

# Lecture 4: Light + Color

# Administrative

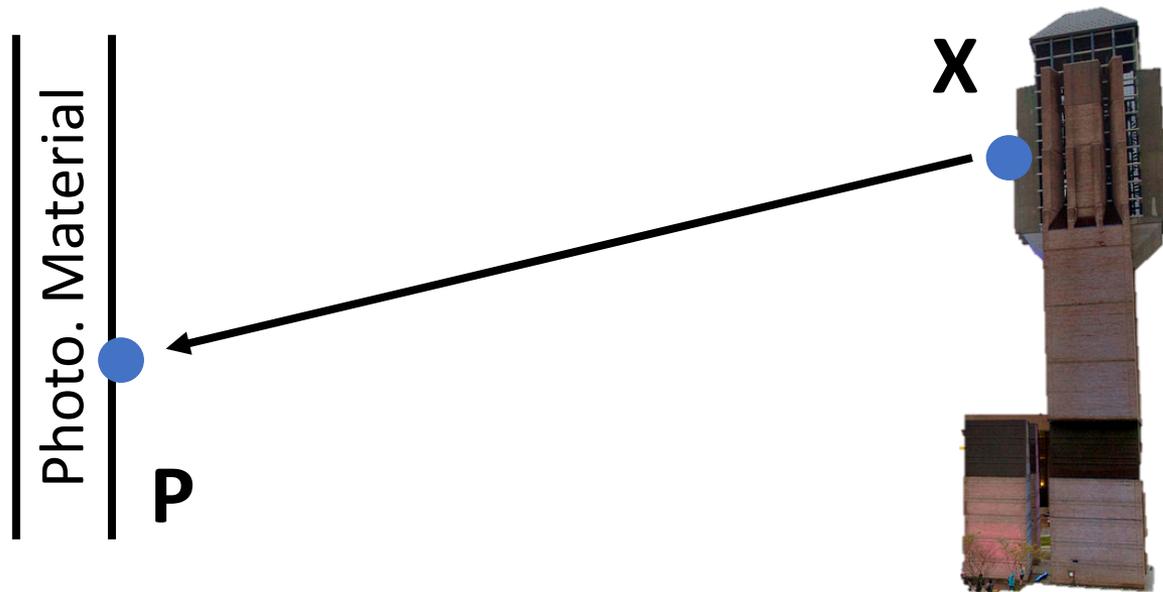
HW0 due Wednesday 1/29  
(1 week from Wednesday)

HW1 out Wednesday 1/22,  
due Wednesday 2/5

# Recap: Projection

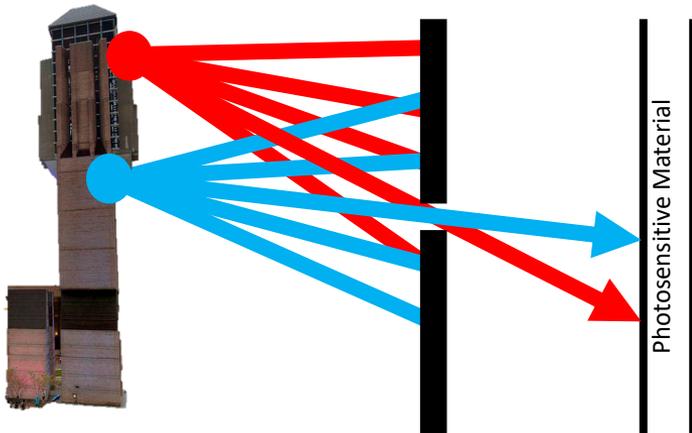
$$\text{Image} \rightarrow \mathbf{P} = \mathbf{K}[\mathbf{R}, \mathbf{t}] \mathbf{X} \leftarrow \text{World}$$

*Intrinsic*      *Extrinsic*



# Recap: Lenses

## Pinhole Model



Mathematically correct  
Not quite correct in practice  
Reasonable approximation

## Reality: Lenses

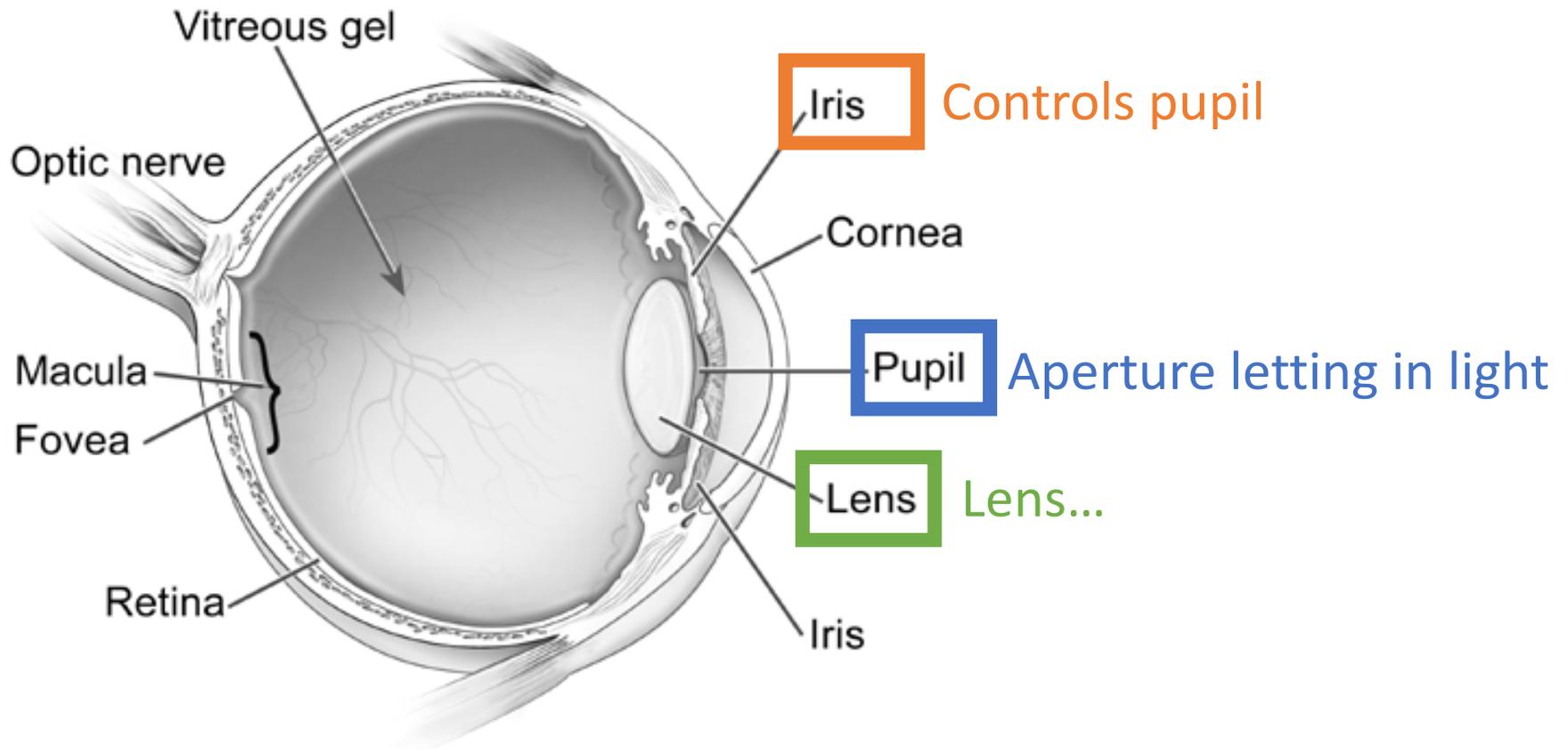


Necessary in practice  
Introduce complications  
Complications fixable

# Today

- A little bit about light and how you represent it
- A little bit about lighting and how it works

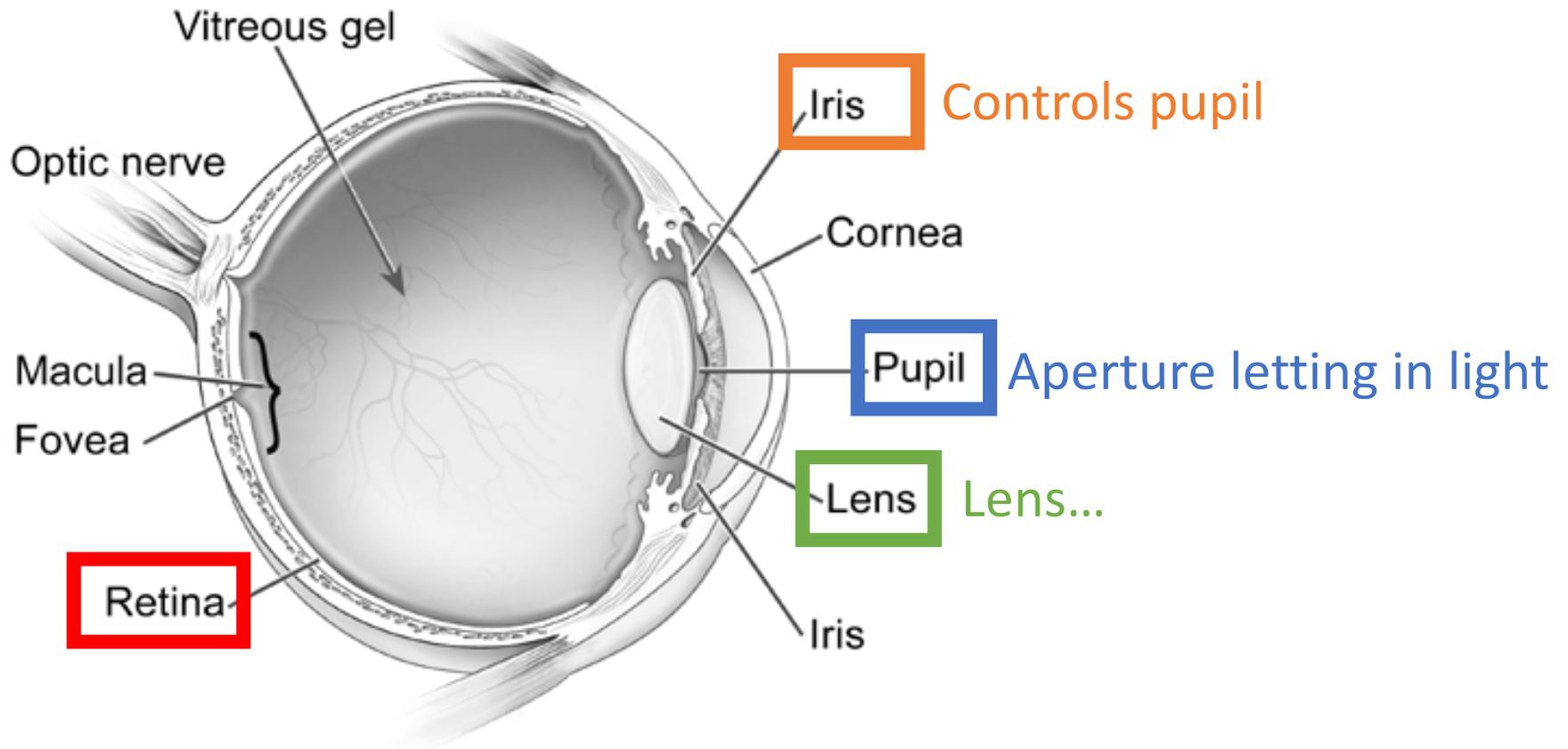
# Your Very Own Camera



**Where's the film/CCD?**

Slide Credit: NIH

# Your Very Own Camera



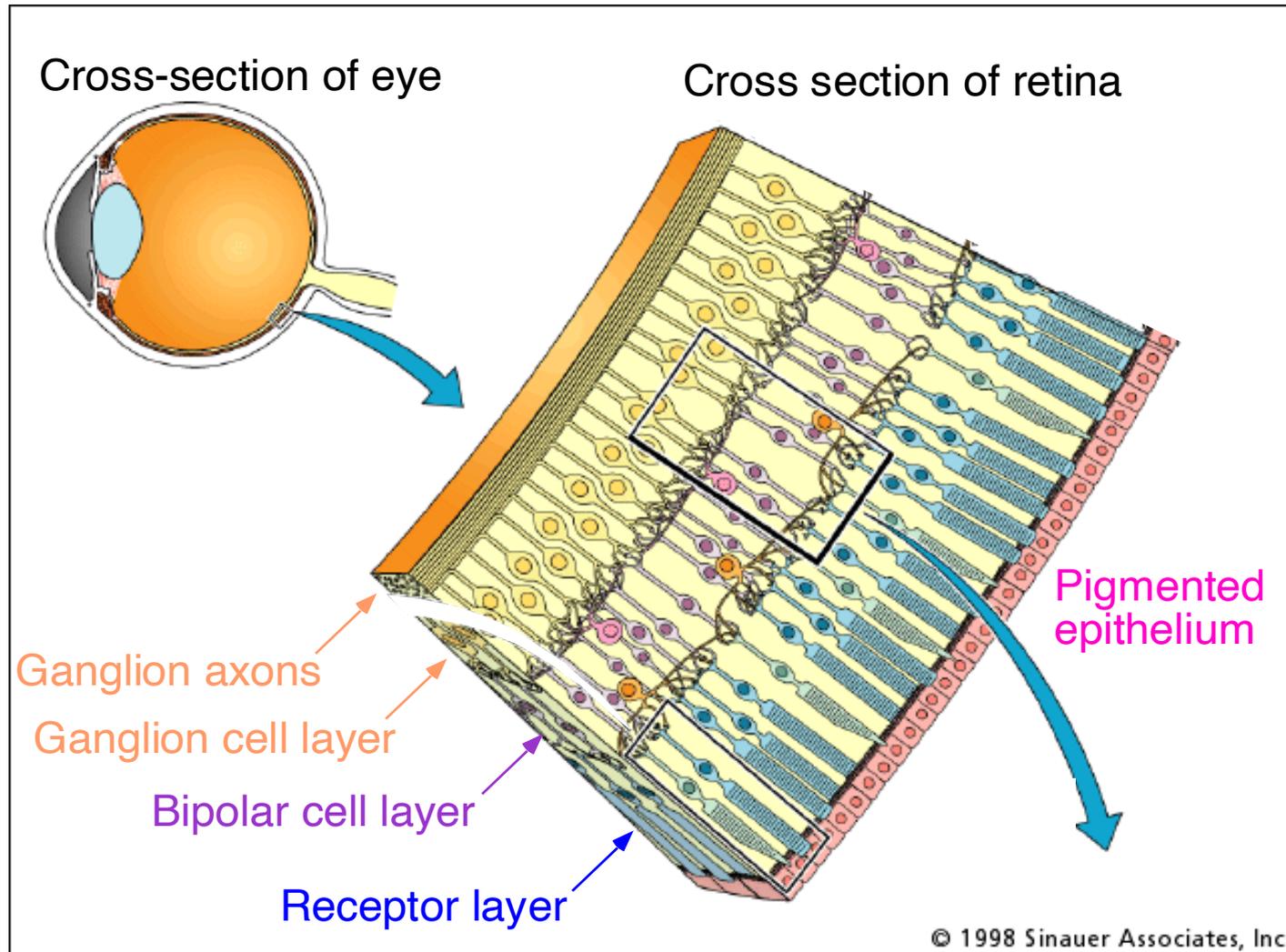
Where's the **film/CCD**?

Slide Credit: NIH

# Demo Time

<https://bit.ly/2INJ3xc>

# What is the Retina made of?



Slide Credit: J. Hays

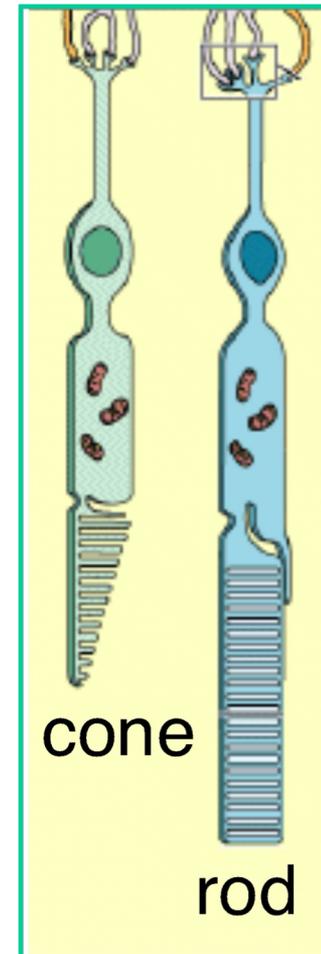
# Two Types of Photo Receptors

## **C**ones

cone-shaped  
less sensitive  
operate in high light  
color vision

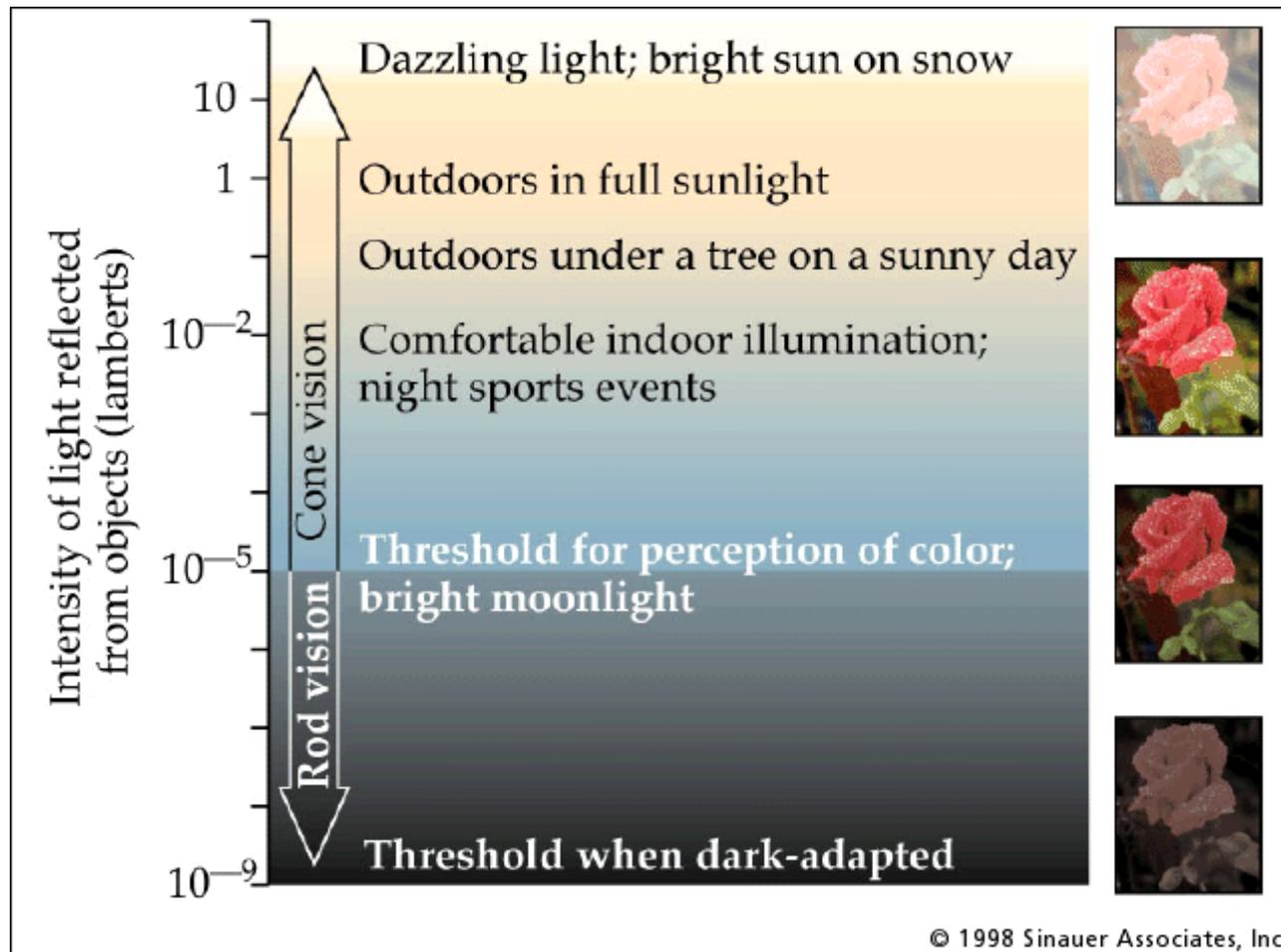
## **R**ods

rod-shaped  
highly sensitive  
operate at night  
gray-scale vision



Slide Credit: J. Hays

# Rod / Cone Sensitivity



Slide Credit: J. Hays

# Rod / Cone Distribution

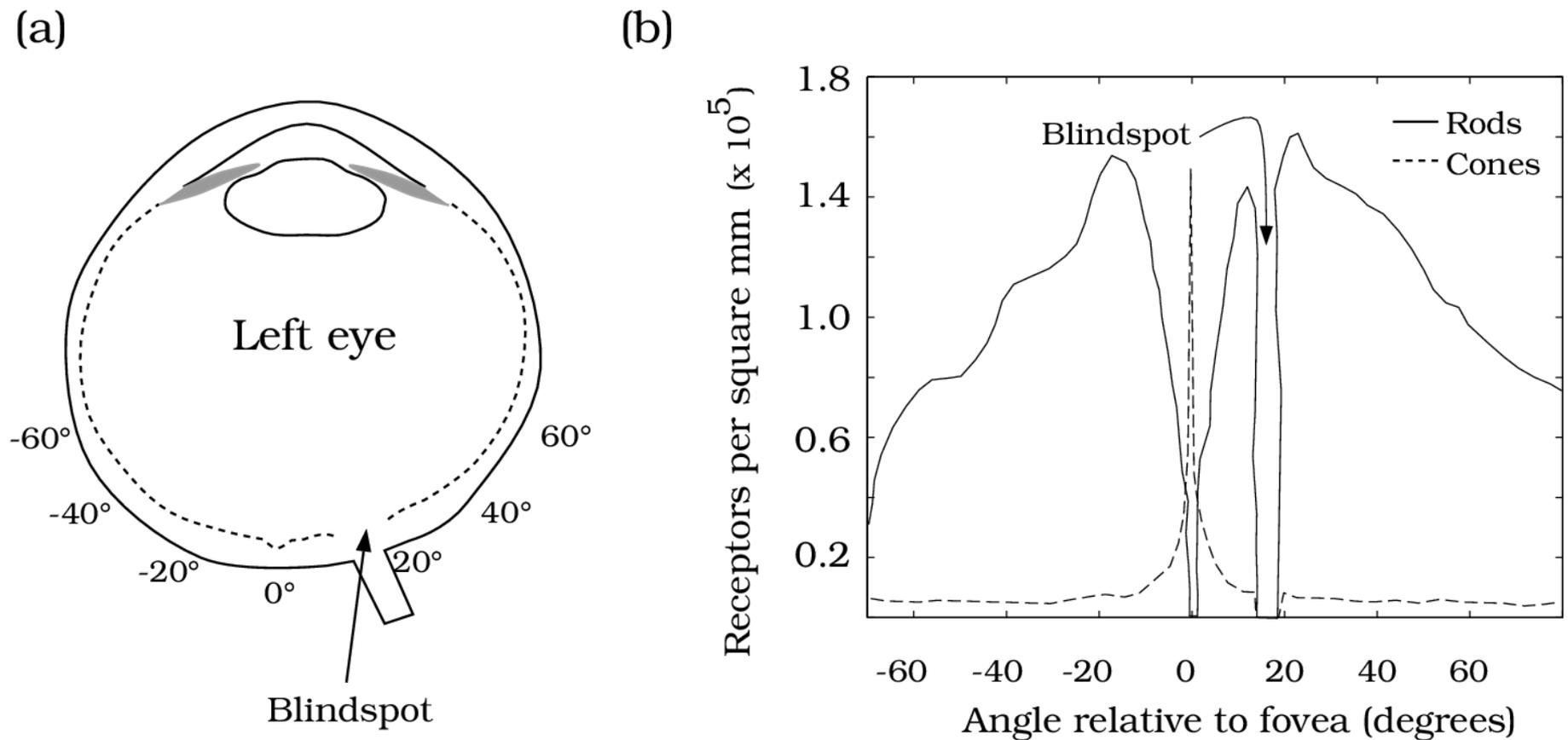
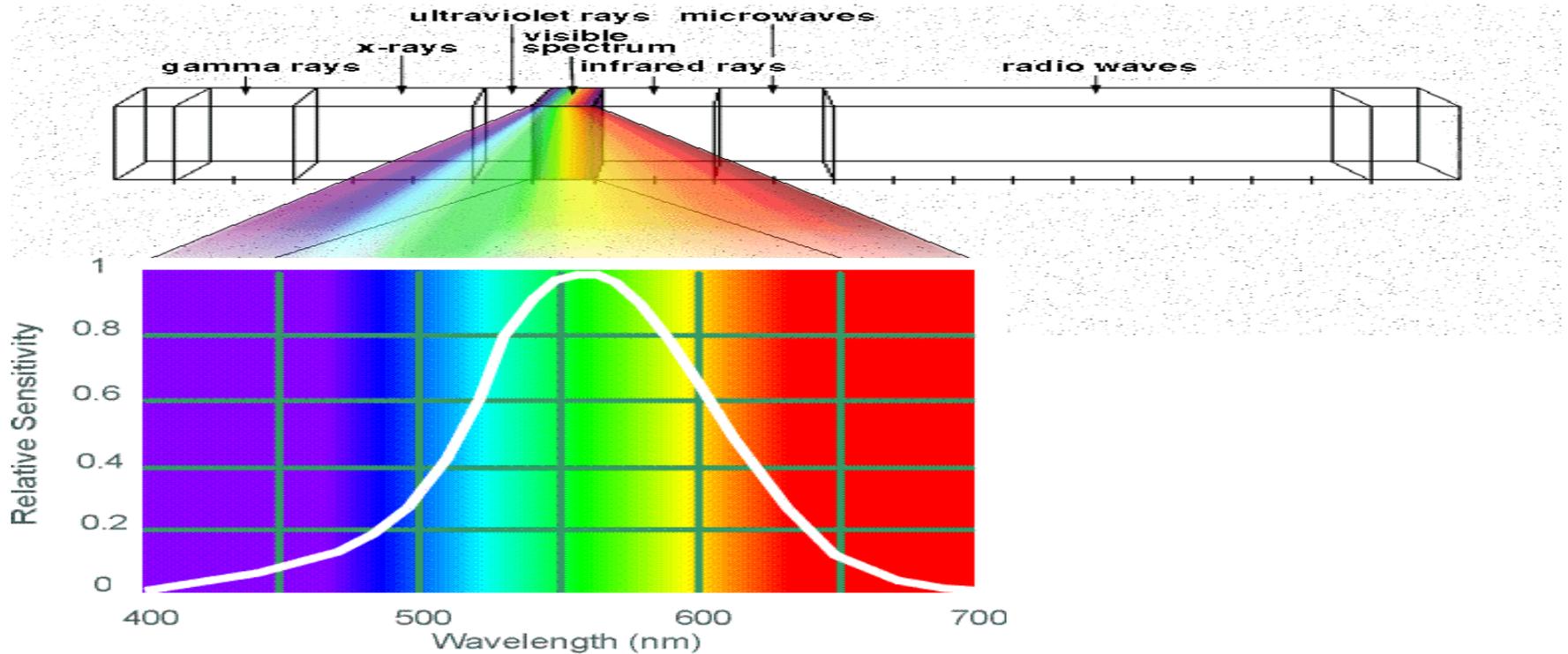


Diagram Credit: B. A. Wandell, *Foundations of Vision*

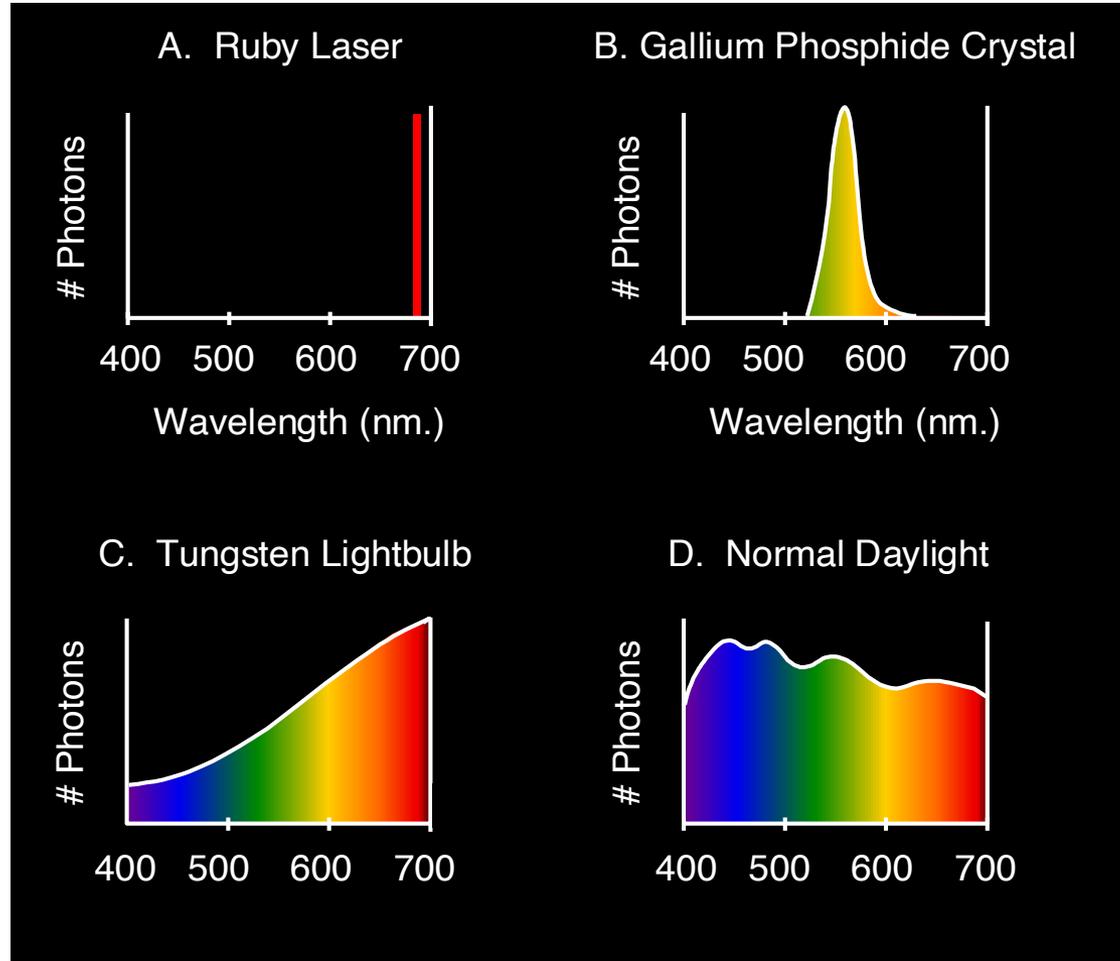
# Electromagnetic Spectrum



**Why do we see light in these wavelengths?**

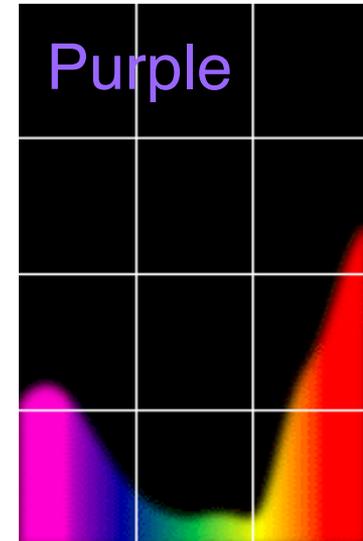
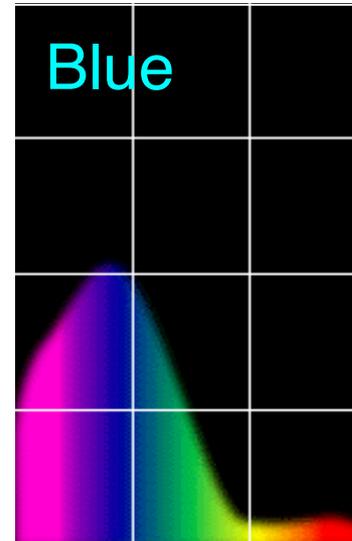
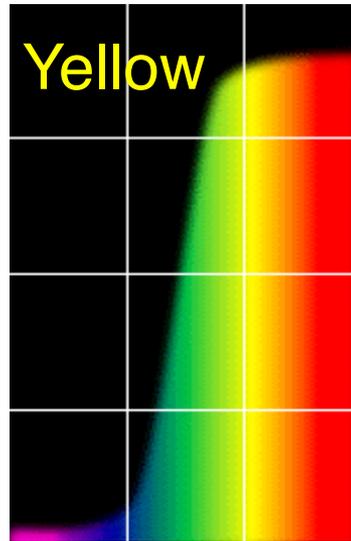
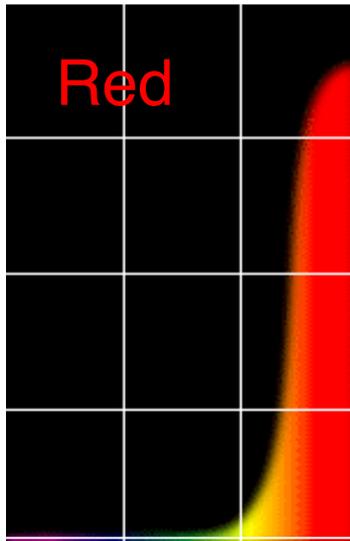
Slide Credit: J. Hays

# The Physics of Light



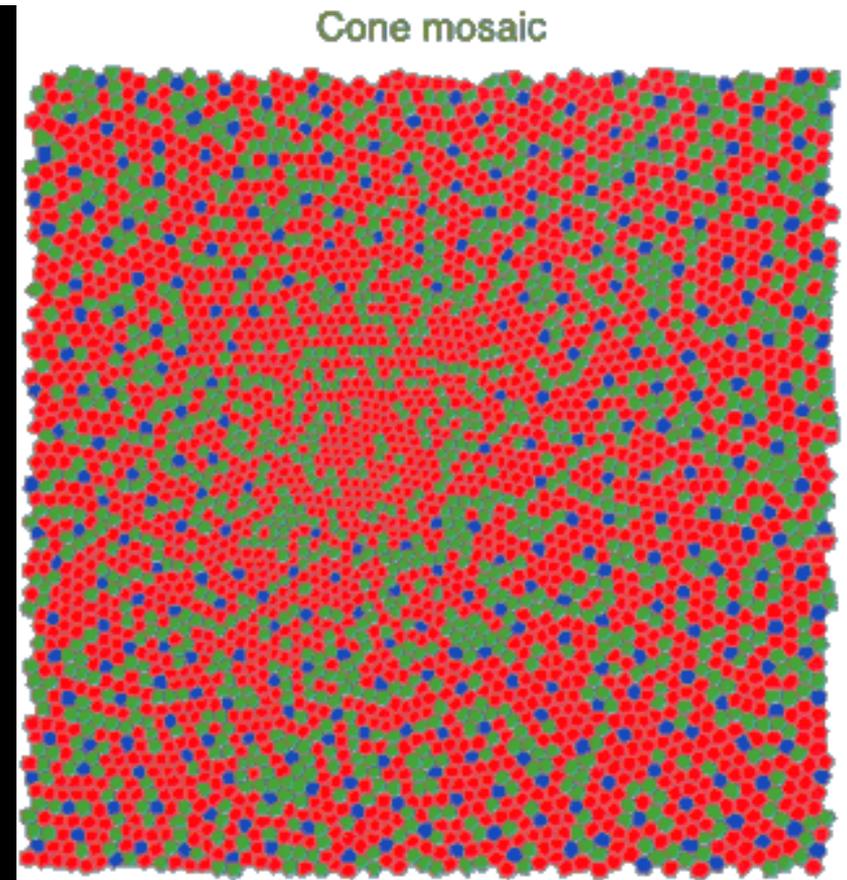
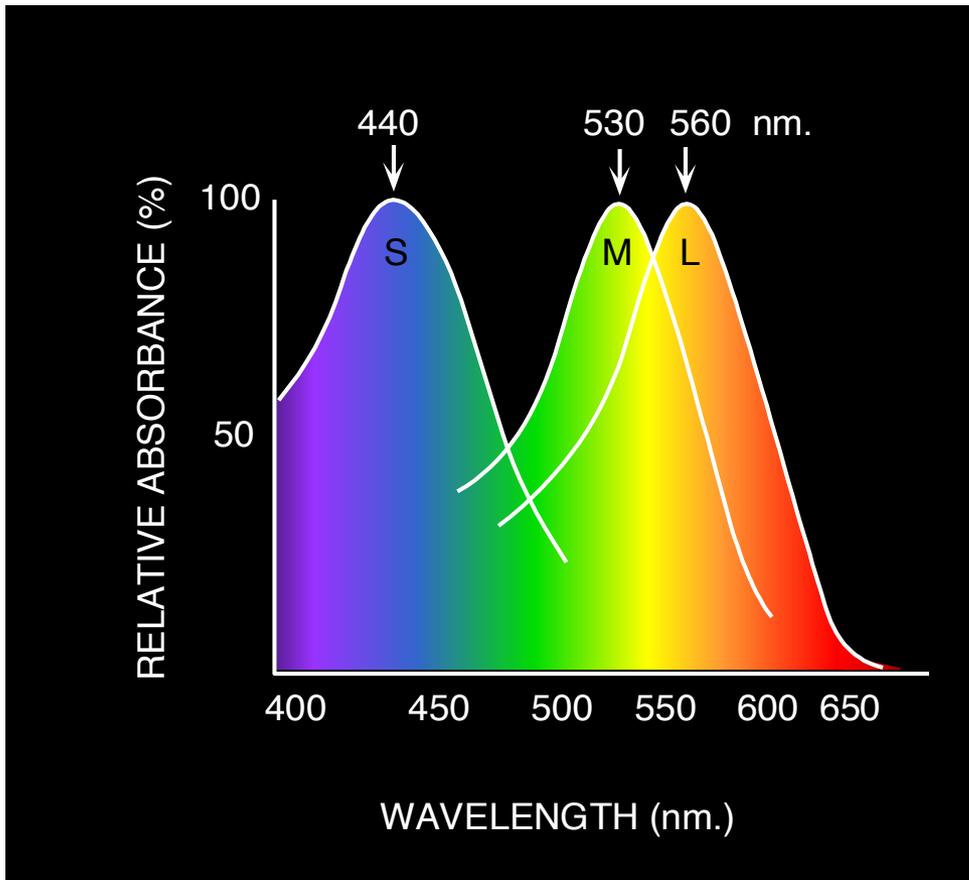
Slide Credit and Copyright: S. Palmer

# The Physics of Light



Slide Credit and Copyright: S. Palmer

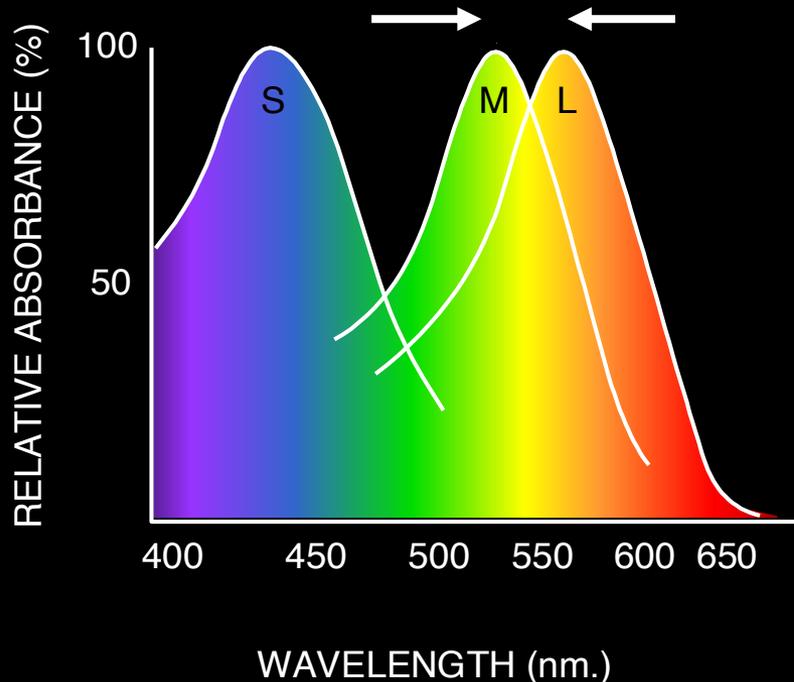
# The Physics of Light



Slide Credit and Copyright: S. Palmer

# Red-Green Color Blindness

"Peaks" of these red/green cones shifted, making it hard to distinguish red and green

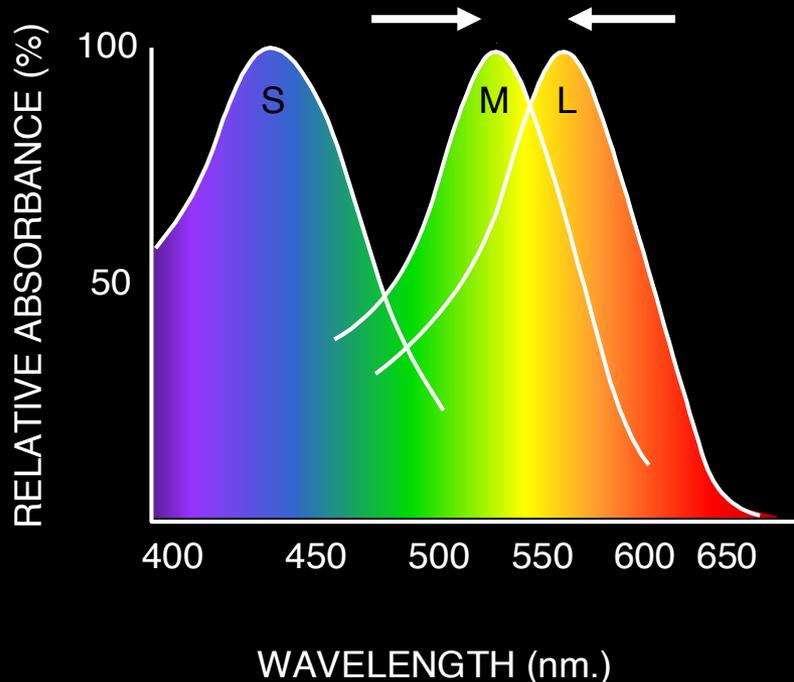


Four possibilities:

- **Deuteranomaly**: Green cone shifted toward red
- **Protanomaly**: Red cone shifted toward green
- **Deuteranopia**: Green cone missing
- **Protanopia**: Red cone missing

# Red-Green Color Blindness

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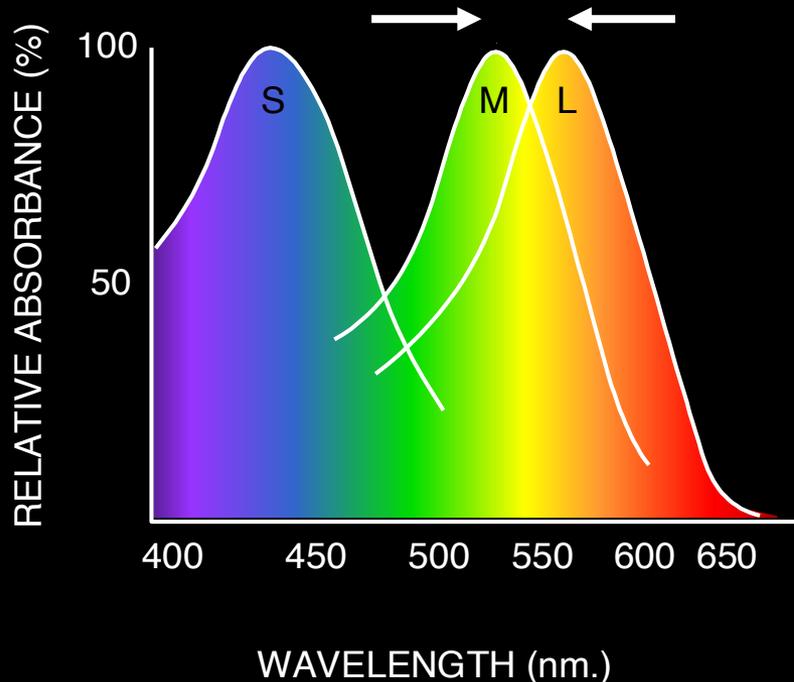


Four possibilities:

- **Deuteranomaly:** Green cone shifted toward red
- **Protanomaly:** Red cone shifted toward green
- **Deuteranopia:** Green cone missing
- **Protanopia:** Red cone missing
- Genes for red and green cones on X chromosome
- Men (XY): ~8% red-green color blind, (Northern European descent)
- Women (XX): ~0.5% red-green color blindness (Northern European descent)

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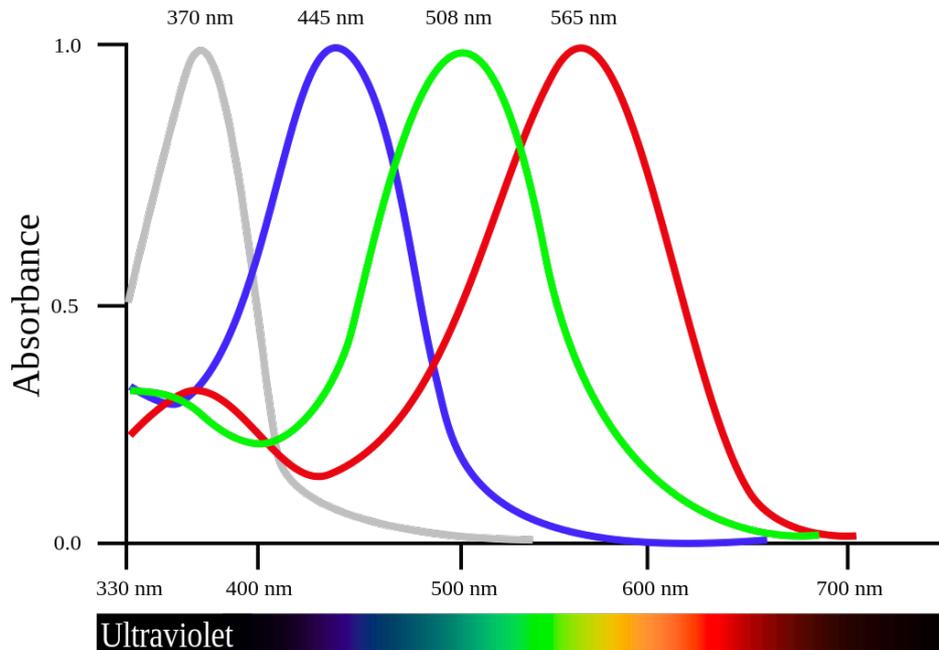
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- Men (XY): ~8% red-green color blind, (Northern European descent)
- Women (XX): ~0.5% red-green color blindness (Northern European descent)
- Up to 15% of women may have four types of cones! (Tetrachromacy)

Jordan and Mollon, "A study of women heterozygous for colour deficiencies", Vision Research 1993

# Color Vision in Animals

Birds have four types of cones:  
can see ultraviolet light



Some flowers have “Nectar Guides” visible under UV light



Visible Light

UV light

Human cones also sensitive to UV light! But blocked by lens

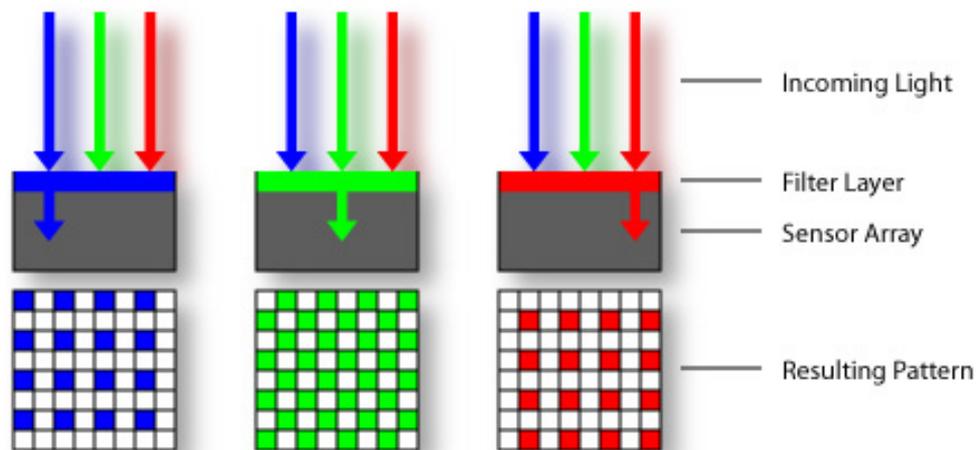
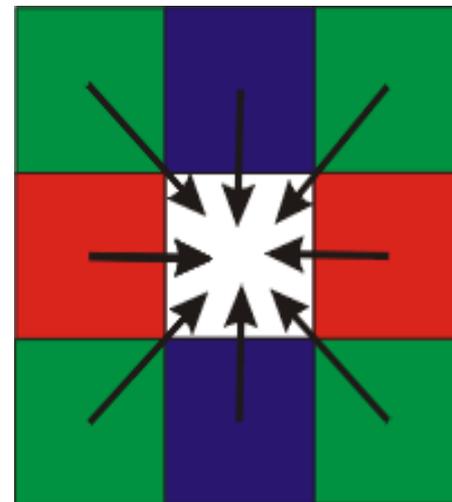
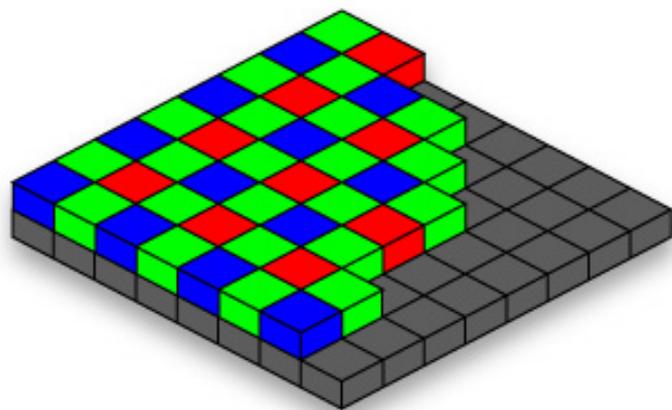
# Color Vision in Animals

Mantis Shrimp: Up to 16 types of photoreceptors!  
Can also detect polarization of light!



Image source: [Wikipedia](#)

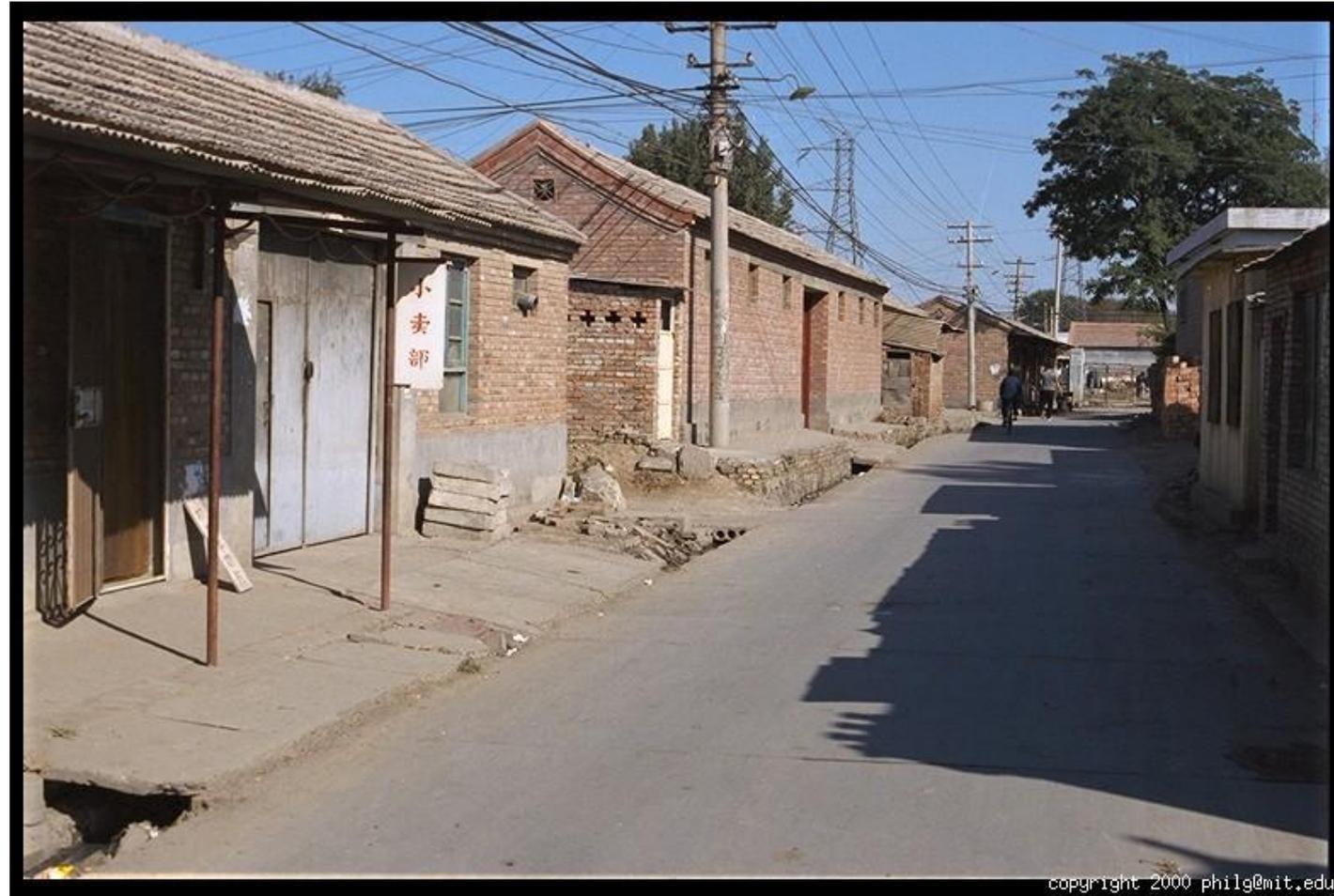
# Artificial Cones



Estimate RGB  
at 'G' cells from  
neighboring values

Slide Credit: S. Seitz

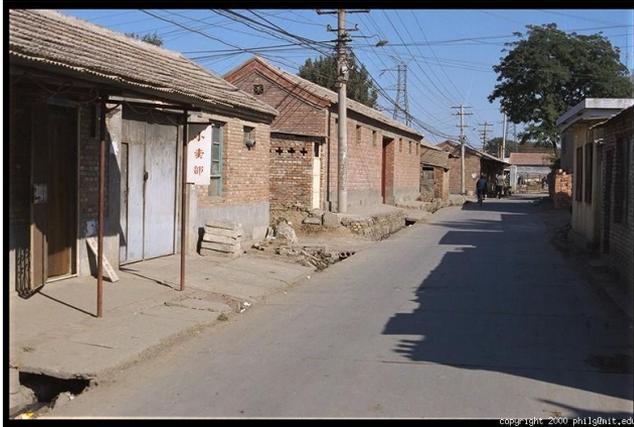
# Color Images



Slide Credit: J. Hays

# Color Images

Combined



Red



Green



Blue



Slide Credit: J. Hays



# Images in Python

Images are matrix / tensor `im`

`im[0,0,0]`

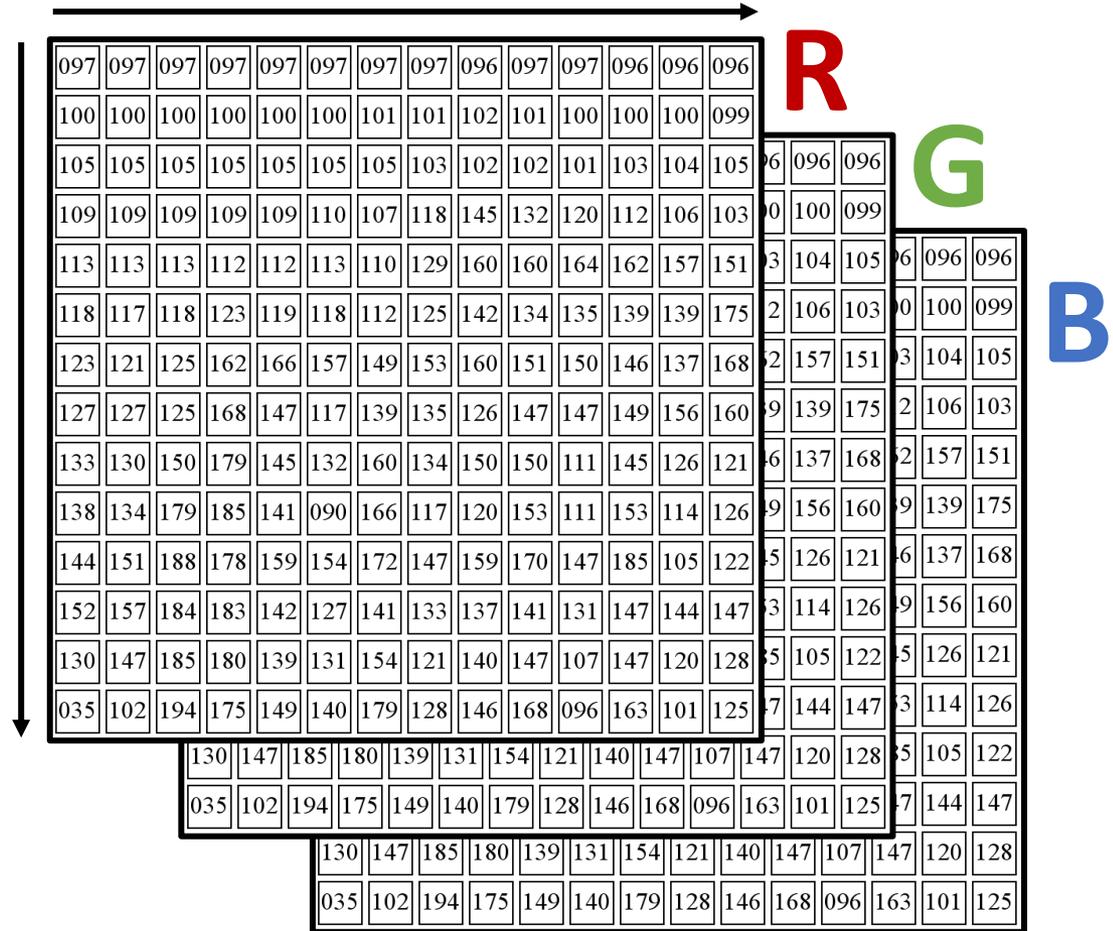
top, left, red

`im[y,x,c]`

row `y`, column `x`, channel `c`

`im[H-1,W-1,2]`

bottom right blue



Slide inspired by James Hays

# 5 Things to Remember

1. Origin is top left
2. Rows are first index (**what's the fastest direction for accessing?**)
3. Usually referred to as HWC (Height x Width x Channel)  
But you'll sometimes see CHW (especially with neural networks)
4. Typically stored as uint8 [0,255]
5. for  $y$  in range(H): for  $x$  in range(W): will run 1 million times for a 1000x1000 image. *A 4GHz processor can do only 4K clock cycles per pixel per second.*

# Representing Colors



**Discussion time: how many numbers do you actually need for colored light? Assume all tuples  $(R,G,B)$  are legitimate colors (they are).**

Image Credit: [http://en.wikipedia.org/wiki/File:RGB\\_illumination.jpg](http://en.wikipedia.org/wiki/File:RGB_illumination.jpg)

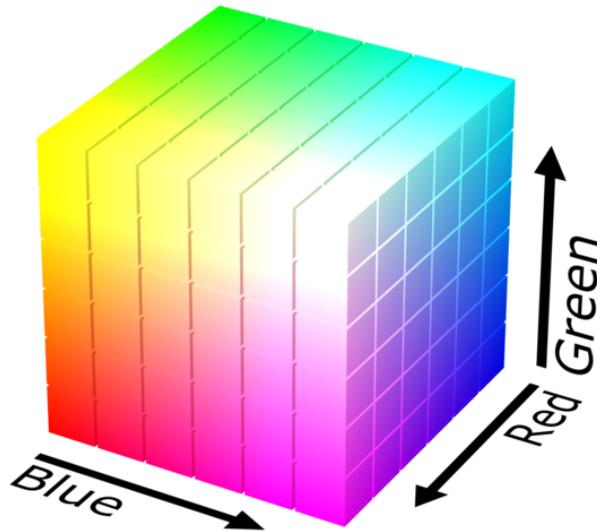
# One Option: RGB

## Pros

1. Simple
2. Common

## Cons

1. Distances don't make sense
2. Correlated



R



G



B

Slide Credit: J. Hays, RGB cube: [https://en.wikipedia.org/wiki/RGB\\_color\\_model](https://en.wikipedia.org/wiki/RGB_color_model)

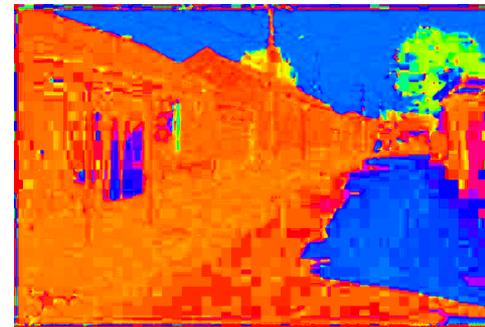
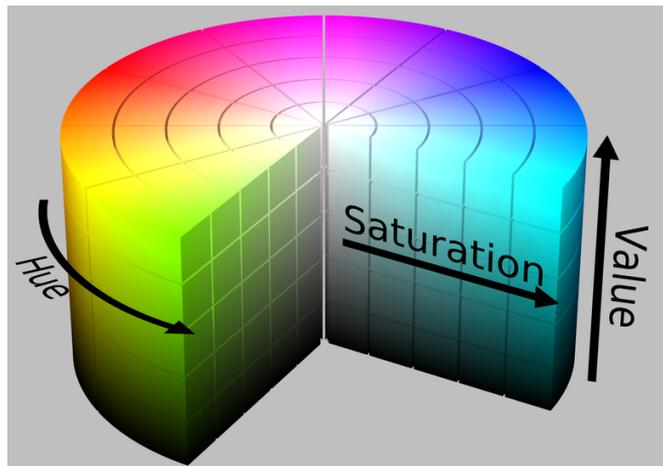
# Another Option: HSV

## Pros

1. Intuitive for picking colors
2. Sort of common
3. Fast to convert

## Cons

1. Not as good as other better spaces



**H**  
(S=1,V=1)



**S**  
(H=1,V=1)



**V**  
(H=1,S=0)

Slide Credit: J. Hays, HSV cylinder: [https://en.wikipedia.org/wiki/HSL\\_and\\_HSV](https://en.wikipedia.org/wiki/HSL_and_HSV)

# Another Option: YUV / YCbCr

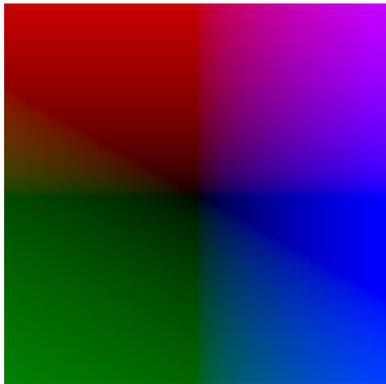
## Pros

1. Great for transmission / compression

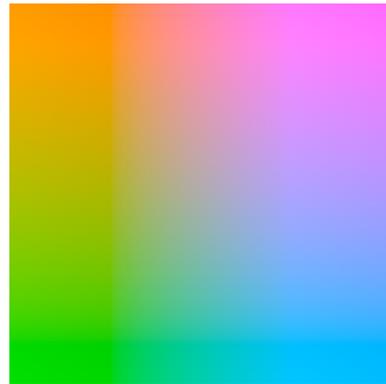
## Cons

1. Not as good as other better smart color spaces

Y = 0



Y = 0.5



**Y**  
(Cb=0.5,  
Cr=0.5)



**Cb**  
(Y=0.5,  
Cr=0.5)



**Cr**  
(Y=0.5,  
Cb=0.5)

Slide Credit: J. Hays, YUV cube: <https://en.wikipedia.org/wiki/YUV>

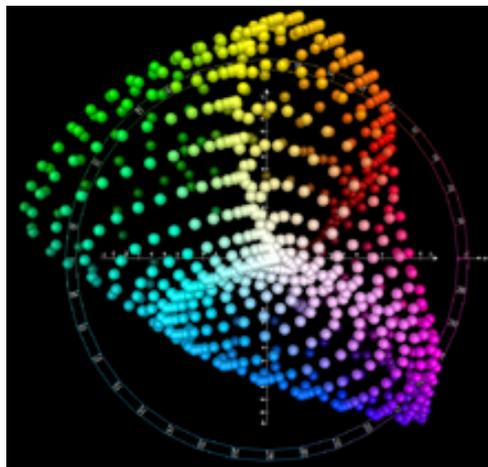
# Another Option: LAB

## Pros

1. Distances correspond with human judgment
2. Safe

## Cons

1. Complex to calculate (don't write it yourself, lots of fp calculations)



**L**  
(a=0,b=0)



**a**  
(L=65,b=0)



**b**  
(L=65,a=0)

Slide Credit: J. Hays, Lab diagram cube: [https://en.wikipedia.org/wiki/CIELAB\\_color\\_space](https://en.wikipedia.org/wiki/CIELAB_color_space)

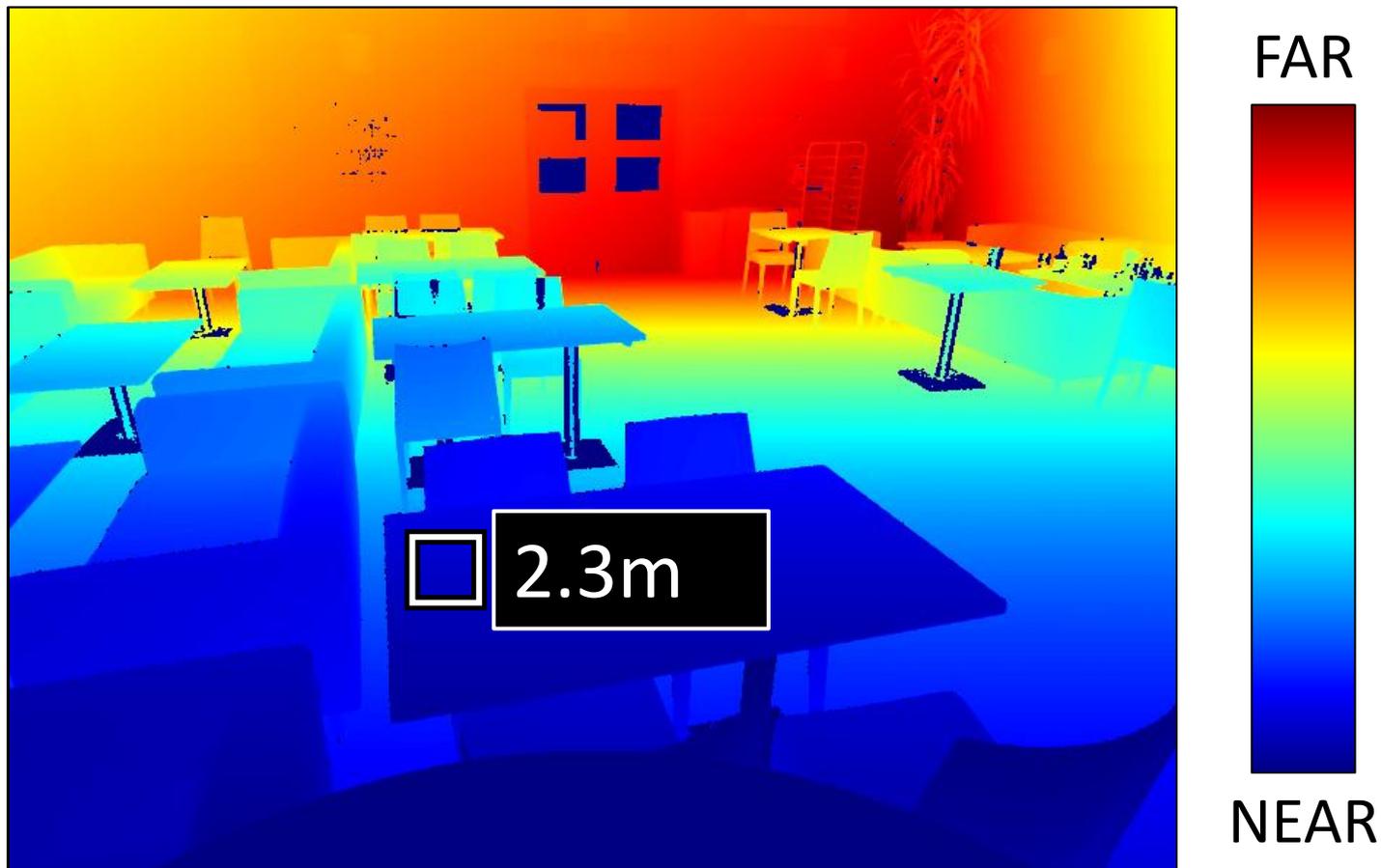
# Why are there so many?

- Each serves different functions
  - RGB: sort of intuitive, standard, everywhere
  - HSV: good for picking, fast to compute
  - YCbCr/YUV: fast to compute, compresses well
  - Lab: the right(?) thing to do, but “slow” to compute
- Pick based on what you need and don't sweat it: color really isn't crucial

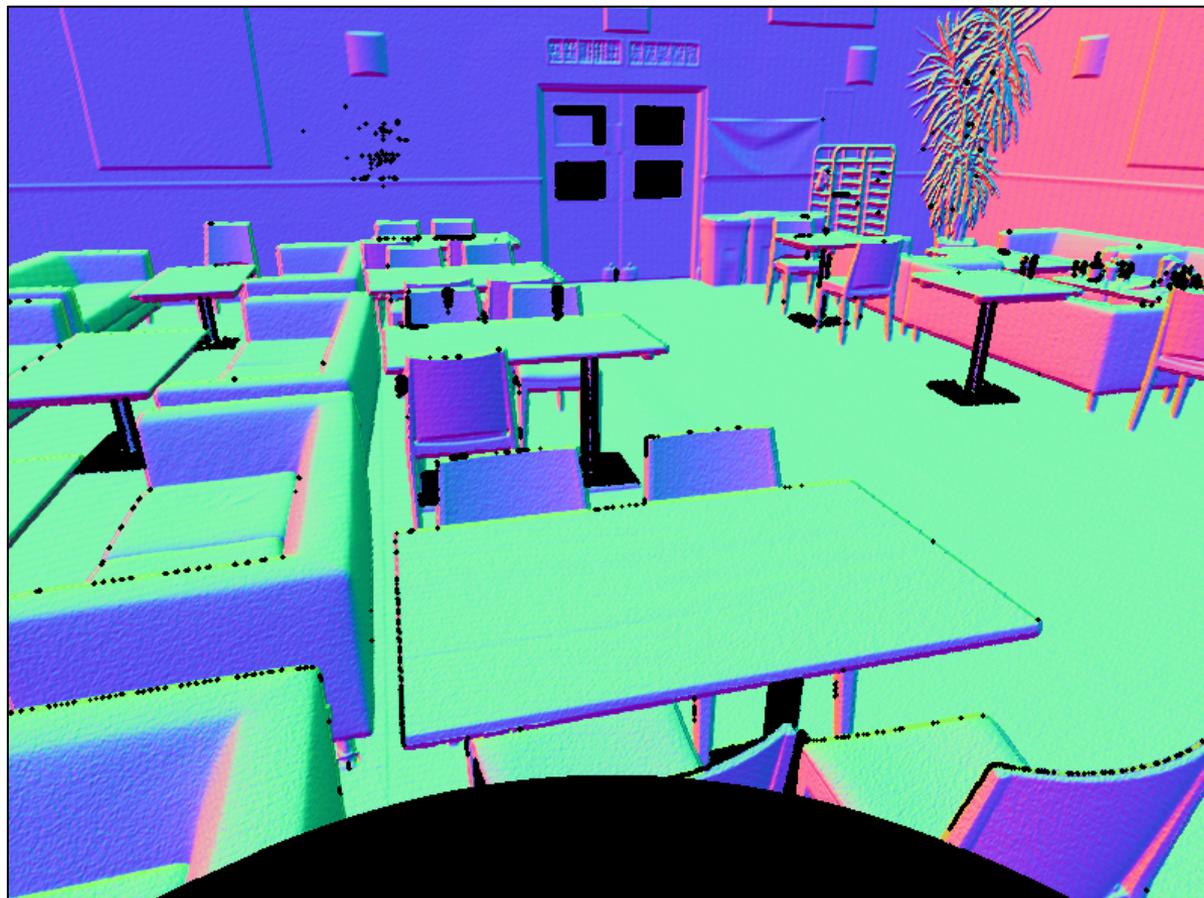
# Other Types of “Images”

- Almost all of this class is about ordinary RGB images because this has driven a lot of applications
- However, there are lots of other images

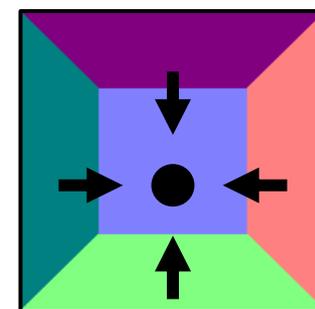
# Depth Map



# Surface Normals



Room



Legend

# Science Data

Magnetic Field in:

x, y, z

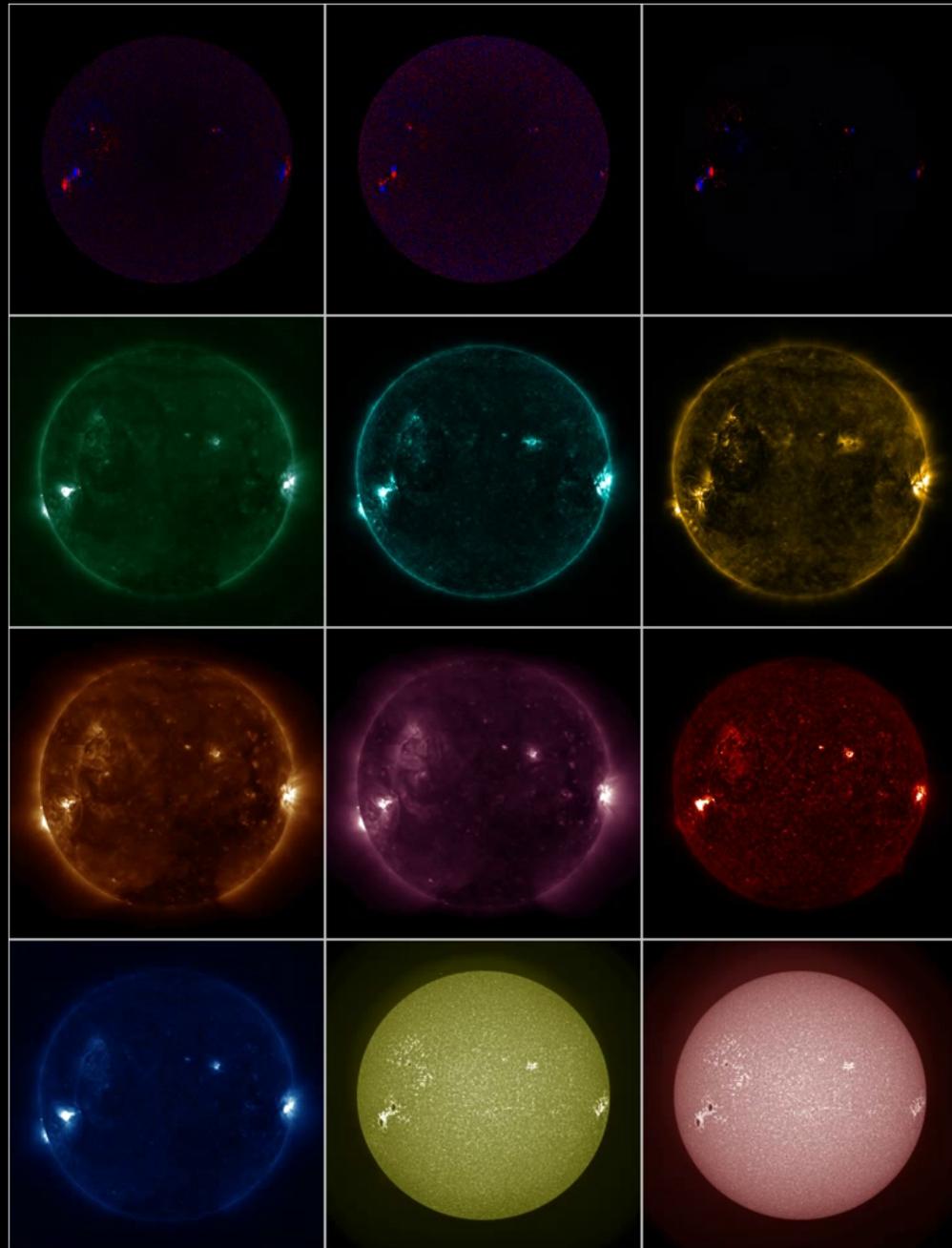
Light at 9 ~wavelenths:

9.4nm, 13.1nm, 17.1nm

19.3nm, 21.1nm, 30.4nm

33.5nm, 160nm, 170nm

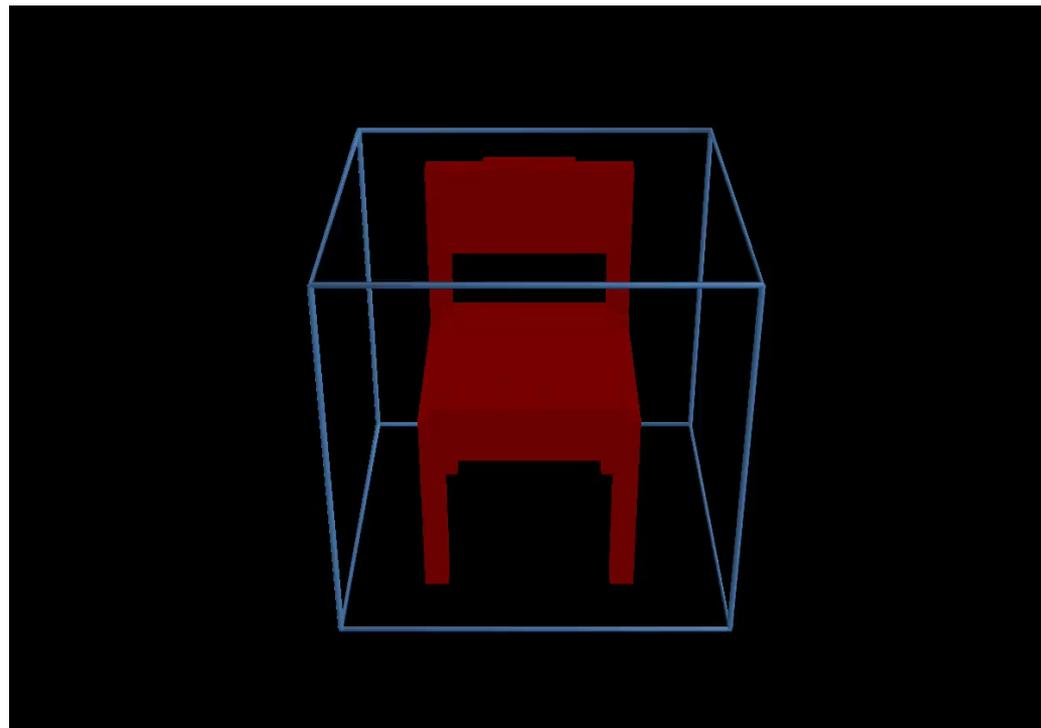
NASA Solar Dynamics Observatory  
observing solar flare



# Volumes

Volumes: images with more dimensions.

Emerge in 3D reconstruction, medical imaging, temporal data



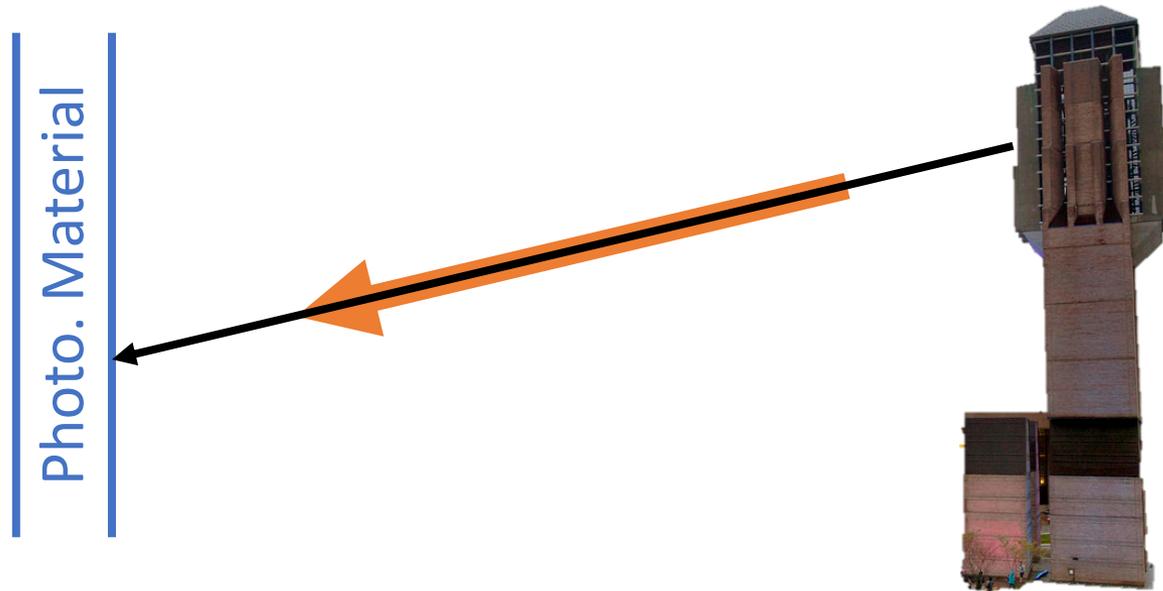
From: Girdhar et al., *Learning a predictable and generative vector representation for objects*. ECCV 2016

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- However, there are lots of other images

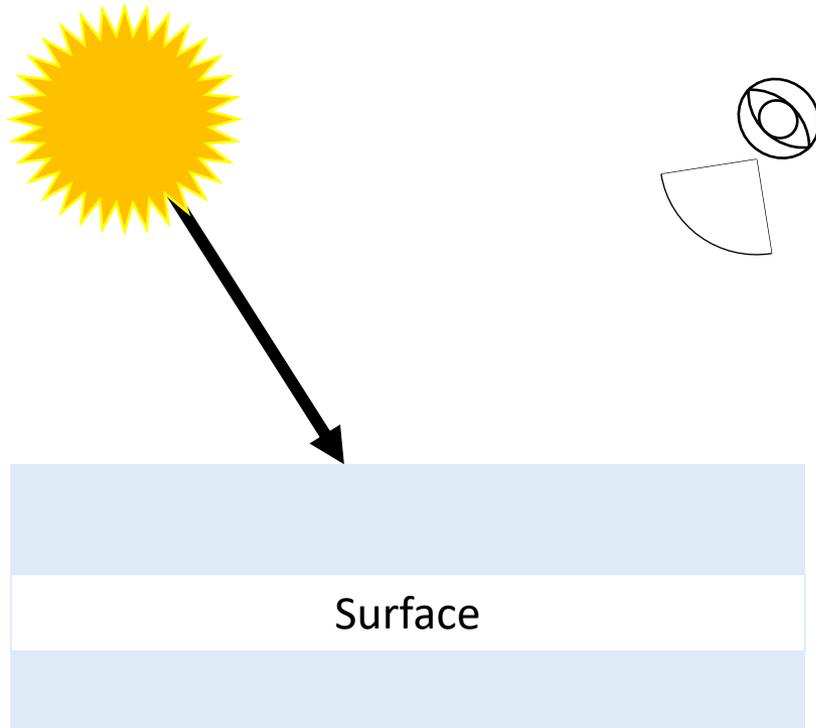
# So Far:

How do we represent **light**  
and its storage on **film**?



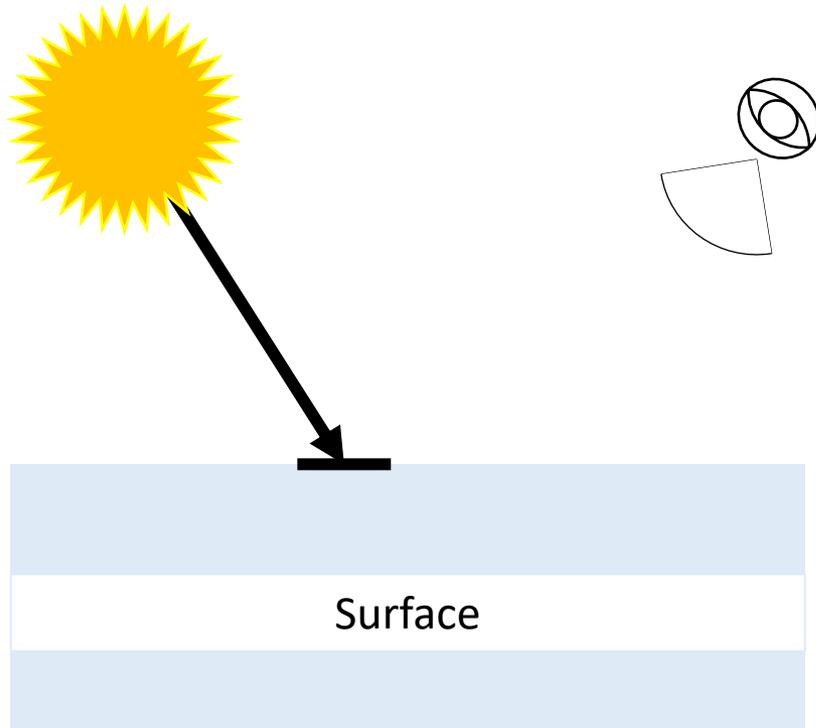


# Light and Surfaces



What happens when light hits a surface?

# Light and Surfaces

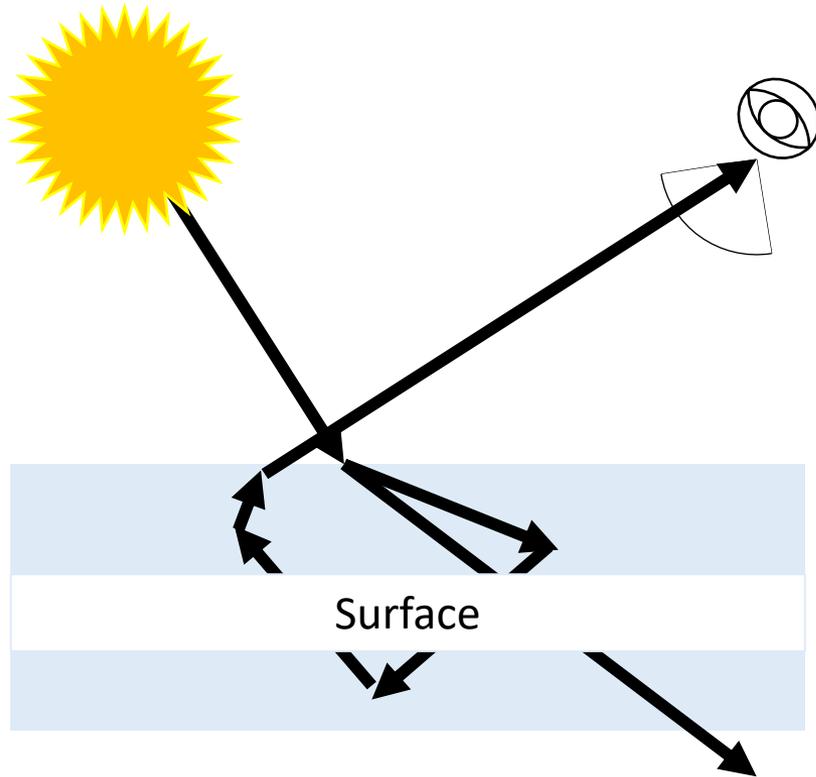


What happens when light hits a surface?

## **1. Absorbed**

It's absorbed and converted into some other form of energy (e.g., a black shirt getting hot in the sun)

# Light and Surfaces

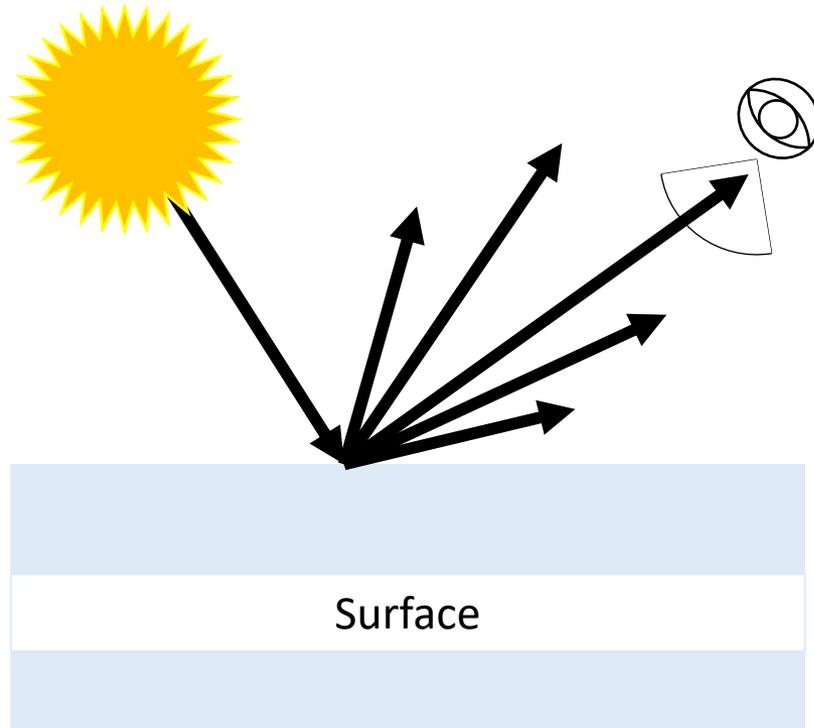


What happens when light hits a surface?

## 2. Transmitted

Possibly bouncing around before going through or out (e.g. lenses bend and go through, milk bounces around)

# Light and Surfaces

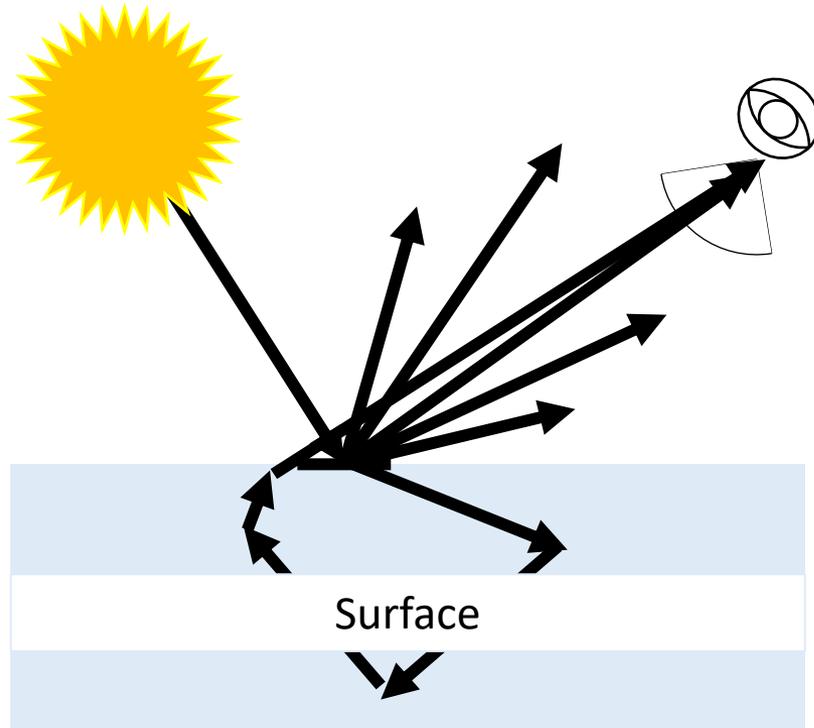


What happens when light hits a surface?

### 3. Reflected

It's reflected back, in one or more directions with varying amounts (e.g., mirror, or a white surface)

# Light and Surfaces

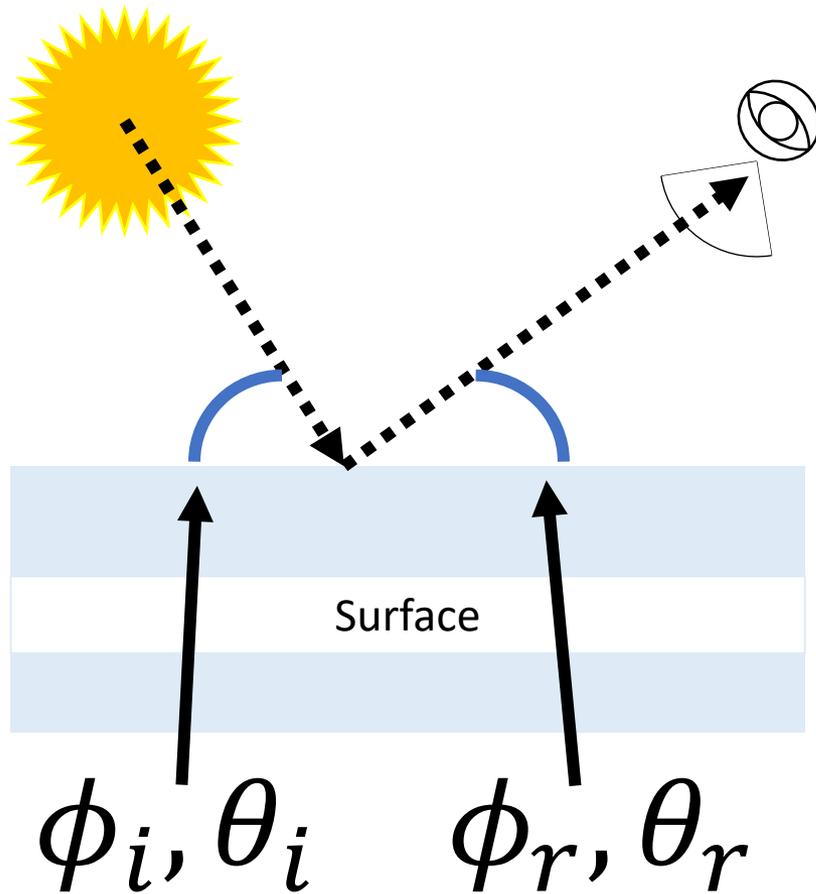


What happens when light hits a surface?

## **4. Everything**

All of the above! Real surfaces often have combinations of all of these options.

# Modeling Light and Surfaces



## Opaque Reflections

**Bi-directional reflectance distribution function (BRDF):**  
% reflected given  
*incident angle* to light  
*reflected angle* to the viewer.

***Note: have not specified form of function.***

# Specular and Diffuse Reflectionv

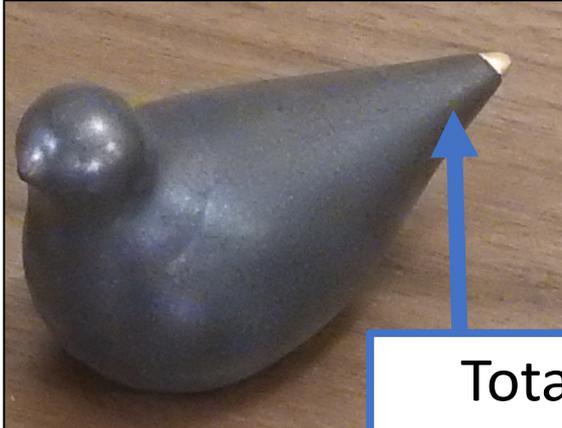
Same lighting, as close as possible camera settings,  
but different **location**



# Specular and Diffuse Reflection

Diffuse

Specular

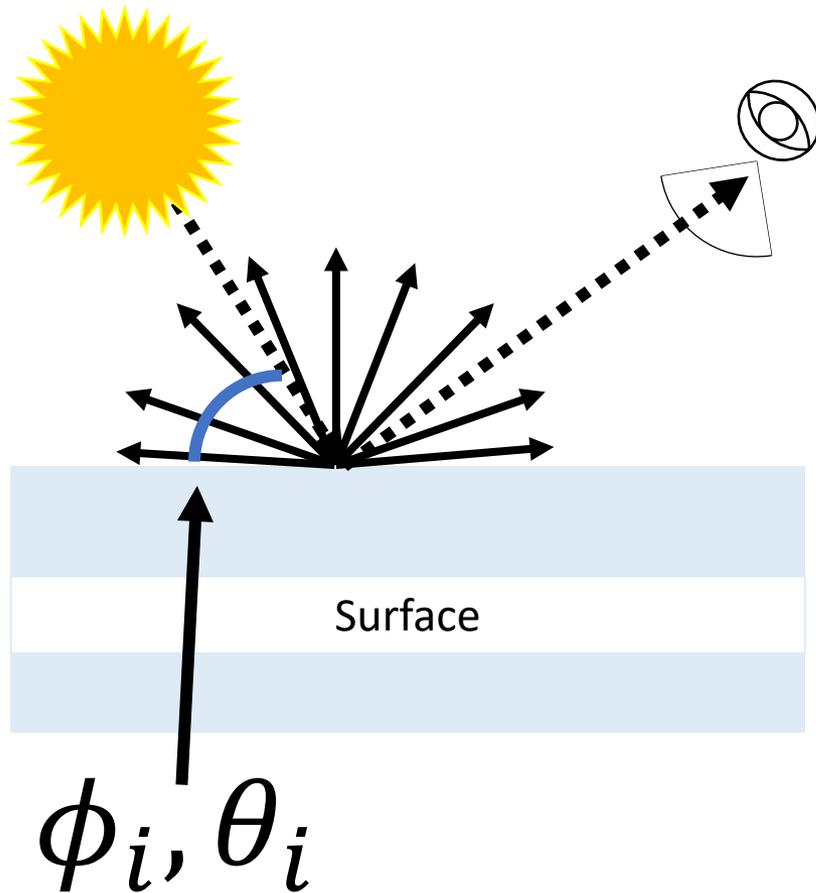


Basically same

Totally different



# Diffuse Reflection



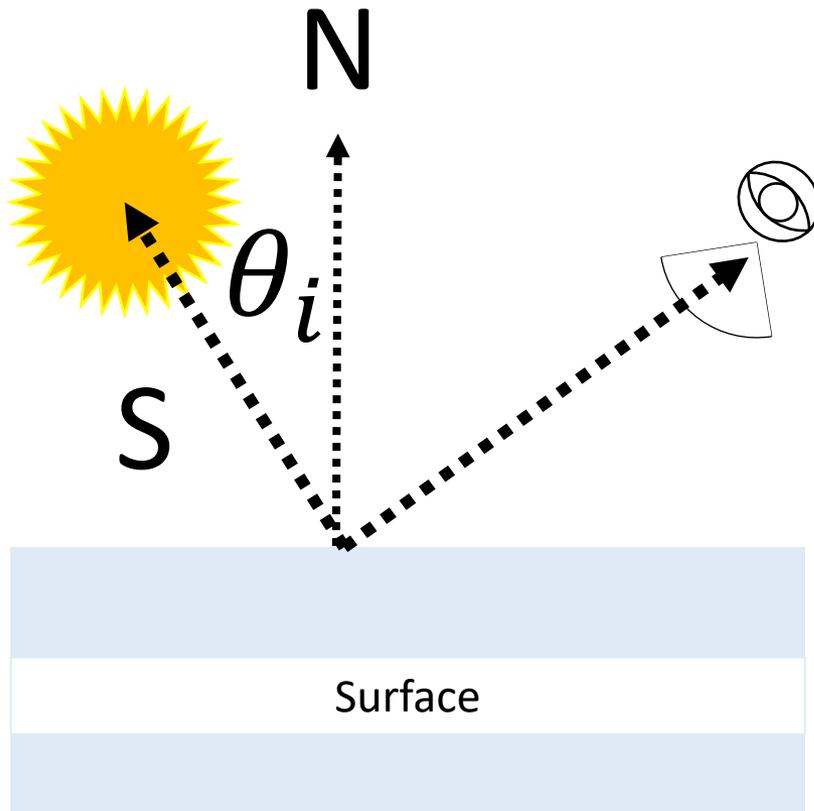
## Lambertian Surface

Light depends **only** on orientation of surface

$$\phi_i, \theta_i$$

to light. Result of random small facets. Looks identical at all views.

# Diffuse Reflection



## Lambert's Law

N: surface normal

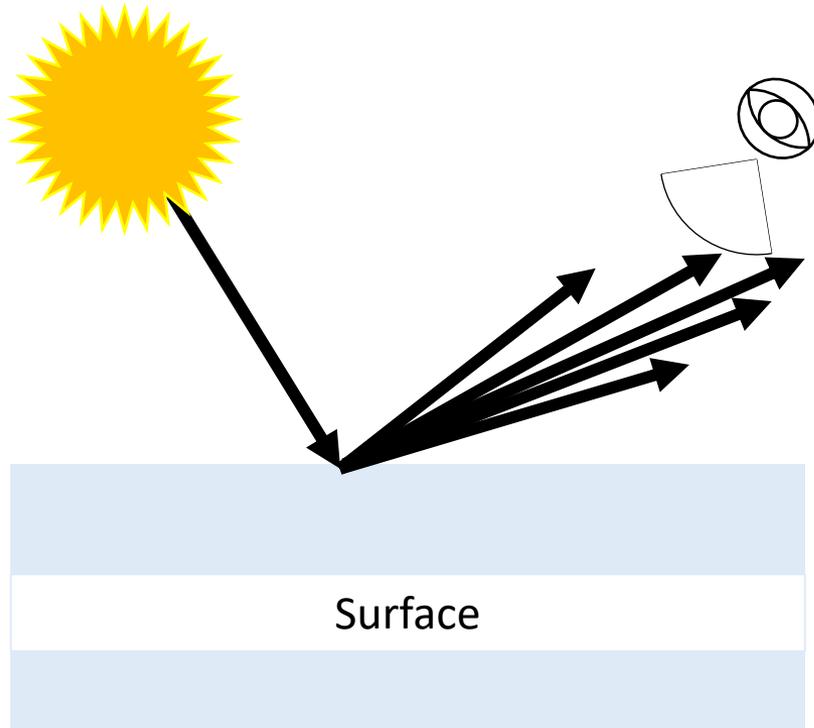
S: source direction **and**  
strength

$\rho$ : how much is reflected

$$B = \rho \mathbf{N} \cdot \mathbf{S}$$

$$B = \rho \|\mathbf{S}\| \cos(\theta)$$

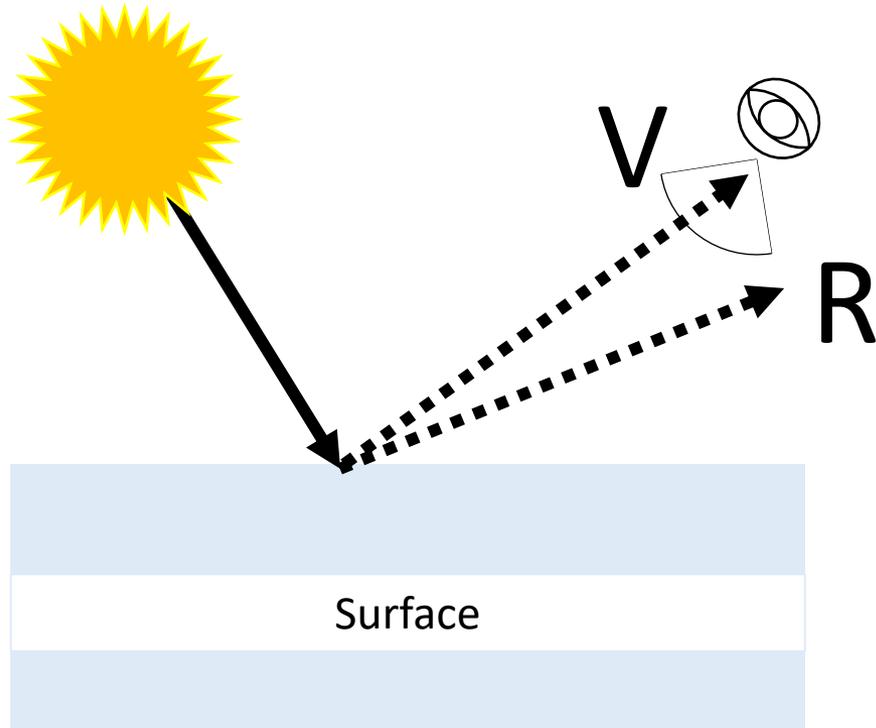
# Specular Reflection



## Specular Surface

Light reflected like a mirror, but spreads out in a “lobe” around the reflection ray

# Specular Reflection



## Phong Model

V: vector to viewer

R: reflection ray

$\alpha$ : shininess constant

$$B = (V^T R)^\alpha$$

# BRDFs can be very complex



Slide Credit: L. Lazebnik

# How is this useful?

## Shape from Shading

Lambert's Law: for every pixel  $i$

$$B_i = \rho N_i \cdot S$$

Reflected Light (1 dim)      Surface Orientation (3? dim)      Illumination Global, (3 dim)

Given: illumination and light, recover normals

**Potential problems?**

# Shape from Shading

$$B_i = \rho N_i \cdot S$$

1D, **fixed**      actually 2D      3D, **fixed**  
**unknown**

- System of equations that's underdetermined (N equations, 2N unknowns, N+3 known)
- **Solution:** Add more equations that enforce smoothness or finding a single surface.

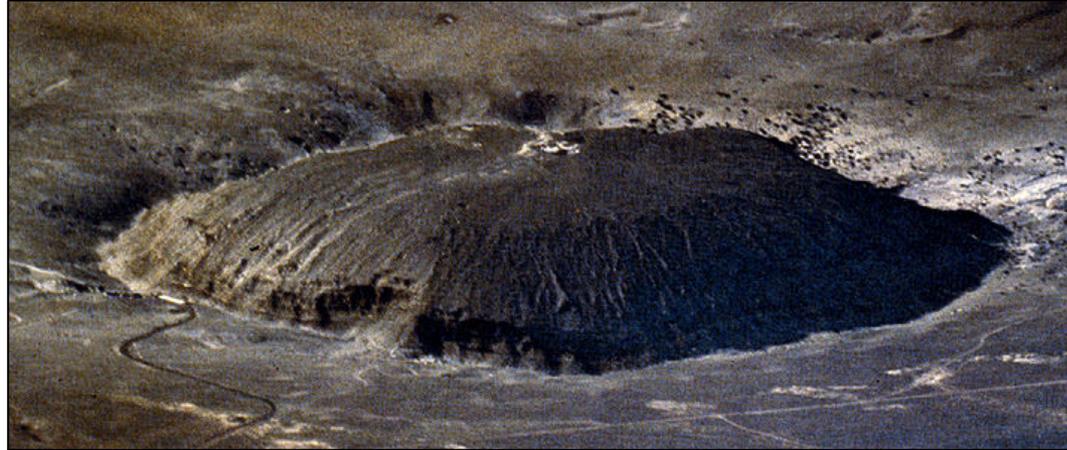
# Realistic Shape from Shading

$$B_i = \rho N_i \cdot S$$

1D, fixed                      2D unknown                      3D, unknown

- System of equations that's underdetermined (N equations,  $2N+3$  unknowns)
- **Solution:** need prior beliefs to disambiguate.

# Ambiguity



# Ambiguity

Humans assume light from above (and the blueness also tells you distance)

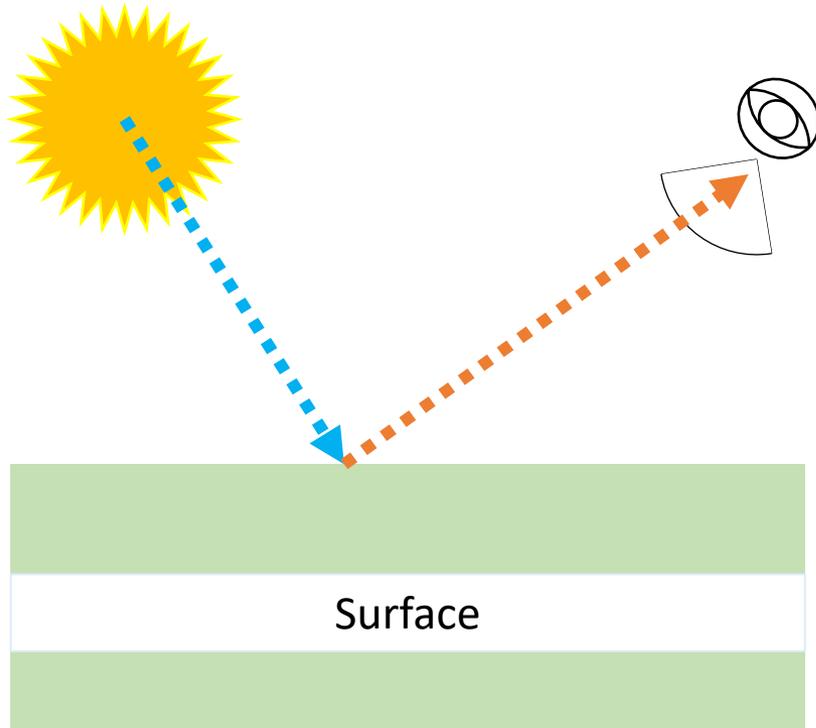


Photo Credit: [https://en.wikipedia.org/wiki/Meteor\\_Crater](https://en.wikipedia.org/wiki/Meteor_Crater)

# Shape from Shading in Practice

<https://www.youtube.com/watch?v=4GiLAOtjHNo>

# Modeling Light and Surfaces



**Color that reaches eye**  
depends on **color of light**  
and **color of material**

# Color Ambiguity: “The Dress”

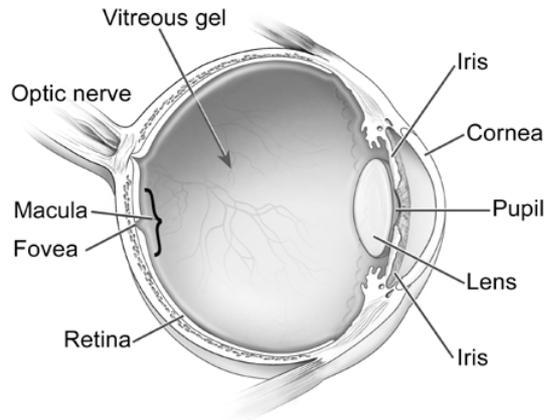
Blue / Black  
dress under  
yellow light?



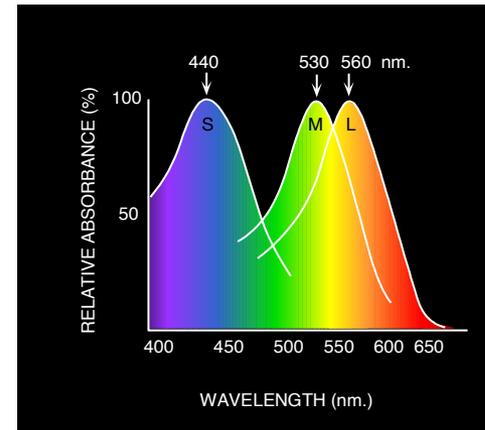
White / Gold  
dress under  
blue light?

[https://en.wikipedia.org/wiki/The\\_dress](https://en.wikipedia.org/wiki/The_dress)

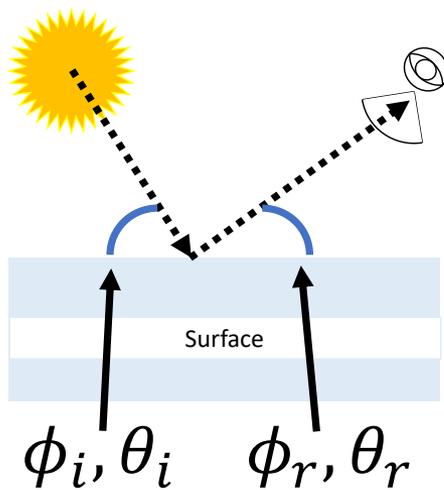
# Recap



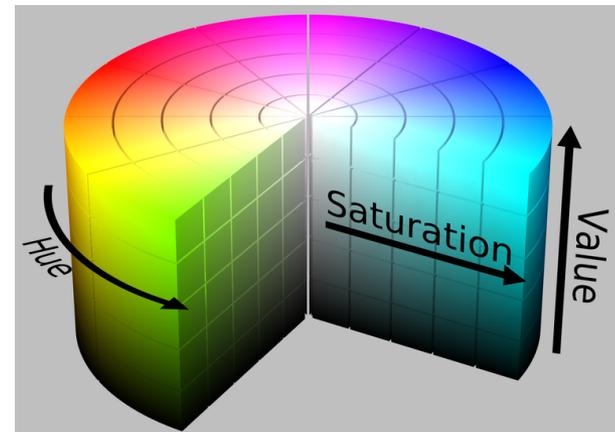
Human Eye



Color Vision



Light and Surfaces



Color Spaces

# Next Two Lectures: Numeric Linear Algebra Recap