Detectors and Descriptors

EECS 442 – Prof. David Fouhey Winter 2019, University of Michigan

http://web.eecs.umich.edu/~fouhey/teaching/EECS442_W19/

Administrivia

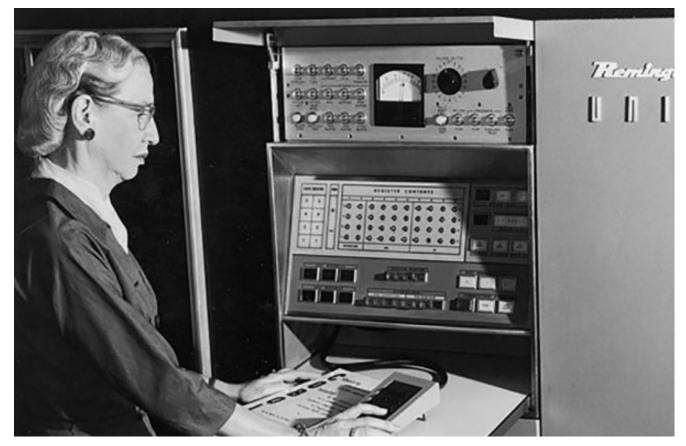
- Today/Thursday: Detecting edges and corners in images and describing them
- Discussion Section: reviewing projection and convolution.
- If you have accommodation needs or need an alternate midterm, please email me *this week.*
- Please do not schedule stuff for the class that is listed as the midterm going forward.

General Hints for Vision Debugging

- Visualize
- <u>Visualize</u>
- <u>Visualize</u>
- Break it into bite-sized chunks; verify each
- Test the smallest version possible
- Use a debugger (pdb or use the jupyter cells)
- Try explaining your code verbally

Goal

How big is this image as a vector? 389x600 = 233,400 dimensions (big)

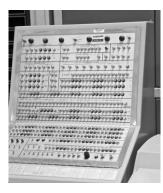


Applications To Have In Mind





Part of the same photo?



Same computer from another angle?

Applications To Have In Mind

Building a 3D Reconstruction Out Of Images



Slide Credit: N. Seitz

Applications To Have In Mind

Stitching photos taken at different angles



One Familiar Example

Given two images: how do you align them?



One (Hopefully Familiar) Solution

for y in range(-ySearch,ySearch+1):
 for x in range(-xSearch,xSearch+1):
 #Touches all HxW pixels!
 check_alignment_with_images()

One Motivating Example

Given these images: how do you align them?



These aren't off by a small 2D translation but instead by a 3D rotation + translation of the camera.

Photo credit: M. Brown, D. Lowe

One (Hopefully Familiar) Solution

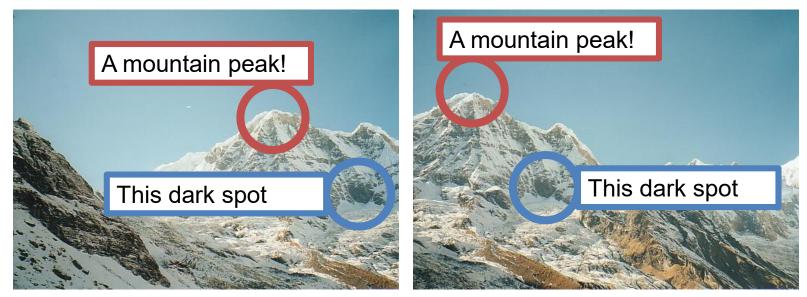
for y in yRange: for x in xRange: for z in zRange: for xRot in xRotVals: for yRot in yRotVals: for zRot in zRotVals: #touches all HxW pixels! check alignment with images()

This code should make you really <u>unhappy</u>

Note: this actually isn't even the full number of parameters; it's actually 8 for loops.

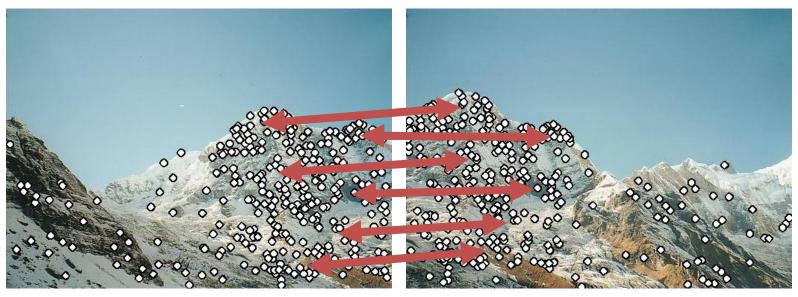
An Alternate Approach

Given these images: how would you align them?



An Alternate Approach

Finding and Matching

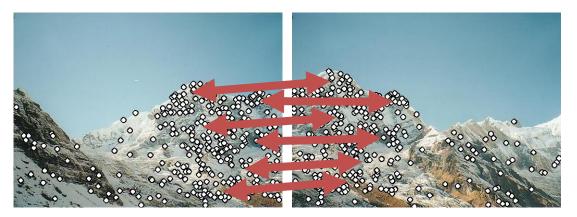


find corners+features match based on local image data

Slide Credit: S. Lazebnik, original figure: M. Brown, D. Lowe

What Now?

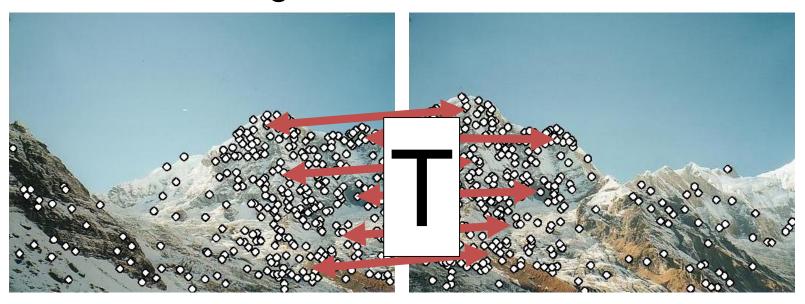
Given pairs p1,p2 of correspondence, how do I align?



Consider translationonly case from HW1.



An Alternate Approach Solving for a Transformation



3: Solve for transformation T (e.g. such that $p1 \equiv T p2$) that fits the matches well

Note the homogeneous coordinates, you'll see them again.

Slide Credit: S. Lazebnik, original figure: M. Brown, D. Lowe

An Alternate Approach Blend Them Together

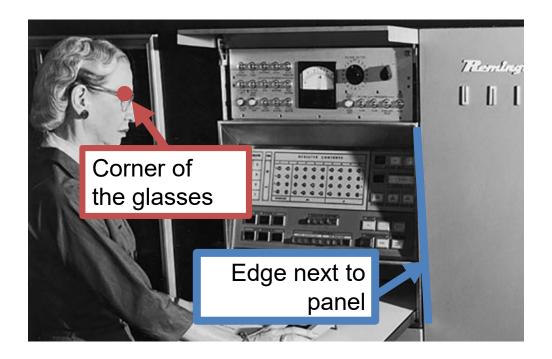


Key insight: we don't work with full image. We work with only parts of the image.

Photo Credit: M. Brown, D. Lowe

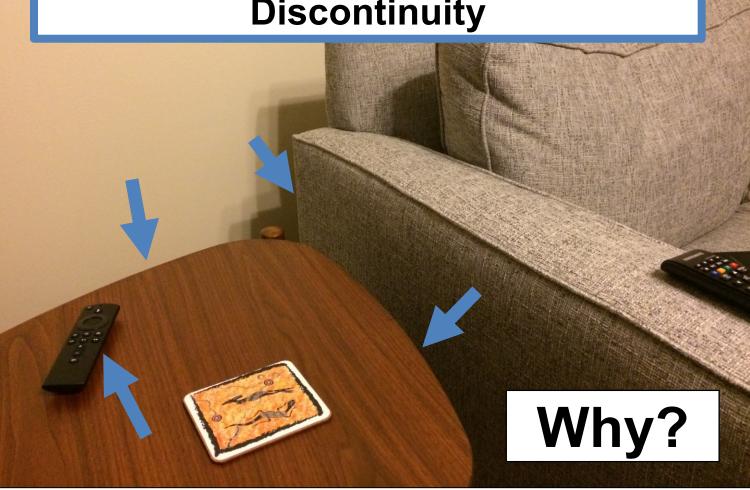
Today

Finding edges (part 1) and corners (part 2) in images.





Depth / Distance Discontinuity

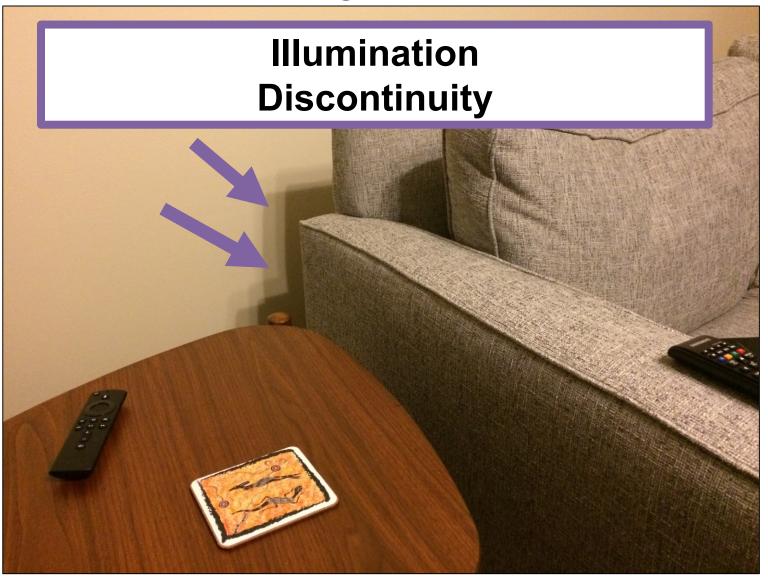


Surface Normal / Orientation Discontinuity

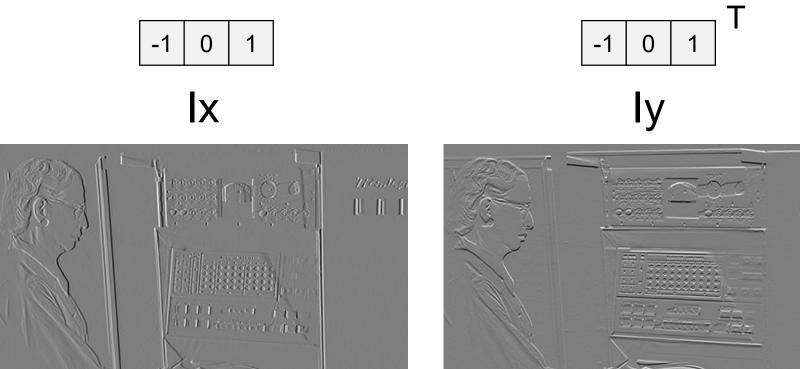


Surface Color / Reflectance Properties Discontinuity





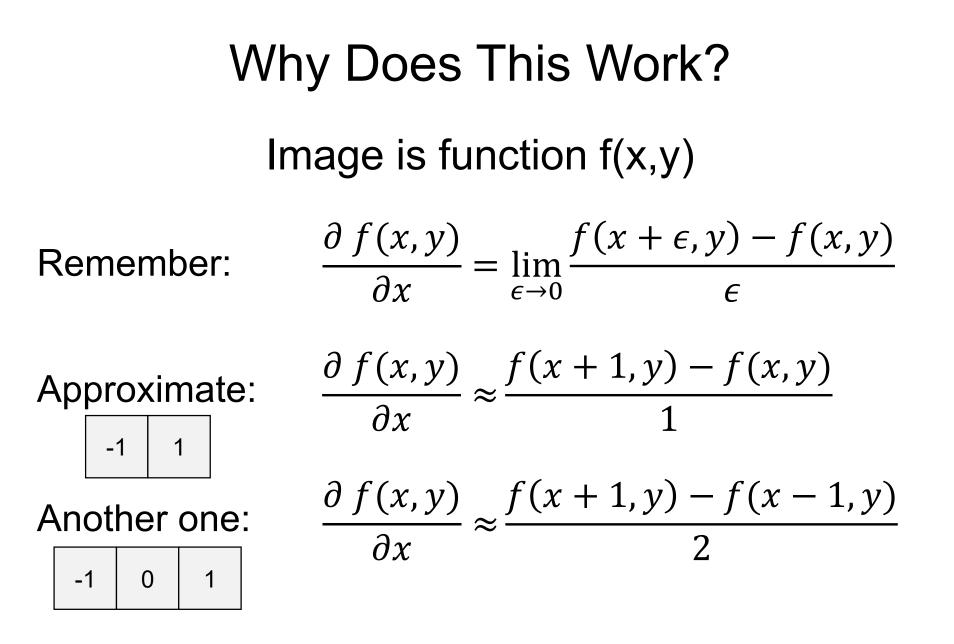
Last Time



Last Time

 $(Ix^2 + Iy^2)^{1/2}$





Other Differentiation Operations

Why might people use these compared to [-1,0,1]?

Review: Gradients

Gradient is just the collection of partial derivatives in each dimension/direction. Points in direction that increases the most.

$$g = \nabla f = \begin{bmatrix} \frac{\partial f}{\partial x_1} \\ \vdots \\ \frac{\partial f}{\partial x_n} \end{bmatrix} g(\mathbf{a}) = \begin{bmatrix} \frac{\partial f}{\partial x_1}(\mathbf{a}) \\ \vdots \\ \frac{\partial f}{\partial x_n}(\mathbf{a}) \end{bmatrix}$$
How much f changes in the direction of x₁ at point a

Images as Functions or Points

Key idea: can treat image as a point in R^(HxW) or as a function of x,y.

 $\nabla I(x,y) = \begin{bmatrix} \frac{\partial I}{\partial x}(x,y) \\ \frac{\partial I}{\partial y}(x,y) \end{bmatrix} \qquad \begin{array}{c} \text{How much the intensity} \\ \text{How much the intensity} \\ \text{of the image changes} \\ \text{as you go horizontally} \\ \text{at } (x,y) \\ \text{(Often called lx)} \end{array}$

Image Gradient Direction

Some gradients

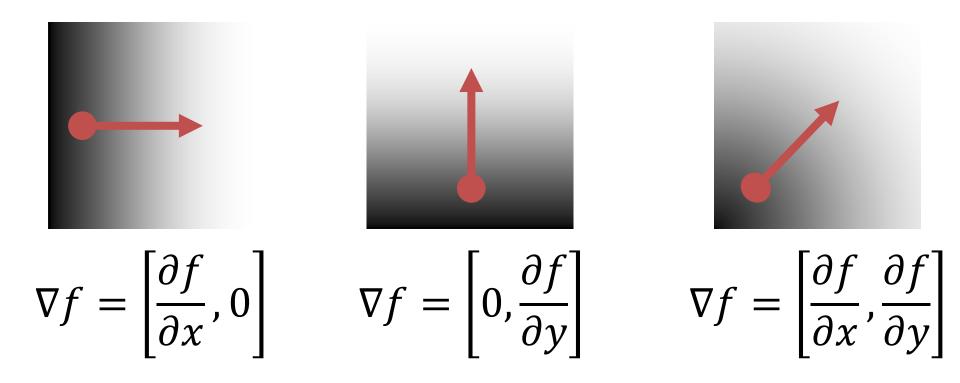
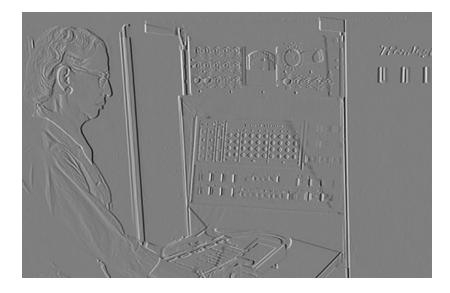


Image Gradient

Gradient: direction of maximum change. What's the relationship to edge direction?

Ix





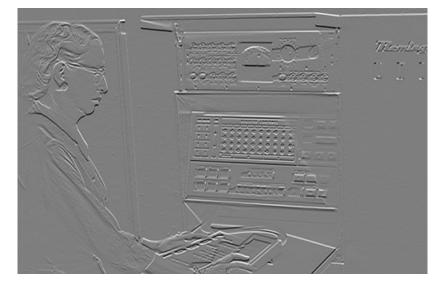
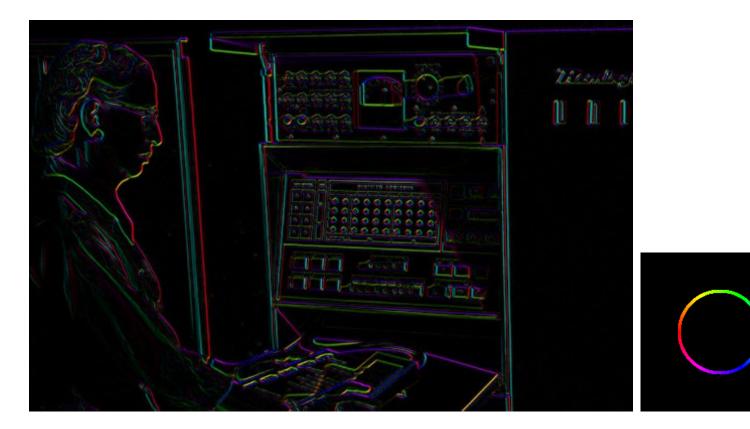


Image Gradient (Ix² + Iy²)^{1/2} : magnitude

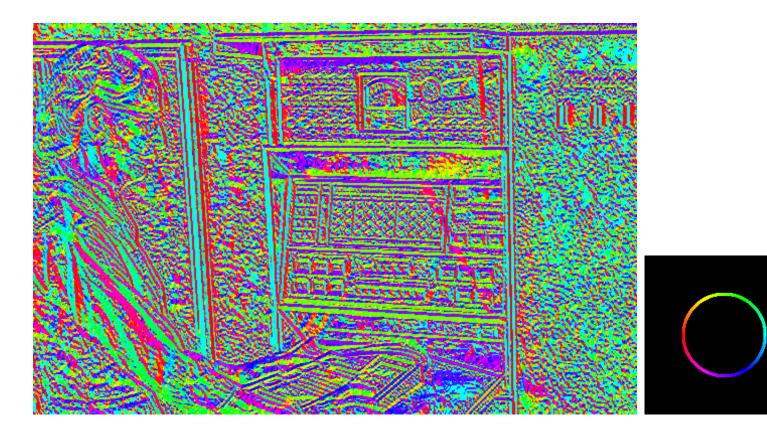


Image Gradient atan2(Iy,Ix): orientation



I'm making the lightness equal to gradient magnitude

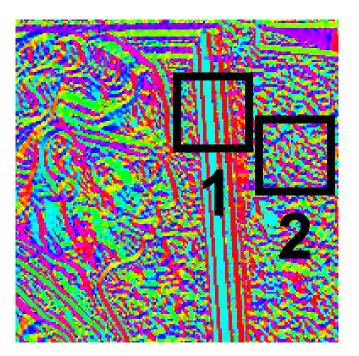
Image Gradient atan2(Iy,Ix): orientation



Now I'm showing all the gradients

Image Gradient atan2(Iy,Ix): orientation

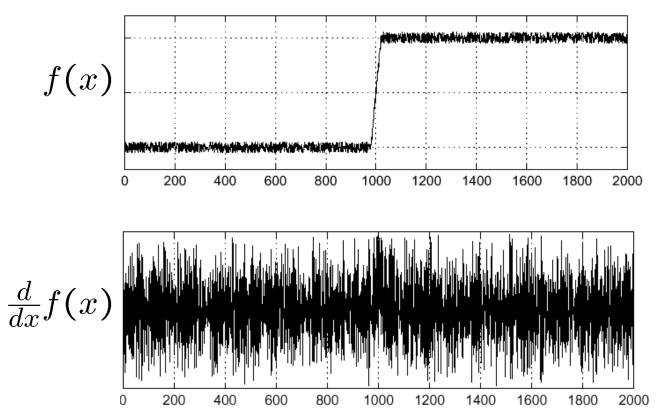
Why is there structure at 1 and not at 2?





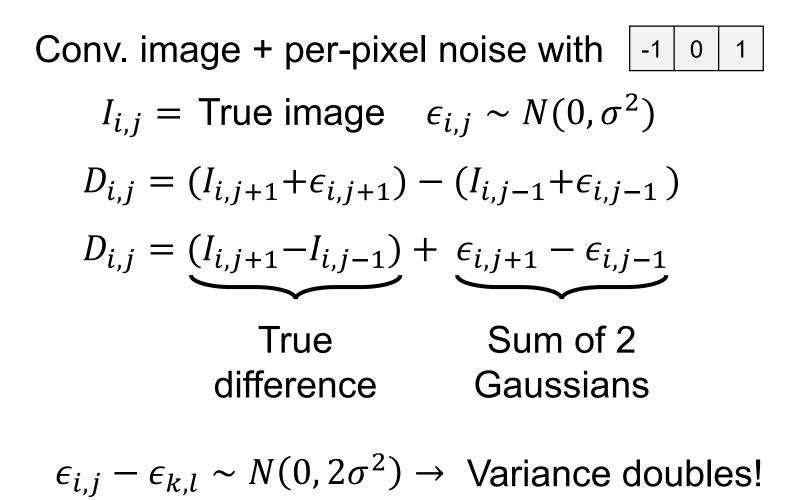
Noise

Consider a row of f(x,y) (i.e., fix y)

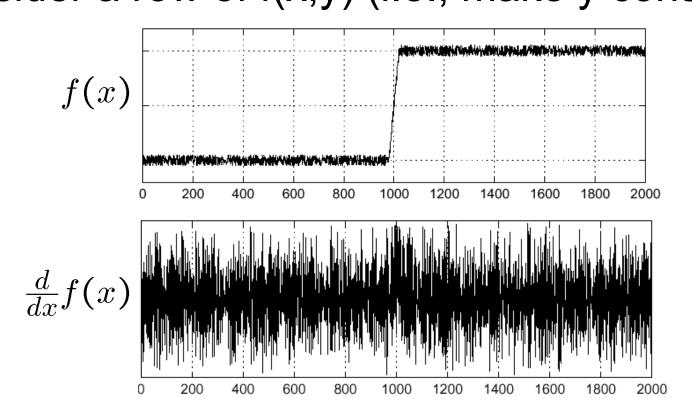


Slide Credit: S. Seitz

Noise

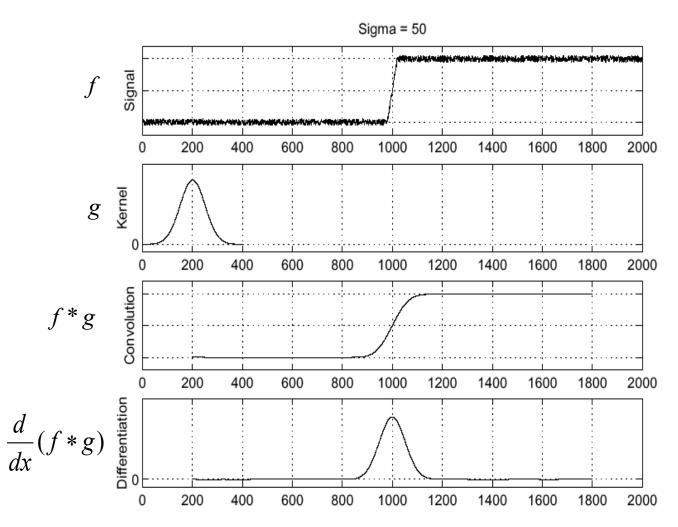


Noise Consider a row of f(x,y) (i.e., make y constant)



How can we use the last class to fix this?

Handling Noise



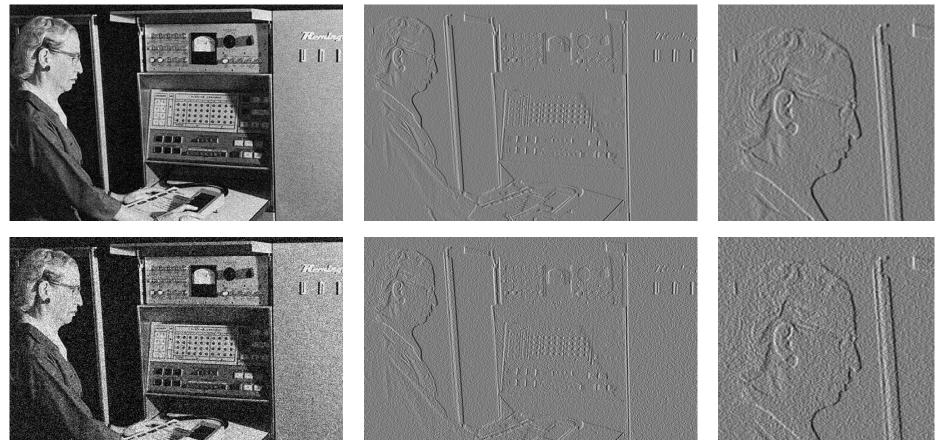
Slide Credit: S. Seitz

Noise in 2D

Noisy Input

Ix via [-1,01]



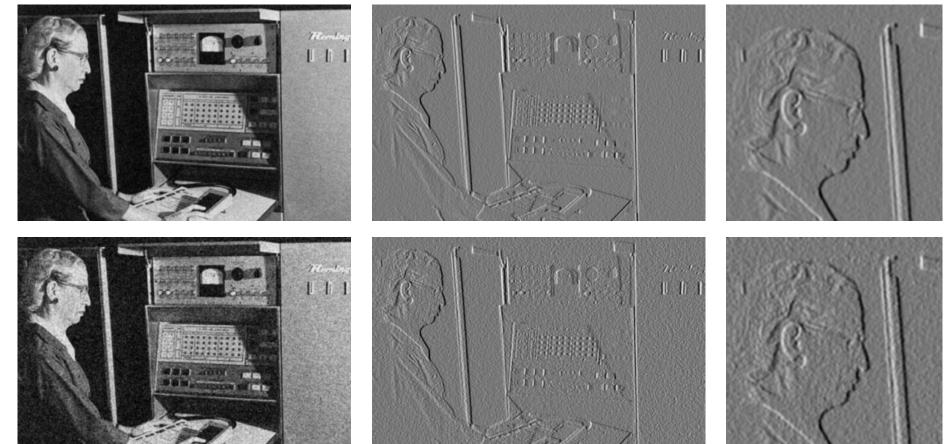


Noise + Smoothing

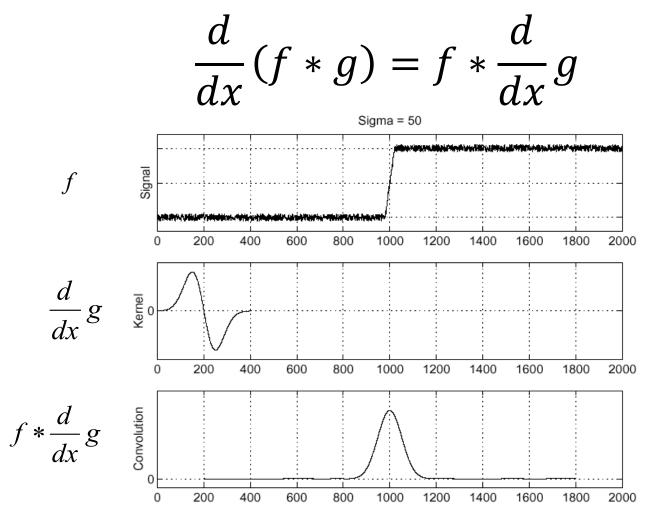
Smoothed Input

Ix via [-1,01]



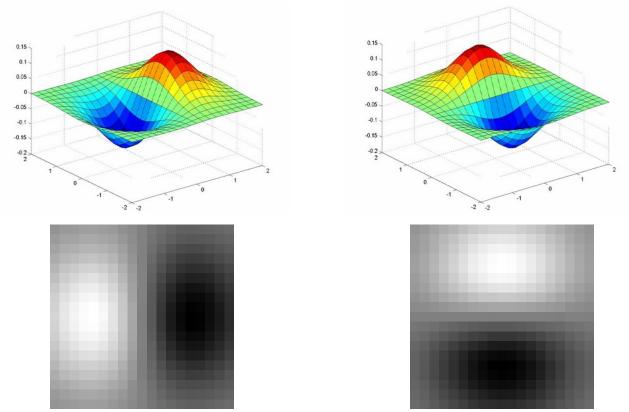


Let's Make It One Pass (1D)



Slide Credit: S. Seitz

Let's Make It One Pass (2D) Gaussian Derivative Filter



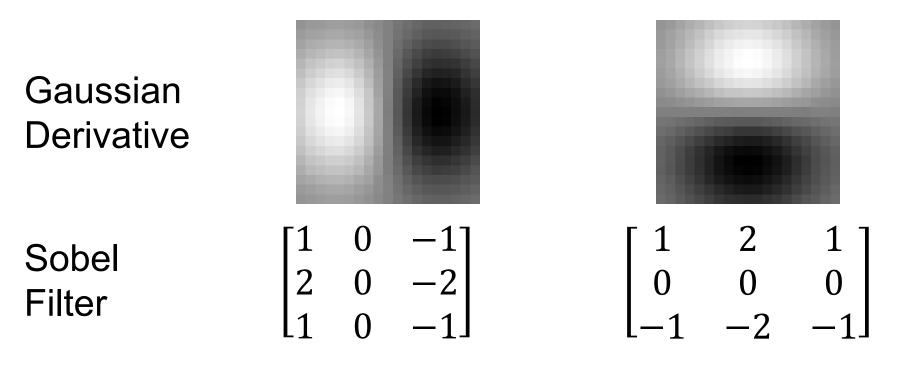
Which one finds the X direction?

Applying the Gaussian Derivative1 pixel3 pixels7 pixels

Removes noise, but blurs edge

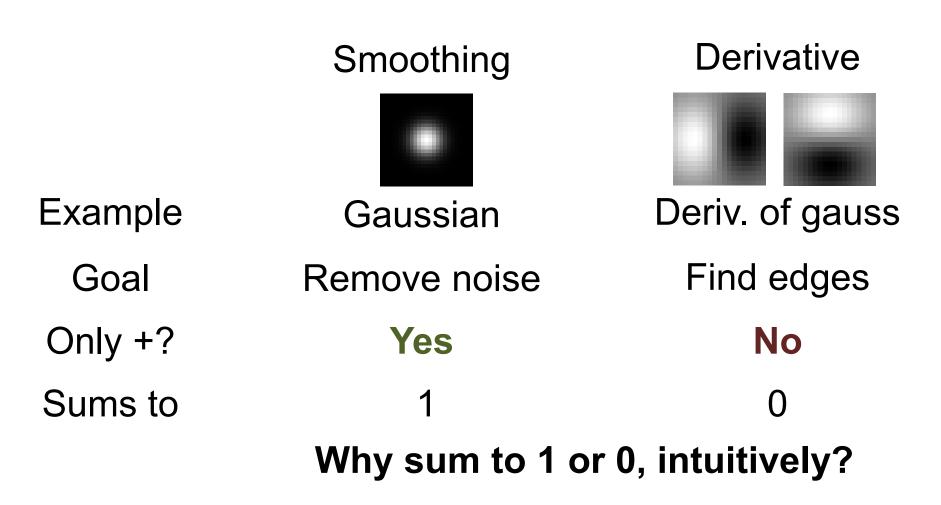
Slide Credit: D. Forsyth

Compared with the Past



Why would anybody use the bottom filter?

Filters We've Seen



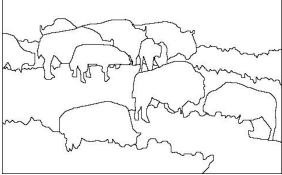
Problems

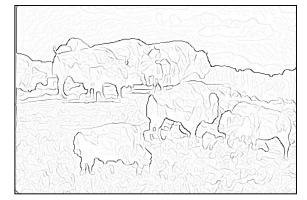
Image

human segmentation

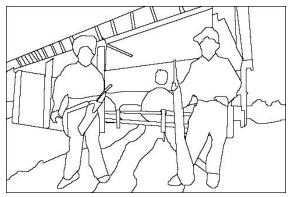
gradient magnitude







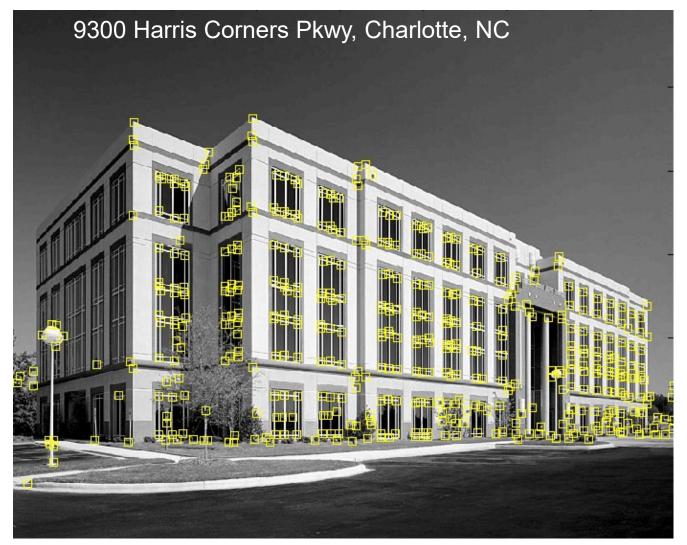






Still an active area of research

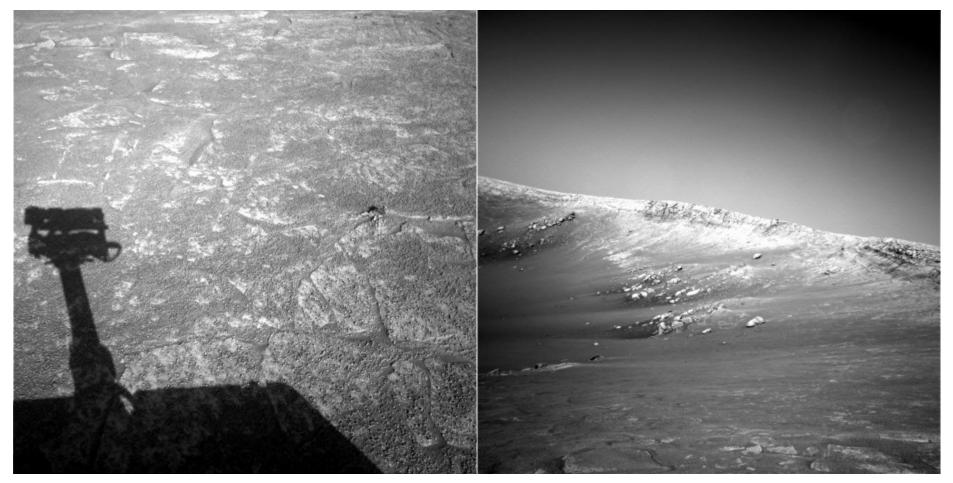
Corners



Desirables

- Repeatable: should find same things even with distortion
- Saliency: each feature should be distinctive
- Compactness: shouldn't just be all the pixels
- Locality: should only depend on local image data

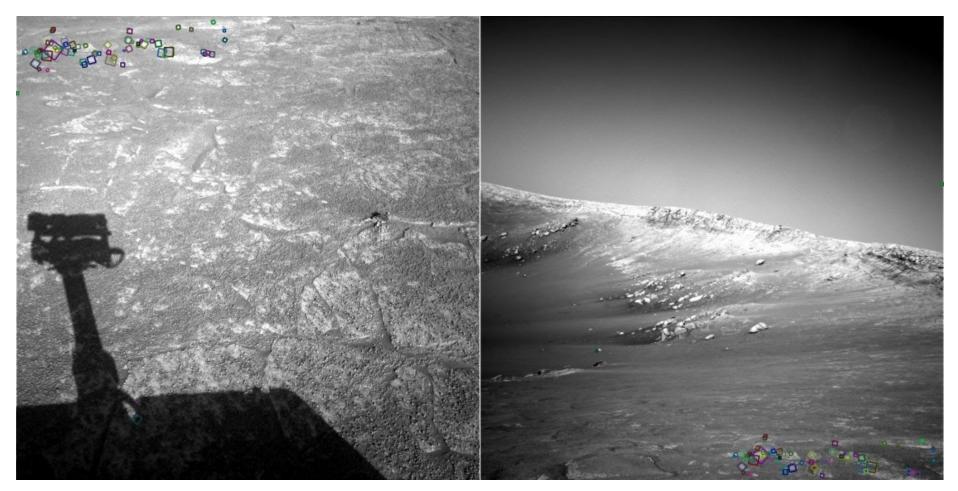
Example



Can you find the correspondences?

Slide credit: N. Snavely

Example Matches

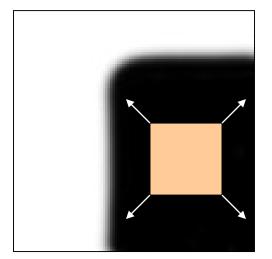


Look for the colored squares

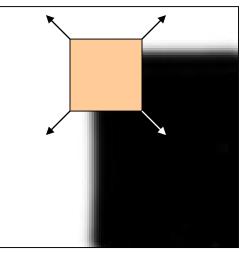
Slide credit: N. Snavely

Basic Idea

Should see where we are based on small window, or any shift \rightarrow big intensity change.



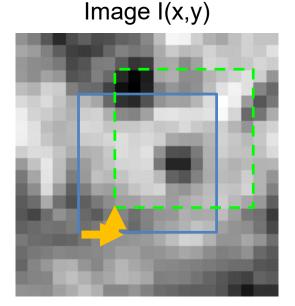
"flat" region: no change in all directions "edge": no change along the edge direction



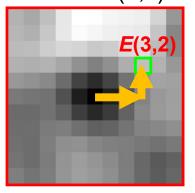
"corner": significant change in all directions

Sum of squared differences between image and image shifted u,v pixels over.

$$E(u,v) = \sum_{(x,y)\in W} (I[x+u,y+v] - I[x,y])^2$$



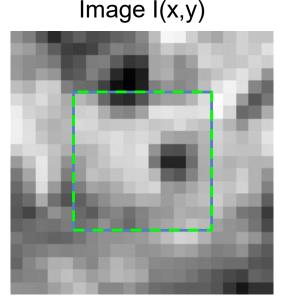
Plot of E(u,v)

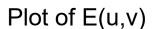


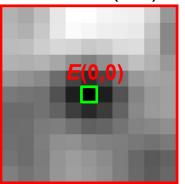
Sum of squared differences between image and image shifted u,v pixels over.

$$E(u,v) = \sum_{(x,y)\in W} (I[x+u,y+v] - I[x,y])^2$$

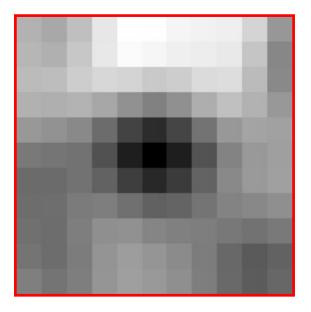
What's the value of E(0,0)?







Can compute E[u,v] for any window and u,v. But we'd like an simpler function of u,v.



Aside: Taylor Series for Images

Recall Taylor Series:

$$f(x+d) \approx f(x) + \frac{\partial f}{\partial x}d$$

Do the same with images, treating them as function of x, y

$$I(x+u, y+v) \approx I(x, y) + I_x u + I_y v$$

$$E(u,v) = \sum_{(x,y)\in W} (I[x+u,y+v] - I[x,y])^2$$

$$\approx \sum_{(x,y)\in W} (I[x,y] + I_x[x,y]u + I_y[x,y]v - I[x,y])^2$$

Cancel

$$= \sum_{(x,y)\in W} \left(I_x[x,y]u + I_y[x,y]v \right)^2$$

Expand

$$= \sum_{(x,y)\in W} I_x u^2 + 2I_x I_y uv + I_y^2 v^2$$

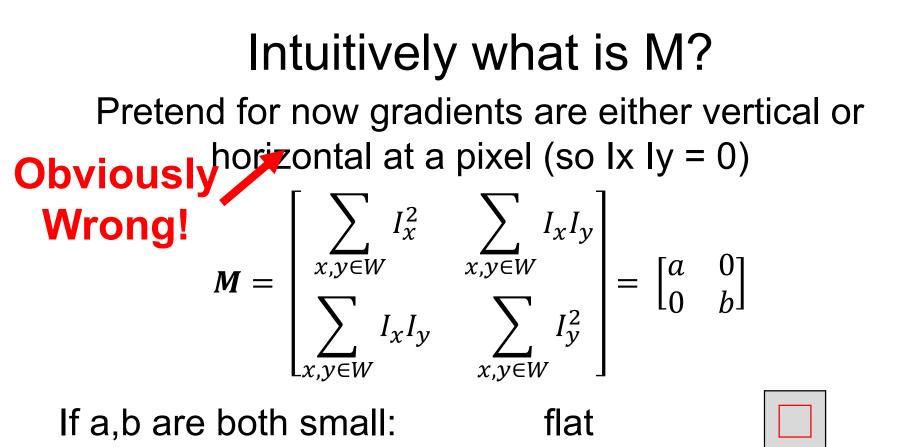
For brevity: Ix = Ix at point (x,y), Iy = Iy at point (x,y)

By linearizing image, we can approximate E(u,v) with quadratic function of u and v

$$E(u,v) \approx \sum_{(x,y)\in W} (I_x^2 u^2 + 2I_x I_y uv + I_y^2 v^2)$$

= $[u,v] \mathbf{M} [u,v]^T$
$$\mathbf{M} = \begin{bmatrix} \sum_{x,y\in W} I_x^2 & \sum_{x,y\in W} I_x I_y \\ \sum_{x,y\in W} I_x I_y & \sum_{x,y\in W} I_y^2 \end{bmatrix}$$

M is called the second moment matrix



If one is big, one is small: edge

If a,b both big:

corner

Review: Quadratic Forms

Suppose have symmetric matrix **M**, scalar a, vector [u,v]:

$$E([u,v]) = [u,v]\boldsymbol{M}[u,v]^T$$

Then the isocontour / slice-through of F, i.e.

$$E([u,v]) = a$$

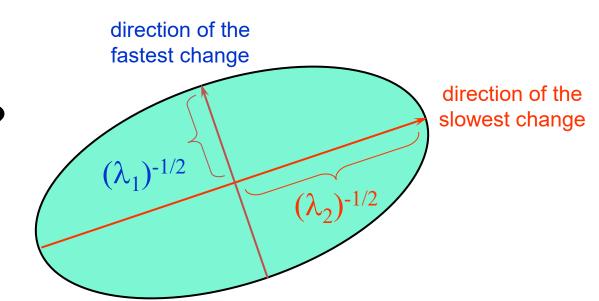
is an ellipse.

Review: Quadratic Forms

We can look at the shape of this ellipse by decomposing M into a rotation + scaling

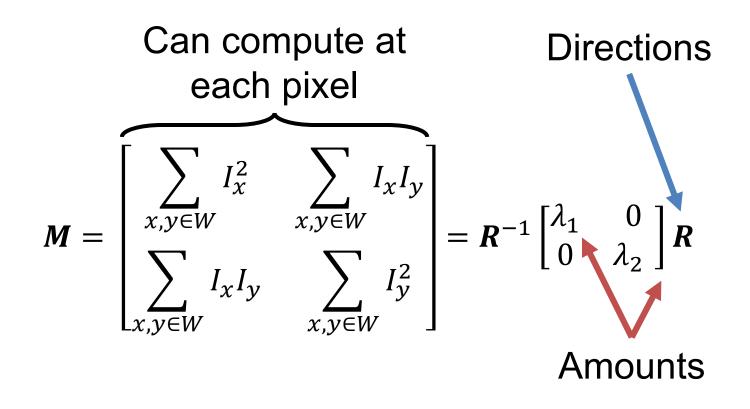
$$\boldsymbol{M} = \boldsymbol{R}^{-1} \begin{bmatrix} \lambda_1 & 0\\ 0 & \lambda_2 \end{bmatrix} \boldsymbol{R}$$

What are λ_1 and λ_2 ?

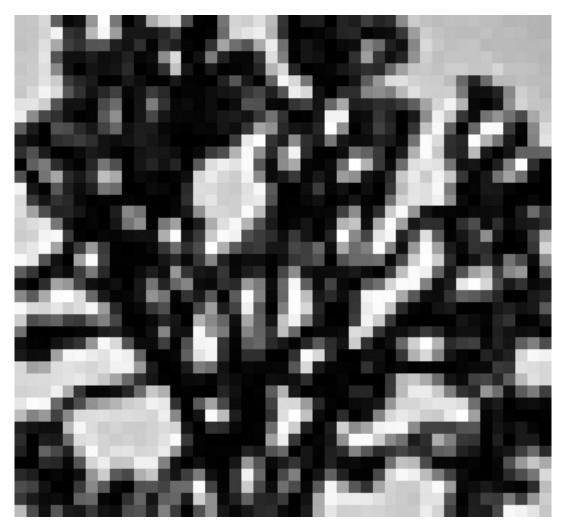


Interpreting The Matrix M

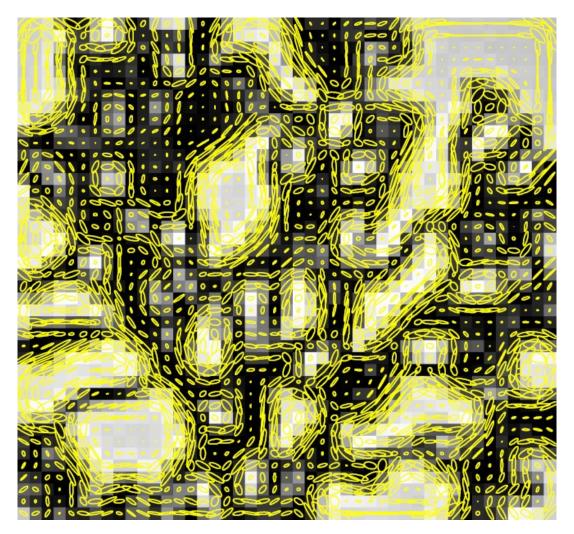
The second moment matrix tells us how quickly the image changes and in which directions.



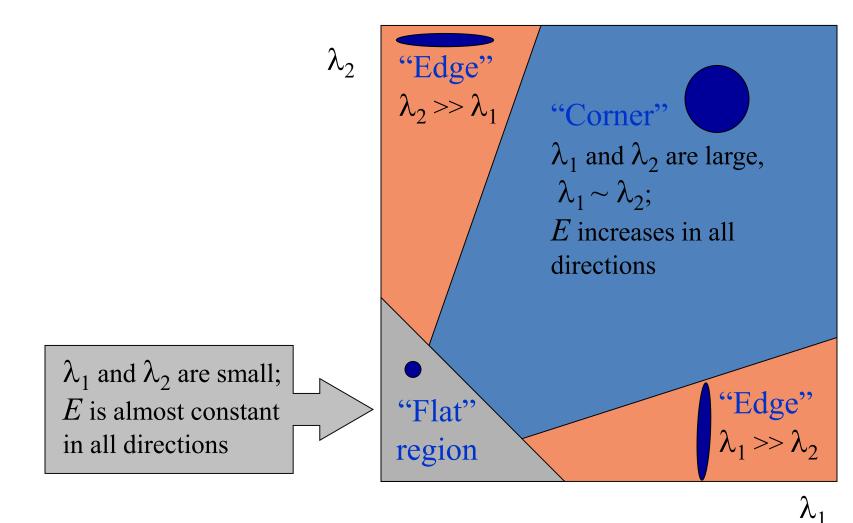
Visualizing M



Visualizing M



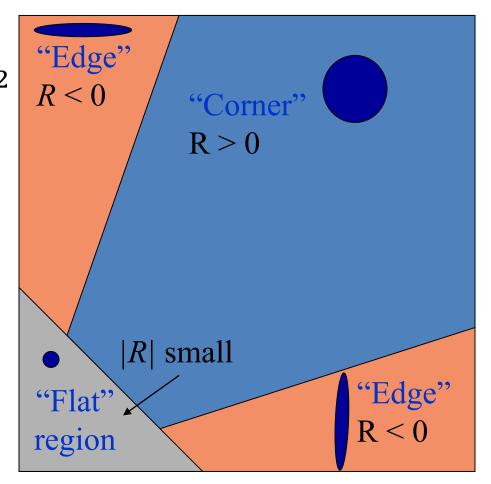
Interpreting Eigenvalues of M



Putting Together The Eigenvalues

$$R = \det(\mathbf{M}) - \alpha \operatorname{trace}(\mathbf{M})^{2}$$
$$= \lambda_{1}\lambda_{2} - \alpha(\lambda_{1} + \lambda_{2})^{2}$$

α: constant (0.04 to 0.06)



In Practice

- 1. Compute partial derivatives Ix, Iy per pixel
- 2. Compute **M** at each pixel, using Gaussian weighting w

$$\boldsymbol{M} = \begin{bmatrix} \sum_{x,y \in W} w(x,y) I_x^2 & \sum_{x,y \in W} w(x,y) I_x I_y \\ \sum_{x,y \in W} w(x,y) I_x I_y & \sum_{x,y \in W} w(x,y) I_y^2 \end{bmatrix}$$

C.Harris and M.Stephens. <u>"A Combined Corner and Edge Detector."</u> *Proceedings of the 4th Alvey Vision Conference*: pages 147—151, 1988.

In Practice

- 1. Compute partial derivatives Ix, Iy per pixel
- 2. Compute **M** at each pixel, using Gaussian weighting w
- 3. Compute response function R

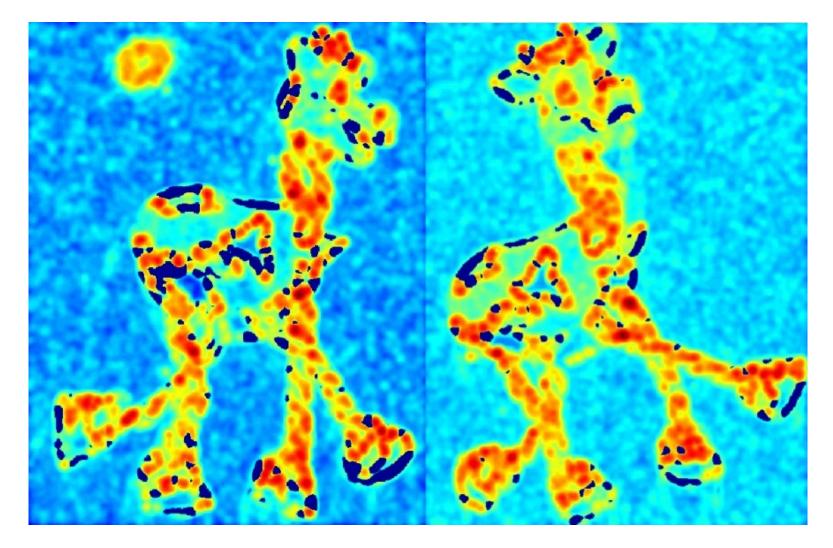
$$R = \det(\mathbf{M}) - \alpha \ trace(\mathbf{M})^{2}$$
$$= \lambda_{1}\lambda_{2} - \alpha(\lambda_{1} + \lambda_{2})^{2}$$

C.Harris and M.Stephens. <u>"A Combined Corner and Edge Detector."</u> *Proceedings of the 4th Alvey Vision Conference*: pages 147—151, 1988.

Computing R



Computing R



In Practice

- 1. Compute partial derivatives Ix, Iy per pixel
- 2. Compute **M** at each pixel, using Gaussian weighting w
- 3. Compute response function R
- 4. Threshold R

C.Harris and M.Stephens. <u>"A Combined Corner and Edge Detector."</u> *Proceedings of the 4th Alvey Vision Conference*: pages 147—151, 1988.

Thresholded R

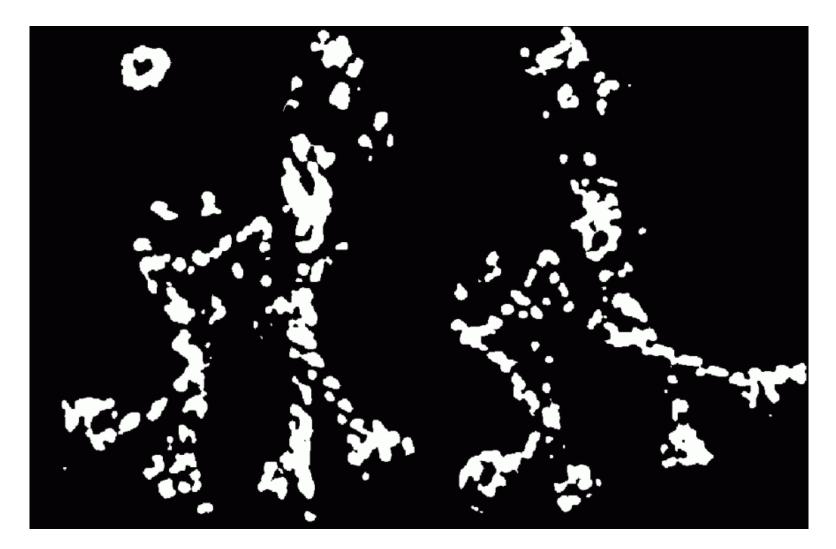


In Practice

- 1. Compute partial derivatives Ix, Iy per pixel
- 2. Compute **M** at each pixel, using Gaussian weighting w
- 3. Compute response function R
- 4. Threshold R
- 5. Take only local maxima (called non-maxima suppression)

C.Harris and M.Stephens. <u>"A Combined Corner and Edge Detector."</u> *Proceedings of the 4th Alvey Vision Conference*: pages 147—151, 1988.

Thresholded, NMS R



Slide credit: S. Lazebnik

Final Results



Slide credit: S. Lazebnik

If our detectors are repeatable, they should be:

- Invariant to some things: image is transformed and corners remain the same
- Covariant/equivariant with some things: image is transformed and corners transform with it.

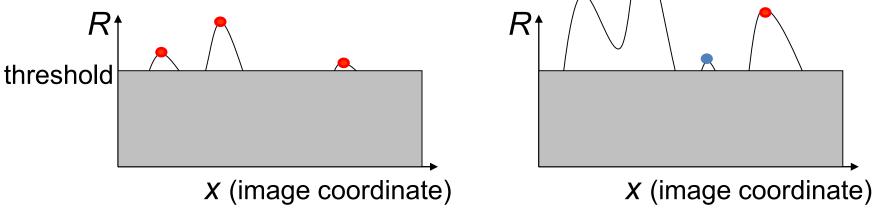
Recall Motivating Problem

Images may be different in lighting and geometry



Affine Intensity Change $I_{new} = aI_{old} + b$

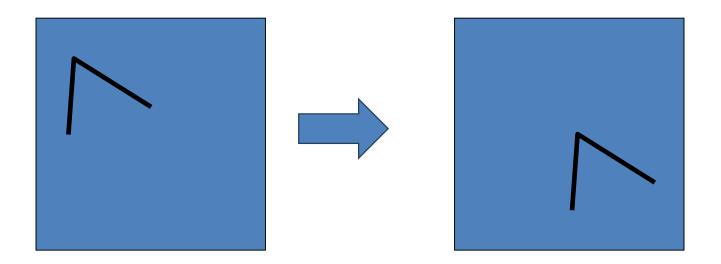
M only depends on derivatives, so b is irrelevant But a scales derivatives and there's a threshold



Partially invariant to affine intensity changes

Slide credit: S. Lazebnik

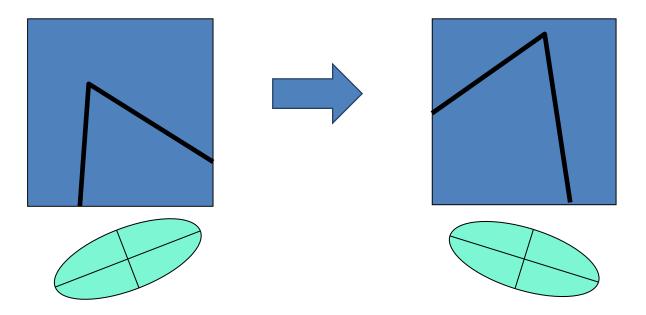
Image Translation



All done with convolution. Convolution is translation invariant.

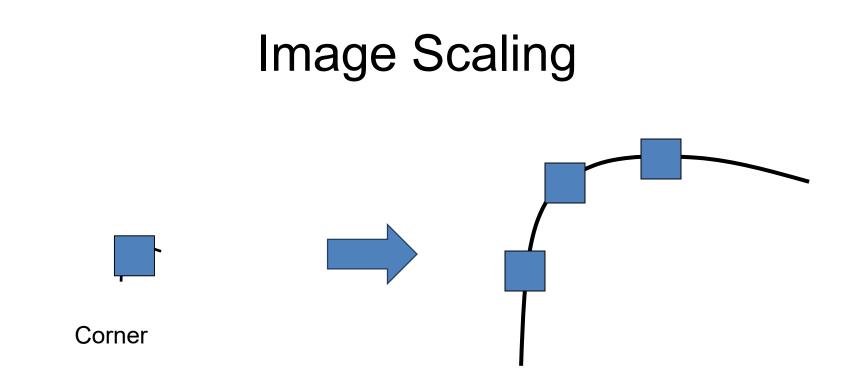
Equivariant with translation

Image Rotation



Rotations just cause the corner rotation to change. Eigenvalues remain the same.

Equivariant with rotation



One pixel can become many pixels and viceversa.

Not equivariant with scaling

Next time

- Fixing this scaling issue
- Describing the corners

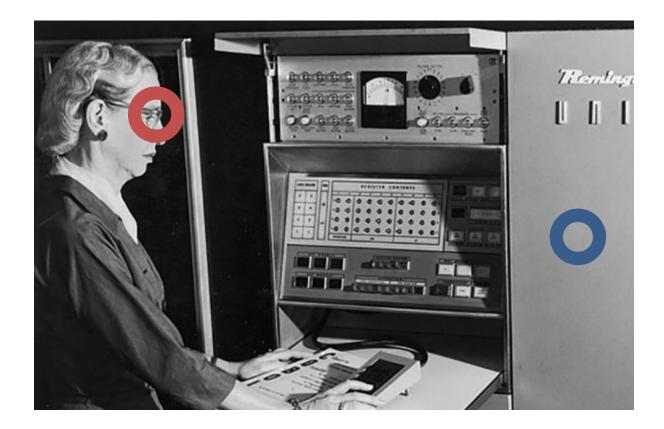
Repeatable: we can find the same place even after photometric metric and geometric distortion.







Compactness: we don't just use all the pixels Saliency: the place is distinctive



Locality: the feature doesn't depend on the whole image but instead some part

