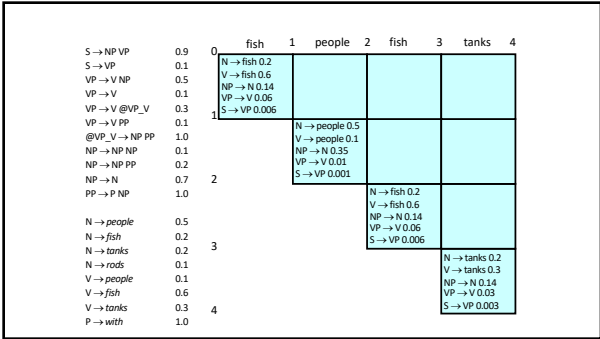
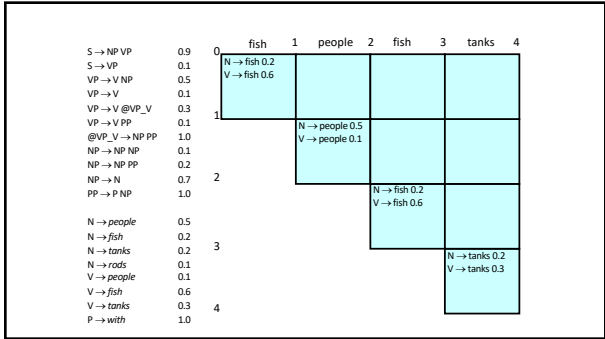
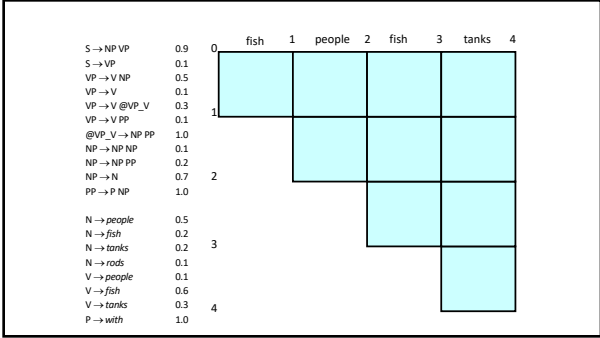
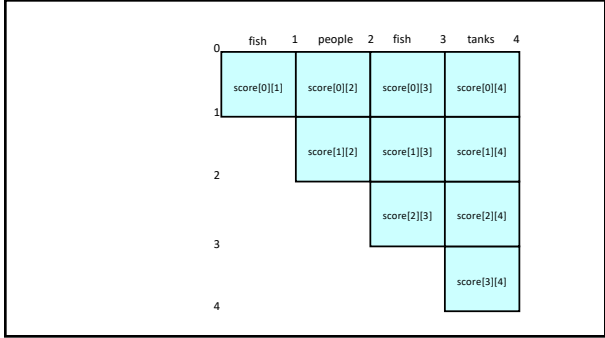


CS 6120/CS4120: Natural Language Processing

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The grammar

$S \rightarrow NP VP$	0.9	$N \rightarrow people$	0.5
$S \rightarrow VP$	0.1	$N \rightarrow fish$	0.2
$VP \rightarrow V NP$	0.5	$N \rightarrow tanks$	0.2
$VP \rightarrow V$	0.1	$N \rightarrow rods$	0.1
$VP \rightarrow V @VP\_V$	0.3	$V \rightarrow people$	0.1
$VP \rightarrow V PP$	0.1	$V \rightarrow fish$	0.6
$@VP\_V \rightarrow NP PP$	1.0	$V \rightarrow tanks$	0.3
$NP \rightarrow NP NP$	0.1	$P \rightarrow with$	1.0
$NP \rightarrow NP PP$	0.2		
$NP \rightarrow N$	0.7		
$PP \rightarrow P NP$	1.0		



S → NP VP	0.9	0	fish	1	people	2	fish	3	tanks	4
S → VP	0.1	N → fish 0.2								
VP → V NP	0.5	V → fish 0.6	NP → NP NP							
VP → V	0.1	NP → N 0.14	VP → V NP	0.0049						
VP → V @VP_V	0.3	VP → V 0.06	S → NP VP	0.105						
VP → V PP	0.1	S → VP 0.006		0.00196						
@VP_V → NP PP	1.0		N → people 0.5	NP → NP NP						
NP → NP NP	0.1		V → people 0.1	VP → V NP	0.0049					
NP → NP PP	0.2		NP → N 0.35	VP → V NP	0.007					
NP → N	0.7		S → VP 0.001	S → NP VP	0.0189					
PP → P NP	1.0									
N → people	0.5									
N → fish	0.2									
N → tanks	0.2									
N → rods	0.1									
V → people	0.1									
V → fish	0.6									
V → tanks	0.3									
P → with	1.0									

S → NP VP	0.9	0	fish	1	people	2	fish	3	tanks	4
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VP → V	0.1	NP → N 0.14	VP → V NP	0.105						
VP → V @VP_V	0.3	VP → V 0.06	S → NP VP	0.105						
VP → V PP	0.1	S → VP 0.006		0.00196						
@VP_V → NP PP	1.0		N → people 0.5	NP → NP NP						
NP → NP NP	0.1		V → people 0.1	VP → V NP	0.0049					
NP → NP PP	0.2		NP → N 0.35	VP → V NP	0.007					
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PP → P NP	1.0									
N → people	0.5									
N → fish	0.2									
N → tanks	0.2									
N → rods	0.1									
V → people	0.1									
V → fish	0.6									
V → tanks	0.3									
P → with	1.0									

S → NP VP	0.9	0	fish	1	people	2	fish	3	tanks	4
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V → tanks	0.3									
P → with	1.0									

S → NP VP	0.9	0	fish	1	people	2	fish	3	tanks	4
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NP → NP PP	0.2		NP → N 0.35	VP → V NP	0.007					
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N → people	0.5									
N → fish	0.2									
N → tanks	0.2									
N → rods	0.1									
V → people	0.1									
V → fish	0.6									
V → tanks	0.3									
P → with	1.0									

S → NP VP	0.9	0	fish	1	people	2	fish	3	tanks	4
S → VP	0.1	N → fish 0.2	NP → NP NP							
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VP → V @VP_V	0.3	VP → V 0.06	S → NP VP	0.105						
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S → NP VP	0.9	0	fish	1	people	2	fish	3	tanks	4
S → VP	0.1									
VP → V NP	0.5									
VP → V	0.1									
VP → V @VP_V	0.3									
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N → tanks	0.2									
N → rods	0.1									
V → people	0.1									
V → fish	0.6									
V → tanks	0.3									
P → with	1.0									

for i in 0, len(words): i++  
 for A in nonterminals  
 if A -> words[i] in grammar  
 score[i][A] = P(A -> words[i])

S → NP VP	0.9	0	fish	1	people	2	fish	3	tanks	4
S → VP	0.1	N → fish 0.2								
VP → V NP	0.5	V → fish 0.6								
VP → V	0.1									
VP → V @VP_V	0.3									
VP → V PP	0.1									
@VP_V → NP PP	1.0									
NP → NP NP	1.0									
NP → NP PP	0.2									
NP → N	0.7									
PP → P NP	1.0									
N → people	0.5									
N → fish	0.2									
N → tanks	0.2									
N → rods	0.1									
V → people	0.1									
V → fish	0.6									
V → tanks	0.3									
P → with	1.0									

// handles unaries  
 boolean added = true  
 while added  
 added = false  
 for A, B in nonterminals  
 if score[|A|][B] > 0.44 A->B in grammar  
 prob = P(A->B)\*score[|A|][B]  
 if prob > score[|end|][A]  
 score[|end|][A] = prob  
 back[|end|][A] = B  
 added = true

S → NP VP	0.9	0	fish	1	people	2	fish	3	tanks	4
S → VP	0.1	N → fish 0.2								
VP → V NP	0.5	V → fish 0.6								
VP → V	0.1									
VP → V @VP_V	0.3									
VP → V PP	0.1									
@VP_V → NP PP	1.0									
NP → NP NP	0.1									
NP → NP PP	0.2									
NP → N	0.7									
PP → P NP	1.0									
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N → tanks	0.2									
N → rods	0.1									
V → people	0.1									
V → fish	0.6									
V → tanks	0.3									
P → with	1.0									

prob:score[begin][split][B]\*score[split][end][C]\*P(A->B)  
 if (prob > score[begin][end][A])  
 score[begin][end][A] = prob  
 back[begin][end][A] = new Triple(split,B,C)

S → NP VP	0.9	0	fish	1	people	2	fish	3	tanks	4
S → VP	0.1	N → fish 0.2	NP → NP NP							
VP → V NP	0.5	V → fish 0.6	VP → V NP							
VP → V	0.1	NP → N 0.14	VP → V NP							
VP → V @VP_V	0.3	VP → V 0.06	S → NP VP							
VP → V PP	0.1	S → VP 0.006	S → NP VP							
@VP_V → NP PP	1.0		NP → NP NP							
NP → NP NP	0.1		VP → V NP							
NP → NP PP	0.2		VP → V 0.01							
NP → N	0.7		S → NP VP							
PP → P NP	1.0		S → VP 0.001							
N → people	0.5									
N → fish	0.2									
N → tanks	0.2									
N → rods	0.1									
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N → tanks	0.2									
N → rods	0.1									
V → people	0.1									
V → fish	0.6									
V → tanks	0.3									
P → with	1.0									

NP split = begin+1 to end-1  
 for A,B,C in nonterminals  
 prob:score[begin][split][B]\*score[split][end][C]\*P(A->B)  
 if (prob > score[begin][end][A])  
 score[begin][end][A] = prob  
 back[begin][end][A] = new Triple(split,B,C)

S → NP VP	0.9	0	fish	1	people	2	fish	3	tanks	4
S → VP	0.1	N → fish 0.2	NP → NP NP							
VP → V NP	0.5	V → fish 0.6	VP → V NP							
VP → V	0.1	NP → N 0.14	VP → V NP							
VP → V @VP_V	0.3	VP → V 0.06	S → NP VP							
VP → V PP	0.1	S → VP 0.006	S → NP VP							
@VP_V → NP PP	1.0		NP → NP NP							
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for split = begin+1 to end-1  
 for A,B,C in nonterminals  
 prob:score[begin][split][B]\*score[split][end][C]\*P(A->B)  
 if (prob > score[begin][end][A])  
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S → NP VP	0.9	0	fish	1	people	2	fish	3	tanks	4
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VP → V @VP_V	0.3	VP → V 0.06	S → NP VP							
VP → V PP	0.1	S → VP 0.006	S → NP VP							
@VP_V → NP PP	1.0		NP → NP NP							
NP → NP NP	0.1		VP → V NP							
NP → NP PP	0.2		VP → V 0.01							
NP → N	0.7		S → NP VP							
PP → P NP	1.0		S → VP 0.001							
N → people	0.5									
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V → fish	0.6									
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P → with	1.0									

for split = begin+1 to end-1  
 for A,B,C in nonterminals  
 prob:score[begin][split][B]\*score[split][end][C]\*P(A->B)  
 if (prob > score[begin][end][A])  
 score[begin][end][A] = prob  
 back[begin][end][A] = new Triple(split,B,C)

S → NP VP	0.9	0	fish	1	people	2	fish	3	tanks	4
S → VP	0.1		N → fish 0.2		NP → NP NP		NP → NP NP		NP → NP NP	
VP → V NP	0.5		V → fish 0.6		NP → V NP		VP → V NP		VP → V NP	
VP → V	0.1		NP → N 0.14		VP → V NP		VP → V NP		VP → V NP	
VP → V @VP_V	0.3		VP → V 0.05		S → VP		S → NP VP		S → NP VP	
VP → V PP	0.1		S → VP 0.006							
@VP_V → NP PP	1.0				N → people 0.5		NP → NP NP		NP → NP NP	
NP → NP NP	0.1				V → people 0.1		VP → V NP		VP → V NP	
NP → NP PP	0.2				NP → N 0.35		VP → V NP		VP → V NP	
NP → N	0.7				NP → V 0.01		S → NP VP		S → NP VP	
PP → P NP	1.0				S → VP 0.001					
N → people	0.5						N → fish 0.2		NP → NP NP	
N → fish	0.2						V → fish 0.6		VP → V NP	
N → tanks	0.2						NP → N 0.14		VP → V NP	
N → rods	0.1						VP → V 0.06		S → VP	
V → people	0.1						S → VP 0.006			
V → fish	0.6								N → tanks 0.2	
V → tanks	0.3								V → tanks 0.3	
P → with	1.0								NP → N 0.14	
									VP → V 0.03	
									S → VP 0.003	

Call back the (score, back) to get the best parse

### Extended CKY parsing

- CKY parsing is usually done after binarization
- Unaries can be incorporated into the algorithm
  - Messy, but doesn't increase algorithmic complexity
- Empties can be incorporated
  - Doesn't increase complexity; essentially like unaries
- Binarization is *vital*
  - Without binarization, you don't get parsing cubic in the length of the sentence and in the number of nonterminals in the grammar

### Treebanks

- English Penn Treebank:** Standard corpus for testing syntactic parsing consists of 1.2 M words of text from the Wall Street Journal (WSJ).
- Typical to train on about 40,000 parsed sentences and test on an additional standard disjoint test set of 2,416 sentences.
- Chinese Penn Treebank:** 100K words from the Xinhua news service.
- Other corpora existing in many languages, see the Wikipedia article "Treebank"

### Computing Evaluation Metrics

**Correct Tree T**

# Constituents: 12

**Computed Tree P**

# Constituents: 12

Recall = 10/12 = 83.3%    Precision = 10/12 = 83.3%    F<sub>1</sub> = 83.3%

### Evaluating constituency parsing

Gold standard brackets: S-(0:11), NP-(0:2), VP-(2:9), VP-(3:9), NP-(4:6), PP-(6:9), NP-(7:9), NP-(9:10)

Candidate brackets: S-(0:11), NP-(0:2), VP-(2:10), VP-(3:10), NP-(4:6), PP-(6:10), NP-(7:10)

### Evaluating constituency parsing

**Gold standard brackets:**  
S-(0:11), NP-(0:2), VP-(2:9), VP-(3:9), NP-(4:6), PP-(6:9), NP-(7:9), NP-(9:10)

**Candidate brackets:**  
S-(0:11), NP-(0:2), VP-(2:10), VP-(3:10), NP-(4:6), PP-(6:10), NP-(7:10)

Labeled Precision	3/7 = 42.9%
Labeled Recall	3/8 = 37.5%
LP/LR F1	40.0%
POS Tagging Accuracy	11/11 = 100.0%

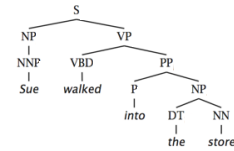
### How good are PCFGs?

- Penn WSJ parsing accuracy: about 73% LP/LR F1 (state-of-the-art is 91-92% F1)
- Robust
  - Usually admit everything, but with low probability
- Partial solution for grammar ambiguity
  - A PCFG gives some idea of the plausibility of a parse
- Give a probabilistic language model
  - But in the simple case it performs worse than a trigram model
- The problem seems to be that PCFGs lack the lexicalization of a trigram model

### (Head) Lexicalization of PCFGs

[Magerman 1995, Collins 1997; Charniak 1997]

- The head word of a phrase gives a good representation of the phrase's structure and meaning (*head words are decided by rules*)
- Puts the properties of words back into a PCFG



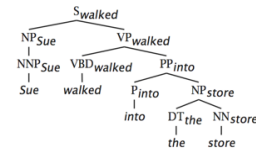
### Head Words

- Syntactic phrases usually have a word in them that is most "central" to the phrase.
- Linguists have defined the concept of a lexical **head** of a phrase.
- Simple rules can identify the head of any phrase by percolating head words up the parse tree.
  - Head of a VP is the main verb
  - Head of an NP is the main noun
  - Head of a PP is the preposition
  - Head of a sentence is the head of its VP

### (Head) Lexicalization of PCFGs

[Magerman 1995, Collins 1997; Charniak 1997]

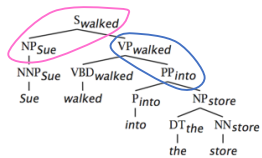
- The head word of a phrase gives a good representation of the phrase's structure and meaning
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### (Head) Lexicalization of PCFGs

[Magerman 1995, Collins 1997; Charniak 1997]

- The head word of a phrase gives a good representation of the phrase's structure and meaning
- Puts the properties of words back into a PCFG



### (Head) Lexicalization of PCFGs

[Magerman 1995, Collins 1997; Charniak 1997]

- Word-to-word affinities are useful for certain ambiguities
  - PP attachment is now (partly) captured in a local PCFG rule.



- Also useful for: coordination scope, verb complement patterns

Lexicalized parsing was seen as *the* parsing breakthrough of the late 1990s

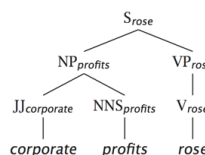
• Eugene Charniak, 2000 JHU workshop: “To do better, it is necessary to condition probabilities on the actual words of the sentence. This makes the probabilities much tighter:

- $p(\text{VP} \rightarrow \text{V NP NP}) = 0.00151$
- $p(\text{VP} \rightarrow \text{V NP NP} \mid \text{said}) = 0.00001$
- $p(\text{VP} \rightarrow \text{V NP NP} \mid \text{gave}) = 0.01980$  ”

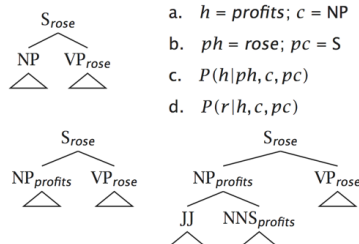
• Michael Collins, 2003 COLT tutorial: “Lexicalized Probabilistic Context-Free Grammars ... perform vastly better than PCFGs (88% vs. 73% accuracy)”

Lexicalization of PCFGs: Charniak (1997)

- A very straightforward model of a lexicalized PCFG
- Probabilistic conditioning is “top-down” like a regular PCFG
  - But actual parsing is bottom-up, somewhat like the CKY algorithm we saw



Charniak (1997) example  
Probabilities that can be modeled (more info)



- a.  $h = \text{profits}; c = \text{NP}$
- b.  $ph = \text{rose}; pc = \text{S}$
- c.  $P(h|ph, c, pc)$
- d.  $P(r|h, c, pc)$

Lexicalization models argument selection by sharpening rule expansion probabilities

- The probability of different verbal complement frames (i.e., “subcategorizations”) depends on the verb:

Local Tree	come	take	think	want
VP → V	9.5%	2.6%	4.6%	5.7%
VP → V NP	1.1%	<b>32.1%</b>	0.2%	13.9%
VP → V PP	<b>34.5%</b>	3.1%	7.1%	0.3%
VP → V SBAR	6.6%	0.3%	<b>73.0%</b>	0.2%
VP → V S	2.2%	1.3%	4.8%	70.8%
VP → V NP S	0.1%	5.7%	0.0%	0.3%
VP → V PRT NP	0.3%	5.8%	0.0%	0.0%
VP → V PRT PP	6.1%	1.5%	0.2%	0.0%

Lexicalization sharpens probabilities:  
Predicting heads

“Bilexical probabilities”

- $P(\text{prices} \mid \text{n-plural}) = .013$
- $P(\text{prices} \mid \text{n-plural, NP}) = .013$
- $P(\text{prices} \mid \text{n-plural, NP, S}) = .025$
- $P(\text{prices} \mid \text{n-plural, NP, S, v-past}) = .052$
- $P(\text{prices} \mid \text{n-plural, NP, S, v-past, fell}) = .146$

Charniak (1997) linear  
interpolation/shrinkage

$$\hat{P}(h|ph, c, pc) = \lambda_1(e)P_{MLE}(h|ph, c, pc) + \lambda_2(e)P_{MLE}(h|C(ph), c, pc) + \lambda_3(e)P_{MLE}(h|c, pc) + \lambda_4(e)P_{MLE}(h|c)$$

- $\lambda_i(e)$  is here a function of how much one would expect to see a certain occurrence, given the amount of training data, word counts, etc.
- $C(ph)$  is semantic class of parent headword
- Techniques like these for dealing with data sparseness are vital to successful model construction

### Charniak (1997) shrinkage example

	$P(\text{prft} \text{rose, NP, S})$	$P(\text{corp} \text{prft, JJ, NP})$
$P(h ph, c, pc)$	0	0.245
$P(h C(ph), c, pc)$	0.00352	0.0150
$P(h c, pc)$	0.000627	0.00533
$P(h c)$	0.000557	0.00418

- Allows utilization of rich highly conditioned estimates, but smoothes when sufficient data is unavailable
- One can't just use MLEs: one commonly sees previously unseen events, which would have probability 0.

### Human Parsing

- Computational parsers can be used to predict human reading time as measured by tracking the time taken to read each word in a sentence.
- Psycholinguistic studies show that words that are more probable given the preceding lexical and syntactic context are read faster.
  - John put the dog in the pen with a **lock**.
  - John put the dog in the pen with a **bone** in the car.
  - John liked the dog in the pen with a **bone**.
- Modeling these effects requires an **incremental** statistical parser that incorporates one word at a time into a continuously growing parse tree.

### Garden Path Sentences

- People are confused by sentences that seem to have a particular syntactic structure but then suddenly violate this structure, so the listener is "lead down the garden path".
  - The horse raced past the barn fell.
    - vs. The horse raced past the barn broke his leg.
  - The complex houses married students.
  - The old man the sea.
  - While Anna dressed the baby spit up on the bed.
- Incremental computational parsers can try to predict and explain the problems encountered parsing such sentences.

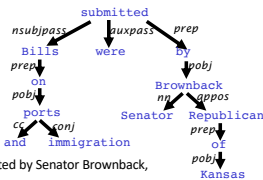
### Center Embedding

- Nested expressions are hard for humans to process beyond 1 or 2 levels of nesting.
  - The rat the cat chased died.
  - The rat the cat the dog bit chased died.
  - The rat the cat the dog the boy owned bit chased died.
- Requires remembering and popping incomplete constituents from a stack and strains human short-term memory.
- Equivalent "tail embedded" (tail recursive) versions are easier to understand since no stack is required.
  - The boy owned a dog that bit a cat that chased a rat that died.

### Dependency Grammar and Dependency Structure

Dependency syntax postulates that syntactic structure consists of lexical items linked by binary asymmetric relations ("arrows") called dependencies

The arrows are commonly typed with the name of grammatical relations (subject, prepositional object, apposition, etc.)

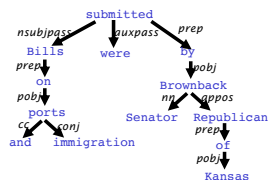


Bills on ports and immigration were submitted by Senator Brownback, Republican of Kansas.

### Dependency Grammar and Dependency Structure

Dependency syntax postulates that syntactic structure consists of lexical items linked by binary asymmetric relations ("arrows") called dependencies

The arrow connects a head (governor, superior, regent) with a dependent (modifier, inferior, subordinate)



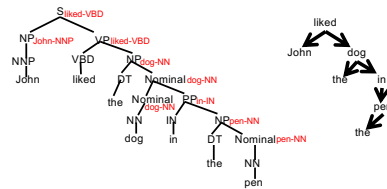
Usually, dependencies form a tree (connected, acyclic, single-head)

### Relation between phrase structure and dependency structure

- A dependency grammar has a notion of a head. Officially, CFGs don't.
- But modern linguistic theory and all modern statistical parsers (Charniak, Collins, Stanford, ...) do, via hand-written phrasal "head rules":
  - The head of a Noun Phrase is a noun/number/adj/...
  - The head of a Verb Phrase is a verb/modal/....
- The head rules can be used to extract a dependency parse from a CFG parse

### Dependency Graph from Parse Tree

- Can convert a phrase structure parse to a dependency tree by making the head of each non-head child of a node depend on the head of the head child.



### Methods of Dependency Parsing

1. Dynamic programming (like in the CKY algorithm)
 

You can do it similarly to lexicalized PCFG parsing: an  $O(n^3)$  algorithm  
Eisner (1996) gives a clever algorithm that reduces the complexity to  $O(n^2)$ , by producing parse items with heads at the ends rather than in the middle
2. Graph algorithms
 

You create a Maximum Spanning Tree for a sentence  
McDonald et al.'s (2005) MSTParser scores dependencies independently using a ML classifier (he uses MIRA, for online learning, but it could be MaxEnt)
3. Constraint Satisfaction
 

Edges are eliminated that don't satisfy hard constraints. Karlsso (1990), etc.
4. "Deterministic parsing"
 

Greedy choice of attachments guided by machine learning classifiers  
MaltParser (Nivre et al. 2008) – discussed in the next segment