Lecture 9: Hardware and Software

Justin Johnson

Lecture 9 - 1

Assignment 3 Released

Assignment 3 is released! It covers:

- Fully-connected networks
- Dropout
- Update rules: SGD+Momentum, RMSprop, Adam
- Convolutional networks
- Batch normalization

Due Friday October 9, 11:59pm

(Website originally said 10/16 – this was a typo!)

Deep Learning Hardware

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Lecture 9 - 3

Inside a computer



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Inside a computer

GPU: "Graphics Processing Unit"



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Inside a computer

CPU: "Central Processing Unit"

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GPU: "Graphics Processing Unit"



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NVIDIA vs AND

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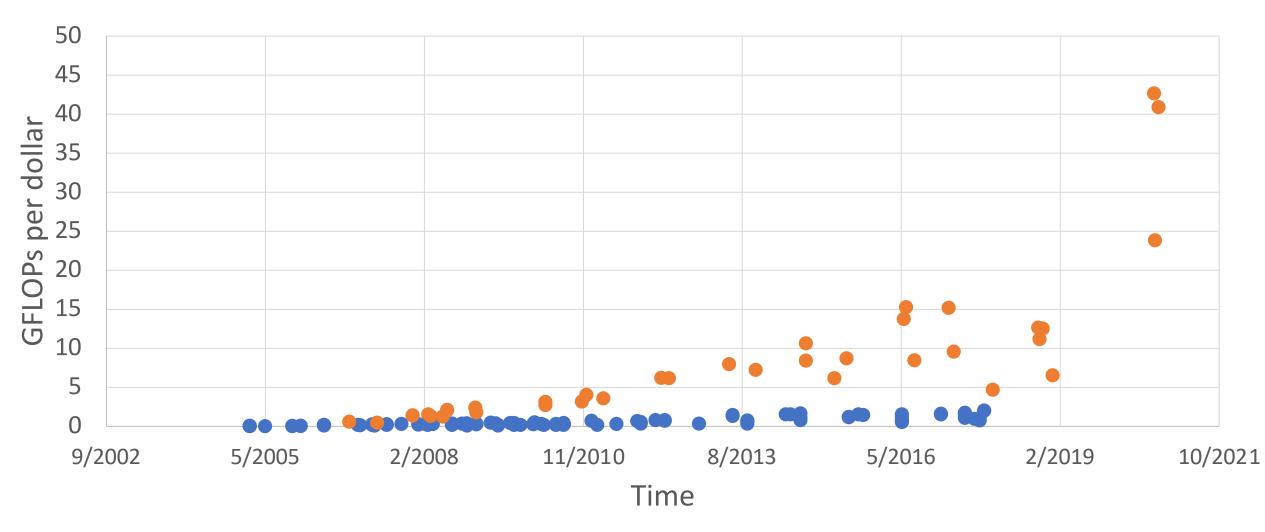
VS

AMD

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• CPU • GPU FP32



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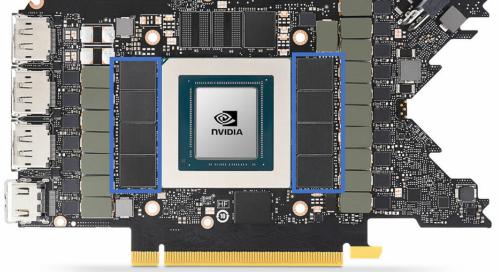
CPU vs GPU

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	Cores	Clock Speed (GHz)	Memory	Price	TFLOP/sec	CPU: Fewer cores, but each core is much faster and much more capable; great at sequential tasks GPU: More cores, but each core is much slower and "dumber"; great for parallel tasks
CPU Ryzen Threadripper 3970X	64 (128 threads with hyperthreading)	3.7 (4.5 boost)	System RAM	\$1999	~6.9 FP32	
GPU NVIDIA RTX 3090	10496	1.4 (1.7 boost)	24 GB GDDR6X	\$1499	~35.6 FP32	

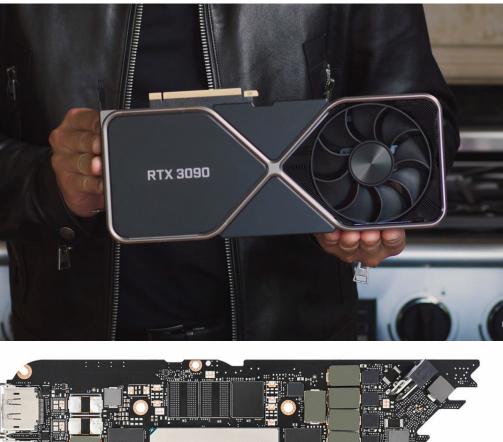
12x 2GB memory modules

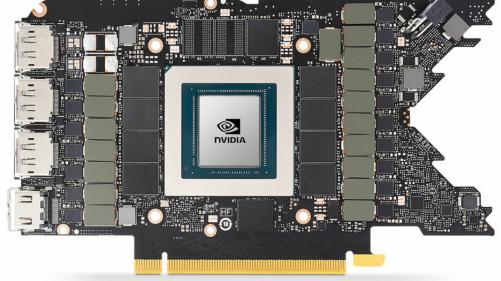




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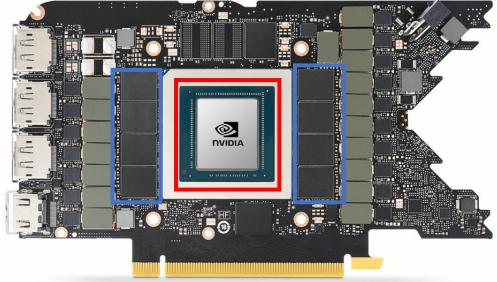
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12x 2GB memory modules

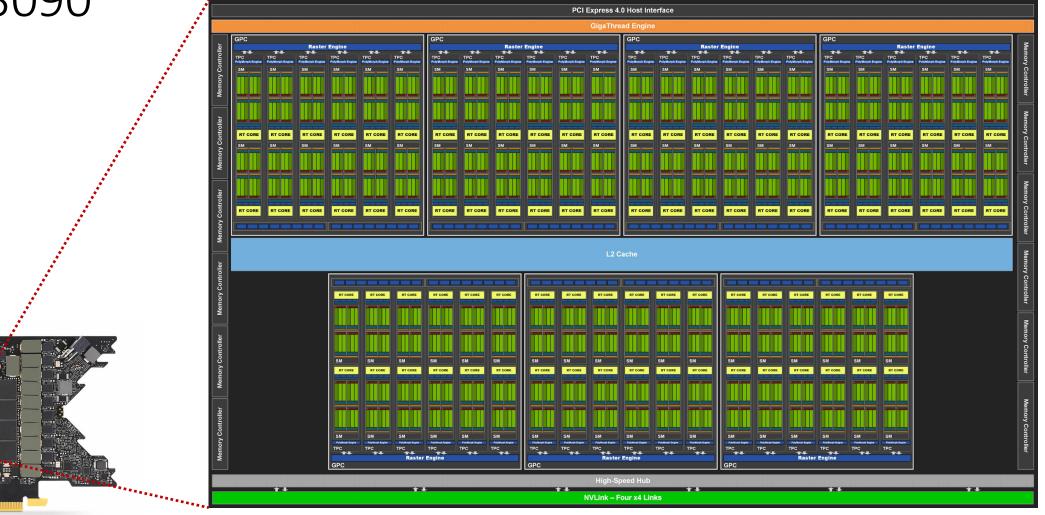
Processor





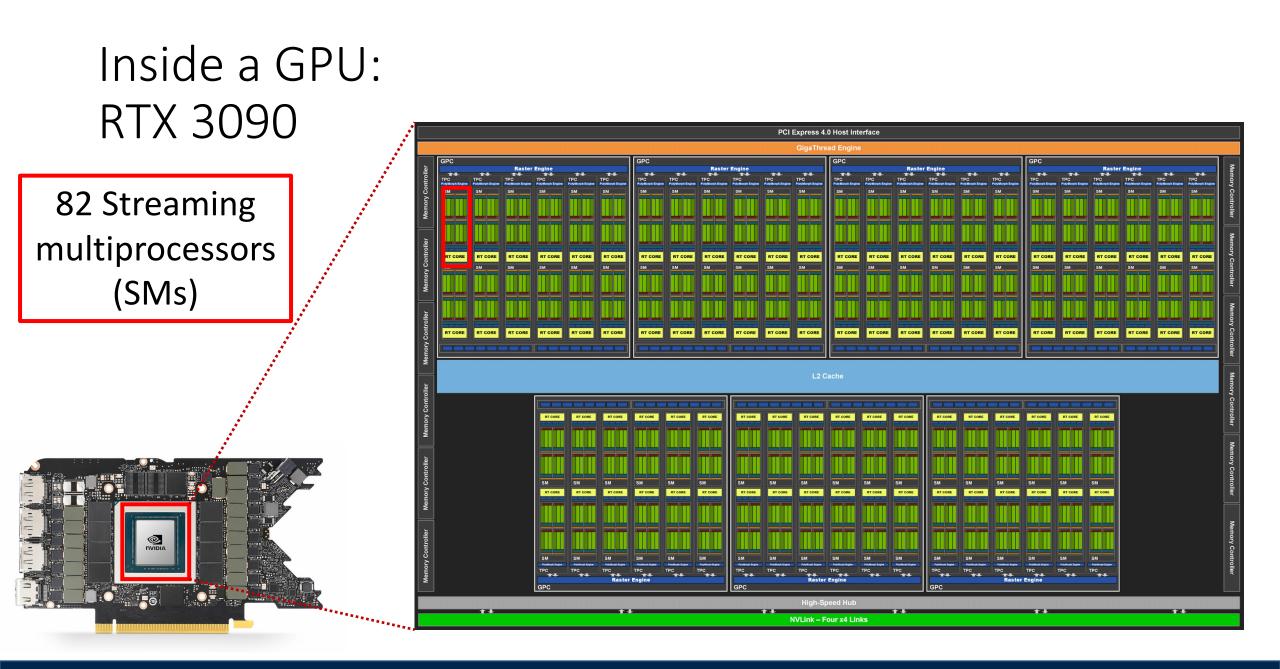
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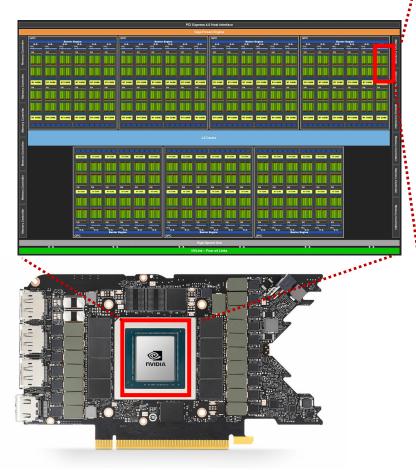
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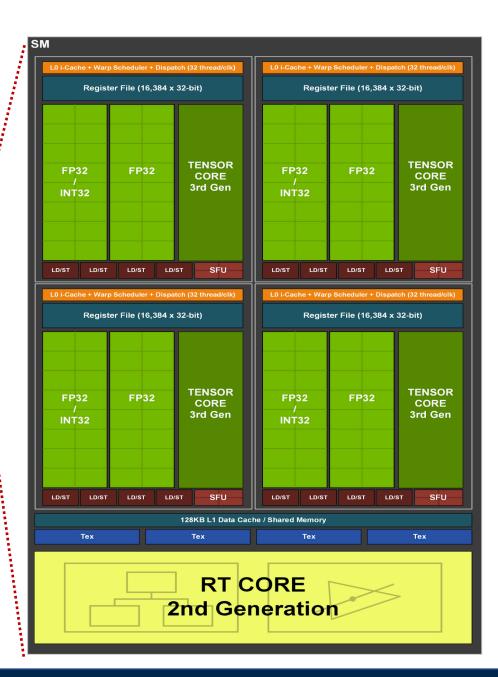
Lecture 8 - 14



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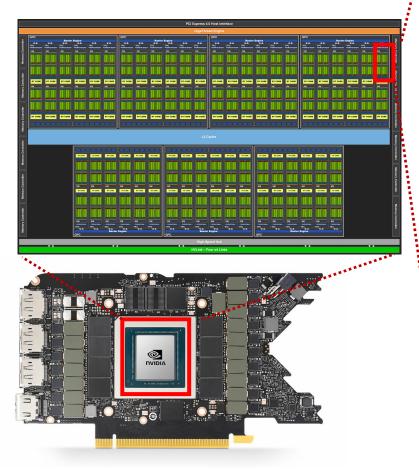
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Lecture 8 - 16



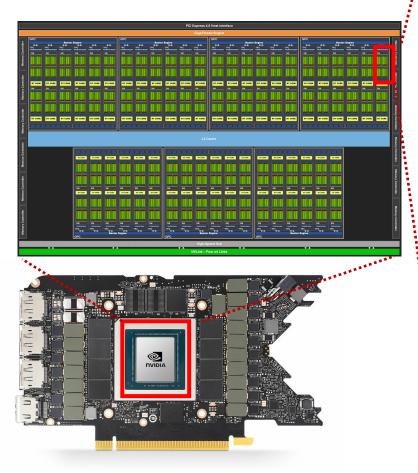


64 FP32 cores per SM

64 INT32/FP32 cores per SM

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64 FP32 cores per SM

64 INT32/FP32 cores per SM

35.6 FP32 TFLOP/sec

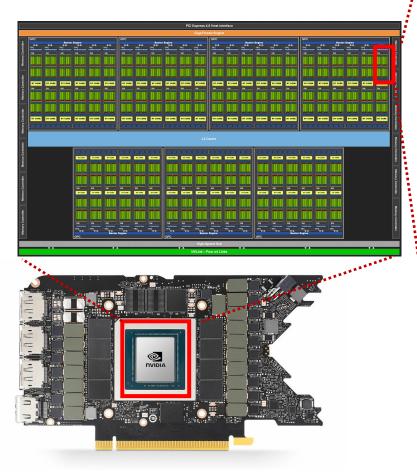
Multiply:

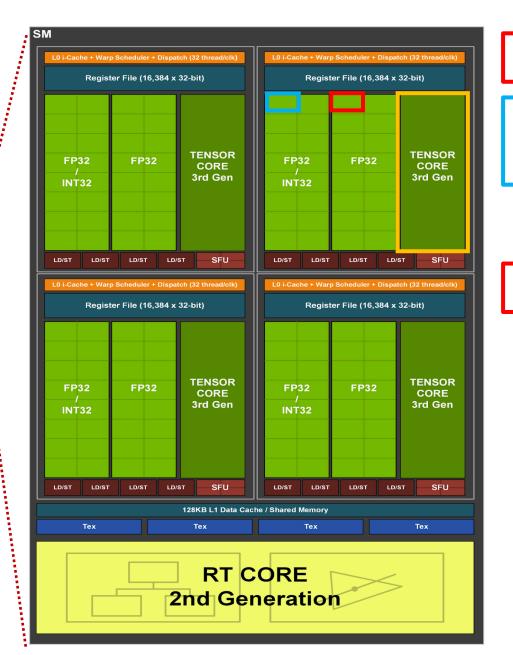
- 82 SM
- 128 FP32 core/SM
- 2 FLOP/cycle
- 1.7 GCycle / sec

= 35.6 TFLOP/sec

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64 FP32 cores per SM

64 INT32/FP32 cores per SM

35.6 FP32 TFLOP/sec

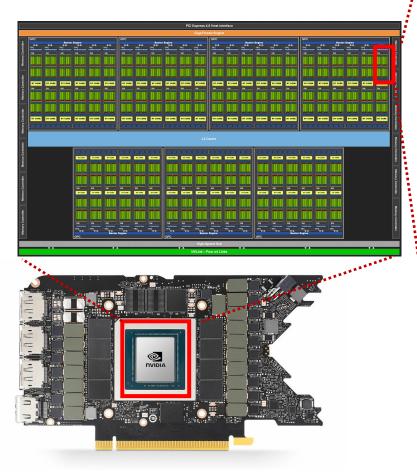
4 Tensor Core per SM

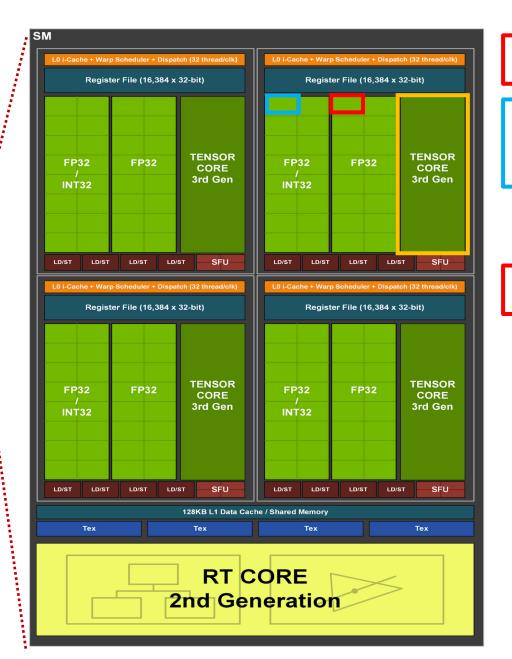
Special hardware!

Let A, B, C be matrices (A 4x4, B,C 4x8). Compute AB+C in one clock cycle (256 FLOP)

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64 FP32 cores per SM

64 INT32/FP32 cores per SM

35.6 FP32 TFLOP/sec

4 Tensor Core per SM

35.6 FP32 TFLOP/sec

Multiply:

- 82 SM
- 4 Tensor Core/SM
- 256 FLOP/cycle
- 1.7 GCycle / sec
- = 142 TFLOP/sec

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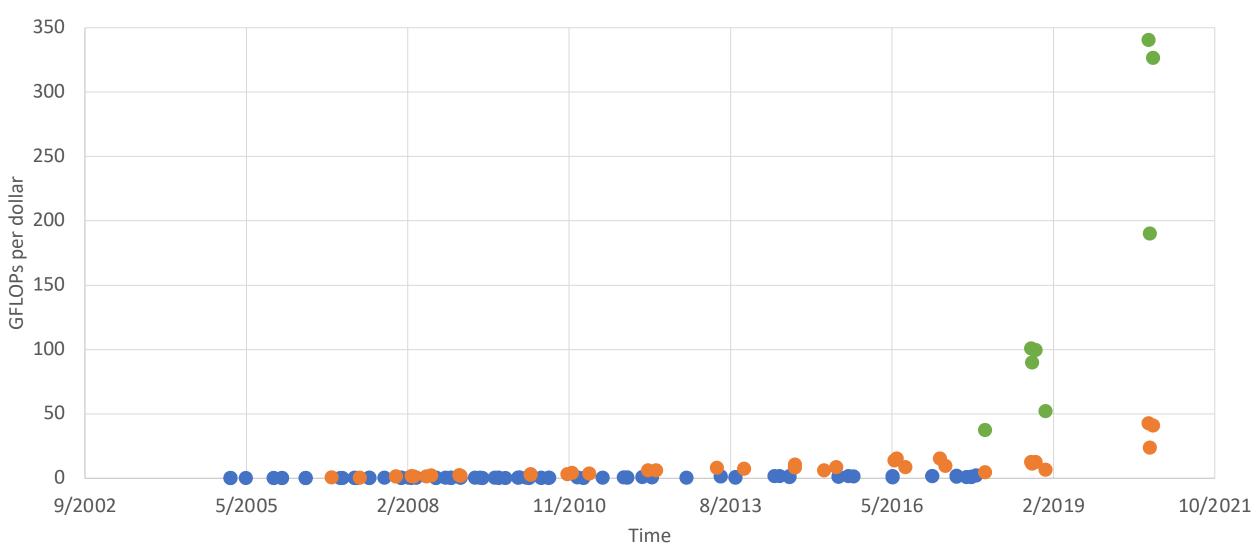
CPU vs GPU

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GPU NVIDIA RTX 3090	10496	1.4 (1.7 boost)	24 GB GDDR6X	\$1499	~35.6 FP32 ~142 TFLOP with Tensor core	

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GFLOPs per Dollar

● CPU ● GPU FP32 ● GPU Tensor Core



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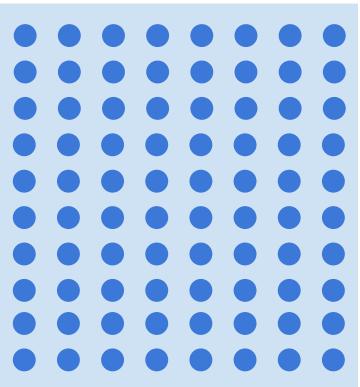
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Example: Matrix Multiplication

BxC A x B

Perfect for GPUs! All output elements are independent, can be trivially parallelized





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Programming GPUs

- CUDA (NVIDIA only)
 - Write C-like code that runs directly on the GPU
 - NVIDIA provides optimized APIs: cuBLAS, cuFFT, cuDNN, etc
- OpenCL
 - Similar to CUDA, but runs on anything
 - Usually slower on NVIDIA hardware
- EECS 598.009: Applied GPU Programming

Scaling up: Typically 8 GPUs per server



NVIDIA DGX-1: 8x V100 GPUs

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Special hardware for matrix multiplication, similar to NVIDIA Tensor Cores; also runs in mixed precision (bfloat16)

<u>Cloud TPU v2-8</u> 180 TFLOP/sec 64 GB HBM memory \$6 / hour (free on Colab!)

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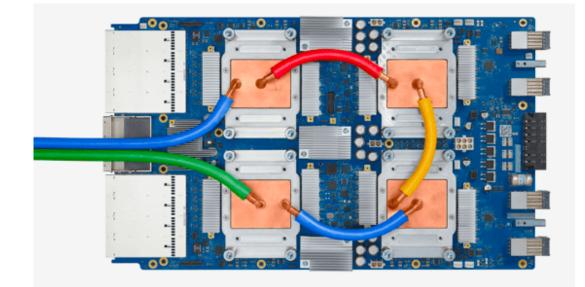


<u>Cloud TPU v2-8</u> 180 TFLOP/sec 64 GB HBM memory \$6 / hour (free on Colab!)

<u>Cloud TPU v2 Pod</u> 16x TPU-v2-8 11.5 PFLOPs \$384 / hour

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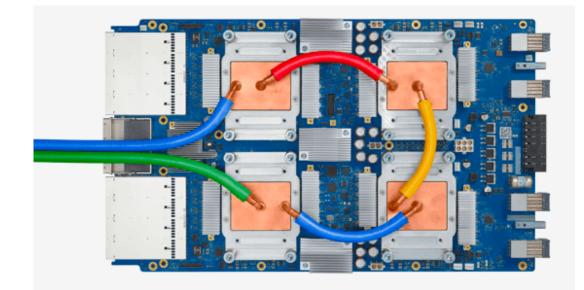


<u>Cloud TPU v3-8</u> 420 TFLOP/sec 128 GB HBM memory \$8 / hour

TPU-v3 image is released under a CC-SA 4.0 International license



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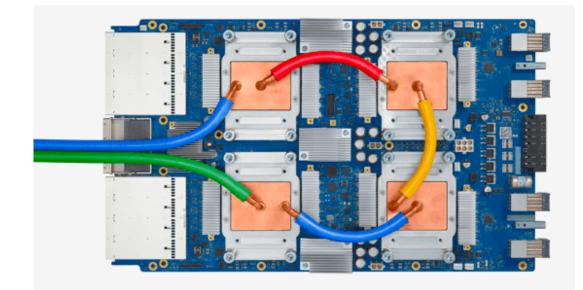




<u>Cloud TPU v3-8</u> 420 TFLOP/sec 128 GB HBM memory \$8 / hour <u>Cloud TPU v3 Pod</u> 256 TPU-v3 107 PFLOPs

TPU-v3 image is released under a CC-SA 4.0 International license

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<u>Cloud TPU v3-8</u> 420 TFLOP/sec 128 GB HBM memory \$8 / hour <u>Cloud TPU v3 Pod</u> 256 TPU-v3 107 PFLOPs **Contact sales rep for pricing**

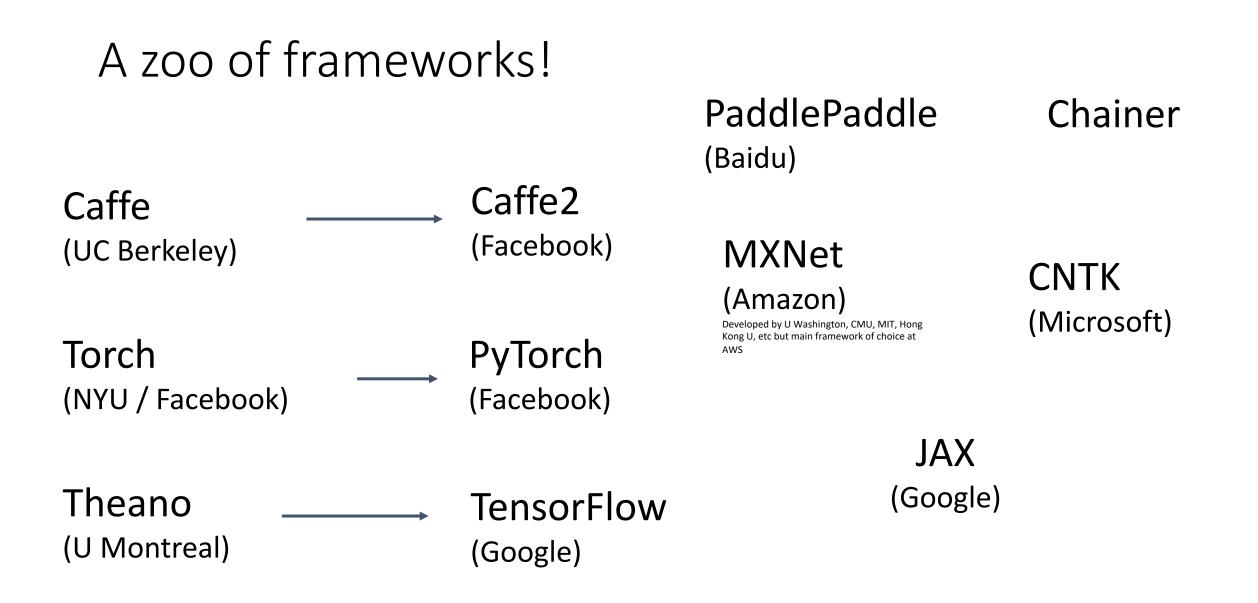
TPU-v3 image is released under a CC-SA 4.0 International license

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Deep Learning Software

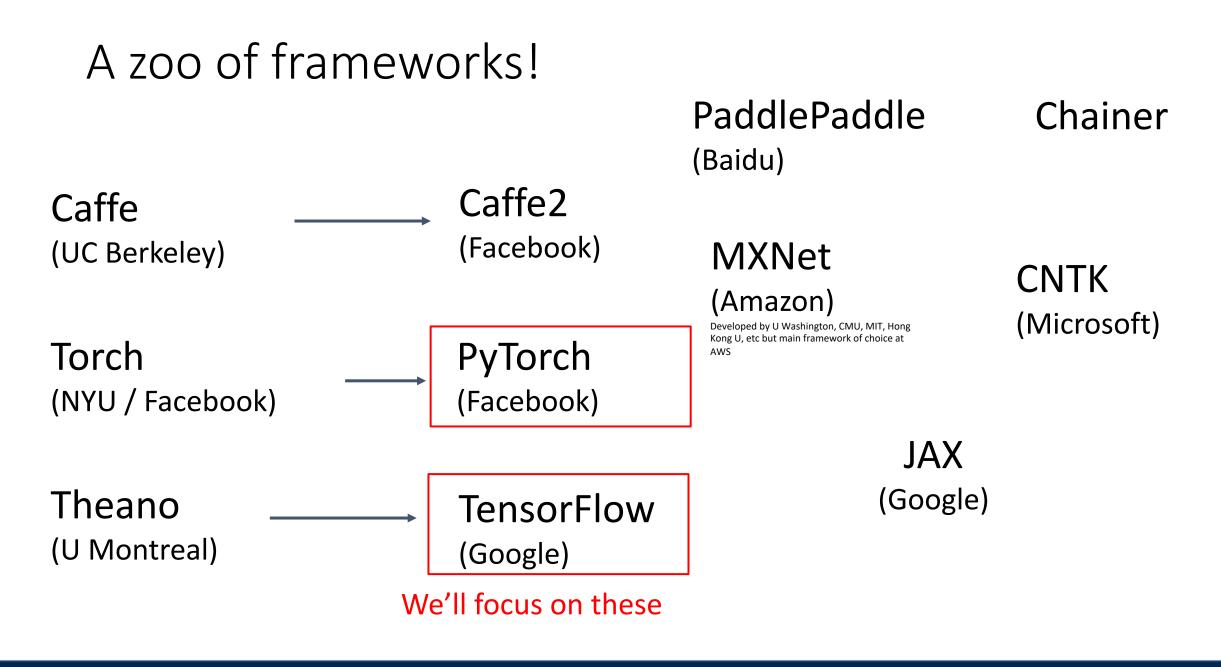
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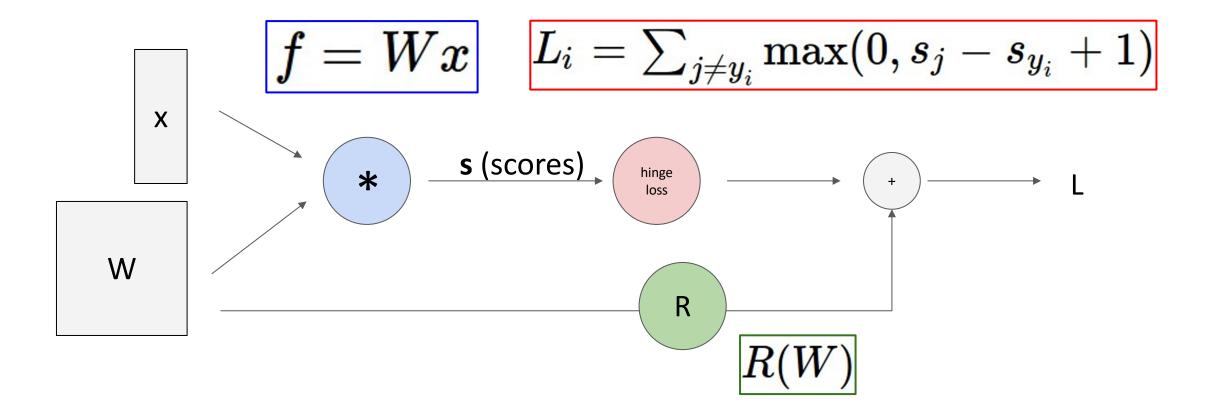
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Lecture 8 - 33

Recall: Computational Graphs



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Lecture 8 - 34

The point of deep learning frameworks

Allow rapid prototyping of new ideas
 Automatically compute gradients for you
 Run it all efficiently on GPU (or TPU)

PyTorch

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For this class we are using **PyTorch version 1.6** (Released July 2020)

Be careful if you are looking at older PyTorch code – the API changed a lot before 1.0 (0.3 to 0.4 had big changes!)

PyTorch: Fundamental Concepts

Tensor: Like a numpy array, but can run on GPU

Autograd: Package for building computational graphs out of Tensors, and automatically computing gradients

Module: A neural network layer; may store state or learnable weights

PyTorch: Fundamental Concepts

Tensor: Like a numpy array, but can run on GPU A1, A2, A3

Autograd: Package for building computational graphs out of Tensors, and automatically computing gradients

Module: A neural network layer; may store state or learnable weights

A4, A5, A6

Running example: Train a two-layer ReLU network on random data with L2 loss

```
import torch
```

```
device = torch.device('cpu')
```

N, D_in, H, D_out = 64, 1000, 100, 10 x = torch.randn(N, D_in, device=device) y = torch.randn(N, D_out, device=device) w1 = torch.randn(D_in, H, device=device) w2 = torch.randn(H, D_out, device=device)

```
learning rate = 1e-6
for t in range(500):
    h = x.mm(w1)
    h relu = h.clamp(min=0)
    y \text{ pred} = h \text{ relu.mm}(w2)
    loss = (y pred - y).pow(2).sum()
    grad y pred = 2.0 * (y \text{ pred} - y)
    grad w2 = h relu.t().mm(grad y pred)
    grad h relu = grad y pred.mm(w2.t())
    grad h = grad h relu.clone()
    grad h[h < 0] = 0
    grad w1 = x.t().mm(grad h)
    w1 -= learning rate * grad w1
    w2 -= learning rate * grad w2
```

Create random tensors for data and weights import torch

```
device = torch.device('cpu')
```

```
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in, device=device)
y = torch.randn(N, D_out, device=device)
w1 = torch.randn(D_in, H, device=device)
w2 = torch.randn(H, D_out, device=device)
```

```
learning rate = 1e-6
for t in range(500):
    h = x.mm(w1)
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    grad w2 = h relu.t().mm(grad y pred)
    grad h relu = grad y pred.mm(w2.t())
    grad h = grad h relu.clone()
    grad h[h < 0] = 0
    grad w1 = x.t().mm(grad h)
    w1 -= learning rate * grad w1
    w2 -= learning rate * grad w2
```

Forward pass: compute predictions and loss

import torch

device = torch.device('cpu')

```
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in, device=device)
y = torch.randn(N, D_out, device=device)
w1 = torch.randn(D_in, H, device=device)
w2 = torch.randn(H, D_out, device=device)
```

```
learning_rate = 1e-6
for t in range(500):
    h = x.mm(w1)
    h_relu = h.clamp(min=0)
    y_pred = h_relu.mm(w2)
    loss = (y_pred - y).pow(2).sum()
```

```
grad_y_pred = 2.0 * (y_pred - y)
grad_w2 = h_relu.t().mm(grad_y_pred)
grad_h_relu = grad_y_pred.mm(w2.t())
grad_h = grad_h_relu.clone()
grad_h[h < 0] = 0
grad_w1 = x.t().mm(grad_h)</pre>
```

```
w1 -= learning_rate * grad_w1
w2 -= learning_rate * grad_w2
```

September 29, 2020

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Backward pass: manually compute gradients

```
import torch
device = torch.device('cpu')
N, D in, H, D out = 64, 1000, 100, 10
x = torch.randn(N, D in, device=device)
y = torch.randn(N, D out, device=device)
w1 = torch.randn(D in, H, device=device)
w2 = torch.randn(H, D out, device=device)
learning rate = 1e-6
for t in range(500):
    h = x.mm(w1)
    h relu = h.clamp(min=0)
    y \text{ pred} = h \text{ relu.mm}(w2)
    loss = (y pred - y).pow(2).sum()
    grad y pred = 2.0 * (y \text{ pred} - y)
    grad w2 = h relu.t().mm(grad y pred)
    grad h relu = grad y pred.mm(w2.t())
    grad h = grad h relu.clone()
    grad h[h < 0] = 0
    grad w1 = x.t().mm(grad h)
```

```
w1 -= learning_rate * grad_w1
w2 -= learning_rate * grad_w2
```

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Gradient descent step on weights

import torch

```
device = torch.device('cpu')
```

```
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in, device=device)
y = torch.randn(N, D_out, device=device)
w1 = torch.randn(D_in, H, device=device)
w2 = torch.randn(H, D_out, device=device)
```

```
learning_rate = 1e-6
for t in range(500):
    h = x.mm(w1)
    h_relu = h.clamp(min=0)
    y_pred = h_relu.mm(w2)
    loss = (y_pred - y).pow(2).sum()

    grad_y_pred = 2.0 * (y_pred - y)
    grad_w2 = h_relu.t().mm(grad_y_pred)
    grad_h_relu = grad_y_pred.mm(w2.t())
    grad_h = grad_h_relu.clone()
    grad_w1 = x.t().mm(grad_h)

    w1 -= learning_rate * grad_w1
```

```
w2 -= learning_rate * grad_w2
```

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To run on GPU, just use a different device!

import torch

```
device = torch.device('cuda:0')
```

```
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in, device=device)
y = torch.randn(N, D_out, device=device)
w1 = torch.randn(D_in, H, device=device)
w2 = torch.randn(H, D_out, device=device)
```

```
learning rate = 1e-6
for t in range(500):
    h = x.mm(w1)
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    y \text{ pred} = h \text{ relu.mm}(w2)
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    grad h relu = grad y pred.mm(w2.t())
    grad h = grad h relu.clone()
    grad h[h < 0] = 0
    grad w1 = x.t().mm(grad h)
    w1 -= learning rate * grad w1
    w2 -= learning_rate * grad_w2
```

PyTorch: Autograd

Creating Tensors with requires_grad=True enables autograd

Operations on Tensors with requires_grad=True cause PyTorch to build a computational graph import torch

```
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
```

```
learning_rate = 1e-6
for t in range(500):
    y_pred = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y_pred - y).pow(2).sum()
```

```
loss.backward()
```

```
with torch.no_grad():
    w1 -= learning_rate * w1.grad
    w2 -= learning_rate * w2.grad
    w1.grad.zero_()
    w2.grad.zero_()
```

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```
PyTorch: Autograd
```

We will not want gradients (of loss) with respect to data

> Do want gradients with respect to weights

```
import torch
```

```
N, D in, H, D out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
```

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learning_rate = 1e-6
for t in range(500):
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```
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```

PyTorch: Autograd

import torch

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x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
```

Forward pass looks exactly the _ same as before, but we don't need to track intermediate values - PyTorch keeps track of them for us in the graph

```
for t in range(500):
    y_pred = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y pred - y).pow(2).sum()
```

```
loss.backward()
```

learning rate = 1e-6

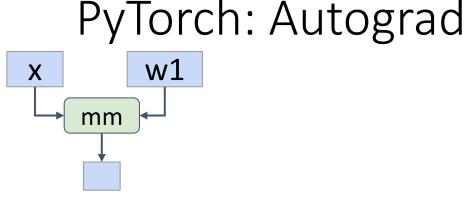
```
with torch.no_grad():
    w1 -= learning_rate * w1.grad
    w2 -= learning_rate * w2.grad
    w1.grad.zero_()
    w2.grad.zero_()
```

PyTorch: Autograd

Computes gradients with respect to all inputs that have requires grad=True! import torch

```
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D in, H, requires grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
learning rate = 1e-6
for t in range(500):
    y pred = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y pred - y).pow(2).sum()
    loss.backward()
    with torch.no grad():
        w1 -= learning rate * w1.grad
        w2 -= learning_rate * w2.grad
        wl.grad.zero ()
```

w2.grad.zero ()



Every operation on a tensor with requires_grad=True will add to the computational graph, and the resulting tensors will also have requires_grad=True import torch

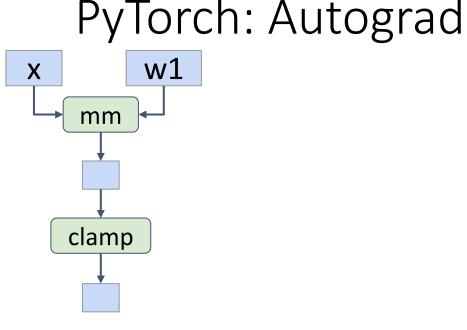
```
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x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
```

```
learning_rate = 1e-6
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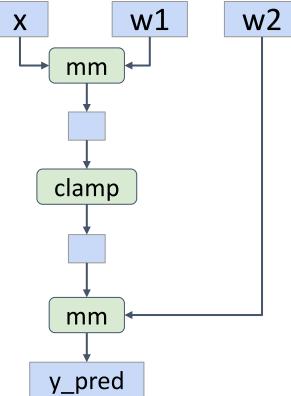
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x = torch.randn(N, D_in)
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import torch

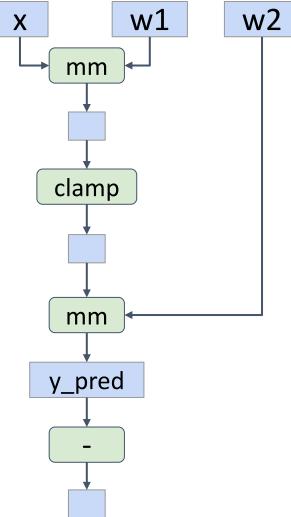
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import torch

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y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
```

```
learning_rate = 1e-6
for t in range(500):
    y_pred = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y_pred - y).pow(2).sum()
```

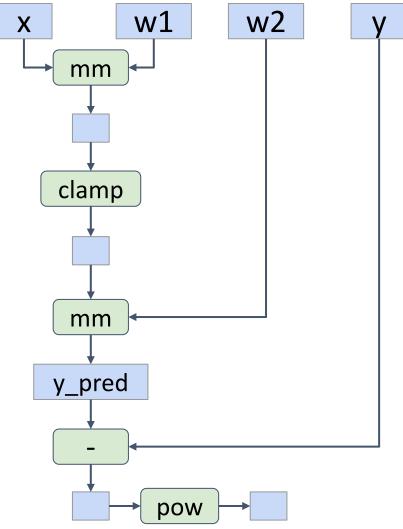
loss.backward()

```
with torch.no_grad():
    w1 -= learning_rate * w1.grad
    w2 -= learning_rate * w2.grad
    w1.grad.zero_()
    w2.grad.zero_()
```

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Lecture 8 - 53

PyTorch: Autograd



import torch

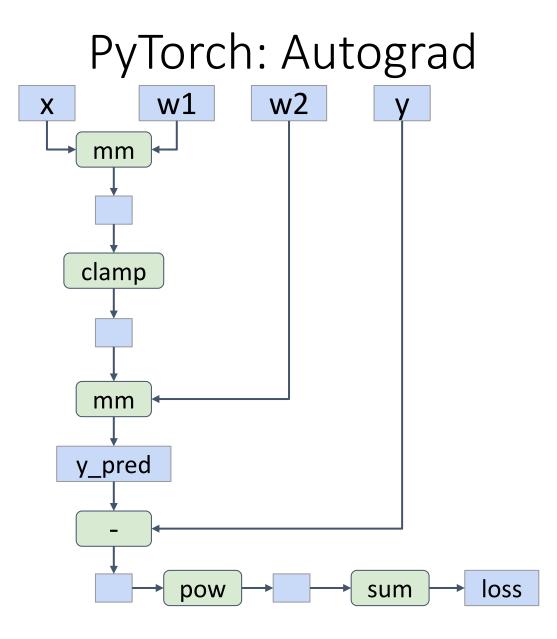
```
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
```

```
learning_rate = 1e-6
for t in range(500):
    y_pred = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y_pred - y).pow(2).sum()
```

loss.backward()

```
with torch.no_grad():
    w1 -= learning_rate * w1.grad
    w2 -= learning_rate * w2.grad
    w1.grad.zero_()
    w2.grad.zero_()
```

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import torch

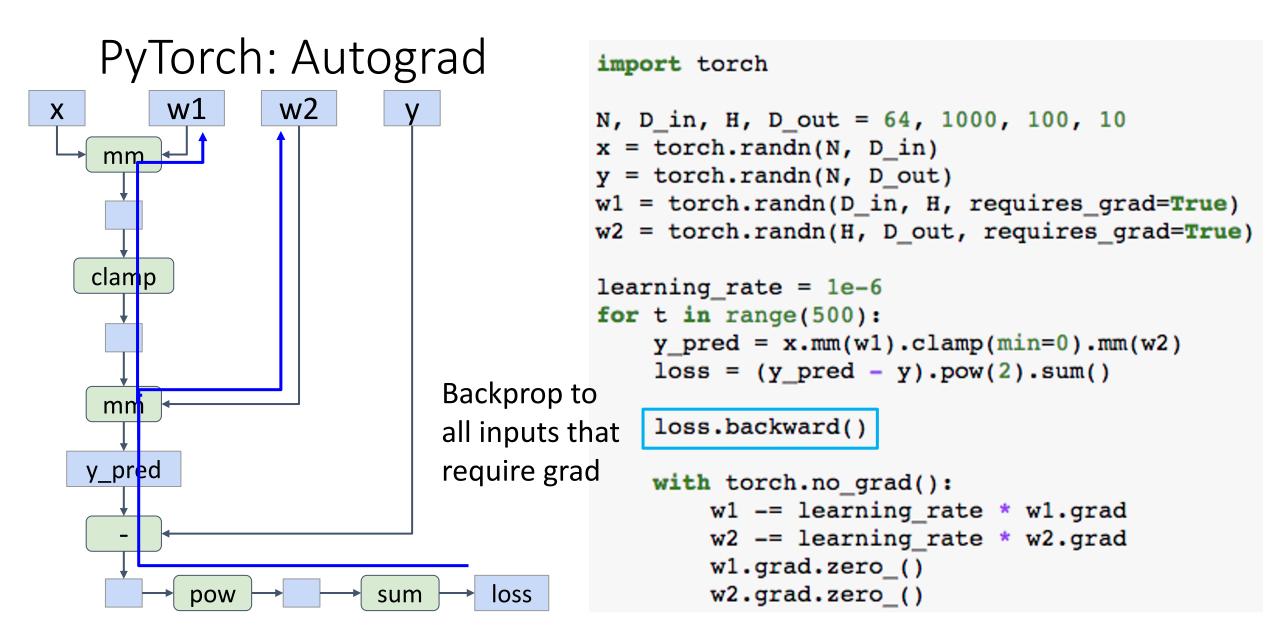
```
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
```

```
learning_rate = 1e-6
for t in range(500):
    y_pred = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y_pred - y).pow(2).sum()
```

```
loss.backward()
```

```
with torch.no_grad():
    w1 -= learning_rate * w1.grad
    w2 -= learning_rate * w2.grad
    w1.grad.zero_()
    w2.grad.zero_()
```

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Lecture 8 - 56



Χ

w1

w2

After backward finishes, gradients are accumulated into w1.grad and w2.grad and the graph is destroyed

import torch

```
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D in)
y = torch.randn(N, D_out)
w1 = torch.randn(D in, H, requires grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
```

```
learning rate = 1e-6
for t in range(500):
    y \text{ pred} = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y pred - y).pow(2).sum()
```

loss.backward()

```
with torch.no_grad():
    w1 -= learning_rate * w1.grad
    w2 -= learning_rate * w2.grad
    wl.grad.zero ()
    w2.grad.zero ()
```

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Lecture 8 - 57

PyTorch: Autograd

Χ

w1

w2

.

After backward finishes, gradients are **accumulated** into w1.grad and w2.grad and the graph is destroyed

Make gradient step on weights

import torch

```
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
```

```
learning_rate = 1e-6
for t in range(500):
    y_pred = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y_pred - y).pow(2).sum()
```

loss.backward()

with torch.no_grad(): w1 -= learning_rate * w1.grad w2 -= learning_rate * w2.grad w1.grad.zero_() w2.grad.zero_()

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Lecture 8 - 58



Χ

X |

w1

w2

After backward finishes, gradients are **accumulated** into w1.grad and w2.grad and the graph is destroyed

Set gradients to zero – forgetting this is a common bug!

import torch

```
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
```

```
learning_rate = 1e-6
for t in range(500):
    y_pred = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y_pred - y).pow(2).sum()
```

loss.backward()

```
with torch.no_grad():
    w1 -= learning_rate * w1.grad
    w2 -= learning_rate * w2.grad
    w1.grad.zero_()
    w2.grad.zero ()
```

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PyTorch: Autograd

Χ

w2

w1

After backward finishes, gradients are **accumulated** into w1.grad and w2.grad and the graph is destroyed

Tell PyTorch not to build a graph for these operations

import torch

```
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
```

```
learning_rate = 1e-6
for t in range(500):
    y_pred = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y pred - y).pow(2).sum()
```

loss.backward()

with torch.no_grad(): w1 -= learning_rate * w1.grad w2 -= learning_rate * w2.grad w1.grad.zero_() w2.grad.zero ()

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Lecture 8 - 60

Can define new operations using Python functions

def sigmoid(x):
 return 1.0 / (1.0 + (-x).exp())

```
import torch
N, D in, H, D out = 64, 1000, 100, 10
x = torch.randn(N, D in)
y = torch.randn(N, D out)
y = torch.randn(N, D out)
w1 = torch.randn(D in, H, requires grad=True)
w2 = torch.randn(H, D out, requires grad=True)
learning rate = 1e-6
for t in range(500):
  y pred = sigmoid(x.mm(w1)).mm(w2)
  loss = (y pred - y).pow(2).sum()
  loss.backward()
  if t % 50 == 0:
    print(t, loss.item())
  with torch.no grad():
    w1 -= learning_rate * w1.grad
   w2 -= learning rate * w2.grad
   wl.grad.zero ()
   w2.grad.zero ()
```

September 29, 2020

Justin Johnson

Can define new operations using Python functions

def sigmoid(x):
 return 1.0 / (1.0 + (-x).exp())

When our function runs, it will add to the graph

Gradients computed with autograd

1.0

import torch

```
N, D in, H, D out = 64, 1000, 100, 10
x = torch.randn(N, D in)
y = torch.randn(N, D out)
y = torch.randn(N, D out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D out, requires grad=True)
learning rate = 1e-6
for t in range(500):
 y pred = sigmoid(x.mm(w1)).mm(w2)
  loss = (y pred - y).pow(2).sum()
  loss.backward()
  if t % 50 == 0:
    print(t, loss.item())
  with torch.no grad():
    w1 -= learning rate * w1.grad
    w2 -= learning rate * w2.grad
   wl.grad.zero ()
    w2.grad.zero ()
```

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+1

Χ

* -1

exp

Can define new operations using Python functions

```
def sigmoid(x):
    return 1.0 / (1.0 + (-x).exp())
```

When our function runs, it will add to the graph

Gradients computed with autograd

1.0

Define new autograd operators by subclassing Function, define forward and backward

```
class Sigmoid(torch.autograd.Function):
  @staticmethod
  def forward(ctx, x):
    y = 1.0 / (1.0 + (-x).exp())
    ctx.save_for_backward(y)
    return y
```

```
@staticmethod
def backward(ctx, grad_y):
    y, = ctx.saved_tensors
    grad_x = grad_y * y * (1.0 - y)
    return grad_x
```

def sigmoid(x):
 return Sigmoid.apply(x)

Recall:

$$\frac{\partial}{\partial x} \Big[\sigma(x) \Big] = (1 - \sigma(x)) \sigma(x)$$

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+1

Χ

* -1

exp

Lecture 8 - 63

Can define new operations using Python functions

```
def sigmoid(x):
    return 1.0 / (1.0 + (-x).exp())
```

When our function runs, it will add to the graph

Gradients computed with autograd

1.0

```
Define new autograd operators
by subclassing Function, define
forward and backward
```

```
class Sigmoid(torch.autograd.Function):
@staticmethod
def forward(ctx, x):
    y = 1.0 / (1.0 + (-x).exp())
    ctx.save_for_backward(y)
    return y
```

```
@staticmethod
def backward(ctx, grad_y):
    y, = ctx.saved_tensors
    grad_x = grad_y * y * (1.0 - y)
    return grad_x
```

```
def sigmoid(x):
    return Sigmoid.apply(x)
```

Now when our function runs, it adds one node to the graph!



+1

Χ

exp

Lecture 8 - 64

Can define new operations using Python functions

```
def sigmoid(x):
    return 1.0 / (1.0 + (-x).exp())
```

When our function runs, it will add to the graph

Gradients computed with autograd

1.0

Define new autograd operators by subclassing Function, define forward and backward

```
class Sigmoid(torch.autograd.Function):
  @staticmethod
  def forward(ctx, x):
    y = 1.0 / (1.0 + (-x).exp())
    ctx.save_for_backward(y)
    return y
  @staticmethod
```

```
def backward(ctx, grad_y):
    y, = ctx.saved_tensors
    grad_x = grad_y * y * (1.0 - y)
    return grad_x
```

def sigmoid(x):
 return Sigmoid.apply(x)

In practice this is pretty rare – in most cases Python functions are good enough

+1

Χ

exp

PyTorch: nn

Higher-level wrapper for working with neural nets

Use this! It will make your life easier

import torch

```
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
```

```
model = torch.nn.Sequential(
    torch.nn.Linear(D_in, H),
    torch.nn.ReLU(),
    torch.nn.Linear(H, D_out))
```

```
learning_rate = 1e-2
for t in range(500):
    y_pred = model(x)
    loss = torch.nn.functional.mse_loss(y_pred, y)
```

```
loss.backward()
```

```
with torch.no_grad():
    for param in model.parameters():
        param -= learning_rate * param.grad
model.zero_grad()
```

PyTorch: nn

Object-oriented API: Define model object as sequence of layers objects, each of which holds weight tensors import torch

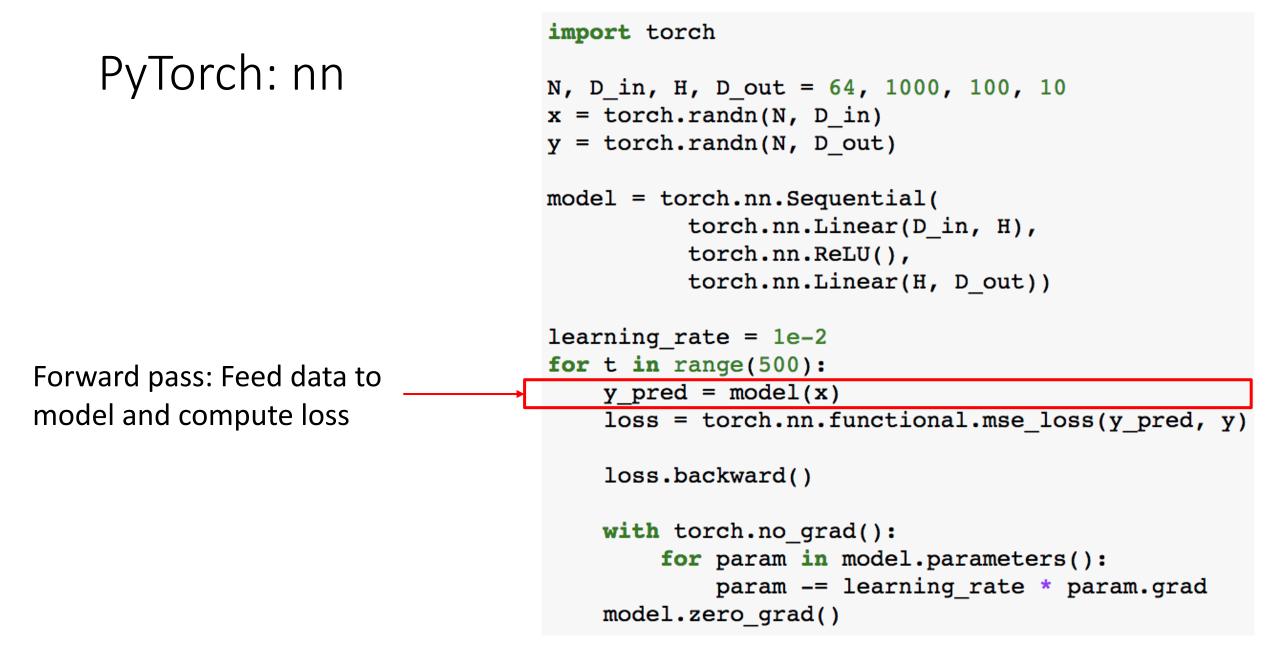
```
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
```

```
model = torch.nn.Sequential(
    torch.nn.Linear(D_in, H),
    torch.nn.ReLU(),
    torch.nn.Linear(H, D_out))
```

```
learning_rate = 1e-2
for t in range(500):
    y_pred = model(x)
    loss = torch.nn.functional.mse_loss(y_pred, y)
    loss.backward()
    with torch.no_grad():
        for param in model.parameters():
            param -= learning_rate * param.grad
    model.zero_grad()
```

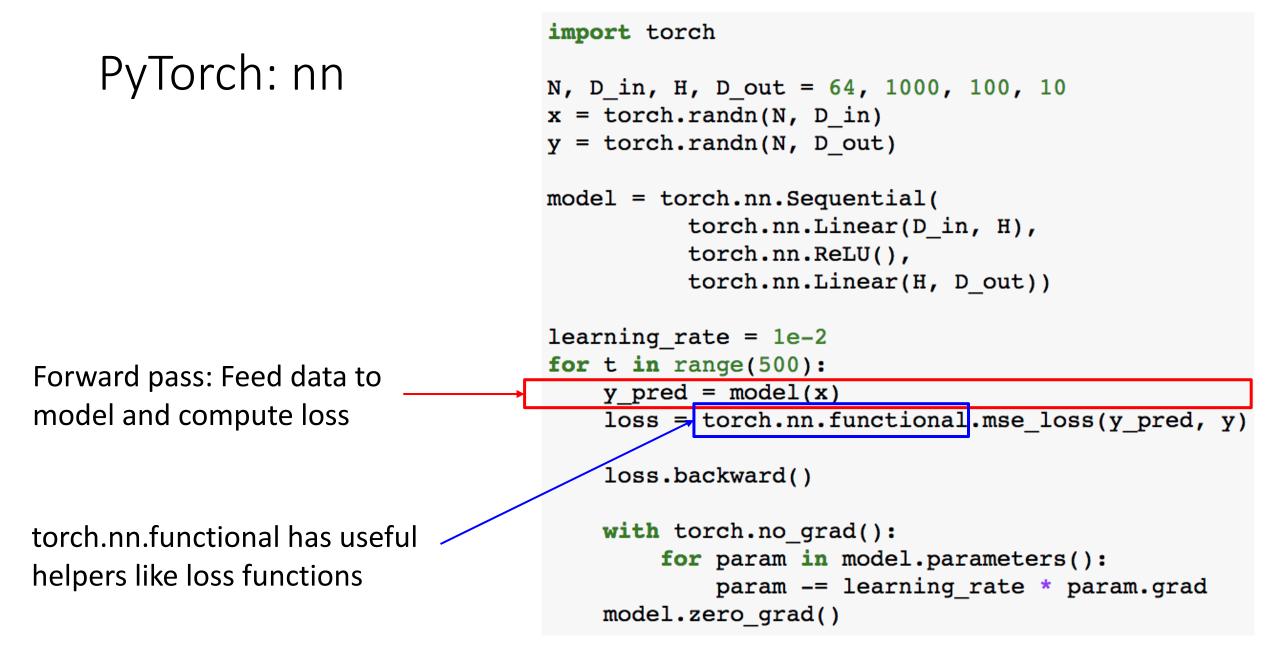
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Lecture 8 - 67



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Lecture 8 - 68



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Lecture 8 - 69

PyTorch: nn

Backward pass: compute gradient with respect to all model weights (they have requires_grad=True) import torch

```
N, D_{in}, H, D_{out} = 64, 1000, 100, 10
x = torch.randn(N, D in)
y = torch.randn(N, D out)
model = torch.nn.Sequential(
          torch.nn.Linear(D in, H),
          torch.nn.ReLU(),
          torch.nn.Linear(H, D out))
learning rate = 1e-2
for t in range(500):
    y \text{ pred} = \text{model}(x)
    loss = torch.nn.functional.mse loss(y pred, y)
    loss.backward()
    with torch.no grad():
        for param in model.parameters():
            param -= learning rate * param.grad
    model.zero grad()
```

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Lecture 8 - 70

PyTorch: nn

import torch

```
N, D_{in}, H, D_{out} = 64, 1000, 100, 10
x = torch.randn(N, D in)
y = torch.randn(N, D out)
model = torch.nn.Sequential(
          torch.nn.Linear(D in, H),
          torch.nn.ReLU(),
          torch.nn.Linear(H, D out))
learning rate = 1e-2
for t in range(500):
    y \text{ pred} = \text{model}(x)
    loss = torch.nn.functional.mse loss(y pred, y)
    loss.backward()
    with torch.no grad():
        for param in model.parameters():
            param -= learning rate * param.grad
    model.zero grad()
```

Make gradient step on each model parameter -(with gradients disabled)

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Lecture 8 - 71

```
import torch
    PyTorch: optim
                                      N, D in, H, D out = 64, 1000, 100, 10
                                      x = torch.randn(N, D_in)
                                      y = torch.randn(N, D out)
                                      model = torch.nn.Sequential(
                                                torch.nn.Linear(D in, H),
                                                 torch.nn.ReLU(),
                                                torch.nn.Linear(H, D_out))
                                      learning rate = 1e-4
Use an optimizer for
                                      optimizer = torch.optim.Adam(model.parameters(),
                                                                    lr=learning rate)
different update rules
                                      for t in range(500):
                                          y \text{ pred} = \text{model}(x)
                                          loss = torch.nn.functional.mse_loss(y_pred, y)
                                          loss.backward()
                                          optimizer.step()
                                          optimizer.zero grad()
```

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Lecture 8 - 72

PyTorch: optim

import torch

```
N, D in, H, D out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D out)
model = torch.nn.Sequential(
          torch.nn.Linear(D_in, H),
          torch.nn.ReLU(),
          torch.nn.Linear(H, D out))
learning_rate = 1e-4
optimizer = torch.optim.Adam(model.parameters(),
                               lr=learning rate)
for t in range(500):
    y \text{ pred} = \text{model}(x)
    loss = torch.nn.functional.mse loss(y pred, y)
    loss.backward()
    optimizer.step()
    optimizer.zero_grad()
```

After computing gradients, use optimizer to ⁻ update and zero gradients

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Lecture 8 - 73

PyTorch: nn Defining Modules

A PyTorch **Module** is a neural net layer; it inputs and outputs Tensors

Modules can contain weights or other modules

Very common to define your own models or layers as custom Modules

```
class TwoLayerNet(torch.nn.Module):
    def __init__(self, D_in, H, D_out):
        super(TwoLayerNet, self).__init__()
        self.linear1 = torch.nn.Linear(D_in, H)
        self.linear2 = torch.nn.Linear(H, D_out)
```

```
def forward(self, x):
    h_relu = self.linear1(x).clamp(min=0)
    y_pred = self.linear2(h_relu)
    return y_pred
```

```
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
```

```
model = TwoLayerNet(D_in, H, D_out)
```

```
optimizer = torch.optim.SGD(model.parameters(), lr=1e-4)
for t in range(500):
    y_pred = model(x)
    loss = torch.nn.functional.mse_loss(y_pred, y)
```

```
loss.backward()
optimizer.step()
optimizer.zero_grad()
```

PyTorch: nn Defining Modules

Define our whole model as a single Module

import torch

```
class TwoLayerNet(torch.nn.Module):
    def init (self, D in, H, D out):
        super(TwoLayerNet, self). init ()
        self.linear1 = torch.nn.Linear(D in, H)
        self.linear2 = torch.nn.Linear(H, D out)
    def forward(self, x):
        h relu = self.linear1(x).clamp(min=0)
        y pred = self.linear2(h relu)
        return y pred
N, D in, H, D out = 64, 1000, 100, 10
x = torch.randn(N, D in)
y = torch.randn(N, D out)
model = TwoLayerNet(D in, H, D out)
optimizer = torch.optim.SGD(model.parameters(), lr=1e-4)
for t in range(500):
    y \text{ pred} = \text{model}(x)
    loss = torch.nn.functional.mse loss(y pred, y)
    loss.backward()
    optimizer.step()
```

optimizer.zero_grad()

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Lecture 8 - 75

PyTorch: nn Defining Modules

Initializer sets up two children (Modules can contain modules)

```
class TwoLayerNet(torch.nn.Module):
```

```
def __init__(self, D_in, H, D_out):
    super(TwoLayerNet, self).__init__()
    self.linear1 = torch.nn.Linear(D_in, H)
    self.linear2 = torch.nn.Linear(H, D_out)
```

```
def forward(self, x):
    h_relu = self.linear1(x).clamp(min=0)
    y_pred = self.linear2(h_relu)
    return y_pred
```

```
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D out)
```

```
model = TwoLayerNet(D_in, H, D_out)
```

```
optimizer = torch.optim.SGD(model.parameters(), lr=1e-4)
for t in range(500):
    y_pred = model(x)
    loss = torch.nn.functional.mse_loss(y_pred, y)
```

```
loss.backward()
optimizer.step()
optimizer.zero_grad()
```

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Lecture 8 - 76

PyTorch: nn Defining Modules

Define forward pass using child modules and tensor operations

No need to define backward autograd will handle it

```
class TwoLayerNet(torch.nn.Module):
    def __init__(self, D_in, H, D_out):
        super(TwoLayerNet, self).__init__()
        self.linear1 = torch.nn.Linear(D_in, H)
        self.linear2 = torch.nn.Linear(H, D_out)
```

```
def forward(self, x):
    h_relu = self.linear1(x).clamp(min=0)
    y_pred = self.linear2(h_relu)
    return y_pred
```

```
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
```

```
model = TwoLayerNet(D_in, H, D_out)
```

```
optimizer = torch.optim.SGD(model.parameters(), lr=1e-4)
for t in range(500):
    y_pred = model(x)
    loss = torch.nn.functional.mse_loss(y_pred, y)
```

```
loss.backward()
optimizer.step()
optimizer.zero_grad()
```

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Lecture 8 - 77

PyTorch: nn Defining Modules

Very common to mix and match custom Module subclasses and Sequential containers

```
class ParallelBlock(torch.nn.Module):
    def __init__(self, D_in, D_out):
        super(ParallelBlock, self).__init__()
        self.linear1 = torch.nn.Linear(D_in, D_out)
        self.linear2 = torch.nn.Linear(D_in, D_out)
    def forward(self, x):
        h1 = self.linear1(x)
        h2 = self.linear2(x)
        return (h1 * h2).clamp(min=0)
N, D_in, H, D_out = 64, 1000, 100, 10
    x = torch.randn(N, D_in)
```

```
y = torch.randn(N, D_out)
```

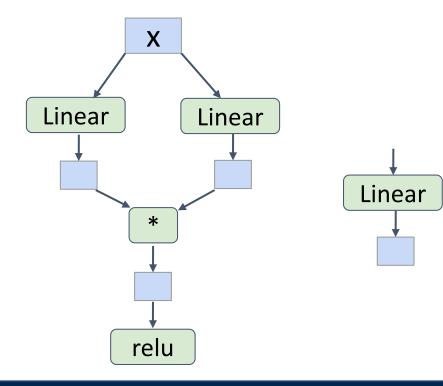
```
optimizer = torch.optim.Adam(model.parameters(), lr=1e-4)
for t in range(500):
    y_pred = model(x)
    loss = torch.nn.functional.mse_loss(y_pred, y)
    loss.backward()
    optimizer.step()
    optimizer.zero grad()
```

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Lecture 8 - 78

PyTorch: nn Defining Modules

Define network component as a Module subclass



import torch

```
class ParallelBlock(torch.nn.Module):
    def __init__(self, D_in, D_out):
        super(ParallelBlock, self).__init__()
        self.linear1 = torch.nn.Linear(D_in, D_out)
        self.linear2 = torch.nn.Linear(D_in, D_out)
    def forward(self, x):
        h1 = self.linear1(x)
        h2 = self.linear2(x)
        return (h1 * h2).clamp(min=0)
```

```
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
```

```
optimizer = torch.optim.Adam(model.parameters(), lr=1e-4)
for t in range(500):
    y_pred = model(x)
    loss = torch.nn.functional.mse_loss(y_pred, y)
    loss.backward()
    optimizer.step()
    optimizer.zero grad()
```

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Lecture 8 - 79

PyTorch: nn Defining Modules

Stack multiple instances of the component in a sequential

Very easy to quickly build complex network architectures!

```
x
Linear
Linear
relu
X
Linear
Linear
relu
Linear
```

```
class ParallelBlock(torch.nn.Module):
    def __init__(self, D_in, D_out):
        super(ParallelBlock, self).__init__()
        self.linear1 = torch.nn.Linear(D_in, D_out)
        self.linear2 = torch.nn.Linear(D_in, D_out)
    def forward(self, x):
        h1 = self.linear1(x)
        h2 = self.linear2(x)
        return (h1 * h2).clamp(min=0)
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D out)
```

```
optimizer = torch.optim.Adam(model.parameters(), lr=1e-4)
for t in range(500):
    y_pred = model(x)
    loss = torch.nn.functional.mse_loss(y_pred, y)
    loss.backward()
    optimizer.step()
    optimizer.zero grad()
```

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Lecture 8 - 80

PyTorch: DataLoaders

A **DataLoader** wraps a **Dataset** and provides minibatching, shuffling, multithreading, for you

When you need to load custom data, just write your own Dataset class

```
import torch
from torch.utils.data import TensorDataset, DataLoader
```

```
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
```

```
loader = DataLoader(TensorDataset(x, y), batch_size=8)
model = TwoLayerNet(D_in, H, D_out)
```

```
optimizer = torch.optim.SGD(model.parameters(), lr=1e-2)
for epoch in range(20):
    for x_batch, y_batch in loader:
        y_pred = model(x_batch)
        loss = torch.nn.functional.mse_loss(y_pred, y_batch)
        loss.backward()
        optimizer.step()
        optimizer.zero grad()
```

Lecture 8 - 81

PyTorch: DataLoaders

loader model = Iterate over loader to form minibatches

import torch from torch.utils.data import TensorDataset, DataLoader N, D in, H, D out = 64, 1000, 100, 10 x = torch.randn(N, D in)y = torch.randn(N, D out)loader = DataLoader(TensorDataset(x, y), batch size=8) model = TwoLayerNet(D_in, H, D_out) optimizer = torch.optim.SGD(model.parameters(), lr=1e-2) for epoch in range(20): for x batch, y batch in loader: y pred = model(x batch) loss = torch.nn.functional.mse_loss(y_pred, y_batch)

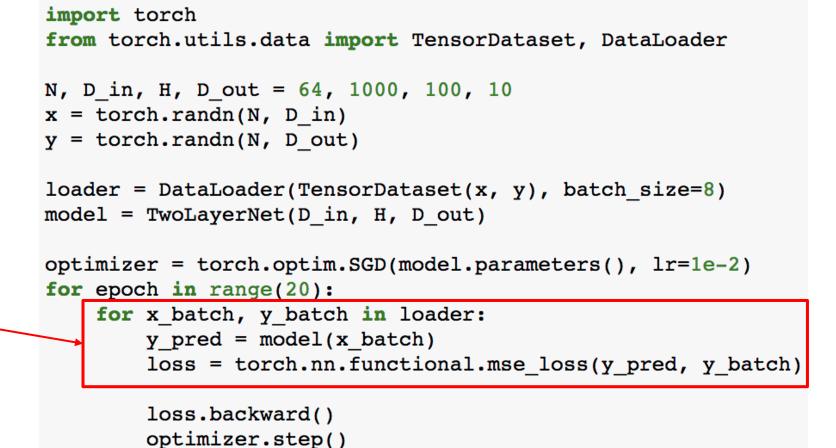
```
loss.backward()
optimizer.step()
optimizer.zero_grad()
```

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Lecture 8 - 82

PyTorch: DataLoaders

Iterate over loader to



```
optimizer.zero_grad()
```

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Lecture 8 - 83

PyTorch: Pretrained Models

Super easy to use pretrained models with torchvision https://github.com/pytorch/vision

import torch
import torchvision

alexnet = torchvision.models.alexnet(pretrained=True)
vgg16 = torchvision.models.vgg16(pretrained=True)
resnet101 = torchvision.models.resnet101(pretrained=True)

import torch

```
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
learning_rate = 1e-6
for t in range(500):
    y_pred = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y_pred - y).pow(2).sum()
    loss.backward()
```

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Lecture 8 - 85

V

Χ

import torch

N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)

```
learning_rate = 1e-6
for t in range(500):
    y_pred = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y_pred - y).pow(2).sum()
```

loss.backward()

Create Tensor objects

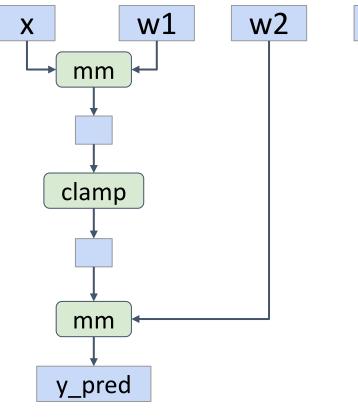
		\mathbf{b}	00
Justin	JO	ททร	ON

w1

w2

Lecture 8 - 86

V



import torch

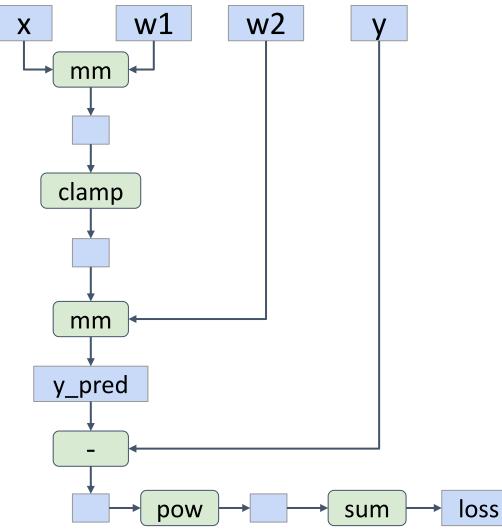
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)

loss.backward()

Build graph data structure AND perform computation

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Lecture 8 - 87



import torch

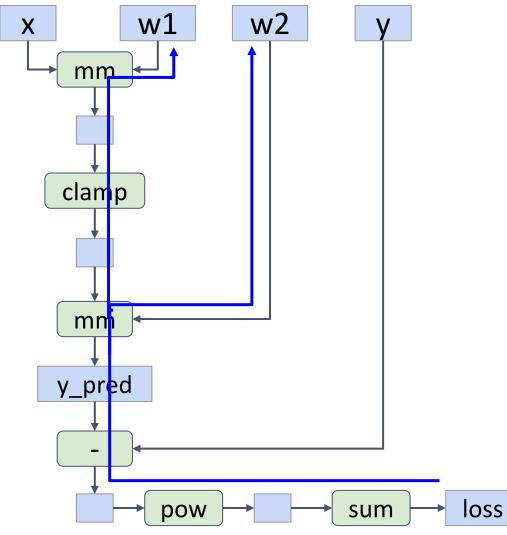
```
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
learning_rate = 1e-6
for t in range(500):
    y pred = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y_pred - y).pow(2).sum()
```

loss.backward()

Build graph data structure AND perform computation

Justin Johnson

Lecture 8 - 88



import torch

```
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
learning_rate = 1e-6
for t in range(500):
    y_pred = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y pred - y).pow(2).sum()
```

loss.backward()

Perform backprop, throw away graph

Justin Johnson

Lecture 8 - 89

V

Χ

import torch

```
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
learning_rate = 1e-6
for t in range(500):
    y_pred = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y_pred - y).pow(2).sum()
```

loss.backward()

Perform backprop, throw away graph

September 29, 2020

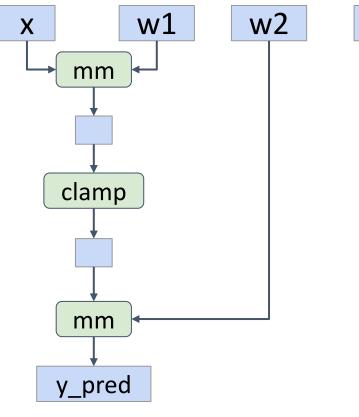
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w1

w2

Lecture 8 - 90

V



import torch

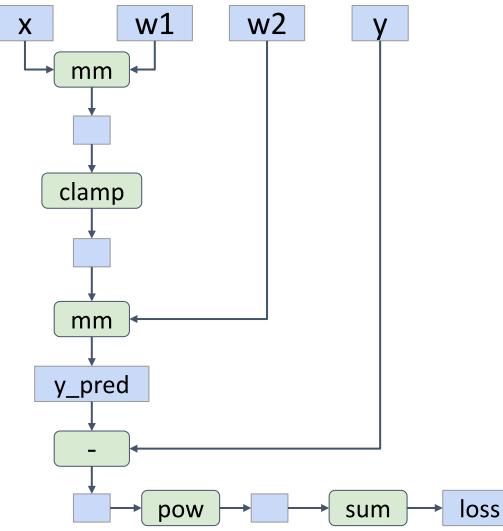
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)

loss.backward()

Build graph data structure AND perform computation

Justin Johnson

Lecture 8 - 91



import torch

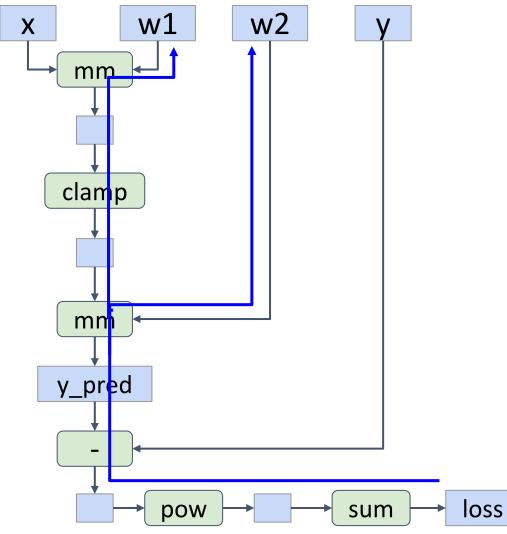
```
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
learning_rate = 1e-6
for t in range(500):
    y pred = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y_pred - y).pow(2).sum()
```

loss.backward()

Build graph data structure AND perform computation

Justin Johnson

Lecture 8 - 92



import torch

```
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
learning_rate = 1e-6
for t in range(500):
    y_pred = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y pred - y).pow(2).sum()
```

loss.backward()

Perform backprop, throw away graph

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Lecture 8 - 93

Dynamic graphs let you use regular Python control flow during the forward pass! import torch

```
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2a = torch.randn(H, D_out, requires_grad=True)
w2b = torch.randn(H, D_out, requires_grad=True)
learning_rate = 1e-6
prev_loss = 5.0
for t in range(500):
  w2 = w2a if prev_loss < 5.0 else w2b
  y_pred = x.mm(w1).clamp(min=0).mm(w2)
  loss = (y pred - y).pow(2).sum()
```

```
loss.backward()
prev_loss = loss.item()
```

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Lecture 8 - 94

Dynamic graphs let you use regular Python control flow during the forward pass!

Initialize two different weight matrices for second layer import torch

```
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2a = torch.randn(H, D_out, requires_grad=True)
w2b = torch.randn(H, D_out, requires_grad=True)
```

```
learning_rate = 1e-6
prev_loss = 5.0
for t in range(500):
    w2 = w2a if prev_loss < 5.0 else w2b
    y_pred = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y_pred - y).pow(2).sum()</pre>
```

```
loss.backward()
prev_loss = loss.item()
```

Dynamic graphs let you use regular Python control flow during the forward pass!

Decide which one to use at each layer based on loss at previous iteration

(this model doesn't makes sense! Just a simple dynamic example)

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import torch

```
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2a = torch.randn(H, D_out, requires_grad=True)
w2b = torch.randn(H, D_out, requires_grad=True)
learning_rate = 1e-6
prev_loss = 5.0
for t in range(500):
w2 = w2a if prev_loss < 5.0 else w2b
y_pred = x.mm(w1).clamp(min=0).mm(w2)
loss = (y_pred - y).pow(2).sum()
loss.backward()
prev_loss = loss.item()
```

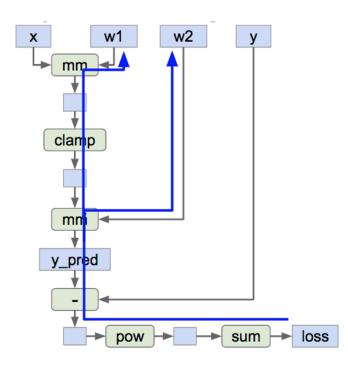
Lecture 8 - 96

Alternative: Static Computation Graphs

Alternative: Static graphs

Step 1: Build computational graph
describing our computation
(including finding paths for backprop)

Step 2: Reuse the same graph on every iteration



graph = build_graph()

```
for x_batch, y_batch in loader:
    run_graph(graph, x=x_batch, y=y_batch)
```

Lecture 8 - 97

```
import torch
                                      def model(x, y, w1, w2a, w2b, prev_loss):
                                        w^2 = w^2a if prev loss < 5.0 else w^2b
Define model as a
                                        y pred = x.mm(w1).clamp(min=0).mm(w2)
Python function
                                        loss = (y pred - y).pow(2).sum()
                                        return loss
                                      N, D_{in}, H, D_{out} = 64, 1000, 100, 10
                                      x = torch.randn(N, D in)
                                      y = torch.randn(N, D out)
                                      w1 = torch.randn(D in, H, requires grad=True)
                                      w2a = torch.randn(H, D_out, requires_grad=True)
                                      w2b = torch.randn(H, D out, requires grad=True)
                                      graph = torch.jit.script(model)
                                      prev loss = 5.0
                                      learning rate = 1e-6
                                      for t in range(500):
                                        loss = graph(x, y, w1, w2a, w2b, prev_loss)
                                        loss.backward()
                                        prev loss = loss.item()
```

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Lecture 8 - 98

Just-In-Time compilation: Introspect the source code of the function, **compile** it into a graph object.

Lots of magic here!

```
import torch
```

```
def model(x, y, w1, w2a, w2b, prev_loss):
  w2 = w2a if prev_loss < 5.0 else w2b
  y_pred = x.mm(w1).clamp(min=0).mm(w2)
  loss = (y_pred - y).pow(2).sum()
  return loss</pre>
```

```
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2a = torch.randn(H, D_out, requires_grad=True)
w2b = torch.randn(H, D out, requires_grad=True)
```

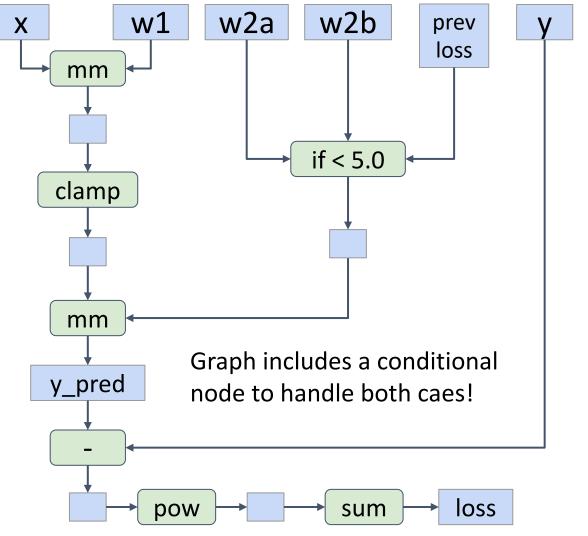
graph = torch.jit.script(model)

```
prev_loss = 5.0
learning_rate = 1e-6
for t in range(500):
    loss = graph(x, y, w1, w2a, w2b, prev_loss)
```

```
loss.backward()
prev_loss = loss.item()
```

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Lecture 8 - 99



import torch

```
def model(x, y, w1, w2a, w2b, prev_loss):
  w2 = w2a if prev_loss < 5.0 else w2b
  y_pred = x.mm(w1).clamp(min=0).mm(w2)
  loss = (y_pred - y).pow(2).sum()
  return loss</pre>
```

```
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2a = torch.randn(H, D_out, requires_grad=True)
w2b = torch.randn(H, D_out, requires_grad=True)
```

graph = torch.jit.script(model)

```
prev_loss = 5.0
learning_rate = 1e-6
for t in range(500):
   loss = graph(x, y, w1, w2a, w2b, prev_loss)
   loss.backward()
```

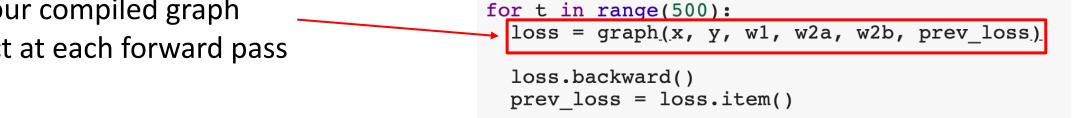
```
prev_loss = loss.item()
```

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Lecture 8 - 100

```
import torch
def model(x, y, w1, w2a, w2b, prev loss):
  w^2 = w^2a if prev loss < 5.0 else w^2b
  y pred = x.mm(w1).clamp(min=0).mm(w2)
  loss = (y pred - y).pow(2).sum()
  return loss
N, D in, H, D out = 64, 1000, 100, 10
x = torch.randn(N, D in)
y = torch.randn(N, D out)
w1 = torch.randn(D in, H, requires grad=True)
w2a = torch.randn(H, D out, requires grad=True)
w2b = torch.randn(H, D out, requires grad=True)
graph = torch.jit.script(model)
prev loss = 5.0
```

Use our compiled graph object at each forward pass



learning rate = 1e-6

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Lecture 8 - 101

Even easier: add **annotation** to function, Python function compiled to a graph when it is defined

Calling function uses graph

```
import torch
@torch.jit.script
def model(x, y, w1, w2a, w2b, prev_loss):
  w2 = w2a if prev_loss < 5.0 else w2b
  y_pred = x.mm(w1).clamp(min=0).mm(w2)
  loss = (y_pred - y).pow(2).sum()
  return loss
N, D_in, H, D_out = 64, 1000, 100, 10
```

```
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2a = torch.randn(H, D_out, requires_grad=True)
w2b = torch.randn(H, D_out, requires_grad=True)
```

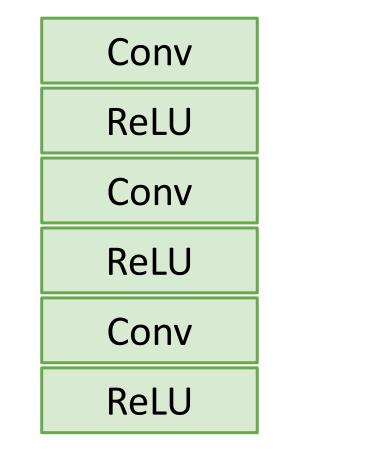
```
loss.backward()
prev_loss = loss.item()
```

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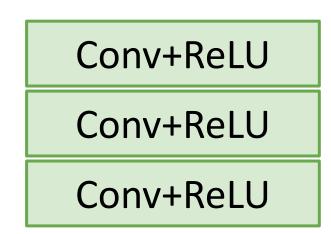
Lecture 8 - 102

Static vs Dynamic Graphs: Optimization

With static graphs, framework can **optimize** the graph for you before it runs! The graph you wrote



Equivalent graph with **fused operations**



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Lecture 8 - 103

Static vs Dynamic Graphs: Serialization

Static

Once graph is built, can **serialize** it and run it without the code that built the graph!

e.g. train model in Python, deploy in C++

Dynamic

Graph building and execution are intertwined, so always need to keep code around

Lecture 8 - 104

Static vs Dynamic Graphs: Debugging

Static

Lots of indirection between the code you write and the code that runs – can be hard to debug, benchmark, etc

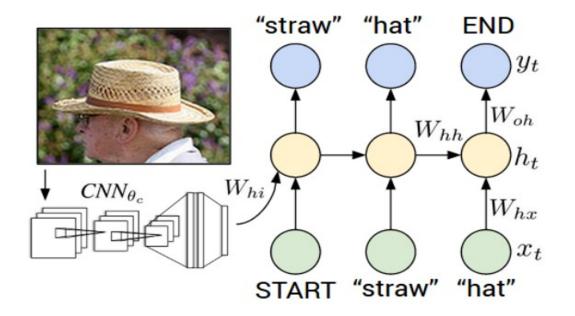
Dynamic

The code you write is the code that runs! Easy to reason about, debug, profile, etc

Dynamic Graph Applications

Model structure depends on the input:

- Recurrent Networks



Karpathy and Fei-Fei, "Deep Visual-Semantic Alignments for Generating Image Descriptions", CVPR 2015

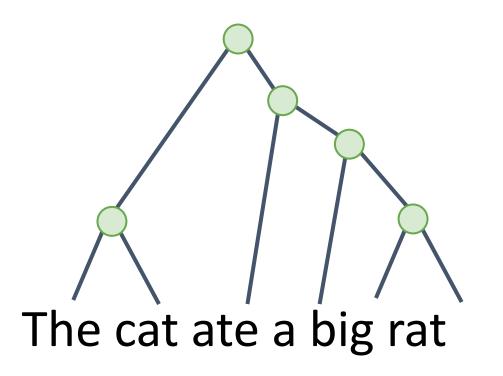
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Lecture 8 - 106

Dynamic Graph Applications

Model structure depends on the input:

- Recurrent Networks
- Recursive Networks



Karpathy and Fei-Fei, "Deep Visual-Semantic Alignments for Generating Image Descriptions", CVPR 2015

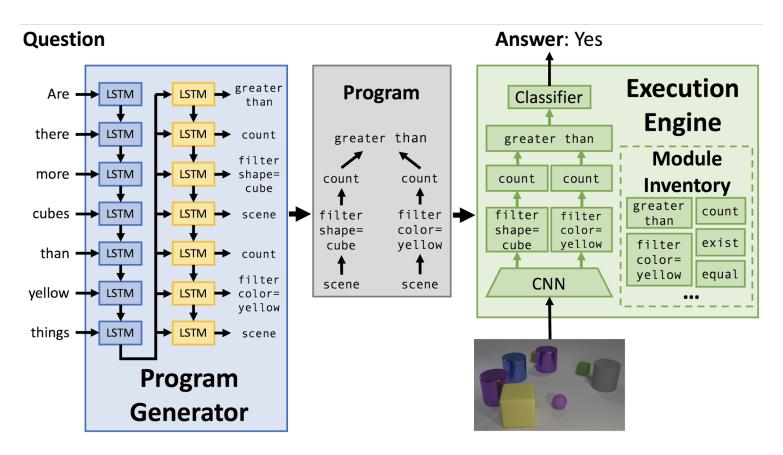
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Lecture 8 - 107

Dynamic Graph Applications

Model structure depends on the input:

- Recurrent Networks
- Recursive Networks
- Modular Networks



Andreas et al, "Neural Module Networks", CVPR 2016

Andreas et al, "Learning to Compose Neural Networks for Question Answering", NAACL 2016 Johnson et al, "Inferring and Executing Programs for Visual Reasoning", ICCV 2017

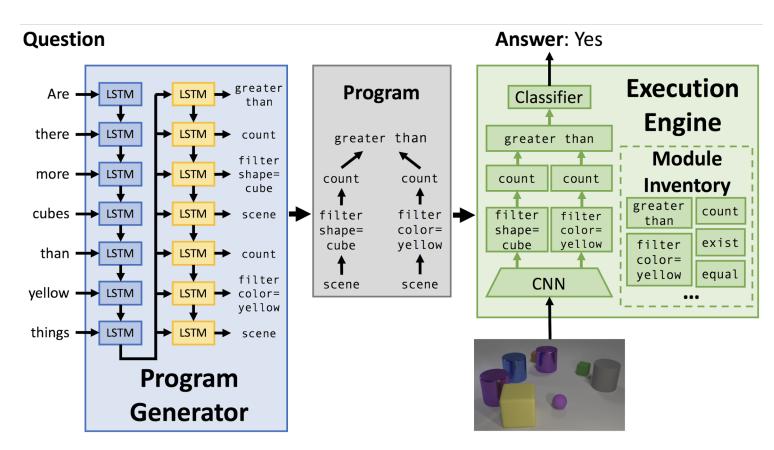
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Lecture 8 - 108

Dynamic Graph Applications

Model structure depends on the input:

- Recurrent Networks
- Recursive Networks
- Modular Networks
- (Your idea here!)



Andreas et al, "Neural Module Networks", CVPR 2016

Andreas et al, "Learning to Compose Neural Networks for Question Answering", NAACL 2016 Johnson et al, "Inferring and Executing Programs for Visual Reasoning", ICCV 2017

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Lecture 8 - 109

TensorFlow

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Lecture 9 - 110

TensorFlow Versions

TensorFlow 1.0

- Final release: 1.15.3
- Default: static graphs
- Optional: dynamic graphs (eager mode)

TensorFlow 2.0

- Current release: 2.3.1
 - Released 9/24
- Default: dynamic graphs
- Optional: static graphs

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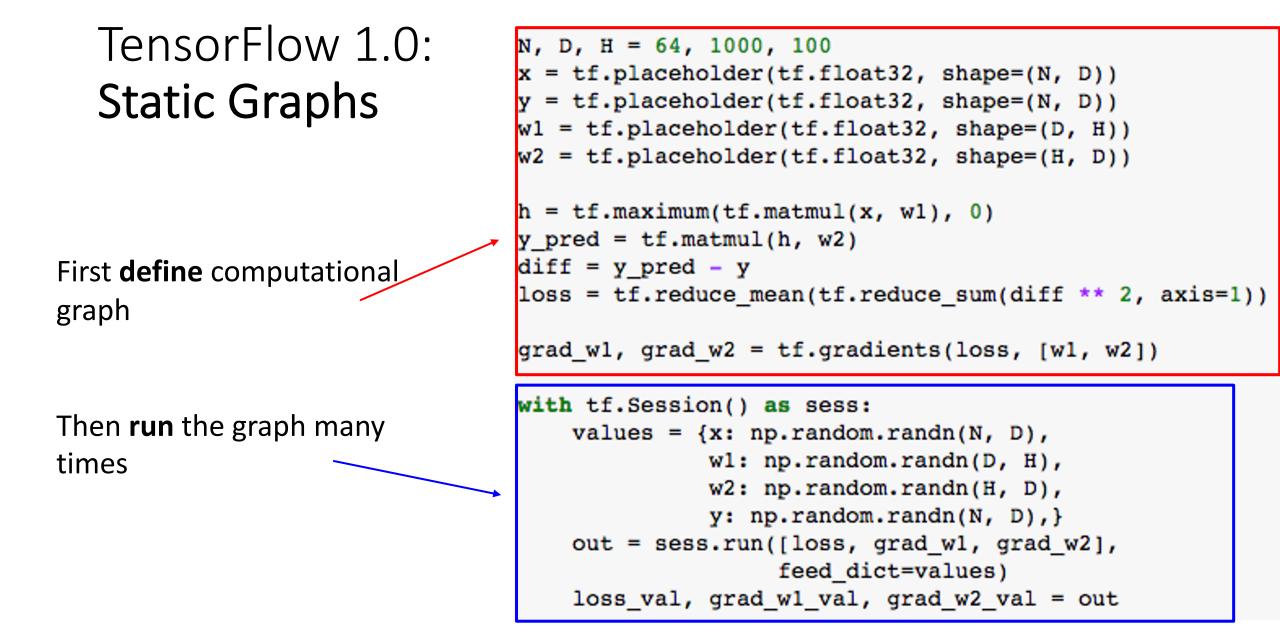
Lecture 8 - 111

TensorFlow 1.0: Static Graphs

import numpy as np
import tensorflow as tf

(Assume imports at the top of each snippet)

```
N, D, H = 64, 1000, 100
x = tf.placeholder(tf.float32, shape=(N, D))
y = tf.placeholder(tf.float32, shape=(N, D))
w1 = tf.placeholder(tf.float32, shape=(D, H))
w2 = tf.placeholder(tf.float32, shape=(H, D))
h = tf.maximum(tf.matmul(x, w1), 0)
y pred = tf.matmul(h, w2)
diff = y pred - y
loss = tf.reduce mean(tf.reduce sum(diff ** 2, axis=1))
grad w1, grad w2 = tf.gradients(loss, [w1, w2])
with tf.Session() as sess:
    values = {x: np.random.randn(N, D),
              wl: np.random.randn(D, H),
              w2: np.random.randn(H, D),
              y: np.random.randn(N, D),}
    out = sess.run([loss, grad w1, grad w2],
                   feed dict=values)
    loss_val, grad_w1_val, grad_w2_val = out
```



TensorFlow 2.0: **Dynamic Graphs**

Create TensorFlow Tensors for data and weights

Weights need to be wrapped in tf.Variable so we can mutate them

```
import tensorflow as tf
```

```
N, Din, H, Dout = 16, 1000, 100, 10
```

```
x = tf.random.normal((N, Din))
y = tf.random.normal((N, Dout))
w1 = tf.Variable(tf.random.normal((Din, H)))
w2 = tf.Variable(tf.random.normal((H, Dout)))
```

```
learning_rate = 1e-6
for t in range(1000):
    with tf.GradientTape() as tape:
        h = tf.maximum(tf.matmul(x, w1), 0)
        y_pred = tf.matmul(h, w2)
        diff = y_pred - y
        loss = tf.reduce_mean(tf.reduce_sum(diff ** 2, axis=1))
        grad_w1, grad_w2 = tape.gradient(loss, [w1, w2])
        w1.assign(w1 - learning_rate * grad_w1)
        w2.assign(w2 - learning rate * grad_w2)
```

```
TensorFlow 2.0:
   Dynamic Graphs
Scope forward pass
under a GradientTape to
tell TensorFlow to start
building a graph
```

```
import tensorflow as tf
N, Din, H, Dout = 16, 1000, 100, 10
x = tf.random.normal((N, Din))
y = tf.random.normal((N, Dout))
w1 = tf.Variable(tf.random.normal((Din, H)))
w2 = tf.Variable(tf.random.normal((H, Dout)))
learning rate = 1e-6
for t in range(1000):
  with tf.GradientTape() as tape:
    h = tf.maximum(tf.matmul(x, w1), 0)
    y pred = tf.matmul(h, w2)
    diff = y \text{ pred} - y
    loss = tf.reduce mean(tf.reduce sum(diff ** 2, axis=1))
  grad w1, grad w2 = tape.gradient(loss, [w1, w2])
  w1.assign(w1 - learning rate * grad w1)
  w2.assign(w2 - learning rate * grad w2)
```

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```
TensorFlow 2.0:
  Dynamic Graphs
Ask the tape to
compute gradients
```

```
import tensorflow as tf
N, Din, H, Dout = 16, 1000, 100, 10
x = tf.random.normal((N, Din))
y = tf.random.normal((N, Dout))
w1 = tf.Variable(tf.random.normal((Din, H)))
w2 = tf.Variable(tf.random.normal((H, Dout)))
learning rate = 1e-6
for t in range(1000):
  with tf.GradientTape() as tape:
    h = tf.maximum(tf.matmul(x, w1), 0)
    y pred = tf.matmul(h, w2)
    diff = y \text{ pred} - y
    loss = tf.reduce mean(tf.reduce sum(diff ** 2, axis=1))
  grad w1, grad w2 = tape.gradient(loss, [w1, w2])
  w1.assign(w1 - learning rate * grad w1)
```

```
w2.assign(w2 - learning_rate * grad_w2)
```

```
TensorFlow 2.0:
  Dynamic Graphs
Gradient descent
step, update weights
```

```
import tensorflow as tf
N, Din, H, Dout = 16, 1000, 100, 10
x = tf.random.normal((N, Din))
y = tf.random.normal((N, Dout))
w1 = tf.Variable(tf.random.normal((Din, H)))
w2 = tf.Variable(tf.random.normal((H, Dout)))
learning rate = 1e-6
for t in range(1000):
  with tf.GradientTape() as tape:
    h = tf.maximum(tf.matmul(x, w1), 0)
    y pred = tf.matmul(h, w2)
    diff = y \text{ pred} - y
    loss = tf.reduce mean(tf.reduce sum(diff ** 2, axis=1))
  grad w1, grad w2 = tape.gradient(loss, [w1, w2])
  w1.assign(w1 - learning rate * grad w1)
  w2.assign(w2 - learning_rate * grad w2)
```

TensorFlow 2.0: Static Graphs

Define a function that implements forward, backward, and update

Annotating with tf.function will compile the function into a graph! (similar to torch.jit.script)

```
@tf.function
def step(x, y, w1, w2):
   with tf.GradientTape() as tape:
    h = tf.maximum(tf.matmul(x, w1), 0)
   y_pred = tf.matmul(h, w2)
   diff = y_pred - y
   loss = tf.reduce_mean(tf.reduce_sum(diff ** 2, axis=1))
   grad_w1, grad_w2 = tape.gradient(loss, [w1, w2])
   w1.assign(w1 - learning_rate * grad_w1)
   w2.assign(w2 - learning_rate * grad_w2)
   return loss
```

```
N, Din, H, Dout = 16, 1000, 100, 10
x = tf.random.normal((N, Din))
y = tf.random.normal((N, Dout))
w1 = tf.Variable(tf.random.normal((Din, H)))
w2 = tf.Variable(tf.random.normal((H, Dout)))
learning_rate = 1e-6
for t in range(1000):
    loss = step(x, y, w1, w2)
```

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TensorFlow 2.0: Static Graphs

Define a function that implements forward, backward, and update

Annotating with tf.function will compile the function into a graph! (similar to torch.jit.script)

(note TF graph can / include gradient computation and update, unlike PyTorch)

```
@tf.function
def step(x, y, w1, w2):
  with tf.GradientTape() as tape:
    h = tf.maximum(tf.matmul(x, w1), 0)
    y pred = tf.matmul(h, w2)
    diff = y \text{ pred} - y
    loss = tf.reduce mean(tf.reduce sum(diff ** 2, axis=1))
  grad w1, grad w2 = tape.gradient(loss, [w1, w2])
  w1.assign(w1 - learning rate * grad w1)
  w2.assign(w2 - learning rate * grad w2)
  return loss
N, Din, H, Dout = 16, 1000, 100, 10
x = tf.random.normal((N, Din))
y = tf.random.normal((N, Dout))
w1 = tf.Variable(tf.random.normal((Din, H)))
w2 = tf.Variable(tf.random.normal((H, Dout)))
learning rate = 1e-6
for t in range(1000):
  loss = step(x, y, w1, w2)
```

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```
TensorFlow 2.0:
                                  @tf.function
                                 def step(x, y, w1, w2):
    Static Graphs
                                   with tf.GradientTape() as tape:
                                     h = tf.maximum(tf.matmul(x, w1), 0)
                                     y pred = tf.matmul(h, w2)
                                     diff = y pred - y
                                     loss = tf.reduce mean(tf.reduce sum(diff ** 2, axis=1))
                                   grad w1, grad w2 = tape.gradient(loss, [w1, w2])
                                   w1.assign(w1 - learning rate * grad w1)
                                   w2.assign(w2 - learning rate * grad w2)
                                   return loss
                                 N, Din, H, Dout = 16, 1000, 100, 10
                                 x = tf.random.normal((N, Din))
                                 y = tf.random.normal((N, Dout))
                                 w1 = tf.Variable(tf.random.normal((Din, H)))
Call the compiled step
                                 w2 = tf.Variable(tf.random.normal((H, Dout)))
function in the training
                                 learning rate = 1e-6
loop
                                 for t in range(1000):
                                   loss = step(x, y, w1, w2)
```

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```
from tensorflow.keras.models import Sequential
from tensorflow.keras.layers import InputLayer, Dense
N, Din, H, Dout = 16, 1000, 100, 10
model = Sequential()
model.add(InputLayer(input shape=(Din,)))
model.add(Dense(units=H, activation='relu'))
model.add(Dense(units=Dout))
params = model.trainable variables
loss fn = tf.keras.losses.MeanSquaredError()
opt = tf.keras.optimizers.SGD(learning rate=1e-6)
x = tf.random.normal((N, Din))
y = tf.random.normal((N, Dout))
for t in range(1000):
  with tf.GradientTape() as tape:
    y \text{ pred} = \text{model}(x)
    loss = loss_fn(y_pred, y)
  grads = tape.gradient(loss, params)
  opt.apply gradients(zip(grads, params))
```

import tensorflow as tf

Object-oriented API: build the model as a stack of layers import tensorflow as tf
from tensorflow.keras.models import Sequential
from tensorflow.keras.layers import InputLayer, Dense

```
N, Din, H, Dout = 16, 1000, 100, 10
```

```
model = Sequential()
model.add(InputLayer(input_shape=(Din,)))
model.add(Dense(units=H, activation='relu'))
model.add(Dense(units=Dout))
params = model.trainable_variables
```

```
loss_fn = tf.keras.losses.MeanSquaredError()
opt = tf.keras.optimizers.SGD(learning_rate=1e-6)
```

```
x = tf.random.normal((N, Din))
y = tf.random.normal((N, Dout))
for t in range(1000):
  with tf.GradientTape() as tape:
    y_pred = model(x)
    loss = loss_fn(y_pred, y)
    grads = tape.gradient(loss, params)
```

```
opt.apply_gradients(zip(grads, params))
```

Keras gives you common loss functions and optimization algorithms

```
import tensorflow as tf
from tensorflow.keras.models import Sequential
from tensorflow.keras.layers import InputLayer, Dense
N, Din, H, Dout = 16, 1000, 100, 10
model = Sequential()
model.add(InputLayer(input_shape=(Din,)))
model.add(Dense(units=H, activation='relu'))
model.add(Dense(units=Dout))
params = model.trainable_variables
loss_fn = tf.keras.losses.MeanSquaredError()
opt = tf.keras.optimizers.SGD(learning_rate=1e-6)
```

```
x = tf.random.normal((N, Din))
y = tf.random.normal((N, Dout))
```

```
for t in range(1000):
    with tf.GradientTape() as tape:
        y_pred = model(x)
        loss = loss_fn(y_pred, y)
        grads = tape.gradient(loss, params)
        opt.apply_gradients(zip(grads, params))
```

Forward pass: Compute loss, build graph

Backward pass: compute gradients

```
import tensorflow as tf
from tensorflow.keras.models import Sequential
from tensorflow.keras.layers import InputLayer, Dense
N, Din, H, Dout = 16, 1000, 100, 10
model = Sequential()
model.add(InputLayer(input shape=(Din,)))
model.add(Dense(units=H, activation='relu'))
model.add(Dense(units=Dout))
params = model.trainable variables
loss fn = tf.keras.losses.MeanSquaredError()
opt = tf.keras.optimizers.SGD(learning_rate=1e-6)
x = tf.random.normal((N, Din))
y = tf.random.normal((N, Dout))
for t in range(1000):
  with tf.GradientTape() as tape:
    y \text{ pred} = \text{model}(x)
    loss = loss fn(y pred, y)
  grads = tape.gradient(loss, params)
  opt.apply gradients(zip(grads, params))
```

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Optimizer object updates parameters

```
import tensorflow as tf
from tensorflow.keras.models import Sequential
from tensorflow.keras.layers import InputLayer, Dense
N, Din, H, Dout = 16, 1000, 100, 10
model = Sequential()
model.add(InputLayer(input shape=(Din,)))
model.add(Dense(units=H, activation='relu'))
model.add(Dense(units=Dout))
params = model.trainable variables
loss fn = tf.keras.losses.MeanSquaredError()
opt = tf.keras.optimizers.SGD(learning rate=1e-6)
x = tf.random.normal((N, Din))
y = tf.random.normal((N, Dout))
for t in range(1000):
  with tf.GradientTape() as tape:
    y \text{ pred} = \text{model}(x)
    loss = loss_fn(y_pred, y)
  grads = tape.gradient(loss, params)
  opt.apply gradients(zip(grads, params))
```

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Define a function that returns the loss

```
import tensorflow as tf
from tensorflow.keras.models import Sequential
from tensorflow.keras.layers import InputLayer, Dense
N, Din, H, Dout = 16, 1000, 100, 10
model = Sequential()
model.add(InputLayer(input shape=(Din,)))
model.add(Dense(units=H, activation='relu'))
model.add(Dense(units=Dout))
params = model.trainable variables
loss fn = tf.keras.losses.MeanSquaredError()
opt = tf.keras.optimizers.SGD(learning rate=1e-6)
x = tf.random.normal((N, Din))
y = tf.random.normal((N, Dout))
def step():
  y \text{ pred} = \text{model}(x)
  loss = loss fn(y pred, y)
  return loss
```

```
for t in range(1000):
    opt.minimize(step, params)
```

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Optimizer computes gradients and updates parameters

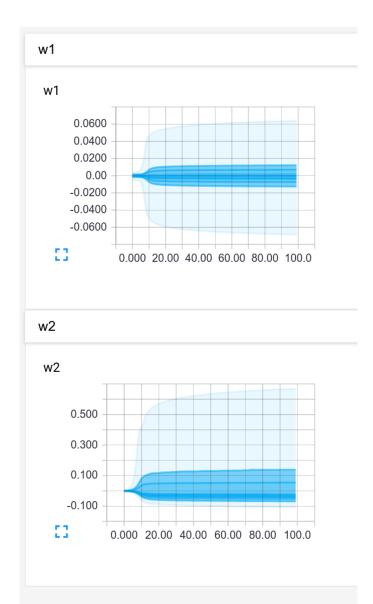
```
import tensorflow as tf
from tensorflow.keras.models import Sequential
from tensorflow.keras.layers import InputLayer, Dense
N, Din, H, Dout = 16, 1000, 100, 10
model = Sequential()
model.add(InputLayer(input shape=(Din,)))
model.add(Dense(units=H, activation='relu'))
model.add(Dense(units=Dout))
params = model.trainable variables
loss fn = tf.keras.losses.MeanSquaredError()
opt = tf.keras.optimizers.SGD(learning rate=1e-6)
x = tf.random.normal((N, Din))
y = tf.random.normal((N, Dout))
def step():
  y \text{ pred} = \text{model}(x)
  loss = loss fn(y pred, y)
  return loss
for t in range(1000):
  opt.minimize(step, params)
```

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TensorBoard

Add logging to code to record loss, stats, etc Run server and get pretty graphs!

TensorBoard	
Regex filter	loss
Split on underscores	loss
Data download links	120
Horizontal Axis	80.0
STEP RELATIVE WALL	40.0
	0.00
Runs	0.000 20.00 40.00 60.00 80.00 100.0



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TensorBoard

Also works with PyTorch: torch.utils.tensorboard

TensorBoard	
 Regex filter Split on underscores 	loss
Data download links	120
Horizontal Axis STEP RELATIVE WALL	80.0 40.0 0.00
Runs .	C3 0.000 20.00 40.00 60.00 80.00 100.0



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PyTorch vs TensorFlow

PyTorch

- My personal favorite
- Clean, imperative API
- Easy dynamic graphs for debugging
- JIT allows static graphs for production
- Cannot use TPUs
- Not easy to deploy on mobile

TensorFlow 1.0

- Static graphs by default
- Can be confusing to debug
- API a bit messy

TensorFlow 2.0

- Dynamic by default
- Standardized on Keras API
- API still confusing

Summary: Hardware

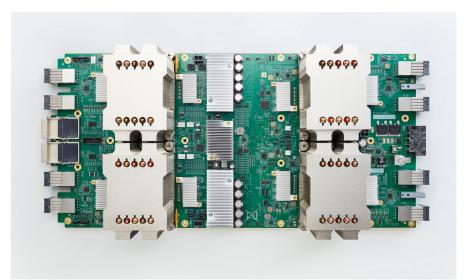
CPU



GPU



TPU



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Summary: Software

Static Graphs vs Dynamic Graphs

PyTorch vs TensorFlow

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Next time: Training Neural Networks

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