

# Transformations and Fitting

EECS 442 – Prof. David Fouhey

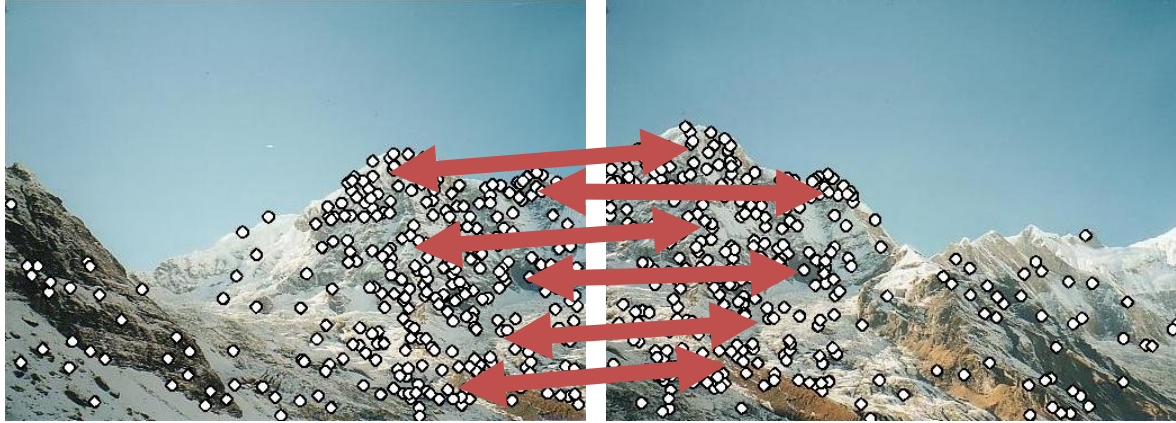
Winter 2019, University of Michigan

[http://web.eecs.umich.edu/~fouhey/teaching/EECS442\\_W19/](http://web.eecs.umich.edu/~fouhey/teaching/EECS442_W19/)

# Administrivia

- HW1 Graded
  - Overall the class did really well (mean: ~90%)
  - A few 0s for stuff like hand-written / not properly marked up homeworks. *Submit a regrade.*
  - We'll do late-day at end of semester. There's a calculator for grade given late hours.
- HW2 Due Thursday 11:59.99PM
  - We've added a contest. Post the highest validation accuracy you can get (***fairly***: without training on the test set, and while doing bag of words).

# So Far



1. How do we find distinctive / easy to locate features? (*Harris/Laplacian of Gaussian*)
2. How do we describe the regions around them? (*histogram of gradients*)
3. How do we match features? (L2 distance)
4. How do we handle outliers? (RANSAC)

# Today

As promised: warping one image to another

# Why Mosaic?

- Compact Camera FOV = 50 x 35°



# Why Mosaic?

- Compact Camera FOV =  $50 \times 35^\circ$
- Human FOV =  $200 \times 135^\circ$



# Why Mosaic?

- Compact Camera FOV =  $50 \times 35^\circ$
- Human FOV =  $200 \times 135^\circ$
- Panoramic Mosaic =  $360 \times 180^\circ$





# Why Bother With This Math?

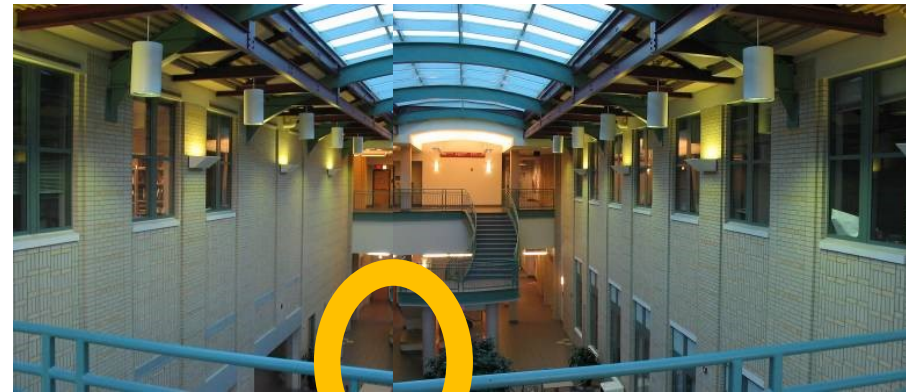
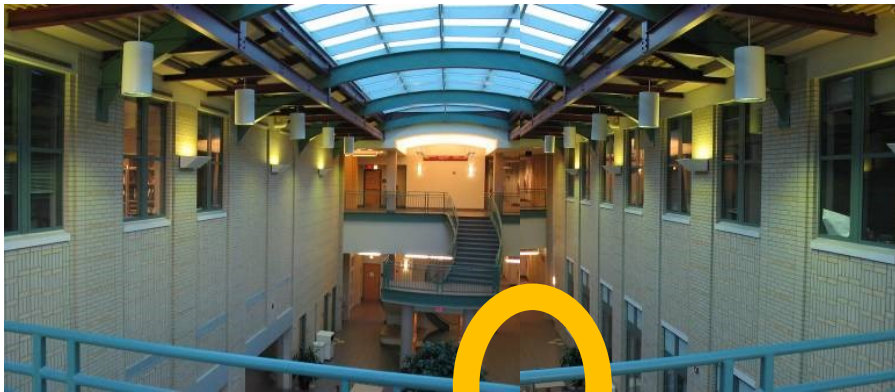




# Homework 1 Style



Translation only via alignment



# Result



# Image Transformations

Image filtering: change range of image

$$g(x) = T(f(x))$$

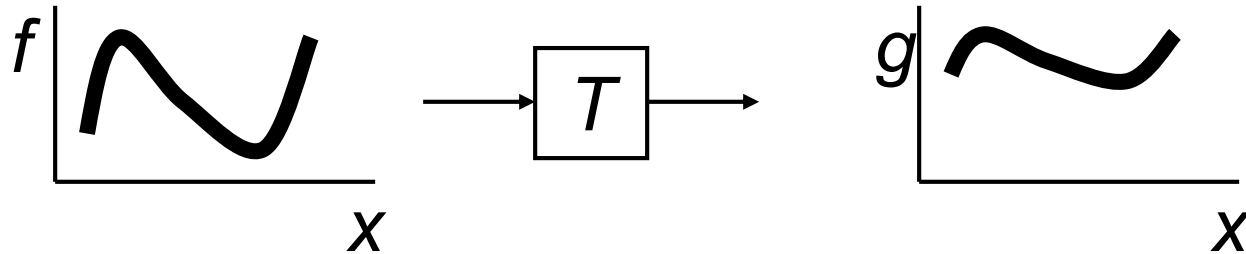
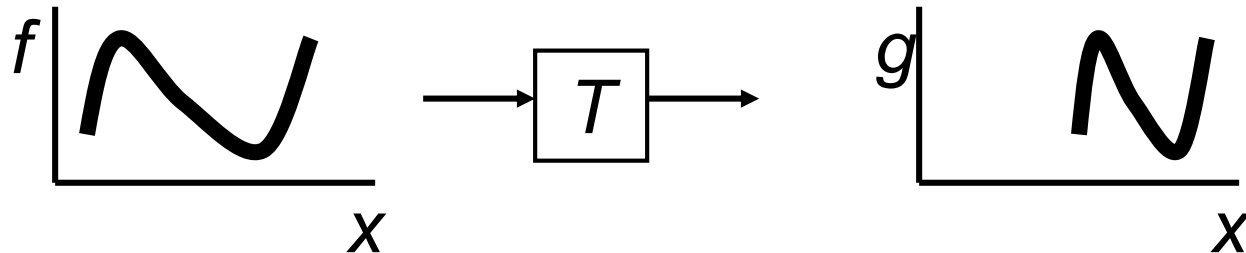


Image warping: change **domain** of image

$$g(x) = f(T(x))$$



# Image Transformations

Image filtering: change range of image

$$g(x) = T(f(x))$$

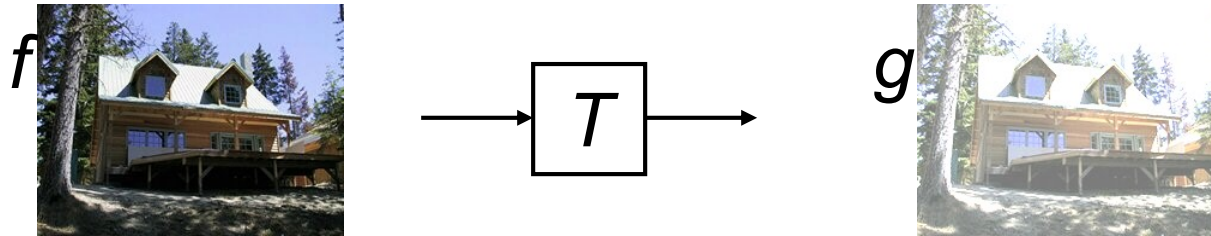
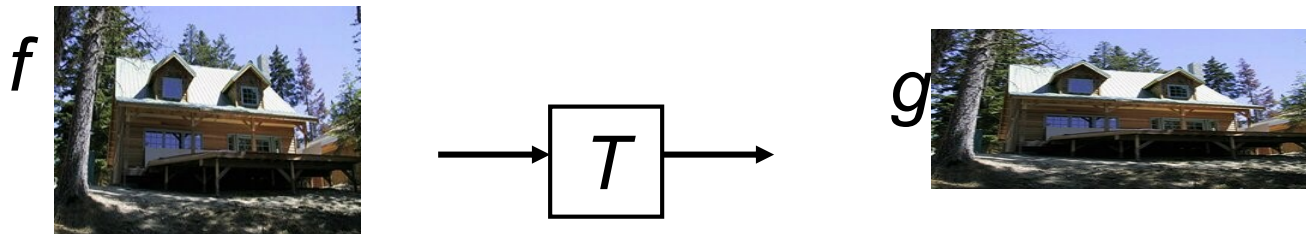


Image warping: change **domain** of image

$$g(x) = f(T(x))$$





# Parametric (Global) warping

## Examples of parametric warps



translation



rotation



aspect



affine



perspective



cylindrical

# Parametric (Global) Warping

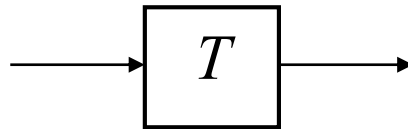
T is a coordinate changing machine

$$\mathbf{p}' = T(\mathbf{p})$$

Note: T is the same for all points, has relatively few parameters, and does **not** depend on image content



$$\mathbf{p} = (x, y)$$



$$\mathbf{p}' = (x', y')$$



# Parametric (Global) Warping

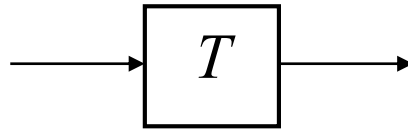
Today we'll deal with linear warps

$$\mathbf{p}' \equiv T\mathbf{p}$$

$T$ : matrix;  $\mathbf{p}$ ,  $\mathbf{p}'$ : 2D points. Start with normal points and  $\equiv$ , then do homogeneous coords and  $\equiv$



$$\mathbf{p} = (x, y)$$

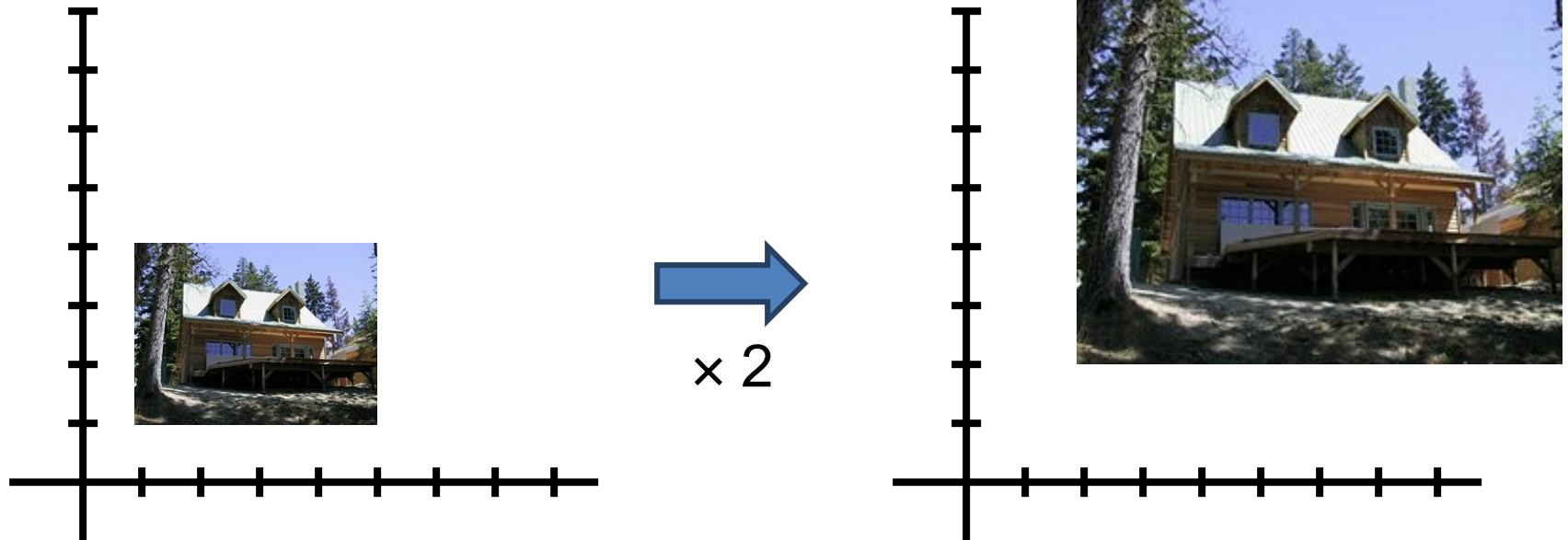


$$\mathbf{p}' = (x', y')$$

# Scaling

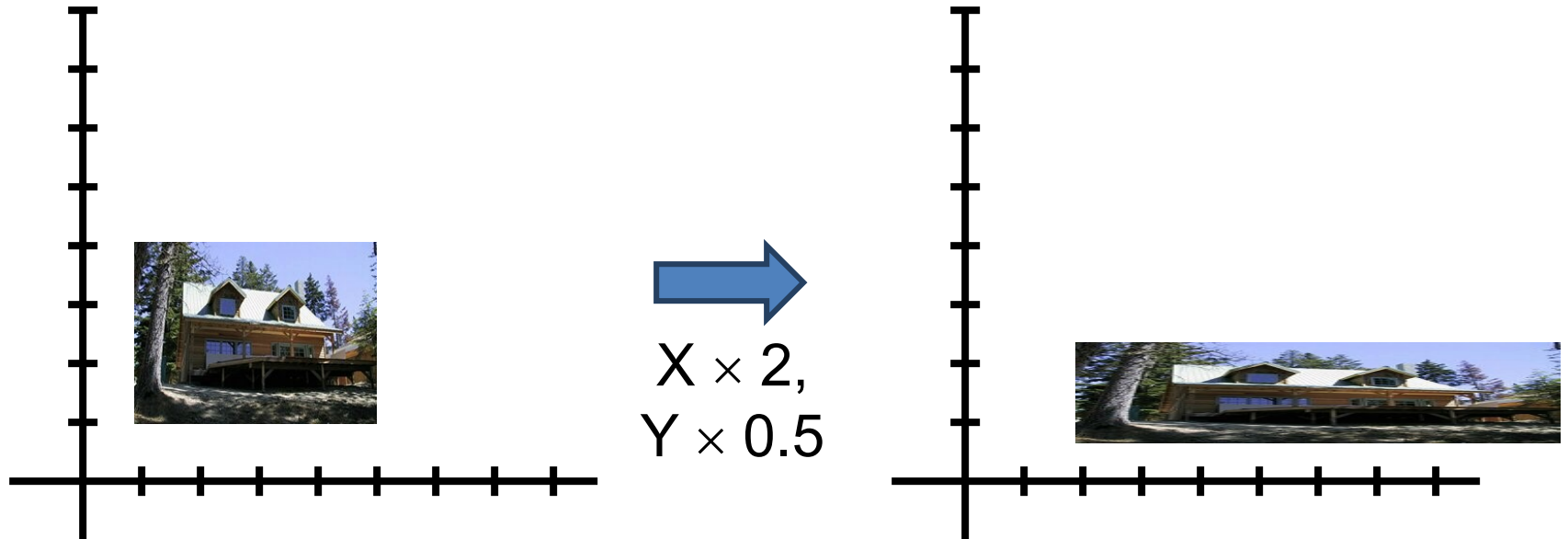
**Scaling** multiplies each component  $(x,y)$  by a scalar.  
**Uniform** scaling is the same for all components.

*Note the corner goes from  $(1,1)$  to  $(2,2)$*



# Scaling

**Non-uniform scaling** multiplies each component by a different scalar.



# Scaling

**What does T look like?**

$$x' = ax$$

$$y' = by$$

Let's convert to a matrix:

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \underbrace{\begin{bmatrix} s_x & 0 \\ 0 & s_y \end{bmatrix}}_{\text{scaling matrix } S} \begin{bmatrix} x \\ y \end{bmatrix}$$

*scaling matrix S*

**What's the inverse of S?**

# 2D Rotation

## Rotation Matrix



$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} \cos(\theta) & -\sin(\theta) \\ \sin(\theta) & \cos(\theta) \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

But wait! Aren't sin/cos non-linear?

$x'$  is a linear combination/function of  $x$ ,  $y$

$x'$  is not a linear function of  $\theta$

What's the inverse of  $R_\theta$ ?  $I = R_\theta^T R_\theta$

# Things You Can Do With 2x2

## Identity / No Transformation



$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

## Shear



$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} 1 & sh_x \\ sh_y & 1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$



# Things You Can Do With 2x2

Before



After



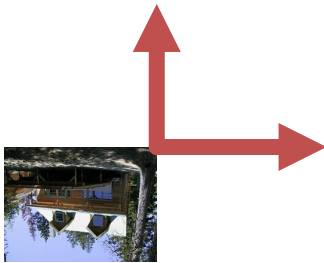
## 2D Mirror About Y-Axis

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

Before



After



## 2D Mirror About X,Y

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} -1 & 0 \\ 0 & -1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

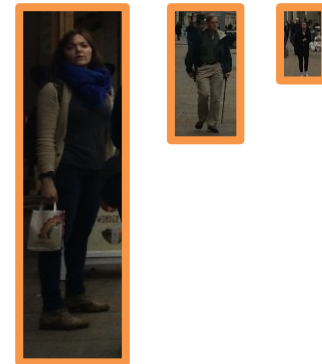
# What's Preserved?



3D lines project to 2D lines  
so lines are preserved

Projections of parallel 3D  
lines are not necessarily  
parallel, so not parallelism

Distant objects are smaller  
so size is not preserved



# What's Preserved With a 2x2

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} a & b \\ c & d \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = T \begin{bmatrix} x \\ y \end{bmatrix}$$

After multiplication by T (irrespective of T)

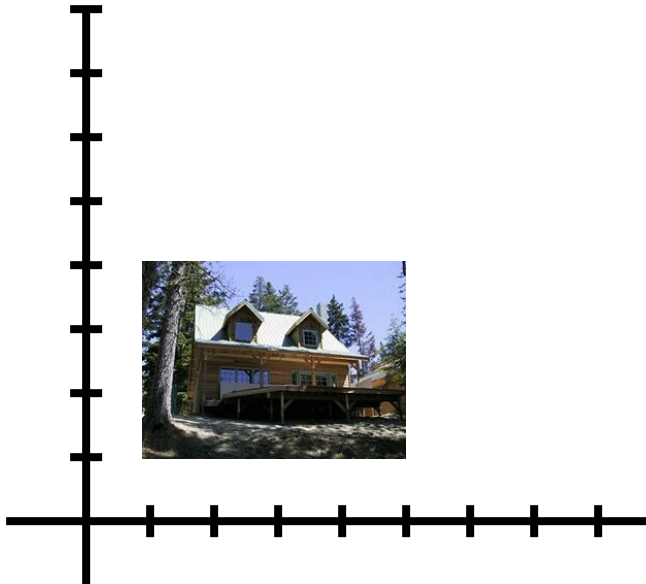
- Origin is origin:  **$\mathbf{0} = T\mathbf{0}$** 
  - Lines are lines
  - Parallel lines are parallel
- Ratios between distances the same **if scaling is uniform (otherwise no)**

# Things You Can't Do With 2x2

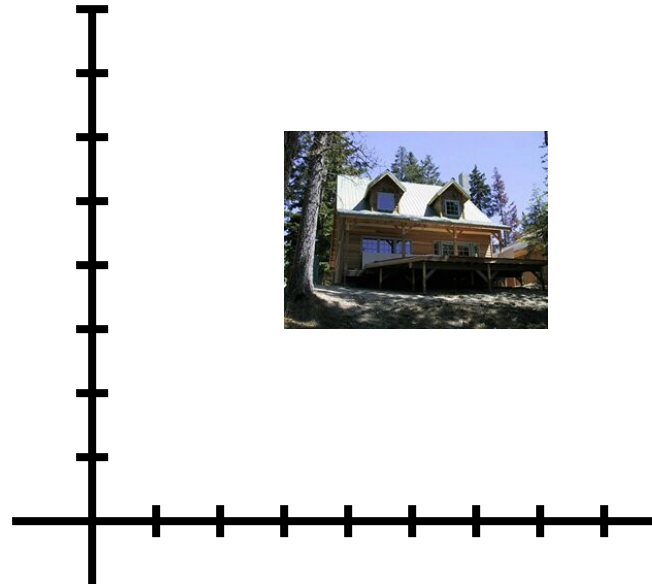
What about translation?

$$x' = x + t_x, y' = y + t_y$$

**How do we fix it?**



➔  
 $+(2,2)$

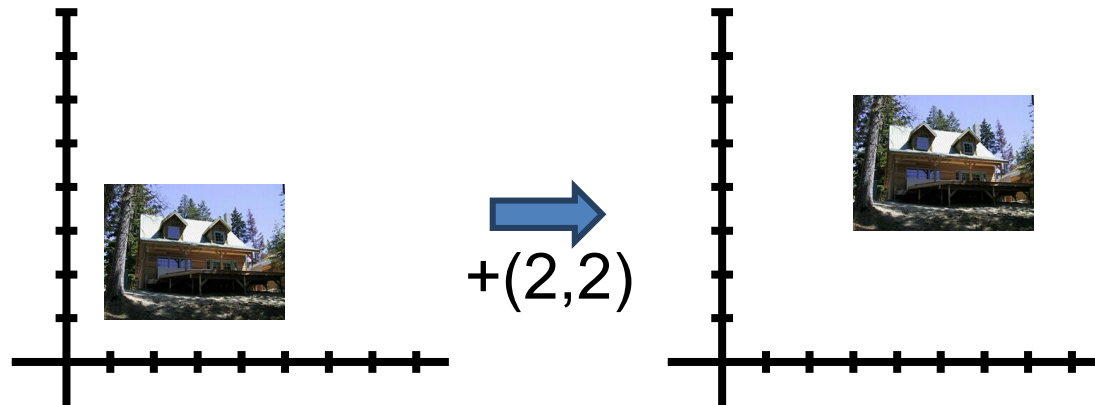


# Homogeneous Coordinates Again

What about translation?

$$x' = x + t_x, y' = y + t_y$$

$$\begin{bmatrix} x + t_x \\ y + t_y \\ 1 \end{bmatrix} \equiv \begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} \equiv \begin{bmatrix} 1 & 0 & t_x \\ 0 & 1 & t_y \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$



# Representing 2D Transformations

How do we represent a 2D transformation?

Let's pick scaling

$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} \equiv \begin{bmatrix} s_x & 0 & a \\ 0 & s_y & b \\ d & e & f \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

What's

<b>a</b>	<b>b</b>	<b>d</b>	<b>e</b>	<b>f</b>
<b>0</b>	<b>0</b>	<b>0</b>	<b>0</b>	<b>1</b>



# Affine Transformations

Affine: *linear transformation plus translation*



$$\begin{bmatrix} x' \\ y' \\ w' \end{bmatrix} \equiv \begin{bmatrix} a & b & c \\ d & e & f \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

**Will the last coordinate always be 1?**

In general (without homogeneous coordinates)

$$\mathbf{x}' = \mathbf{Ax} + \mathbf{b}$$

# Matrix Composition

We can combine transformations via matrix multiplication.

$$\begin{bmatrix} x' \\ y' \\ w' \end{bmatrix} \equiv \underbrace{\begin{bmatrix} 1 & 0 & t_x \\ 0 & 1 & t_y \\ 0 & 0 & 1 \end{bmatrix}}_{T(t_x, t_y)} \underbrace{\begin{bmatrix} \cos(\theta) & -\sin(\theta) & 0 \\ \sin(\theta) & \cos(\theta) & 0 \\ 0 & 0 & 1 \end{bmatrix}}_{R(\theta)} \underbrace{\begin{bmatrix} s_x & 0 & 0 \\ 0 & s_y & 0 \\ 0 & 0 & 1 \end{bmatrix}}_{S(s_x, s_y)} \begin{bmatrix} x \\ y \\ w \end{bmatrix}$$

**Does order matter?**

# What's Preserved With Affine

$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} \equiv \begin{bmatrix} a & b & c \\ d & e & f \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix} \equiv T \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

After multiplication by T (irrespective of T)

- ~~Origin is origin:  $0 = T0$~~ 
  - Lines are lines
  - Parallel lines are parallel
- Ratios between distances? (If scaling is uniform: yes, otherwise no)

# Perspective Transformations

Set bottom row to not  $[0,0,1]$

Called a perspective/projective transformation or a ***homography***



$$\begin{bmatrix} x' \\ y' \\ w' \end{bmatrix} \equiv \begin{bmatrix} a & b & c \\ d & e & f \\ g & h & i \end{bmatrix} \begin{bmatrix} x \\ y \\ w \end{bmatrix}$$

**How many degrees of freedom?**

# How Many Degrees of Freedom?

Recall: can always scale by non-zero value

Perspective 
$$\begin{bmatrix} x' \\ y' \\ w' \end{bmatrix} \equiv \begin{bmatrix} a & b & c \\ d & e & f \\ g & h & i \end{bmatrix} \begin{bmatrix} x \\ y \\ w \end{bmatrix}$$

$$\begin{bmatrix} x' \\ y' \\ w' \end{bmatrix} \equiv \frac{1}{i} \begin{bmatrix} x' \\ y' \\ w' \end{bmatrix} \equiv \frac{1}{i} \begin{bmatrix} a & b & c \\ d & e & f \\ g & h & i \end{bmatrix} \begin{bmatrix} x \\ y \\ w \end{bmatrix} \equiv \begin{bmatrix} a/i & b/i & c/i \\ d/i & e/i & f/i \\ g/i & h/i & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ w \end{bmatrix}$$

Homography can always be re-scaled by  $\lambda \neq 0$

# What's Preserved With Perspective

$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} \equiv \begin{bmatrix} a & b & c \\ d & e & f \\ g & h & i \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix} \equiv \mathbf{T} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

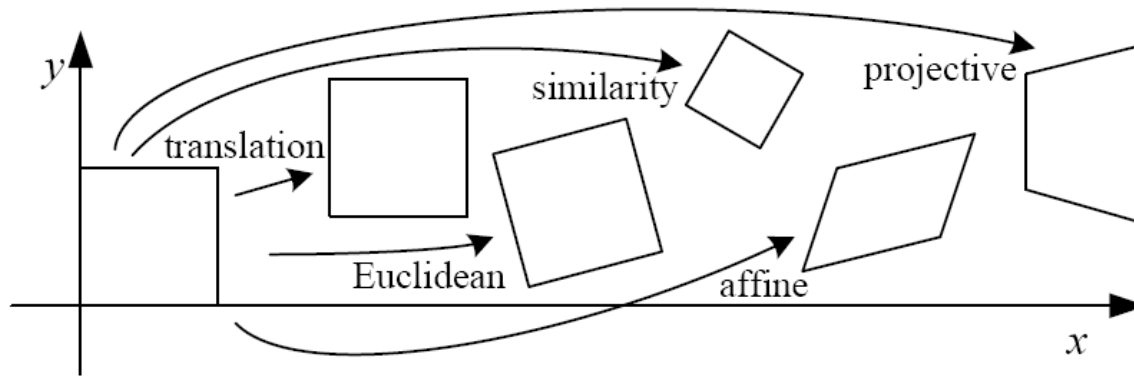
After multiplication by T (irrespective of T)

- ~~• Origin is origin:  $0 = T0$~~ 
  - Lines are lines
- ~~• Parallel lines are parallel~~
- ~~• Ratios between distances~~



# Transformation Families

In general: transformations are a nested set of groups



Name	Matrix	# D.O.F.	Preserves:	Icon
translation	$\begin{bmatrix} \mathbf{I} & \mathbf{t} \end{bmatrix}_{2 \times 3}$	2	orientation + ...	
rigid (Euclidean)	$\begin{bmatrix} \mathbf{R} & \mathbf{t} \end{bmatrix}_{2 \times 3}$	3	lengths + ...	
similarity	$\begin{bmatrix} s\mathbf{R} & \mathbf{t} \end{bmatrix}_{2 \times 3}$	4	angles + ...	
affine	$\begin{bmatrix} \mathbf{A} \end{bmatrix}_{2 \times 3}$	6	parallelism + ...	
projective	$\begin{bmatrix} \tilde{\mathbf{H}} \end{bmatrix}_{3 \times 3}$	8	straight lines	

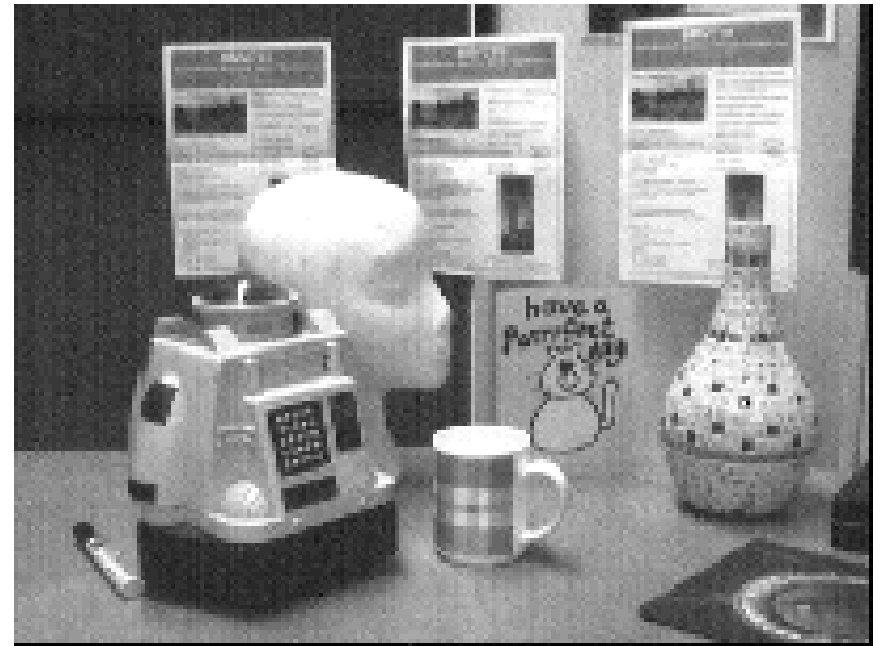
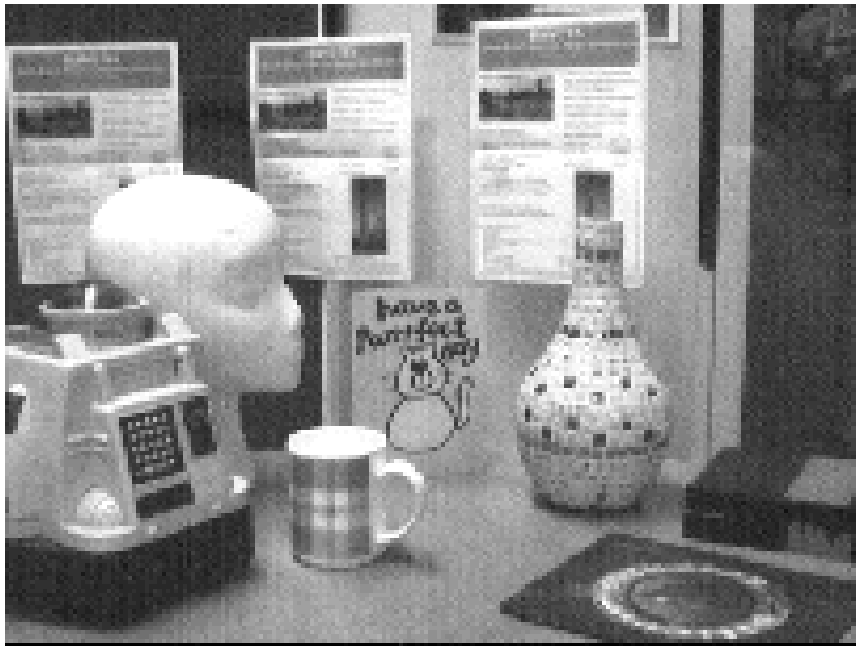
# What Can Homographies Do?

Homography example 1: any two views of a *planar* surface

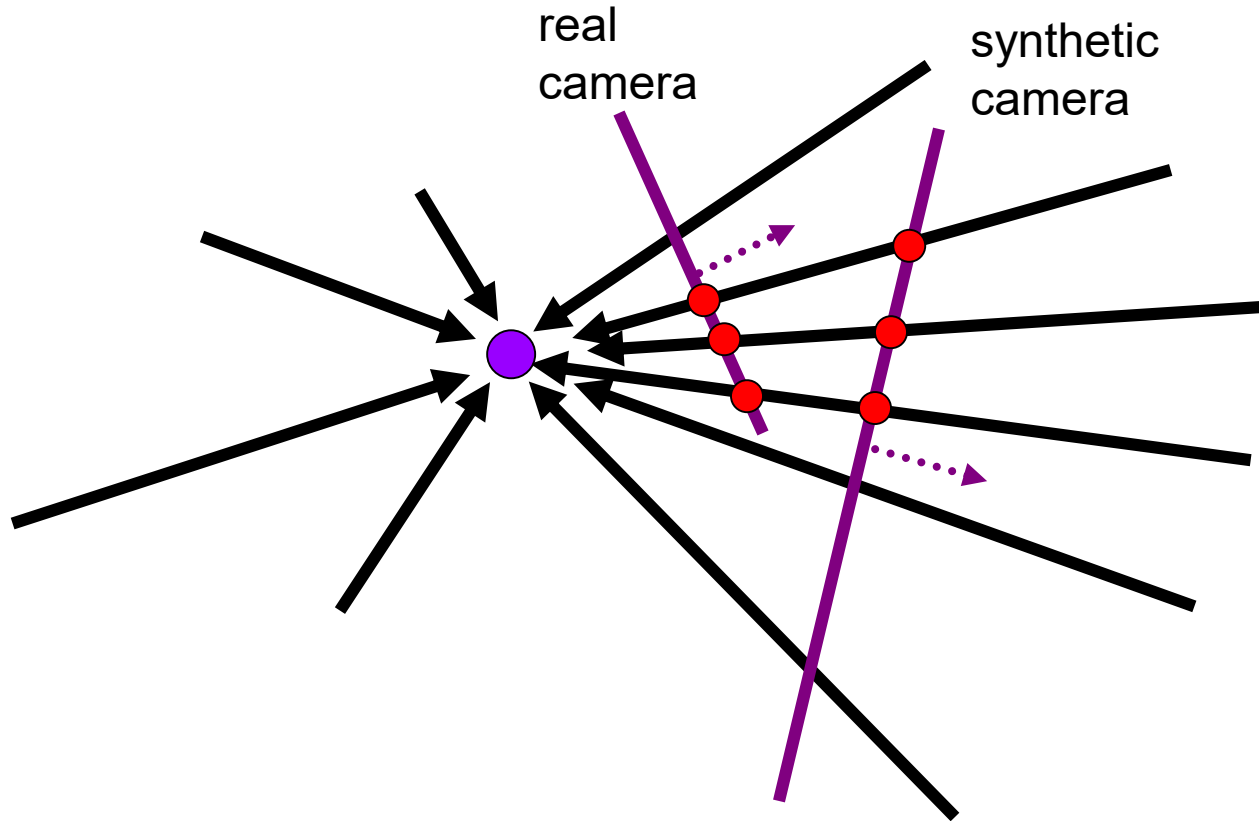


# What Can Homographies Do?

Homography example 2: any images from two cameras sharing a camera center



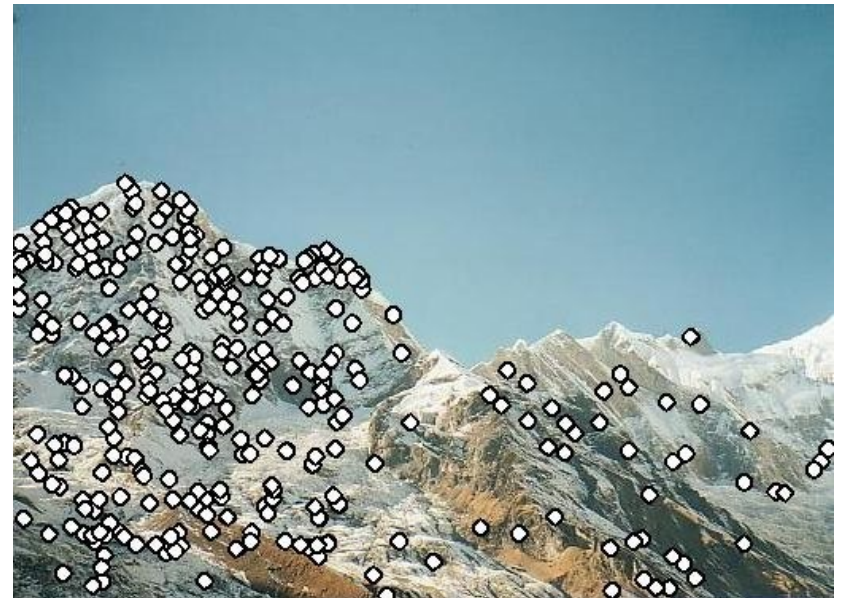
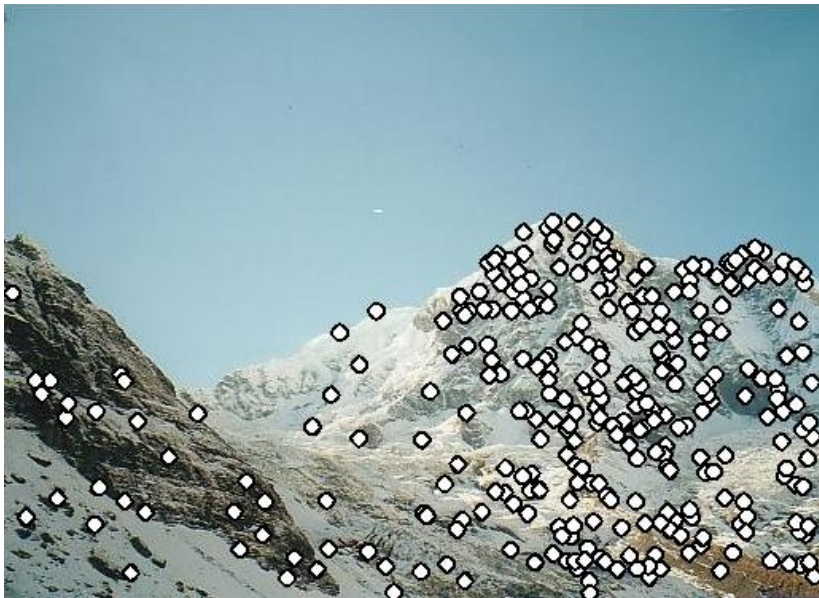
# A pencil of rays contains all views



Can generate any synthetic camera view as long as it has **the same center of projection!**

# What Can Homographies Do?

Homography sort of example “3”: far away scene that can be approximated by a plane



# Fun With Homographies

Original image

St. Petersburg  
photo by A. Tikhonov



Virtual camera rotations

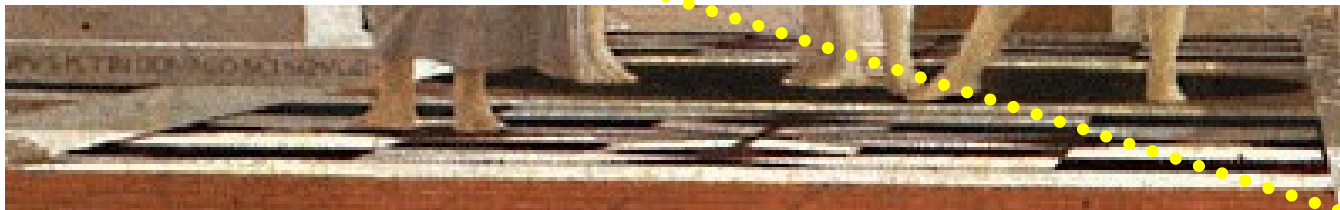




# Analyzing Patterns



**Homography**



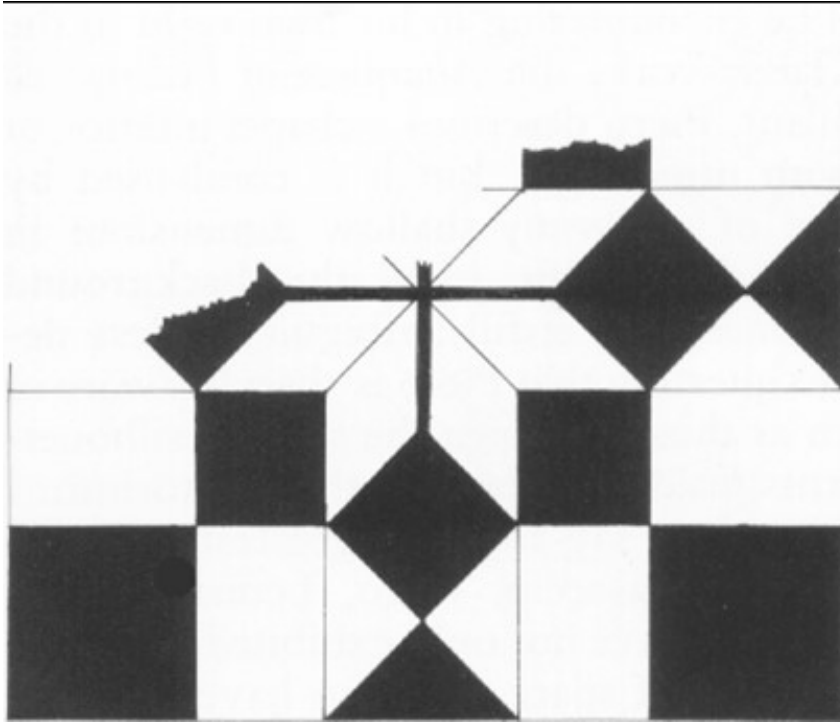
**The floor (enlarged)**

Slide from A. Criminisi



**Automatically  
rectified floor**

# Analyzing Patterns



From Martin Kemp *The Science of Art*  
(*manual reconstruction*)

Automatic rectification





# Analyzing Patterns

What is the (complicated) shape of the floor pattern?



***St. Lucy Altarpiece, D. Veneziano***

Slide from A. Criminisi

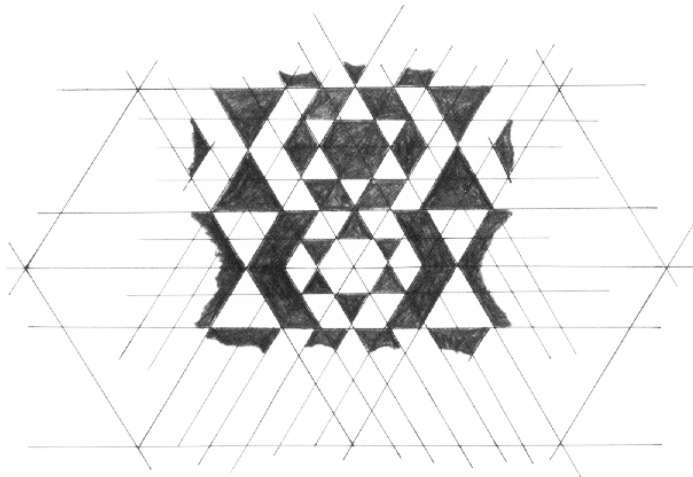


**Automatically rectified floor**

# Analyzing Patterns



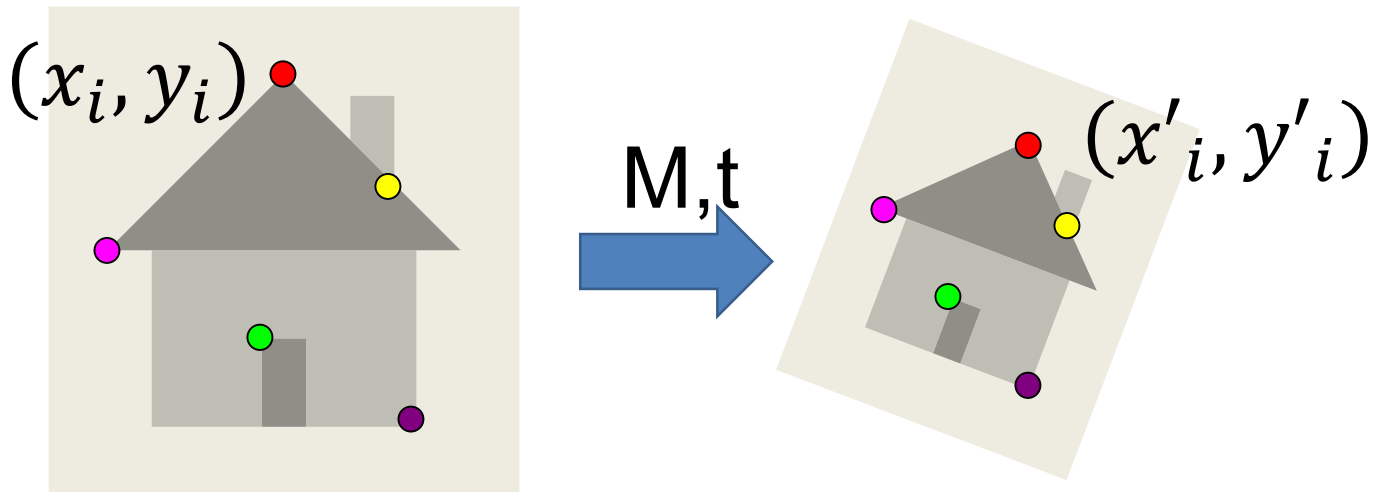
**Automatic  
rectification**



**From Martin Kemp, *The Science of Art*  
(*manual reconstruction*)**

# Fitting Transformations

Setup: have pairs of correspondences



$$\begin{bmatrix} x'_i \\ y'_i \end{bmatrix} = \mathbf{M} \begin{bmatrix} x_i \\ y_i \end{bmatrix} + \mathbf{t}$$

# Fitting Transformation

Affine Transformation:  $M, t$

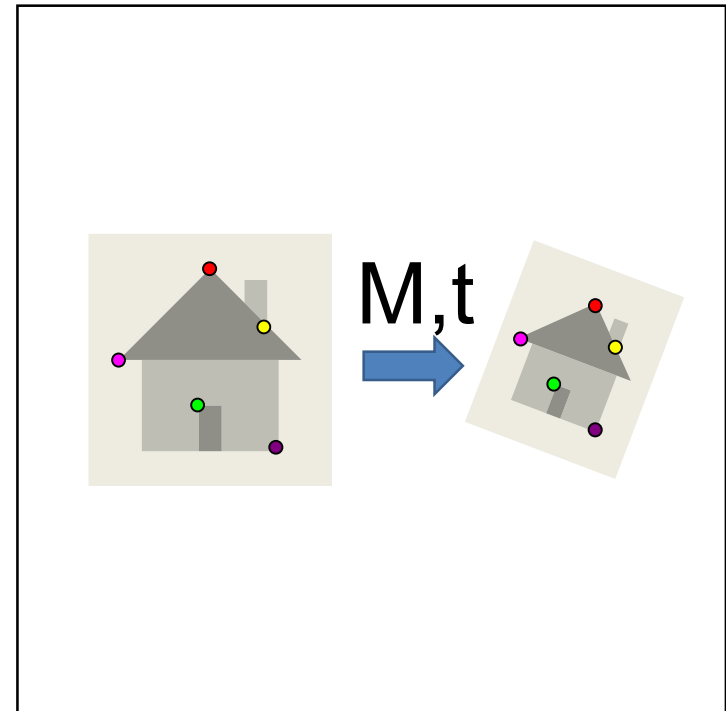
Data:  $(x_i, y_i, x'_i, y'_i)$  for  $i=1, \dots, k$

Model:

$$[x'_i, y'_i] = \mathbf{M}[x_i, y_i] + \mathbf{t}$$

Objective function:

$$\| [x'_i, y'_i] - \mathbf{M}[x_i, y_i] + \mathbf{t} \|^2$$



# Fitting Transformations

Given correspondences:  $\mathbf{p}' = [x'_i, y'_i]$ ,  $\mathbf{p} = [x_i, y_i]$

$$\begin{bmatrix} x'_i \\ y'_i \end{bmatrix} = \begin{bmatrix} m_1 & m_2 \\ m_3 & m_4 \end{bmatrix} \begin{bmatrix} x_i \\ y_i \end{bmatrix} + \begin{bmatrix} t_x \\ t_y \end{bmatrix}$$

Set up two equations per point

$$\begin{bmatrix} \vdots \\ x'_i \\ y'_i \\ \vdots \end{bmatrix} = \begin{bmatrix} & & \dots & & & & \\ x_i & y_i & 0 & 0 & 1 & 0 & \\ 0 & 0 & x_i & y_i & 0 & 1 & \\ & & \dots & & & & \end{bmatrix} \begin{bmatrix} m_1 \\ m_2 \\ m_3 \\ m_4 \\ t_x \\ t_y \end{bmatrix}$$

# Fitting Transformations

$$\begin{bmatrix} \vdots \\ x'_i \\ y'_i \\ \vdots \end{bmatrix} = \begin{bmatrix} & & \dots & & & & \\ x_i & y_i & 0 & 0 & 1 & 0 & \\ 0 & 0 & x_i & y_i & 0 & 1 & \\ & & \dots & & & & \end{bmatrix} \begin{bmatrix} m_1 \\ m_2 \\ m_3 \\ m_4 \\ t_x \\ t_y \end{bmatrix}$$

2 equations per point, 6 unknowns

**How many points do we need?**

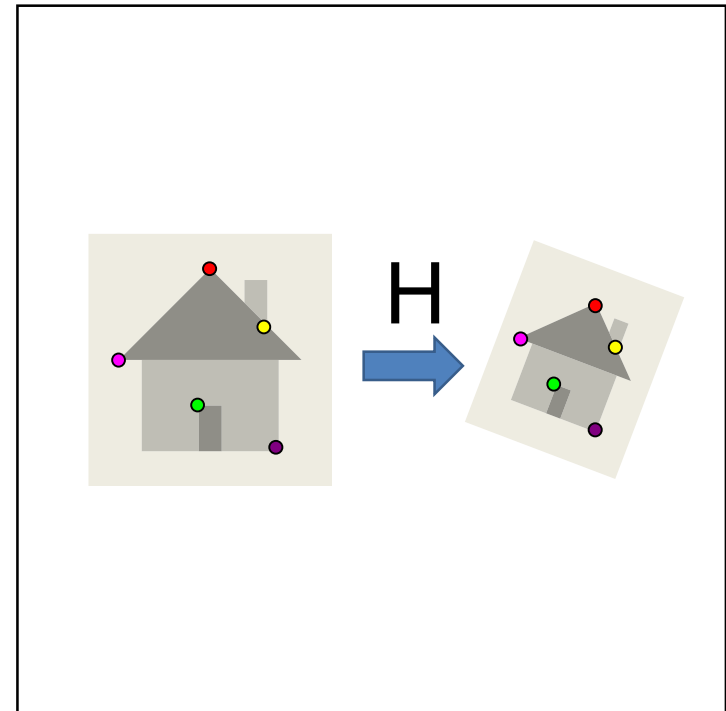
# Fitting Transformation

Homography:  $H$

Data:  $(x_i, y_i, x'_i, y'_i)$  for  
 $i=1, \dots, k$

Model:  
 $[x'_i, y'_i, 1] \equiv H[x_i, y_i, 1]$

Objective function:  
It's complicated



# Fitting Transformation

**Want:** 
$$\begin{bmatrix} x'_i \\ y'_i \\ w'_i \end{bmatrix} \equiv \begin{bmatrix} a & b & c \\ d & e & f \\ g & h & i \end{bmatrix} \begin{bmatrix} x_i \\ y_i \\ w_i \end{bmatrix}$$

$$\begin{bmatrix} a & b & c \\ d & e & f \\ g & h & i \end{bmatrix} \begin{bmatrix} x_i \\ y_i \\ w_i \end{bmatrix} \equiv \mathbf{H} \mathbf{x}_i \equiv \begin{bmatrix} \mathbf{h}_1^T \\ \mathbf{h}_2^T \\ \mathbf{h}_3^T \end{bmatrix} \mathbf{x}_i \equiv \begin{bmatrix} \mathbf{h}_1^T \mathbf{x}_i \\ \mathbf{h}_2^T \mathbf{x}_i \\ \mathbf{h}_3^T \mathbf{x}_i \end{bmatrix}$$

**Recall:**  $\mathbf{a} \equiv \mathbf{b} \rightarrow \mathbf{a} = \lambda \mathbf{b} \rightarrow \mathbf{a} \times \mathbf{b} = \mathbf{0}$



# Fitting Transformation

**Want:**

$$\begin{bmatrix} x'_i \\ y'_i \\ w'_i \end{bmatrix} \times \begin{bmatrix} \mathbf{h}_1^T \mathbf{x}_i \\ \mathbf{h}_2^T \mathbf{x}_i \\ \mathbf{h}_3^T \mathbf{x}_i \end{bmatrix} = \mathbf{0}$$

Cross-product

$$\begin{bmatrix} y'_i \mathbf{h}_3^T \mathbf{x}_i - w'_i \mathbf{h}_2^T \mathbf{x}_i \\ w'_i \mathbf{h}_1^T \mathbf{x}_i - x'_i \mathbf{h}_3^T \mathbf{x}_i \\ x'_i \mathbf{h}_2^T \mathbf{x}_i - y'_i \mathbf{h}_1^T \mathbf{x}_i \end{bmatrix} = \mathbf{0}$$

Re-arrange  
and put 0s in

$$\begin{bmatrix} \mathbf{h}_1^T \mathbf{0} - w'_i \mathbf{h}_2^T \mathbf{x}_i + y'_i \mathbf{h}_3^T \mathbf{x}_i \\ w'_i \mathbf{h}_1^T \mathbf{x}_i + \mathbf{h}_2^T \mathbf{0} - x'_i \mathbf{h}_3^T \mathbf{x}_i \\ -y'_i \mathbf{h}_1^T \mathbf{x}_i + x'_i \mathbf{h}_2^T \mathbf{x}_i + \mathbf{h}_3^T \mathbf{0} \end{bmatrix} = \mathbf{0}$$

# Fitting Transformation

Equation

$$\begin{bmatrix} \mathbf{h}_1^T \mathbf{0} - w'_i \mathbf{h}_2^T \mathbf{x}_i + y'_i \mathbf{h}_3^T \mathbf{x}_i \\ w'_i \mathbf{h}_1^T \mathbf{x}_i + \mathbf{h}_2^T \mathbf{0} - x'_i \mathbf{h}_3^T \mathbf{x}_i \\ -y'_i \mathbf{h}_1^T \mathbf{x}_i + x'_i \mathbf{h}_2^T \mathbf{x}_i + \mathbf{h}_3^T \mathbf{0} \end{bmatrix} = \mathbf{0}$$

Pull out h

$$\begin{bmatrix} \mathbf{0}^T & -w'_i \mathbf{x}_i & y'_i \mathbf{x}_i \\ w'_i \mathbf{x}_i & \mathbf{0}^T & -x'_i \mathbf{x}_i \\ -y'_i \mathbf{x}_i & x'_i \mathbf{x}_i & \mathbf{0}^T \end{bmatrix} \begin{bmatrix} \mathbf{h}_1 \\ \mathbf{h}_2 \\ \mathbf{h}_3 \end{bmatrix} = \mathbf{0}$$

Only two linearly independent equations

# Fitting Transformation

N points  $\rightarrow$

$$\begin{array}{c}
 \left[ \begin{array}{ccc}
 \mathbf{0}^T & -w'_1 \mathbf{x}_1 & y'_1 \mathbf{x}_1 \\
 w'_1 \mathbf{x}_1 & \mathbf{0}^T & -x'_1 \mathbf{x}_1 \\
 \vdots & \vdots & \vdots \\
 \mathbf{0}^T & -w'_n \mathbf{x}_n & y'_n \mathbf{x}_n \\
 w'_n \mathbf{x}_n & \mathbf{0}^T & -x'_n \mathbf{x}_n
 \end{array} \right]
 \begin{bmatrix}
 h_1 \\
 h_2 \\
 h_3
 \end{bmatrix}
 = \mathbf{0}
 \end{array}$$

$Ah = \mathbf{0}$

If  $h$  is up to scale, what do we use from last time?

$$h^* = \arg \min_{\|h\|=1} \|Ah\|^2 \rightarrow \text{Eigenvector of } A^T A \text{ with smallest eigenvalue}$$

# Small Nudging Detail

$\|Ah\|^2$  doesn't measure model fit (it's called an *algebraic error* that's mainly just convenient to minimize)

Really want *geometric error*:

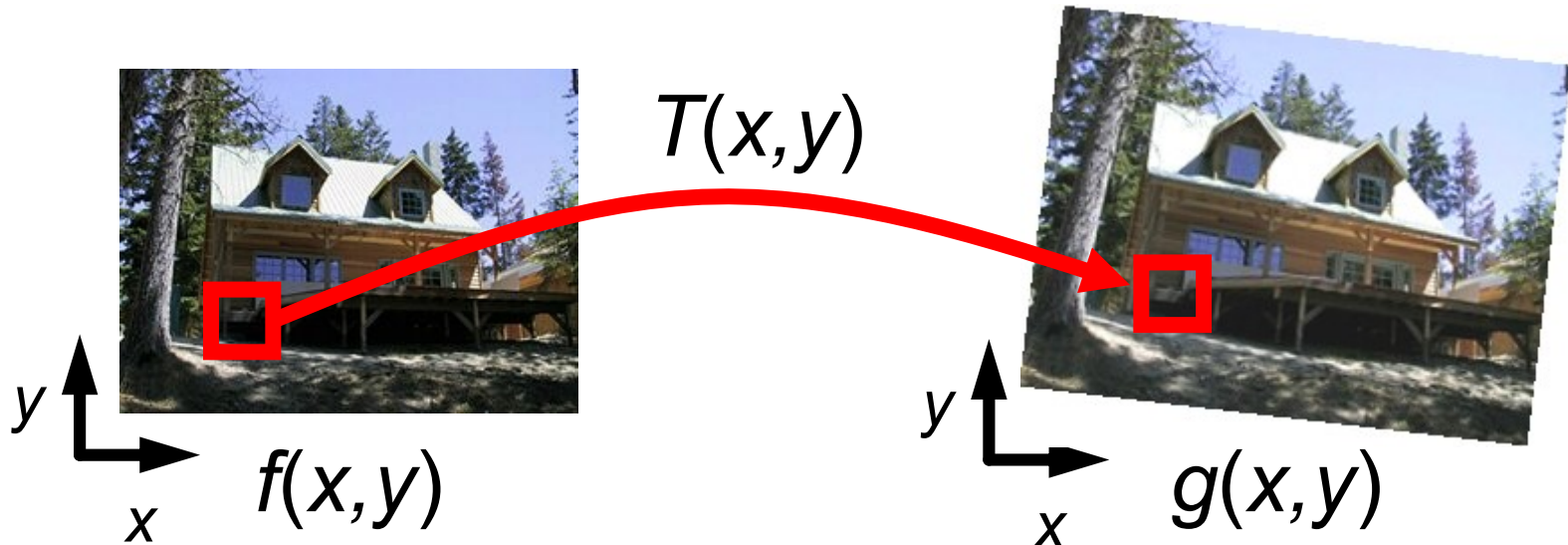
$$\sum_{i=1}^k \|[x'_i, y'_i] - T([x_i, y_i])\|^2 + \|[x_i, y_i] - T^{-1}([x'_i, y'_i])\|^2$$

# Small Nagging Detail

Solution: initialize with algebraic ( $\min ||Ah||$ ), optimize with geometric using standard non-linear optimizer

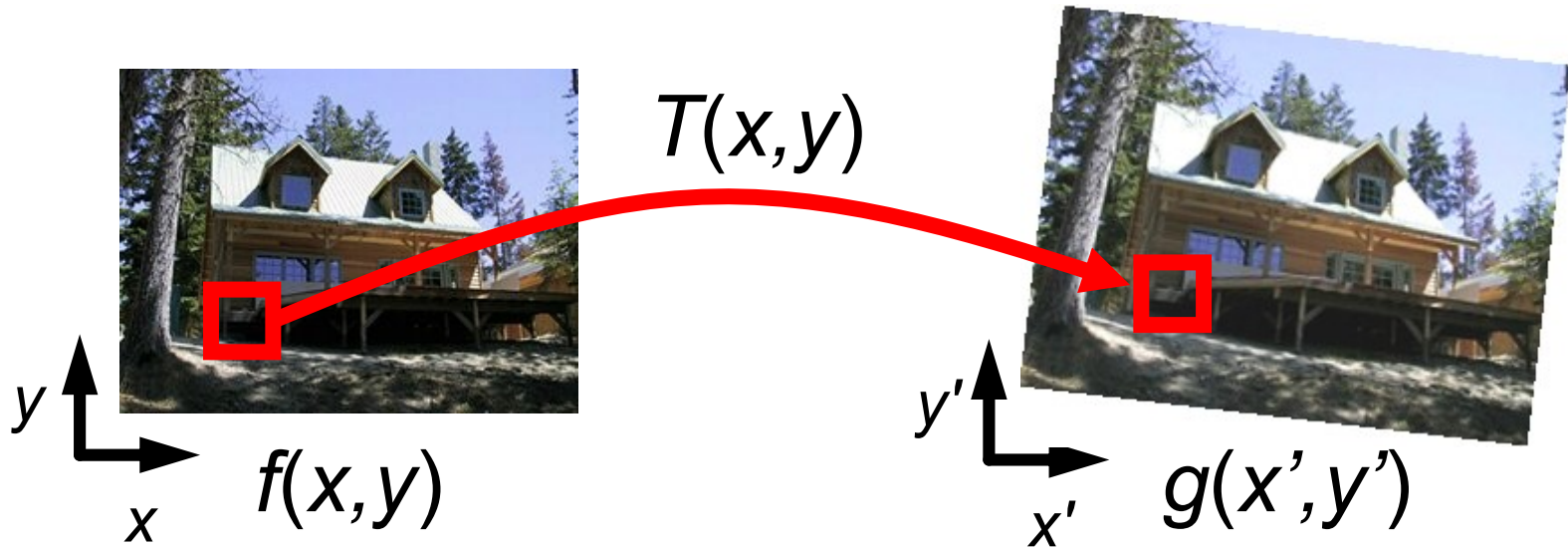
**In RANSAC, we always take just enough points to fit. Why might this not make a big difference when fitting a model with RANSAC?**

# Image Warping



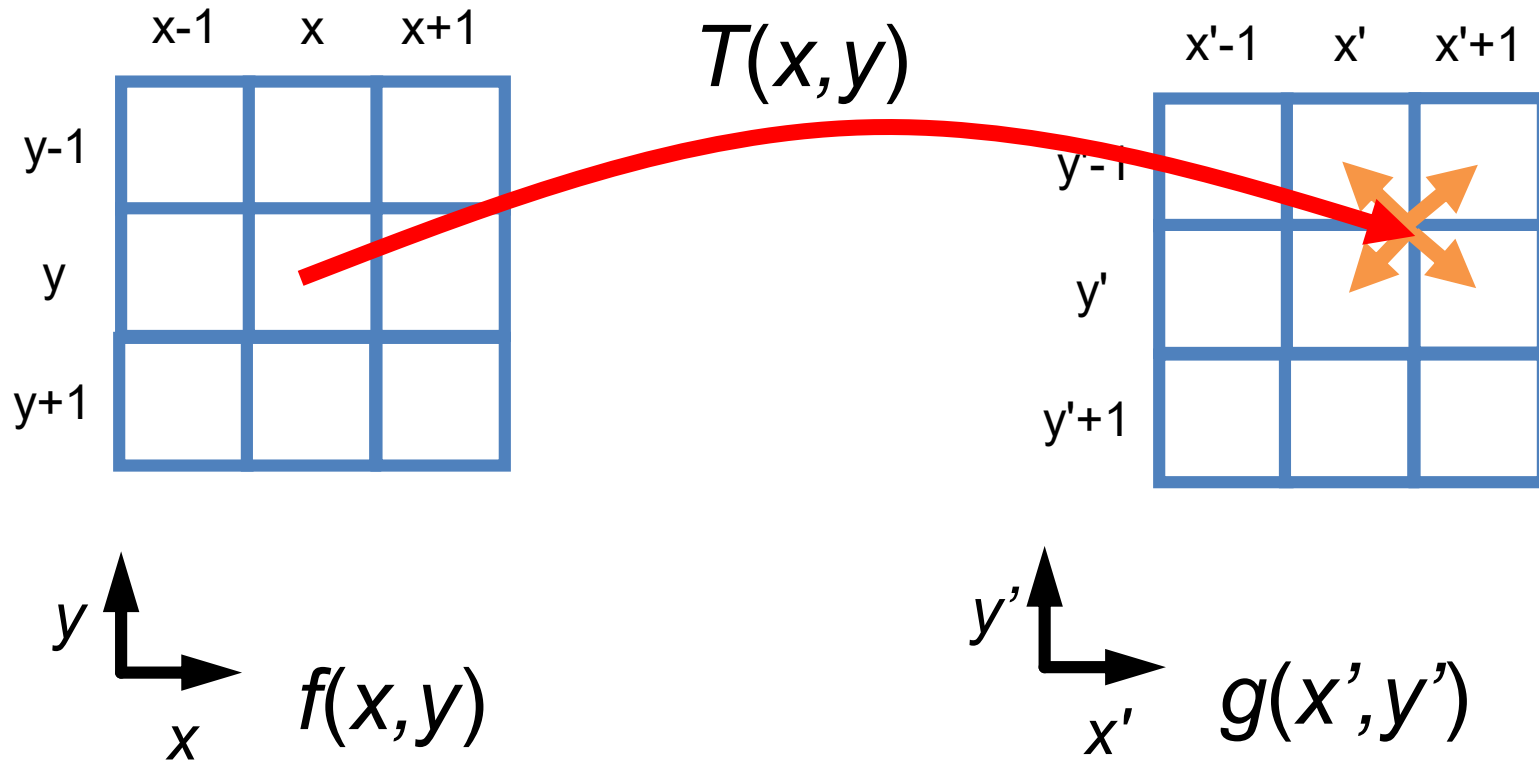
Given a coordinate transform  $(x', y') = T(x, y)$  and a source image  $f(x, y)$ , how do we compute a transformed image  $g(x', y') = f(T(x, y))$ ?

# Forward Warping



Send the value at each pixel  $(x, y)$  to  
the new pixel  $(x', y') = T([x, y])$

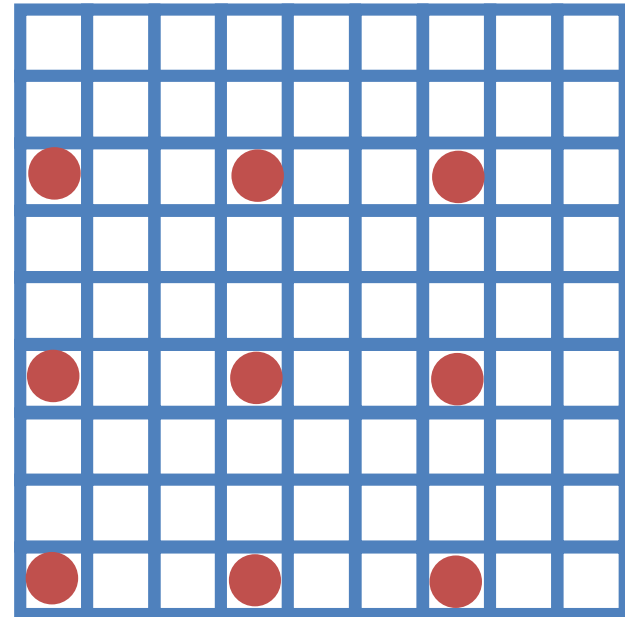
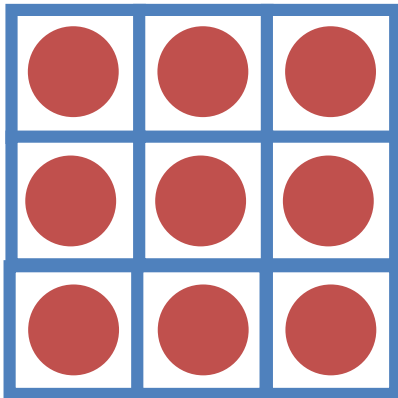
# Forward Warping



If you don't hit an exact pixel, give the value to each of the neighboring pixels ("splatting").

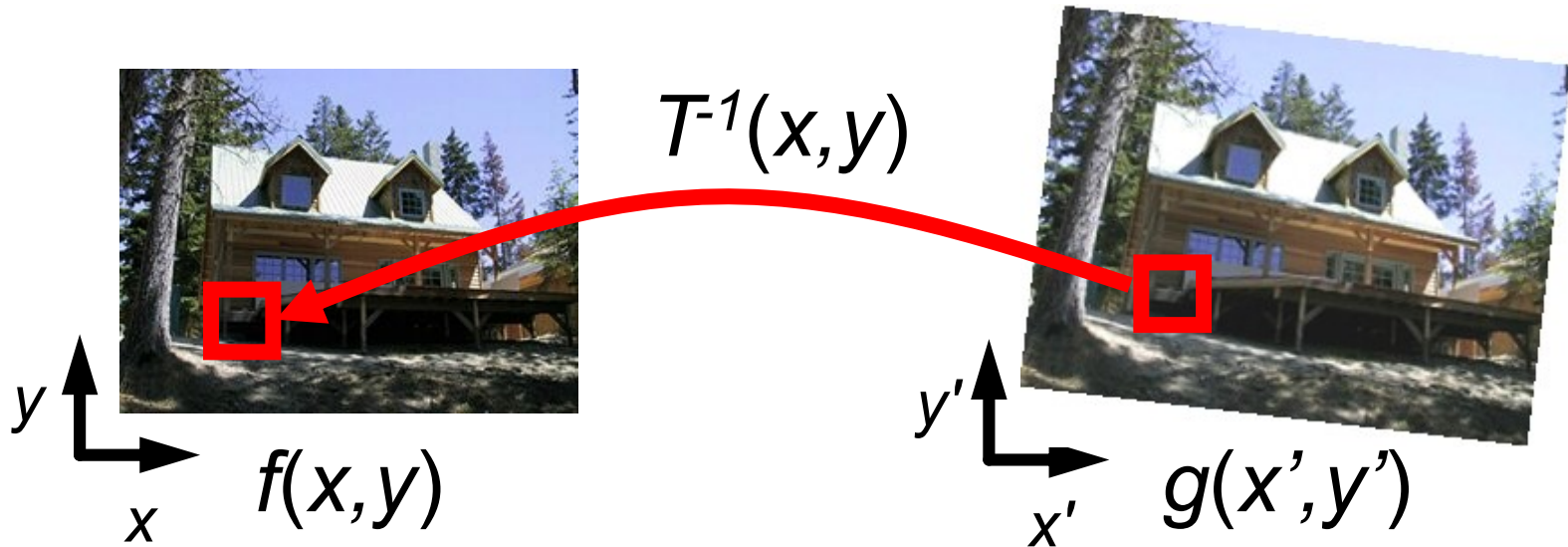


# Forward Warping



Suppose  $T(x,y)$  scales by a factor of 3.  
Hmmmm.

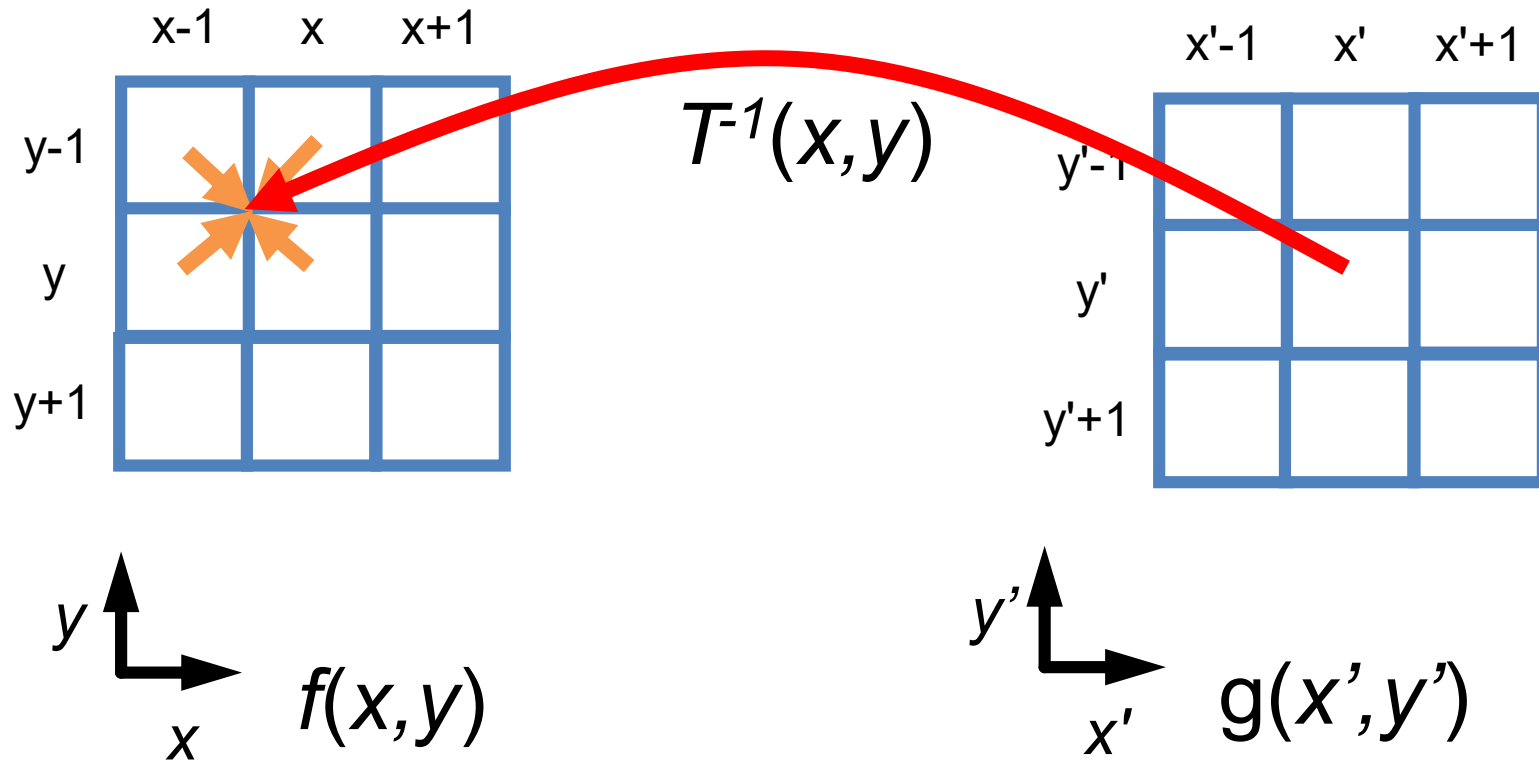
# Inverse Warping



Find out where each pixel  $g(x', y')$  should get its value from, and steal it.

Note: requires ability to invert  $T$

# Inverse Warping



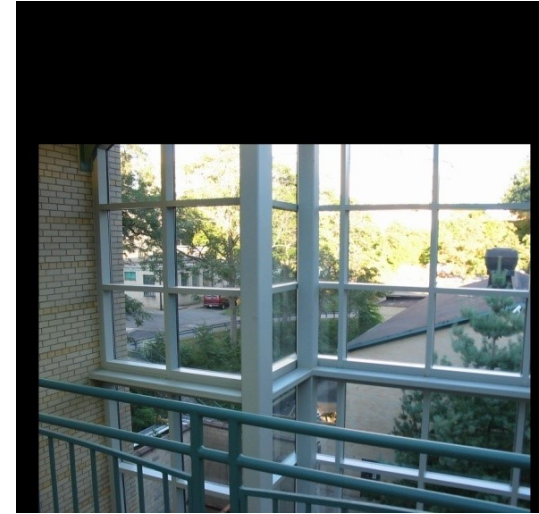
If you don't hit an exact pixel, figure out how to take it from the neighbors.

# Mosaicing

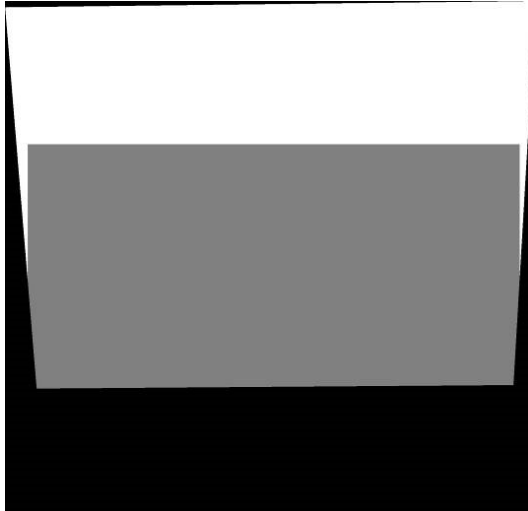
Warped  
Input 1  
 $I_1$



Warped  
Input 2  
 $I_2$



$\alpha$



$\alpha I_1 +$   
 $(1-\alpha)I_2$



# Simplification: Two-band Blending

- Brown & Lowe, 2003
  - Only use two bands: high freq. and low freq.
  - Blend low freq. smoothly
  - Blend high freq. with no smoothing: binary alpha



Figure Credit: Brown & Lowe



# 2-band “Laplacian Stack” Blending



Low frequency ( $\lambda > 2$  pixels)



High frequency ( $\lambda < 2$  pixels)

# Linear Blending





# 2-band Blending





# Putting it Together

How do you make a panorama?

Step 1: Find “features” to match

Step 2: Describe Features

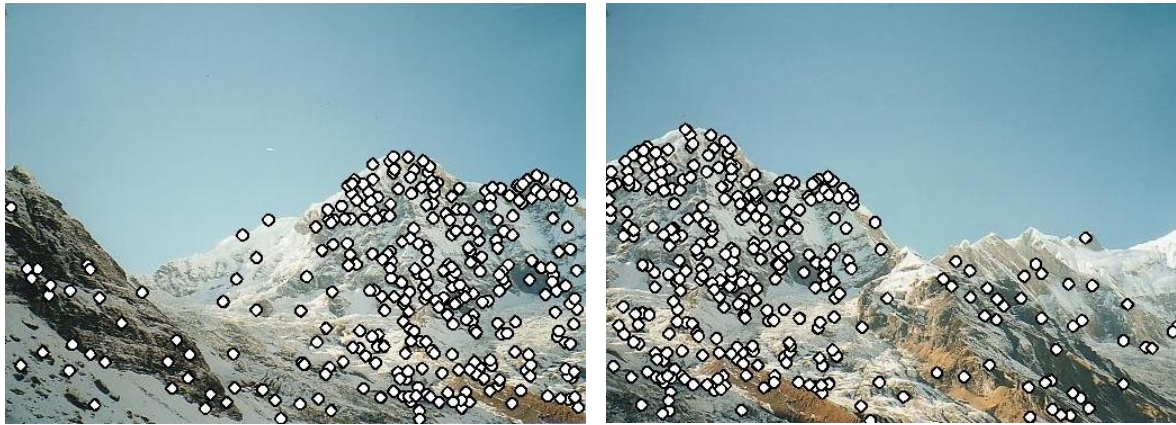
Step 3: Match by Nearest Neighbor

Step 4: Fit  $H$  via RANSAC

Step 5: Blend Images

# Putting It Together 1

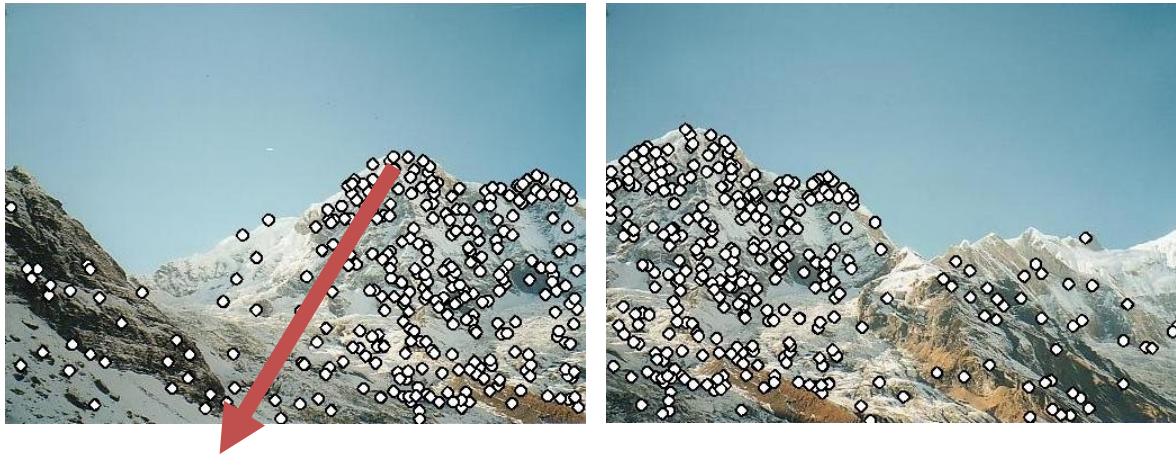
Find corners/blobs



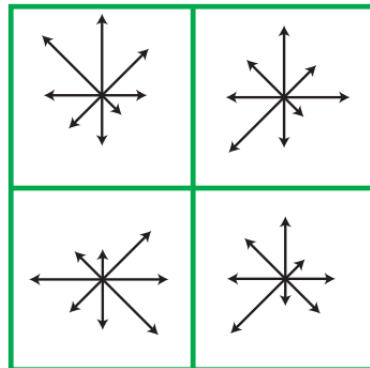
- (Multi-scale) Harris; or
- Laplacian of Gaussian

# Putting It Together 2

Describe Regions Near Features



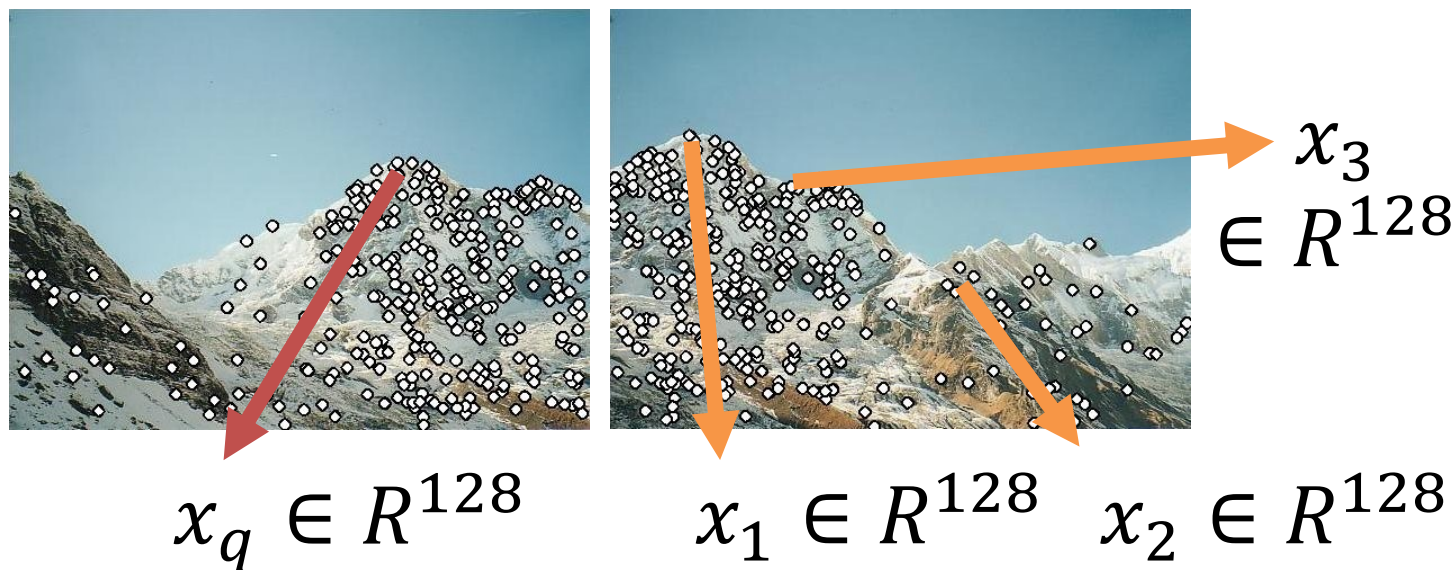
$$x_q \in R^{128}$$



Build histogram of  
gradient  
orientations (SIFT)

# Putting It Together 3

## Match Features Based On Region



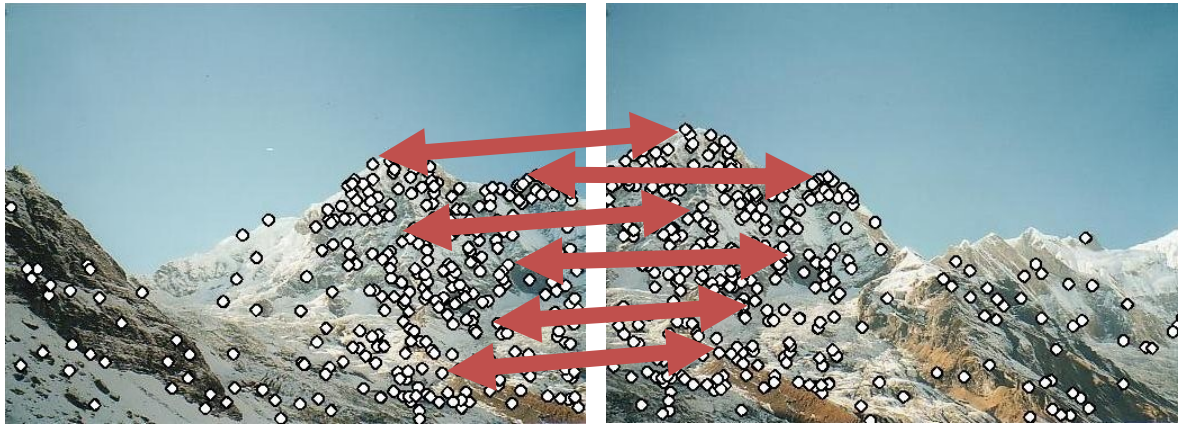
Sort by distance to:  $x_q$   $\|x_q - x_1\| < \|x_q - x_2\| < \|x_q - x_3\|$

Accept match if:  $\|x_q - x_1\| / \|x_q - x_2\|$

Nearest neighbor is far closer than 2<sup>nd</sup> nearest neighbor

# Putting It Together 4

Fit transformation  $H$  via RANSAC



for trial in range(Ntrials):

Pick sample

Fit model

Check if more inliers

Re-fit model with most inliers

$$\arg \min_{\|h\|=1} \|Ah\|^2$$

# Putting It Together 5

Warp images together



Resample images with inverse  
warping and blend