Synthesizing Grid Data with Cyber Resilience and Privacy Guarantees

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2025 INFORMS Annual Meeting — Atlanta

October 26, 2025



Power systems as a stroll in the fog

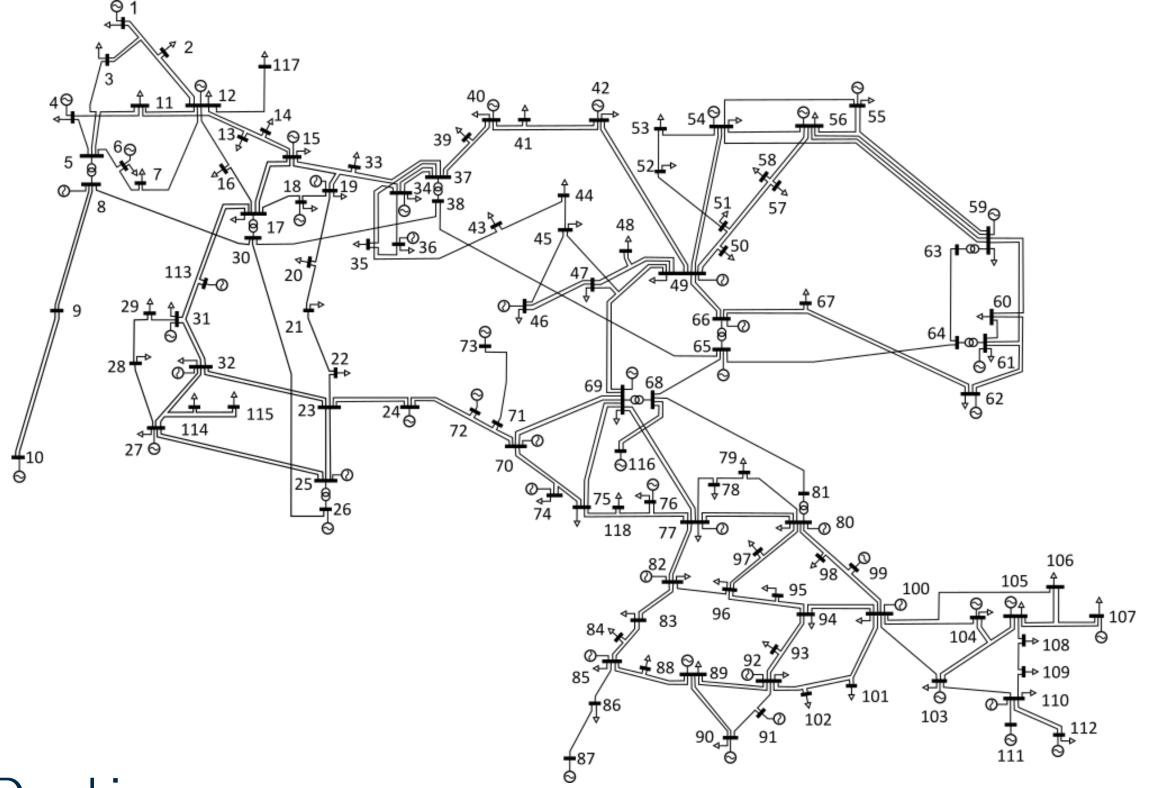


- Power systems are critical infrastructures with most of data being classified
- ► We have only a limited observably, e.g., ISO data disclosure portals
- Grid stakeholders hence act on a limited set of system data



Hedgehog in the Fog Yuri Norstein (1975)

Example: DC optimal power flow (OPF) in the (small) IEEE 118-bus system

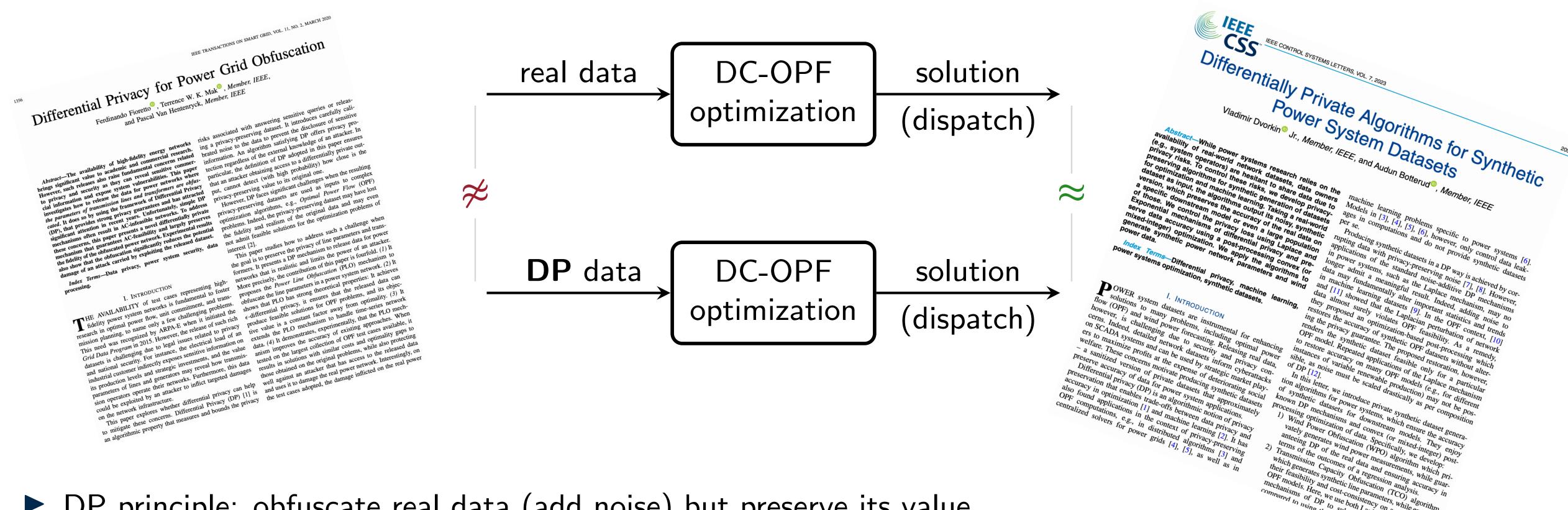


- ► 1079 rows of element-specific data
- Each generator owns only 2 rows
- The rest of system data is not *explicitly* disclosed to power producers

How to disclose grid data in a controllable manner?

Differential privacy (DP) enables controlled disclosure of grid data





- ► DP principle: obfuscate real data (add noise) but preserve its value
- In the DC-OPF setting: obfuscate grid data but preserve the OPF solution
- Formal *privacy guarantee*: released DP data does NOT disclose the real data
- Many applications to synthesizing high-quality transmission, load and generation data

Example: Synthesizing transmission line capacities using DP and optimization



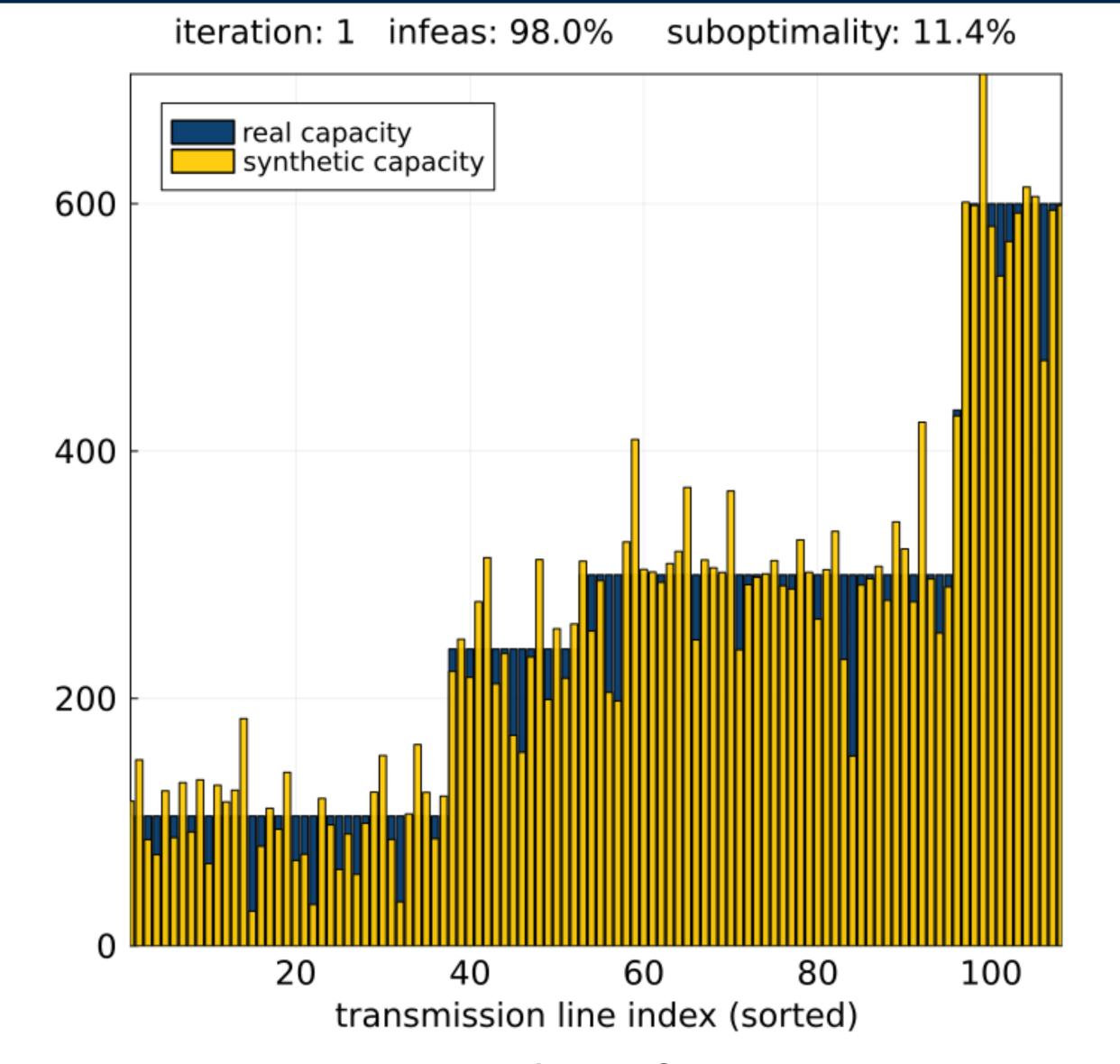
- ► IEEE 73-RTS benchmark
- Step 1: add random noise to trans capacity

$$\varphi_1 = \overline{f} + \text{calibrated noise}$$

Step 2: post-process φ_1 to ensure OPF feasibility and cost-consistency w.r.t. real trans capacity

$$arphi_2 \in \operatorname*{argmin}_{arphi} \quad \|c(\overline{f}) - c(arphi)\| + \|arphi - arphi_1\|$$
 s.t. $c(arphi) = \min_{p} \quad c(p) \quad opf \; cost$ s.t. $p \in \mathcal{P}(arphi) \quad opf \; feas$

► Step 3-N: repeat Step 2 until OPF feasibility and cost-consistency are restored across many scenarios



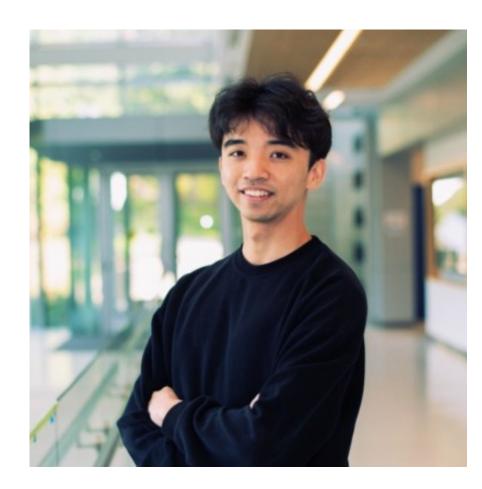
Dvorkin, V., Botterud A. Differentially private algorithms for synthetic power system datasets, IEEE Control Systems Letters, 2023.

Challenge: If DP synthetic datasets are so good, do they pose any security risks?



- Grid datasets are used for calibrating cyberattacks on power grids
- ightharpoonup Hypothesis: high-quality synthetic data ightharpoonup well-calibrated attacks
- Classes of cyberattacks: false data injection, line outage masking, physical attacks, ...

Contribution: We identify cyberattack risks in releasing DP grid data and propose new algorithms to guarantee both privacy and cyber resilience to source grids



Shengyang Wu

Load redistribution attack



lacktriangle Given load **d**, the attack corrupts the load ${f d}+{m \delta}$ with bus injection ${m \delta}$ from admissible set ${f \Delta}$

$$\Delta \triangleq \left\{ \begin{array}{c|c} \underline{\delta} & \underline{\delta} \leqslant \overline{\delta} & \text{injection limits for each bus} \\ \mathbf{1}^{\top} \underline{\delta} = 0 & \text{total load remains unchanged} \end{array} \right\}$$

Amounts solving a bi-level optimization problem:

$$C_{ ext{att}}^{ ext{BO}}(\mathbf{d}) = \max_{oldsymbol{\delta} \in \Delta} \quad C_{ ext{opf}}(\mathbf{d} + oldsymbol{\delta})$$
 s.t. $C_{ ext{opf}}(\mathbf{d} + oldsymbol{\delta}) = \min_{\mathbf{x}} \quad \mathbf{c}^{\top}\mathbf{x}$ s.t. $\mathbf{a}_k^{\top}\mathbf{x} + \mathbf{b}_k^{\top}(\mathbf{d} + oldsymbol{\delta}) + e_k \leqslant \mathbf{0}$

maximize the cost

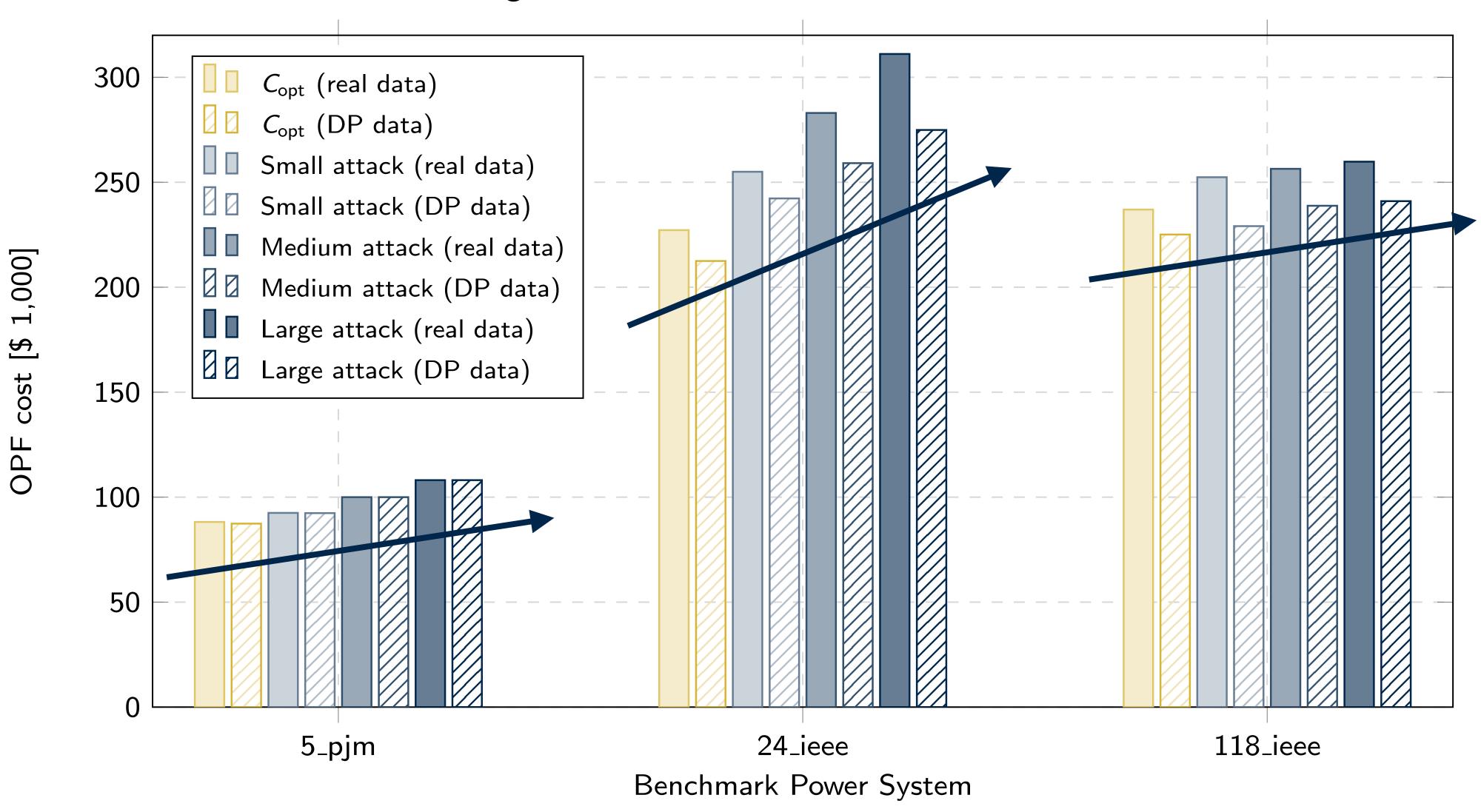
feedback from OPF

► The problem seeks a *stealthy* attack vector that maximizes the OPF cost

Can DP grid data be used to successfully execute the load redistribution attack?







Post-processing optimization to minimize attack damage



Figure: Tri-level structure of the cyber-resilient post-processing of DP load data.

- ▶ Step 1: add random noise to real loads: $\mathbf{d}_1 = \mathbf{d} + \text{calibrated noise}$
- ► Step 2: post-process d_1 by solving a tri-level optimization:
 - Level-1: Optimize synthetic load d to balance attack damage and cost-consistency
 - Level-2: Feedback from both OPF and attack optimization
 - ► Level-3: Embedded OPF for attack calibration
- Result: DP load vector d balancing attack damage and cost-consistency

Tractable approximation of the tri-level problem



- Optimizing synthetic loads over bi-level optimization is computationally challenging
- ► We drawn on the connection between bi-level and robust (single-level) optimization

Bi-level attack optimization

$$C_{ ext{att}}^{ ext{BO}}(extbf{d}) = \max_{oldsymbol{\delta} \in \Delta} C_{ ext{opf}}(extbf{d} + oldsymbol{\delta})$$
 $extbf{x} \in \operatorname*{argmin} \ extbf{c}^{ op} extbf{x}$
 $ext{s.t.} \ extbf{a}_k^{ op} extbf{x} + extbf{b}_k^{ op} (extbf{d} + oldsymbol{\delta}) + e_k \leqslant extbf{0} \quad orall k$

$$(uniform attack)$$

Robust optimization (RO) approximation

$$C_{\text{att}}^{\text{RO}}(\mathbf{d}) = \min_{\mathbf{x}} \ \mathbf{c}^{\top} \mathbf{x}$$
s.t.
$$\max_{\boldsymbol{\delta}_k \in \Delta} \left[\mathbf{a}_k^{\top} \mathbf{x} + \mathbf{b}_k^{\top} (\mathbf{d} + \boldsymbol{\delta}_k) + e_k \right] \leqslant \mathbf{0} \quad \forall k$$

(per constraint attack)

Proposition: For any feasible load **d**, relation $C_{\text{att}}^{\text{RO}}(\mathbf{d}) \geqslant C_{\text{att}}^{\text{BO}}(\mathbf{d})$ holds.

Cyber Resilient Obfuscation (CRO) Algorithm

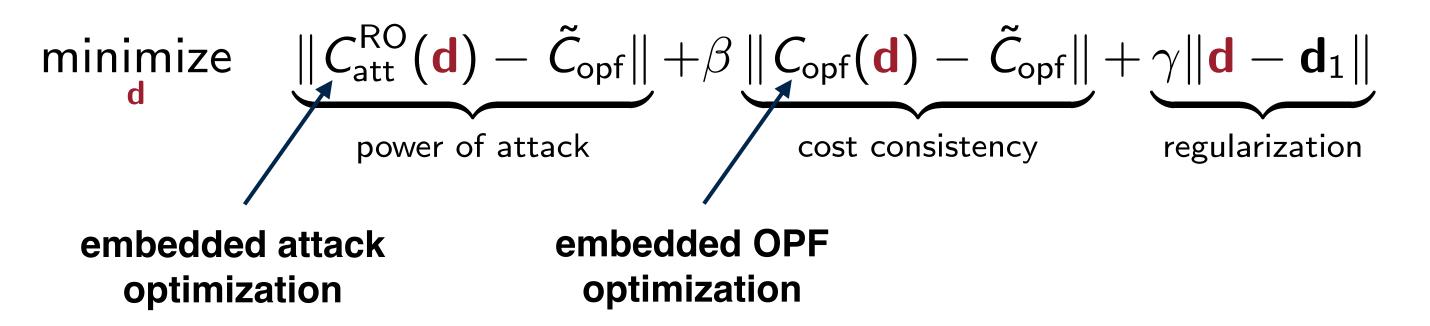


Step 1: Obfuscate real load data

DP load $\mathbf{d}_1 = \mathbf{d} + \text{calibrated noise}$

DP estimation of OPF costs: $\tilde{C}_{opf} = C_{opf}(\mathbf{d}) + \text{calibrated noise}$

ightharpoonup Step 2: Post-process d_1 to balance cost-consistency and cyber resilience P



► Replacing the two embedded optimization problems with their Karush–Kuhn–Tucker conditions leads to a single-level mixed-integer problem.

CRO-Exp: selecting only important constraints for post-processing



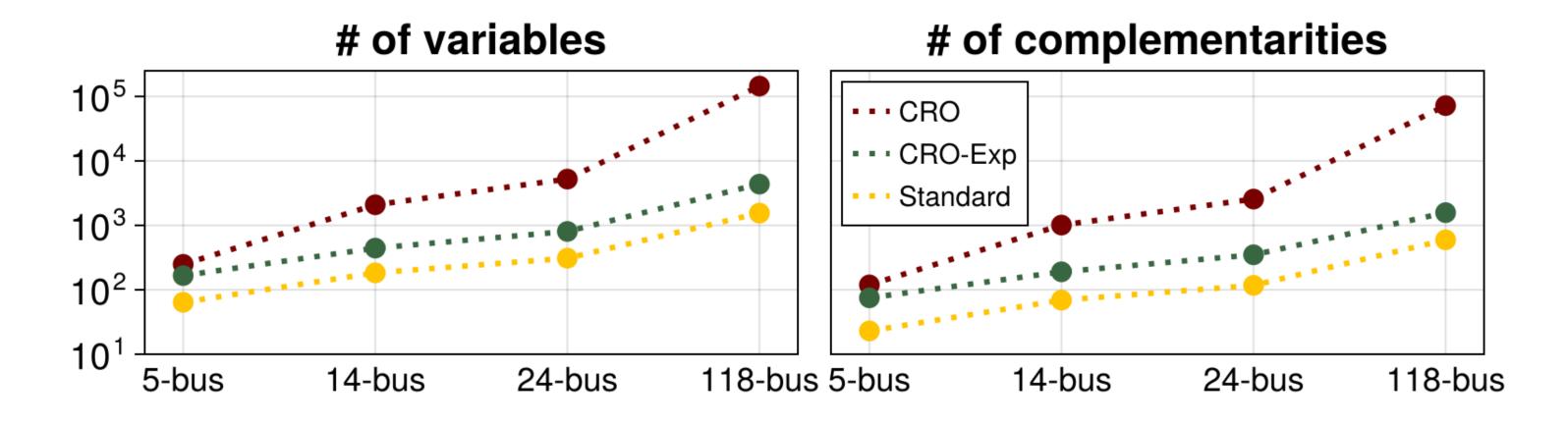
$$C_{\text{att},\tau}^{\text{RO}}(\mathbf{d}) = \min_{\mathbf{x}} \ \mathbf{c}^{\top}\mathbf{x}$$
s.t.
$$\max_{\boldsymbol{\delta}_k \in \Delta} \left[\mathbf{a}_k^{\top}\mathbf{x} + \mathbf{b}_k^{\top}(\mathbf{d} + \boldsymbol{\delta}_k) + e_k \right] \leqslant \mathbf{0} \quad \forall k \in \mathcal{K}'$$

$$\left[\mathbf{a}_k^{\top}\mathbf{x} + \mathbf{b}_k^{\top} \mathbf{d} + e_k \right] \leqslant \mathbf{0} \quad \forall k \in \mathcal{K}$$

RO-reformulated cons

original problem cons

- ightharpoonup We select only most important τ constraints for RO reformulation
- ightharpoonup Most important constraints in \mathcal{K}' are function of original loads
- lacktriangle Exponential mechanism of DP to obfuscate loads when selecting \mathcal{K}'



Selecting only important constraints substantially reduces the computational burden

CRO-Exp with privacy and cyber resilience guarantees



Algorithm 1: Privacy-preserving CRO-Exp

Input: real load **d**, DP parameters $(\alpha, \varepsilon_1, \varepsilon_2, \varepsilon_3)$, attack data $(\beta, \gamma, \Delta, \tau)$, $\mathcal{K} = \{\emptyset\}$ **1** DP obfuscation of load and OPF costs:

$$\tilde{\mathbf{d}}^0 = \mathbf{d} + \operatorname{Lap}\left(\frac{\alpha}{\varepsilon_1}\right)^n$$
 $\tilde{C}_{\mathrm{opf}} = C_{\mathrm{opf}}(\mathbf{d}) + \operatorname{Lap}\left(\frac{\alpha\overline{c}}{\varepsilon_2}\right)$

2 DP estimation of the set \mathcal{K} of the worst-case constraints

$$\begin{array}{l|l} \textbf{for} \ t = 1, \dots, \tau \ \textbf{do} \\ \hline & \textbf{for} \ k = 1, \dots, K \ \textbf{do} \\ \hline & C_k = C_{\mathsf{att},t}^{\mathsf{RO}}(\textbf{d}) + \mathsf{Lap}\left(\frac{\alpha\overline{c}}{\varepsilon_3}\right) \\ \\ \textbf{end} \\ & k_t \leftarrow \mathsf{argmax}_k \ C_k \\ \hline & \mathcal{K} \leftarrow \mathcal{K} \cup \{k_t\} \end{array}$$

end

3 Post-processing optimization of the synthetic load vector

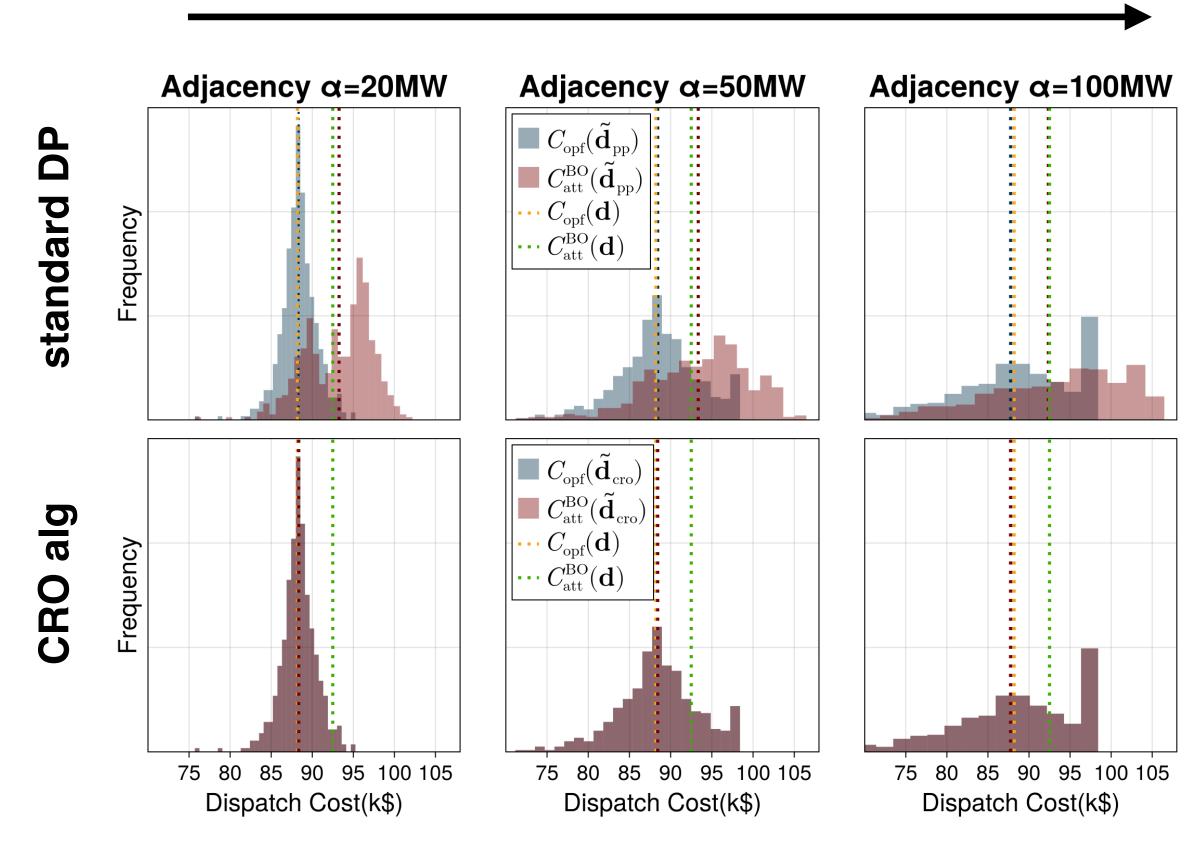
$$\tilde{\mathbf{d}} \in \operatorname{argmin} \|C_{\operatorname{opf}}(\tilde{\mathbf{d}}) - \tilde{C}_{\operatorname{opf}}\|_1 + \beta \|C_{\operatorname{att},\tau}^{\operatorname{RO}}(\tilde{\mathbf{d}}) - \tilde{C}_{\operatorname{opf}}\|_1 + \gamma \|\tilde{\mathbf{d}} - \tilde{\mathbf{d}}^0\|_1$$

Output: Synthetic load vector d

CRO application to PJM 5-Bus system







OPF cost distributions in normal and post-attack operation

- ► Blue distributions normal operation
- Red distributions post-attack operation
- Top row standard DP post-processing
- Bottom row proposed CRO post-processing

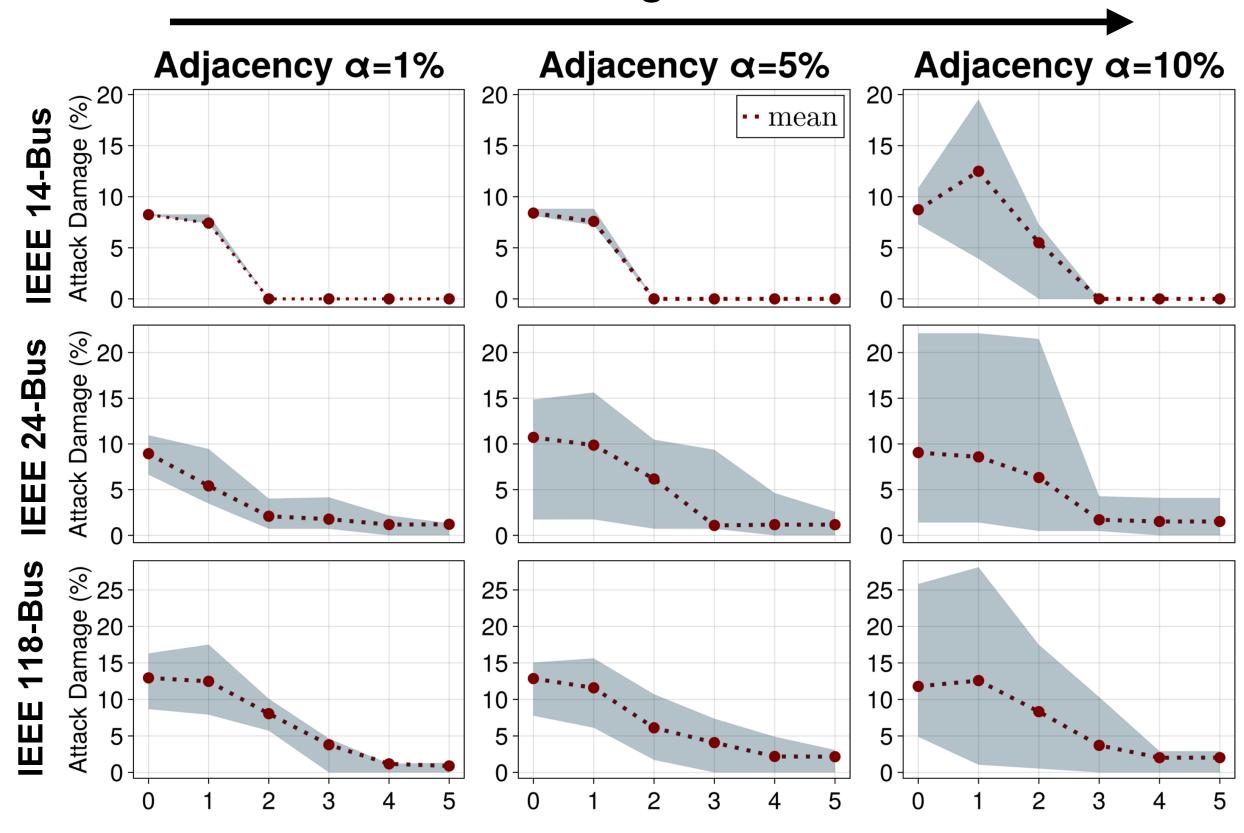
CRO sends important signal to attackers: the attacks do not lead to extra OPF cost to the system.

(normal and post-attack distributions overlap)

CRO-Exp application to larger systems







Number of iterations τ of Exponential Mechanism in Alg. 2

Post-attack damage as a function of constraints selected for post-processing optimization

- ightharpoonup The more constraints under attack ightharpoonup more resilent the source grid to load redistribution attacks
- ► 5 constraints on average to minimize the damage

After 5 iterations, the CRO-Exp algorithm identified the most important constraints for post-processing synthetic loads and ensuring grid resilience.

Conclusions



- Synthetic grid data is optimized to guarantee privacy, quality and cyber resilience simultaneously
- Trade-offs under linear cost functions are "flat": resilience is achieved with little to no impact on data quality
- ► The tri-level post-processing optimization can be efficiently collapsed to single-level optimization under reasonable and judicious approximations (connecting bilevel and robust optimization techniques)

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Synthesizing Grid Data With Cyber Resilience and Privacy Guarantees

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Abstract—Differential privacy (DP) provides a principled approach to synthesizing data (e.g., loads) from real-world power systems while limiting the exposure of sensitive information. However, adversaries may exploit synthetic data to calibrate cyberattacks on the source grids. To control these risks, we propose new DP algorithms for synthesizing data that provide the source grids with both cyber resilience and privacy guarantees. The algorithms incorporate both normal operation and attack optimization models to balance the fidelity of synthesized data and cyber resilience. The resulting post-processing optimization is reformulated as a robust optimization problem, which is compatible with the exponential mechanism of DP to moderate its computational burden.

Index Terms—Power systems, synthetic dataset, differential privacy, cyber security.

with such releases remain largely unexplored. Possible cyber attacks include *false data injection*, which subtly alters state estimation results [13], *line outage masking*, which disconnects a transmission line and misguides a control center to seek outage elsewhere [14], and *load redistribution*, which manipulates demand measurements to increase OPF cost and constraint violation [15]. The latter is of main interest to this letter. Executing such attacks requires some grid knowledge [16], which is traditionally difficult to obtain. However, the availability of synthetic grid data may unintentionally inform adversaries and help them calibrate the attack.

Contribution: Recognizing the risks that synthetic grid parameters may inform cyber adversaries, we develop new DP algorithms that simultaneously guarantee cyber resilience and privacy for the source power grids. Our algorithms

Check paper for details on:

- DP guarantees of CRO and CRO-Exp
- Connection between Bi-level and RO
- Experiment settings, data and code

Miscellaneous



Our work on energy data privacy:

- 1 Synthesizing grid data with cyber resilience and privacy guarantees IEEE Control Systems Letters, 2025
- 2 Differentially private algorithms for synthetic power system datasets IEEE Control Systems Letters, 2023
- 3 Privacy-preserving convex optimization: When differential privacy meets stochastic programming 2025 IEEE Conference on Decision and Control
- 4 Differentially private optimal power flow for distribution grids
 IEEE Transactions on Power Systems, 2021. ♀ Best 2019–2021 Paper Award
- 5 Differentially private distributed optimal power flow 2020 IEEE Conference on Decision and Control

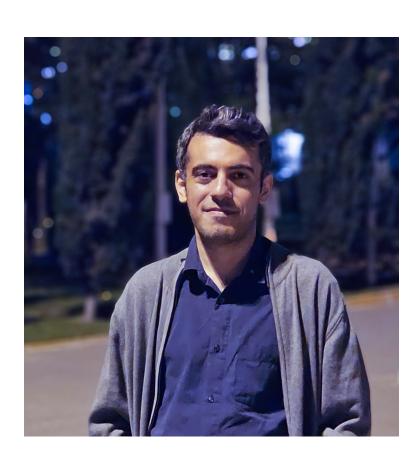
New perspective on energy data privacy via diffusion models:

Monday, October 27, 2025 at 2:57 PM – 3:09 PM EDT

Synthesizing Representative Power Flow Datasets via Constrained Diffusion Models

Part of MD31 – Grid Modeling, Simulation, and Resilience | Building B Level 2 B205

Track: Contributed



Milad Hoseinpour