\theta(x|z)] - E_z\left[\log \frac{q_\phi(z|x)}{p(z)}\right] + E_z\left[\log \frac{q_\phi(z|x)}{p_\theta(z|x)}\right]$$

 $= E_{z \sim q_{\phi}(z|x)} [\log p_{\theta}(x|z)] - D_{KL} \left(q_{\phi}(z|x), p(z) \right) + D_{KL} (q_{\phi}(z|x), p_{\theta}(z|x))$ KL is >= 0, so dropping this term gives a **lower bound** on the data likelihood:

March 28, 2022

Justin Johnson

$$\log p_{\theta}(x) = \log \frac{p_{\theta}(x \mid z)p(z)}{p_{\theta}(z \mid x)} = \log \frac{p_{\theta}(x \mid z)p(z)q_{\phi}(z \mid x)}{p_{\theta}(z \mid x)q_{\phi}(z \mid x)}$$

$$= E_z[\log p_\theta(x|z)] - E_z\left[\log \frac{q_\phi(z|x)}{p(z)}\right] + E_z\left[\log \frac{q_\phi(z|x)}{p_\theta(z|x)}\right]$$

 $= E_{z \sim q_{\phi}(z|x)}[\log p_{\theta}(x|z)] - D_{KL}(q_{\phi}(z|x), p(z)) + D_{KL}(q_{\phi}(z|x), p_{\theta}(z|x))$ $\log p_{\theta}(x) \ge E_{z \sim q_{\phi}(z|x)}[\log p_{\theta}(x|z)] - D_{KL}(q_{\phi}(z|x), p(z))$

Justin Johnson

Jointly train **encoder** q and **decoder** p to maximize the **variational lower bound** on the data likelihood Also called **Evidence Lower Bound (ELBo**)

$$\begin{split} \log p_{\theta}(x) \geq & E_{z \sim q_{\phi}(z|x)}[\log p_{\theta}(x|z)] - D_{KL}\left(q_{\phi}(z|x), p(z)\right) \\ & \text{Encoder Network} \end{split} \quad & \text{Decoder Network} \end{split}$$

 $q_{\phi}(z \mid x) = N(\mu_{z \mid x}, \Sigma_{z \mid x})$ $\mu_{z \mid x} \qquad \Sigma_{z \mid x}$

$$p_{\theta}(x \mid z) = N(\mu_{x|z}, \Sigma_{x|z})$$



Justin Johnson

Example: Fully-Connected VAE

x: 28x28 image, flattened to 784-dim vector z: 20-dim vector

Encoder Network

$$q_{\phi}(z \mid x) = N(\mu_{z \mid x}, \Sigma_{z \mid x})$$





$$p_{\theta}(x \mid z) = N(\mu_{x \mid z}, \Sigma_{x \mid z})$$



Justin Johnson

Lecture 19 - 106

Train by maximizing the **variational lower bound**

$$E_{z \sim q_{\phi}(z|x)}[\log p_{\theta}(x|z)] - D_{KL}\left(q_{\phi}(z|x), p(z)\right)$$



	lic	+i	n		0	h	n	c		n
J	u s			J	U			2	U	

Lecture 19 - 107

Train by maximizing the **variational lower bound**

$$E_{z \sim q_{\phi}(z|x)}[\log p_{\theta}(x|z)] - D_{KL}\left(q_{\phi}(z|x), p(z)\right)$$

1. Run input data through **encoder** to get a distribution over latent codes



March 28, 2022

Lecture 19 - 108

Justin Johnson
Train by maximizing the **variational lower bound**

$$E_{z \sim q_{\phi}(z|x)}[\log p_{\theta}(x|z)] - D_{KL}\left(q_{\phi}(z|x), p(z)\right)$$

1. Run input data through **encoder** to get a distribution over latent codes

Justin Johnson

2. Encoder output should match the prior p(z)!

Lecture 19 - 109



Train by maximizing the **variational lower bound**

$$E_{z \sim q_{\phi}(z|x)}[\log p_{\theta}(x|z)] - D_{KL}(q_{\phi}(z|x), p(z))$$

- Run input data through encoder to get a distribution over latent codes
- 2. Encoder output should match the prior p(z)!

$$-D_{KL}\left(q_{\phi}(z|x), p(z)\right) = \int_{Z} q_{\phi}(z|x) \log \frac{p(z)}{q_{\phi}(z|x)} dz$$
$$= \int_{Z} N(z; \mu_{z|x}, \Sigma_{z|x}) \log \frac{N(z; 0, I)}{N(z; \mu_{z|x}, \Sigma_{z|x})} dz$$
$$= \frac{1}{2} \sum_{j=1}^{J} \left(1 + \log \left(\left(\Sigma_{z|x}\right)_{j}^{2}\right) - \left(\mu_{z|x}\right)_{j}^{2} - \left(\Sigma_{z|x}\right)_{j}^{2}\right)$$

Closed form solution when q_{ϕ} is diagonal Gaussian and p is unit Gaussian! (Assume z has dimension J)



Justin Johnson

Lecture 19 - 110

Train by maximizing the variational lower bound

$$E_{z \sim q_{\phi}(z|x)}[\log p_{\theta}(x|z)] - D_{KL}\left(q_{\phi}(z|x), p(z)\right)$$

- 1. Run input data through **encoder** to get a distribution over latent codes
- 2. Encoder output should match the prior p(z)!

Lecture 19 - 111

3. Sample code z from encoder output

Justin Johnson



Train by maximizing the variational lower bound

$$E_{z \sim q_{\phi}(z|x)}[\log p_{\theta}(x|z)] - D_{KL}\left(q_{\phi}(z|x), p(z)\right)$$

- 1. Run input data through **encoder** to get a distribution over latent codes
- 2. Encoder output should match the prior p(z)!
- 3. Sample code z from encoder output
- 4. Run sampled code through **decoder** to get a distribution over data samples



Train by maximizing the **variational lower bound**

$$E_{z \sim q_{\phi}(z|x)}[\log p_{\theta}(x|z)] - D_{KL}\left(q_{\phi}(z|x), p(z)\right)$$

- 1. Run input data through **encoder** to get a distribution over latent codes
- 2. Encoder output should match the prior p(z)!
- 3. Sample code z from encoder output
- 4. Run sampled code through **decoder** to get a distribution over data samples
- 5. Original input data should be likely under the distribution output from (4)!



Train by maximizing the variational lower bound

$$E_{z \sim q_{\phi}(z|x)}[\log p_{\theta}(x|z)] - D_{KL}\left(q_{\phi}(z|x), p(z)\right)$$

- Run input data through **encoder** to get a 1. distribution over latent codes
- Encoder output should match the prior p(z)! 2.
- Sample code z from encoder output 3.
- Run sampled code through **decoder** to get a 4. distribution over data samples
- **Original input data should be likely under** 5. the distribution output from (4)!
- Can sample a reconstruction from (4) 6.



After training we can generate new data!

1. Sample z from prior p(z)



J	lust	in.	lo	hn	sor
-					•• •

After training we can generate new data!

- 1. Sample z from prior p(z)
- 2. Run sampled z through decoder to get distribution over data x



Justin Johnson

After training we can generate new data!

- 1. Sample z from prior p(z)
- 2. Run sampled z through decoder to get distribution over data x
- 3. Sample from distribution in (2) to generate data



Justin Johnson

Lecture 19 - 117

32x32 CIFAR-10



Labeled Faces in the Wild



Figures from (L) Dirk Kingma et al. 2016; (R) Anders Larsen et al. 2017.

Justin Johnson

Lecture 19 - 118

The diagonal prior on p(z) causes dimensions of z to be independent

"Disentangling factors of variation"

000000000000000000

Vary z₁

Vary z,

Kingma and Welling, Auto-Encoding Variational Beyes, ICLR 2014

Justin Johnson

Variational Autoencoders After training we can **edit images**

1. Run input data through **encoder** to get a distribution over latent codes

Justin Johnson



March 28, 2022

Variational Autoencoders After training we can **edit images**

- 1. Run input data through **encoder** to get a distribution over latent codes
- 2. Sample code z from encoder output

Justin Johnson



March 28, 2022

After training we can **edit images**

- 1. Run input data through **encoder** to get a distribution over latent codes
- 2. Sample code z from encoder output
- 3. Modify some dimensions of sampled code



March 28, 2022

Lecture 19 - 122

Justin Johnson

After training we can **edit images**

- 1. Run input data through **encoder** to get a distribution over latent codes
- 2. Sample code z from encoder output
- 3. Modify some dimensions of sampled code
- 4. Run modified z through **decoder** to get a distribution over data sample



After training we can **edit images**

- 1. Run input data through **encoder** to get a distribution over latent codes
- 2. Sample code z from encoder output
- 3. Modify some dimensions of sampled code
- 4. Run modified z through **decoder** to get a distribution over data samples
- 5. Sample new data from (4)





Variational Autoencoders: Image Editing



Original Reconstuction Light direction varied

Kulkarni et al, "Deep Convolutional Inverse Graphics Networks", NeurIPS 2014

Justin Johnson

Variational Autoencoder: Summary

Probabilistic spin to traditional autoencoders => allows generating data Defines an intractable density => derive and optimize a (variational) lower bound

Pros:

- Principled approach to generative models
- Allows inference of q(z|x), can be useful feature representation for other tasks

Cons:

- Maximizes lower bound of likelihood: okay, but not as good evaluation as PixelRNN/PixelCNN
- Samples blurrier and lower quality compared to state-of-the-art (GANs)

Active areas of research:

- More flexible approximations, e.g. richer approximate posterior instead of diagonal Gaussian, e.g., Gaussian Mixture Models (GMMs)
- Incorporating structure in latent variables, e.g., Categorical Distributions

Next Time: Generative Models, part 2

More Variational Autoencoders, Generative Adversarial Networks

Justin Johnson

Lecture 19 - 128