

CS 6120/CS4120: Natural Language Processing

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Assignment/report submission

- Assignment submission problem, e.g. format
 - Contact Tirthraj, Manthan
- Project reports submission problem
 - Contact Liwen
- **Academic integrity:** Declaration on submission
 - Code from Github, stackoverflow, etc
 - Discussion with XX, etc

Project Progress Report

- What changes you have made for the task compared to the proposal, including problem/task, models, datasets, or evaluation methods? If there is any change, please explain why.
- Describe data preprocessing process. This includes data cleaning, selection, feature generation or other representation you have used, etc.
- What methods or models you have tried towards the project goal? And why do you choose the methods (you can including related work on similar task or relevant tasks)?
- What results you have achieved up to now based on your proposed evaluation methods? What is working or what is wrong with the model?
- How can you improve your models? What are the next steps?
- Grading: For 2-5, each aspect will take about 25 points.
- Length: Length: 2 page (or more if necessary)

Two views of linguistic structure:

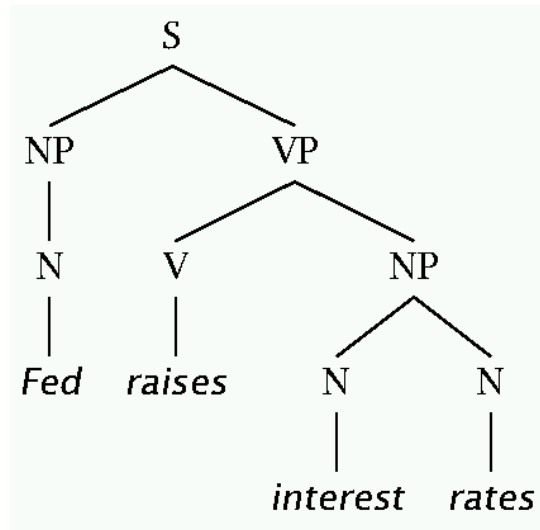
1. Constituency (phrase structure)

- Phrase structure organizes words into nested constituents.
 - Fed raises interest rates

Two views of linguistic structure:

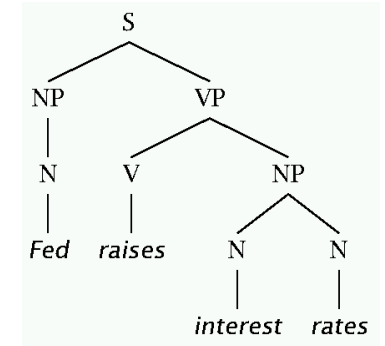
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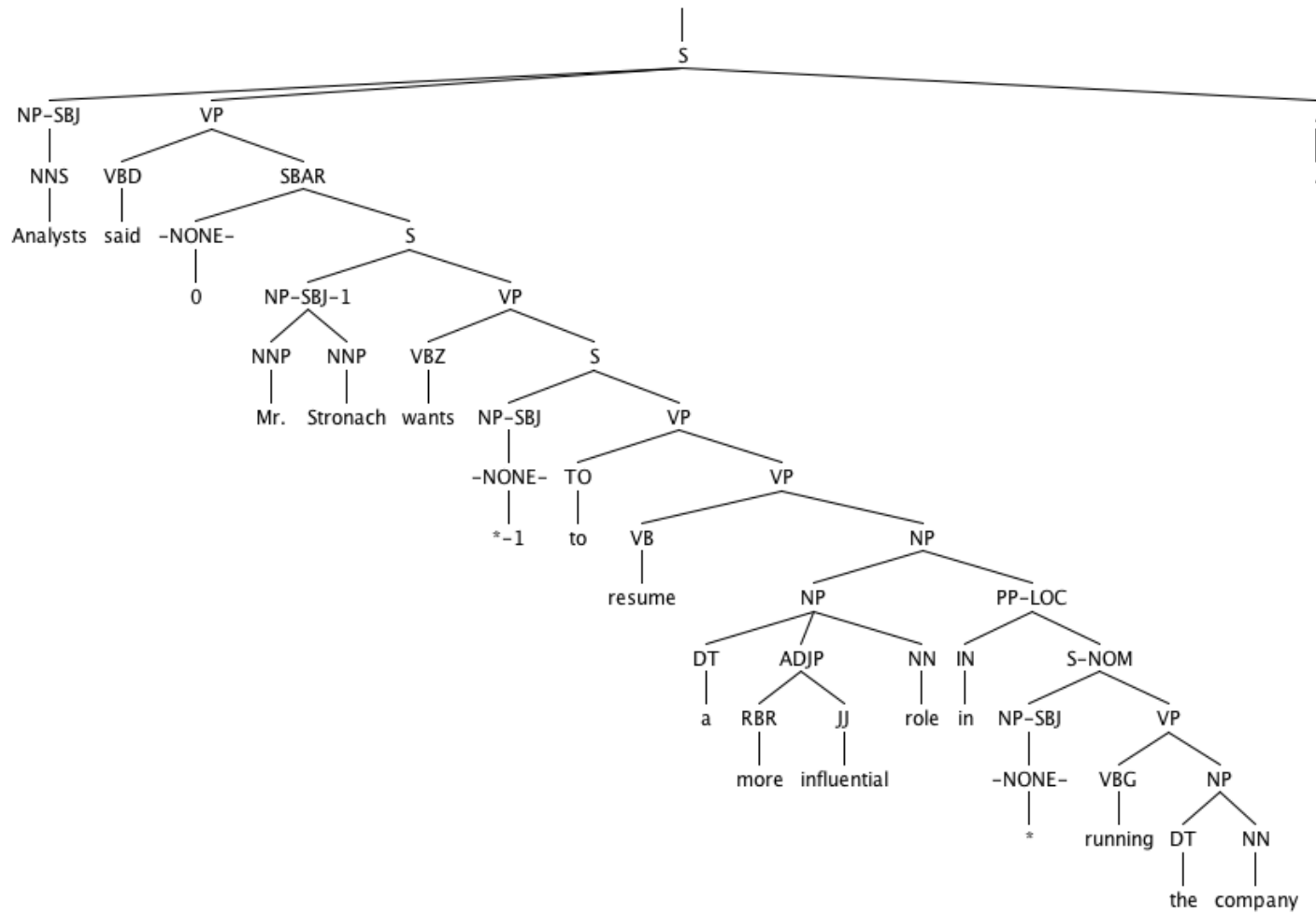


Two views of linguistic structure:

1. Constituency (phrase structure)



- Phrase structure organizes words into nested constituents.
- How do we know what is a **constituent**? (Not that linguists don't argue about some cases.)
 - Distribution: a constituent behaves as a unit that can appear in different places:
 - John talked [to the children] [about drugs].
 - John talked [about drugs] [to the children].
 - *John talked drugs to the children about
 - Substitution/expansion/pronoun (pro-forms):
 - I sat [on the box/right on top of the box/there].

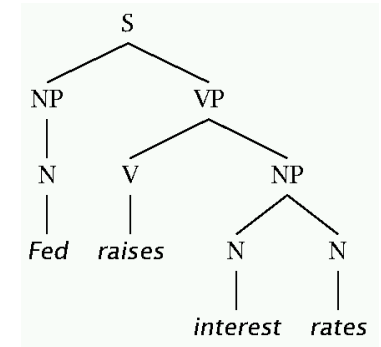


Headed phrase structure

- Context-free grammar
- $VP \rightarrow \dots VB^* \dots$
- $NP \rightarrow \dots NN^* \dots$
- $ADJP \rightarrow \dots JJ^* \dots$
- $ADVP \rightarrow \dots RB^* \dots$

- $SBAR(Q) \rightarrow S | SINV | SQ \rightarrow \dots NP VP \dots$

- Plus minor phrase types:
 - QP (quantifier phrase in NP), CONJP (multi word constructions: *as well as*), INTJ (interjections), etc.



Two views of linguistic structure:

2. Dependency structure

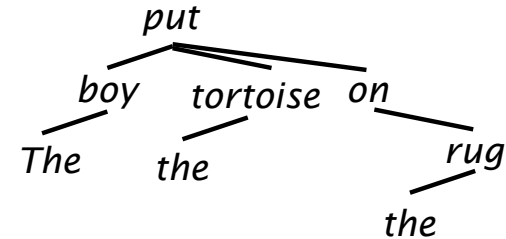
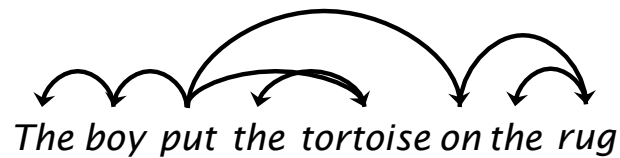
- Dependency structure shows which words depend on (modify or are arguments of) which other words.

The boy put the tortoise on the rug

Two views of linguistic structure:

2. Dependency structure

- Dependency structure shows which words depend on (modify or are arguments of) which other words.



Phrase Chunking

- Find all non-recursive noun phrases (NPs) and verb phrases (VPs) in a sentence.
 - [NP I] [VP ate] [NP the spaghetti] [PP with] [NP meatballs].
 - [NP He] [VP reckons] [NP the current account deficit] [VP will narrow] [PP to] [NP only 1.8 billion] [PP in] [NP September]

Phrase Chunking as Sequence Labeling

- Tag individual words with one of 3 tags
 - B (Begin) word starts new target phrase
 - I (Inside) word is part of target phrase but not the first word
 - O (Other) word is not part of target phrase
- Sample for NP chunking
 - He reckons **the current account deficit** will narrow to **only 1.8 billion** in **September**.

Begin

Inside

Other

Evaluating Chunking

Per token accuracy does not evaluate finding correct full chunks. Instead use:

$$\text{Precision} = \frac{\text{Number of correct chunks found}}{\text{Total number of chunks found}}$$

$$\text{Recall} = \frac{\text{Number of correct chunks found}}{\text{Total number of actual chunks}}$$

Take harmonic mean to produce a single evaluation metric called F measure.

$$F = \frac{(\beta^2 + 1)PR}{\beta^2 P + R} \quad F_1 = \frac{1}{\left(\frac{1}{P} + \frac{1}{R}\right)/2} = \frac{2PR}{P + R}$$

Current Chunking Results

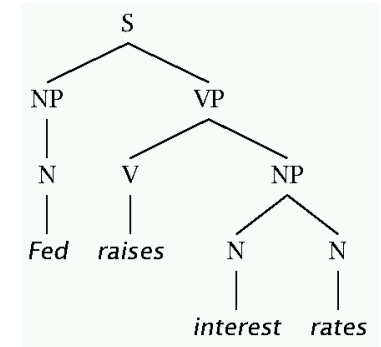
- Best system for NP chunking: $F_1=96\%$
- Typical results for finding range of chunk types (CONLL 2000 shared task: NP, VP, PP, ADV, SBAR, ADJP) is $F_1=92-94\%$

Headed phrase structure

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- Plus minor phrase types:
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A Brief Parsing History

Pre 1990 (“Classical”) NLP Parsing

- Wrote symbolic grammar (CFG or often richer) and lexicon

$S \rightarrow NP VP$	$NN \rightarrow \textit{interest}$
$NP \rightarrow (DT) NN$	$NNS \rightarrow \textit{rates}$
$NP \rightarrow NN NNS$	$NNS \rightarrow \textit{raises}$
$NP \rightarrow NNP$	$VBP \rightarrow \textit{interest}$
$VP \rightarrow V NP$	$VBZ \rightarrow \textit{rates}$

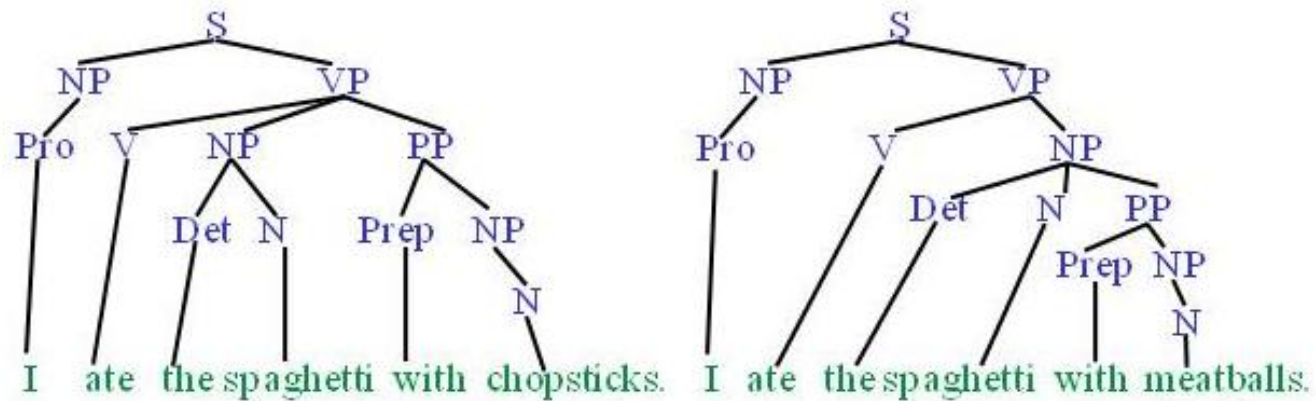
- Used grammar systems to prove parses from words
- This scaled very badly and didn't give coverage. For sentence:

Fed raises interest rates 0.5% in effort to control inflation

- Minimal grammar: 36 parses
- Simple 10 rule grammar: 592 parses
- Real-size broad-coverage grammar: millions of parses

Syntactic Parsing

- Produce the correct syntactic parse tree for a sentence.



An exponential number of attachments

Attachment ambiguities

- A key parsing decision is how we 'attach' various constituents
 - PPs, adverbial or participial phrases, infinitives, coordinations, etc.

The board approved [its acquisition] [by Royal Trustco Ltd.]
[of Toronto]
[for \$27 a share]
[at its monthly meeting].

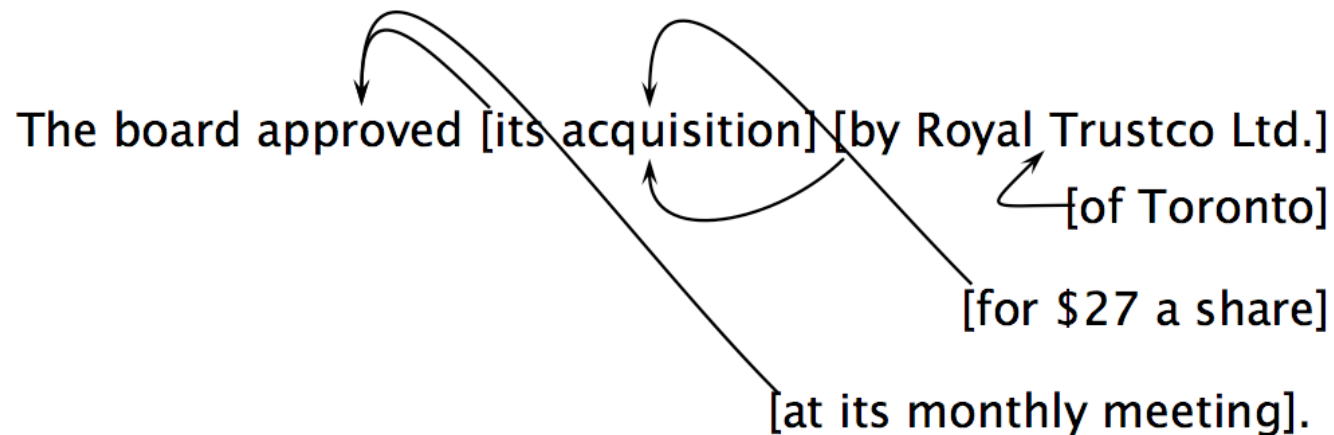
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Attachment ambiguities

- A key parsing decision is how we 'attach' various constituents
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Classical NLP Parsing: The problem and its solution

- Categorical constraints can be added to grammars to limit unlikely/weird parses for sentences
 - But the attempt make the grammars not robust
 - In traditional systems, commonly 30% of sentences in even an edited text would have *no* parse.
- A less constrained grammar can parse more sentences
 - But simple sentences end up with ever more parses with no way to choose between them
- We need mechanisms that allow us to find the most likely parse(s) for a sentence
 - Statistical parsing lets us work with very loose grammars that admit millions of parses for sentences but still quickly find the best parse(s)

The rise of annotated data: The Penn Treebank

[Marcus et al. 1993, *Computational Linguistics*]

```
((S
  (NP-SBJ (DT The) (NN move))
  (VP (VBD followed)
    (NP
      (NP (DT a) (NN round))
      (PP (IN of)
        (NP
          (NP (JJ similar) (NNS increases))
          (PP (IN by)
            (NP (JJ other) (NNS lenders))))
          (PP (IN against)
            (NP (NNP Arizona) (JJ real) (NN estate) (NNS loans))))))
    (, ,)
    (S-ADV
      (NP-SBJ (-NONE- *))
      (VP (VBG reflecting)
        (NP
          (NP (DT a) (VBG continuing) (NN decline))
          (PP-LOC (IN in)
            (NP (DT that) (NN market))))))
      (. .)))
```


The rise of annotated data

- Starting off, building a treebank seems a lot slower and less useful than building a grammar
- But a treebank gives us many things
 - Reusability of the labor
 - Many parsers, POS taggers, etc.
 - Valuable resource for linguistics
 - Broad coverage
 - Frequencies and distributional information
 - A way to evaluate systems

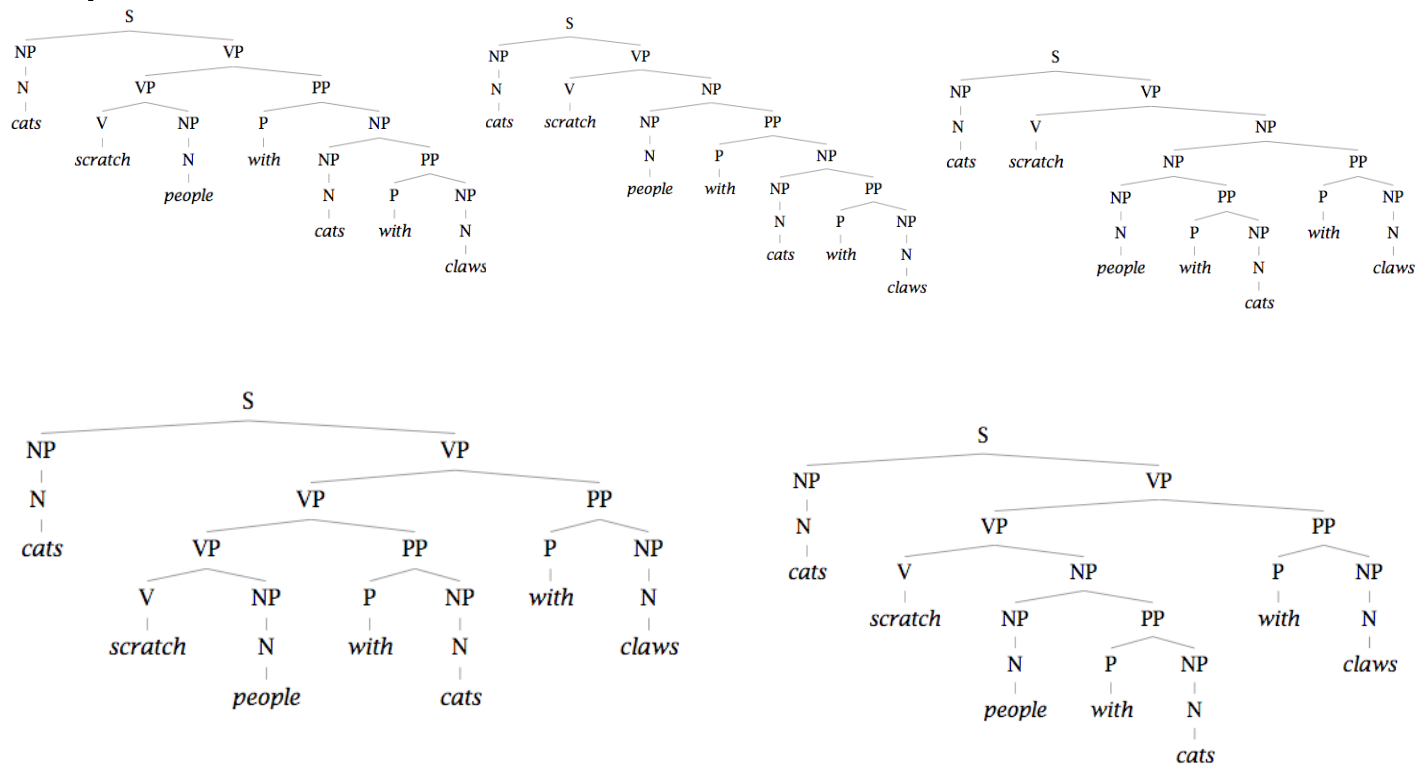
Statistical parsing applications

Statistical parsers are now robust and widely used in larger NLP applications:

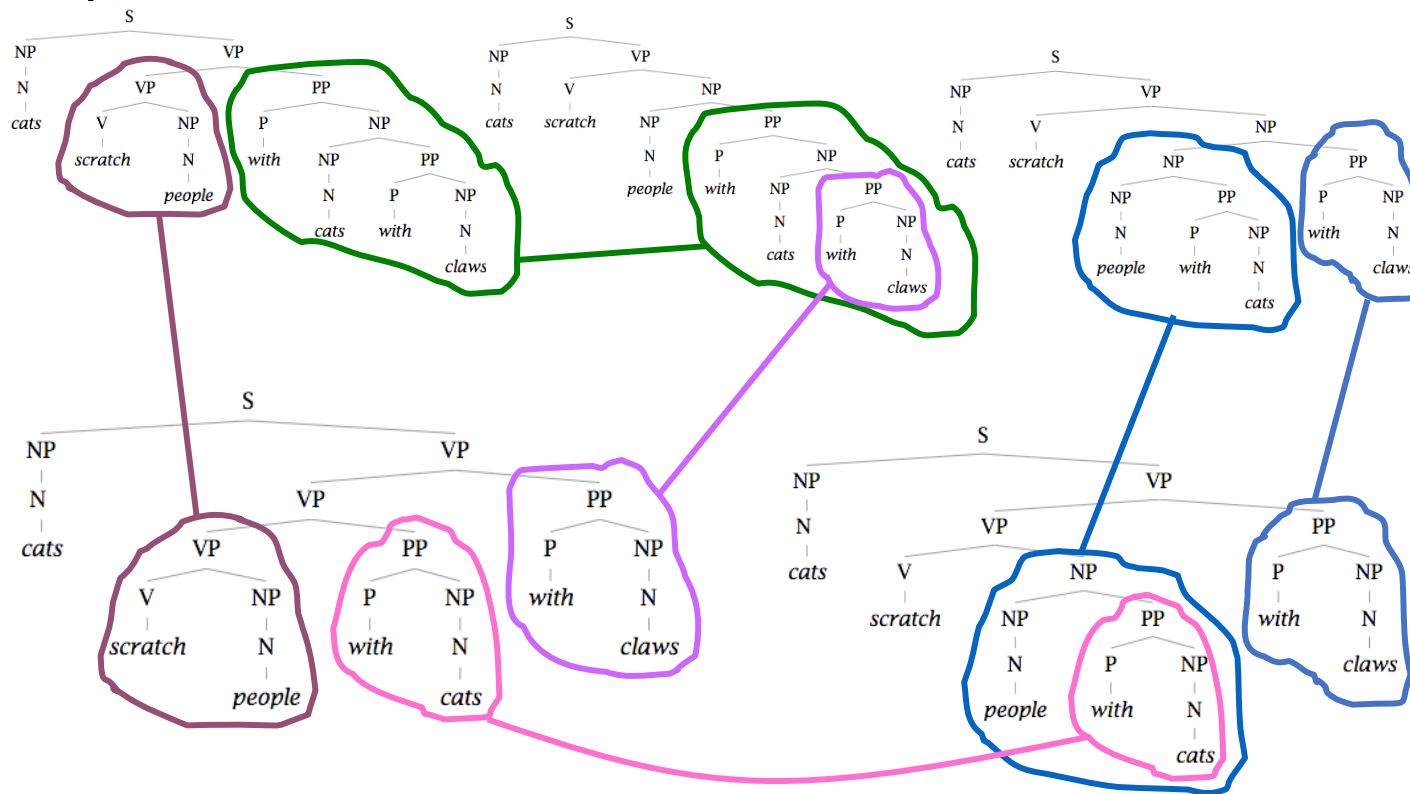
- High precision question answering [Pasca and Harabagiu SIGIR 2001]
- Improving biological named entity finding [Finkel et al. JNLPBA 2004]
- Syntactically based sentence compression [Lin and Wilbur 2007]
- Extracting opinions about products [Bloom et al. NAACL 2007]
- Improved interaction in computer games [Gorniak and Roy 2005]
- Helping linguists find data [Resnik et al. BLS 2005]
- Source sentence analysis for machine translation [Xu et al. 2009]
- Relation extraction systems [Fundel et al. Bioinformatics 2006]

Two problems to solve:

1. Repeated work...



Two problems to solve:
1. Repeated work...



Two problems to solve:

2. Choosing the correct parse

- How do we work out the correct attachment:
 - She saw the man with a telescope
- Words are good predictors of attachment, even absent full understanding
 - Moscow sent more than 100,000 soldiers into Afghanistan ...
 - Sydney Water breached an agreement with NSW Health ...
- Our statistical parsers will try to exploit such statistics.

(Probabilistic) Context-Free Grammars

- CFG
- PCFG

A phrase structure grammar

$S \rightarrow NP VP$

$VP \rightarrow V NP$

$VP \rightarrow V NP PP$

$NP \rightarrow NP NP$

$NP \rightarrow NP PP$

$NP \rightarrow N$

$NP \rightarrow e$

$PP \rightarrow P NP$

$N \rightarrow \text{people}$

$N \rightarrow \text{fish}$

$N \rightarrow \text{tanks}$

$N \rightarrow \text{rods}$

$V \rightarrow \text{people}$

$V \rightarrow \text{fish}$

$V \rightarrow \text{tanks}$

$P \rightarrow \text{with}$

people fish tanks

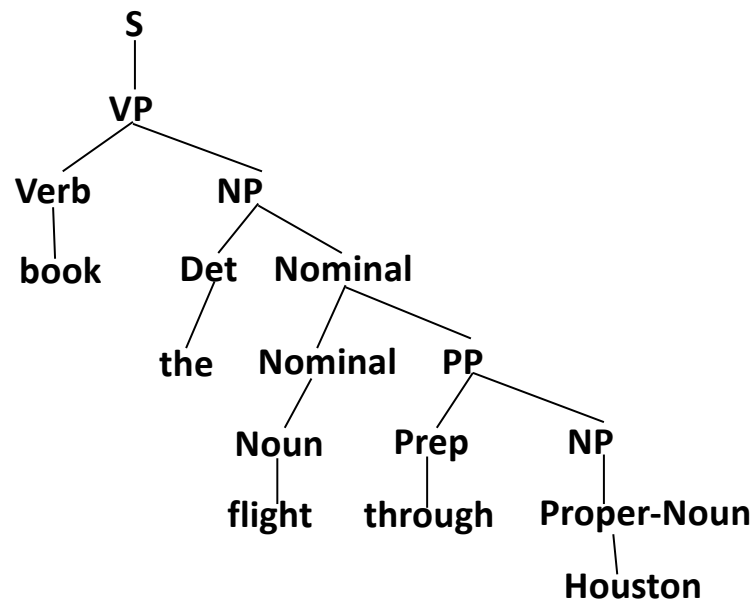
people fish with rods

Phrase structure grammars = context-free grammars (CFGs)

- $G = (T, N, S, R)$
 - T is a set of terminal symbols
 - N is a set of nonterminal symbols
 - S is the start symbol ($S \in N$)
 - R is a set of rules/productions of the form $X \rightarrow \gamma$
 - $X \in N$ and $\gamma \in (N \cup T)^*$
- A grammar G generates a language L.

Sentence Generation

- Sentences are generated by recursively rewriting the start symbol using the productions until only terminal symbols remain.



Phrase structure grammars in NLP

- $G = (T, C, N, S, L, R)$
 - T is a set of terminal symbols
 - C is a set of preterminal symbols
 - N is a set of nonterminal symbols
 - S is the start symbol ($S \in N$)
 - L is the lexicon, a set of items of the form $X \rightarrow x$
 - $X \in C$ and $x \in T$
 - R is the grammar, a set of items of the form $X \rightarrow \gamma$
 - $X \in N$ and $\gamma \in (N \cup C)^*$
- By usual convention, S is the start symbol, but in statistical NLP, we usually have an extra node at the top (ROOT, TOP)
- We usually write ϵ for an empty sequence, rather than nothing

A phrase structure grammar

$S \rightarrow NP VP$

$VP \rightarrow V NP$

$VP \rightarrow V NP PP$

$NP \rightarrow NP NP$

$NP \rightarrow NP PP$

$NP \rightarrow N$

$NP \rightarrow e$

$PP \rightarrow P NP$

people fish tanks

people fish with rods

$N \rightarrow \textit{people}$

$N \rightarrow \textit{fish}$

$N \rightarrow \textit{tanks}$

$N \rightarrow \textit{rods}$

$V \rightarrow \textit{people}$

$V \rightarrow \textit{fish}$

$V \rightarrow \textit{tanks}$

$P \rightarrow \textit{with}$

Probabilistic – or stochastic – context-free grammars (PCFGs)

- $G = (T, N, S, R, P)$
 - T is a set of terminal symbols
 - N is a set of nonterminal symbols
 - S is the start symbol ($S \in N$)
 - R is a set of rules/productions of the form $X \rightarrow \gamma$
 - P is a probability function
 - $P: R \rightarrow [0,1]$
 - $\forall X \in N, \sum_{X \rightarrow \gamma \in R} P(X \rightarrow \gamma) = 1$
- A grammar G generates a language model L.

A PCFG

$S \rightarrow NP VP$	1.0	$N \rightarrow \textit{people}$	0.5
$VP \rightarrow V NP$	0.6	$N \rightarrow \textit{fish}$	0.2
$VP \rightarrow V NP PP$	0.4	$N \rightarrow \textit{tanks}$	0.2
$NP \rightarrow NP NP$	0.1	$N \rightarrow \textit{rods}$	0.1
$NP \rightarrow NP PP$	0.2	$V \rightarrow \textit{people}$	0.1
$NP \rightarrow N$	0.7	$V \rightarrow \textit{fish}$	0.6
$PP \rightarrow P NP$	1.0	$V \rightarrow \textit{tanks}$	0.3
		$P \rightarrow \textit{with}$	1.0

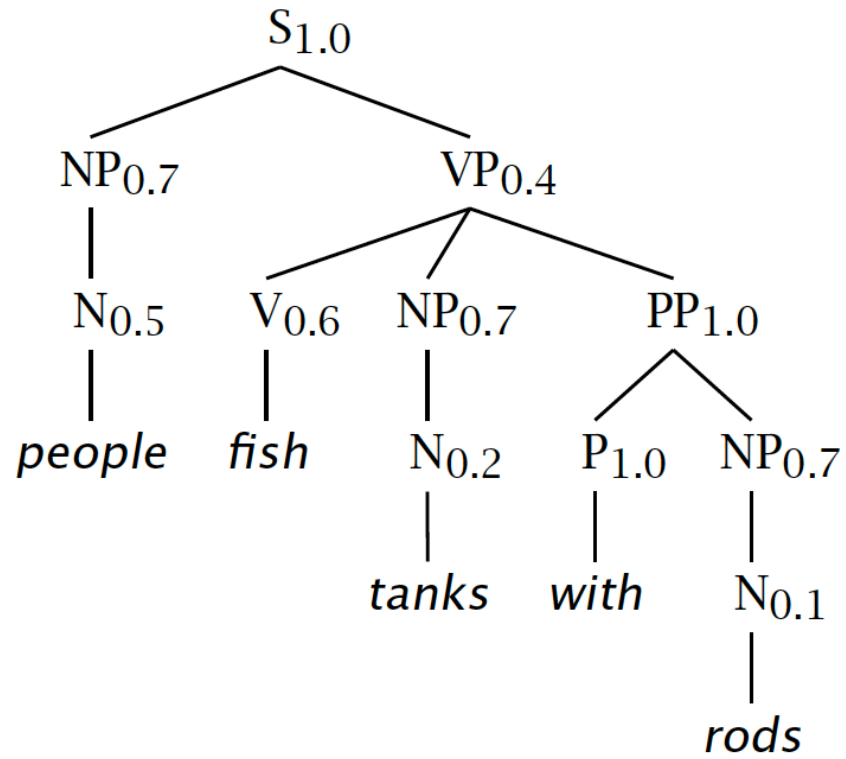
[With empty NP removed so
less ambiguous]

The probability of trees and strings

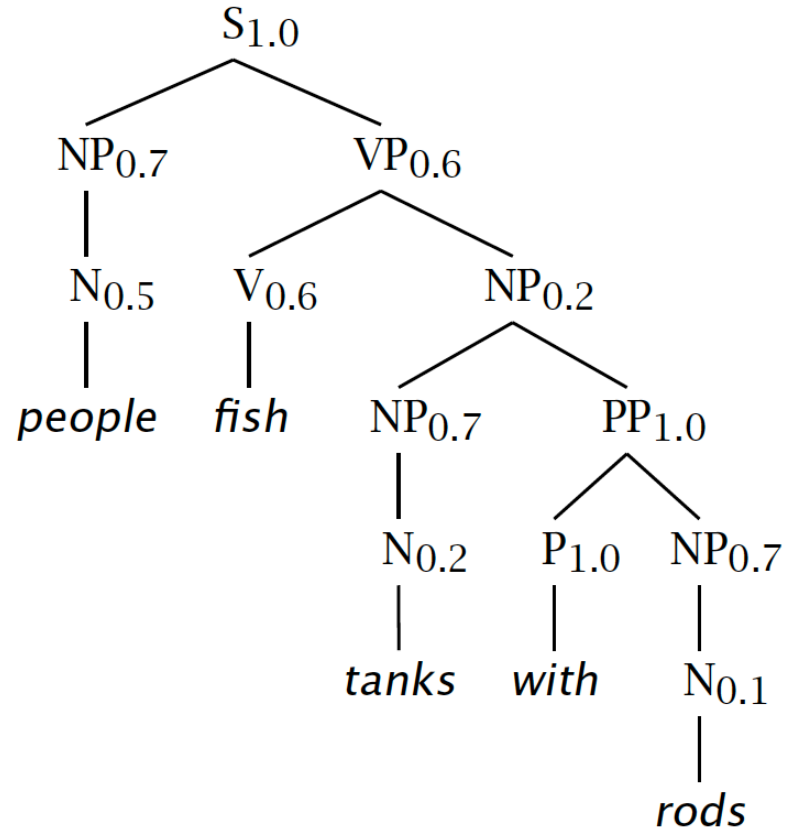
- $P(t)$ – The probability of a tree t is the product of the probabilities of the rules used to generate it.
- $P(s)$ – The probability of the string s is the sum of the probabilities of the trees which have that string as their yield

$$\begin{aligned} P(s) &= \sum_t P(s, t) \text{ where } t \text{ is a parse of } s \\ &= \sum_t P(t) \end{aligned}$$

t_1 :



t_2 :



Tree and String Probabilities

- $s = \textit{people fish tanks with rods}$

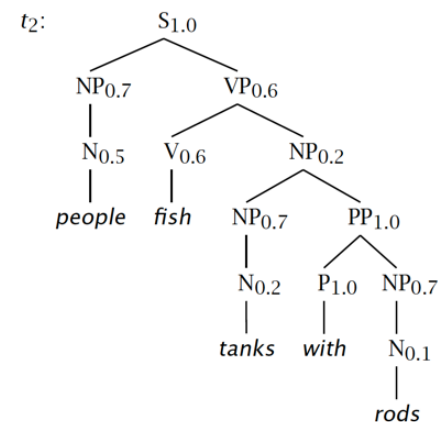
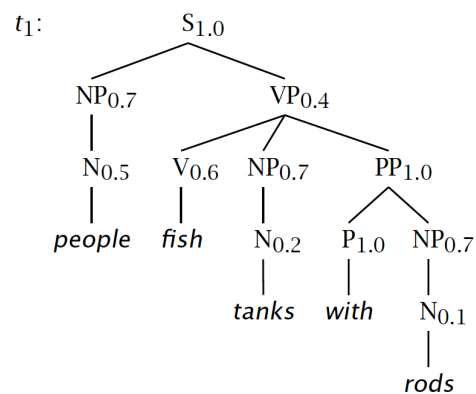
- $P(t_1) = 1.0 \times 0.7 \times 0.4 \times 0.5 \times 0.6 \times 0.7$
 $\times 1.0 \times 0.2 \times 1.0 \times 0.7 \times 0.1$
 $= 0.0008232$

Verb attach

- $P(t_2) = 1.0 \times 0.7 \times 0.6 \times 0.5 \times 0.6 \times 0.2$
 $\times 0.7 \times 1.0 \times 0.2 \times 1.0 \times 0.7 \times 0.1$
 $= 0.00024696$

Noun attach

- $P(s) = P(t_1) + P(t_2)$
 $= 0.0008232 + 0.00024696$
 $= 0.00107016$



Chomsky Normal Form

- All rules are of the form $X \rightarrow YZ$ or $X \rightarrow w$
 - $X, Y, Z \in N$ and $w \in T$
- A transformation to this form doesn't change the generative capacity of a CFG
 - That is, it recognizes the same language
 - But maybe with different trees
- Empties and unaries are removed recursively
- n-ary rules are divided by introducing new nonterminals ($n > 2$)

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$N \rightarrow \textit{people}$

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$N \rightarrow \textit{tanks}$

$N \rightarrow \textit{rods}$

$V \rightarrow \textit{people}$

$V \rightarrow \textit{fish}$

$V \rightarrow \textit{tanks}$

$P \rightarrow \textit{with}$

Chomsky Normal Form steps

$S \rightarrow NP VP$

$S \rightarrow VP$

$VP \rightarrow V NP$

$VP \rightarrow V$

$VP \rightarrow V NP PP$

$VP \rightarrow V PP$

$NP \rightarrow NP NP$

$NP \rightarrow NP$

$NP \rightarrow NP PP$

$NP \rightarrow PP$

$NP \rightarrow N$

$PP \rightarrow P NP$

$PP \rightarrow P$

$N \rightarrow \textit{people}$

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Chomsky Normal Form steps

$S \rightarrow NP VP$

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$VP \rightarrow V$

$S \rightarrow V$

$VP \rightarrow V NP PP$

$S \rightarrow V NP PP$

$VP \rightarrow V PP$

$S \rightarrow V PP$

$NP \rightarrow NP NP$

$NP \rightarrow NP$

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$NP \rightarrow PP$

$NP \rightarrow N$

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Chomsky Normal Form steps

$S \rightarrow NP VP$

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$S \rightarrow V PP$

$NP \rightarrow NP NP$

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$NP \rightarrow NP PP$

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$V \rightarrow \textit{people}$

$S \rightarrow \textit{people}$

$V \rightarrow \textit{fish}$

$S \rightarrow \textit{fish}$

$V \rightarrow \textit{tanks}$

$S \rightarrow \textit{tanks}$

$P \rightarrow \textit{with}$

Chomsky Normal Form steps

$S \rightarrow NP VP$

$VP \rightarrow V NP$

$S \rightarrow V NP$

$VP \rightarrow V NP PP$

$S \rightarrow V NP PP$

$VP \rightarrow V PP$

$S \rightarrow V PP$

$NP \rightarrow NP NP$

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Chomsky Normal Form steps

$S \rightarrow NP VP$

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$S \rightarrow V PP$

$NP \rightarrow NP NP$

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$V \rightarrow \textit{tanks}$

$S \rightarrow \textit{tanks}$

$VP \rightarrow \textit{tanks}$

$P \rightarrow \textit{with}$

$PP \rightarrow \textit{with}$

Chomsky Normal Form steps

$S \rightarrow NP VP$

$VP \rightarrow V NP$

$S \rightarrow V NP$

$VP \rightarrow V @VP_V$

$@VP_V \rightarrow NP PP$

$S \rightarrow V @S_V$

$@S_V \rightarrow NP PP$

$VP \rightarrow V PP$

$S \rightarrow V PP$

$NP \rightarrow NP NP$

$NP \rightarrow NP PP$

$NP \rightarrow P NP$

$PP \rightarrow P NP$

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$V \rightarrow \textit{tanks}$

$S \rightarrow \textit{tanks}$

$VP \rightarrow \textit{tanks}$

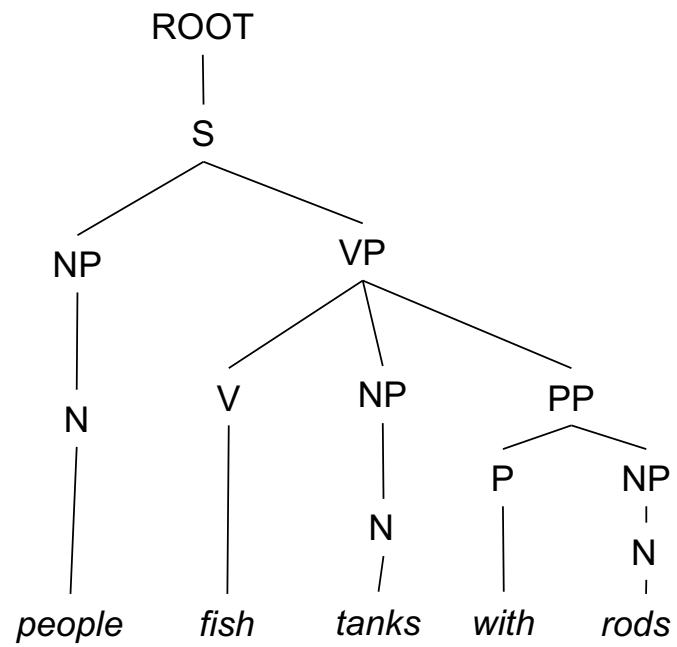
$P \rightarrow \textit{with}$

$PP \rightarrow \textit{with}$

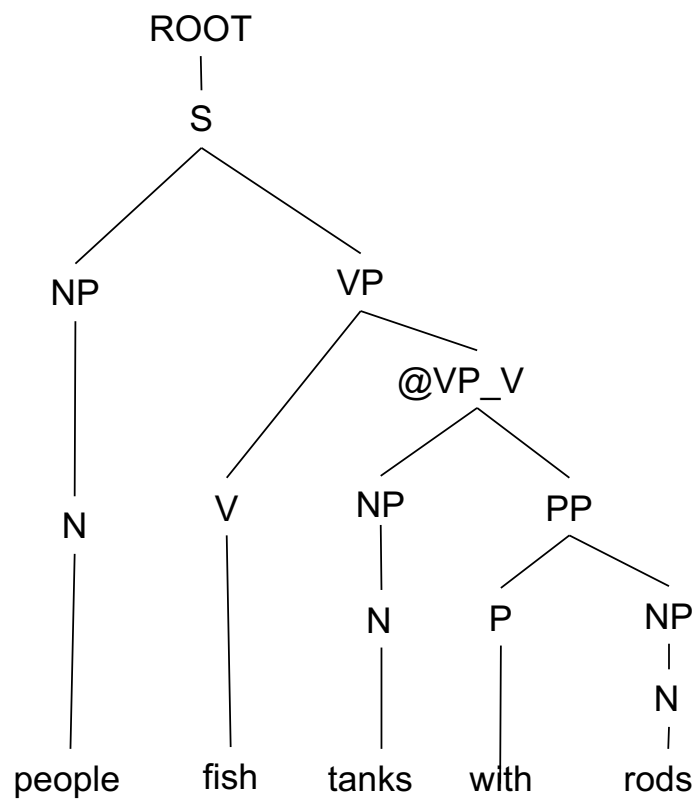
Chomsky Normal Form

- You should think of this as a transformation for efficient parsing
- **Binarization** is crucial for cubic time CFG parsing
- The rest isn't necessary; it just makes the algorithms cleaner and a bit quicker

An example: before binarization...



After binarization on VP

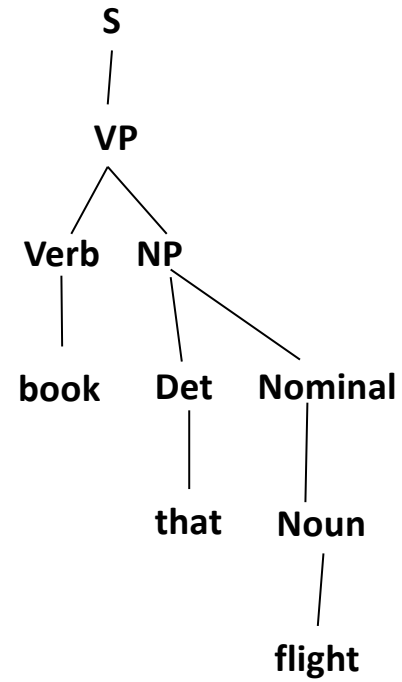


Parsing

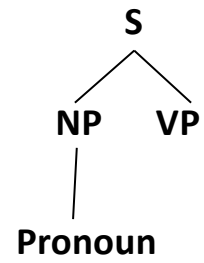
- Given a string of terminals and a CFG, determine if the string can be generated by the CFG.
 - Also return a parse tree for the string
 - Also return all possible parse trees for the string
- Must search space of derivations for one that derives the given string.
 - **Top-Down Parsing**: Start searching space of derivations for the start symbol.
 - **Bottom-up Parsing**: Start search space of reverse derivations from the terminal symbols in the string.

Parsing Example

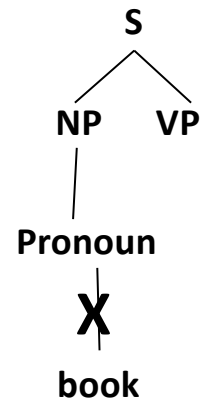
book that flight



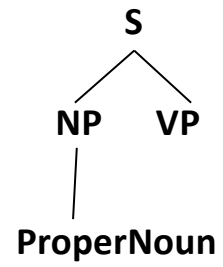
Top Down Parsing



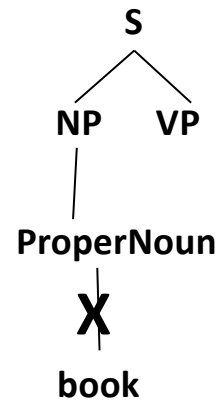
Top Down Parsing



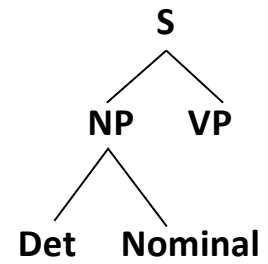
Top Down Parsing



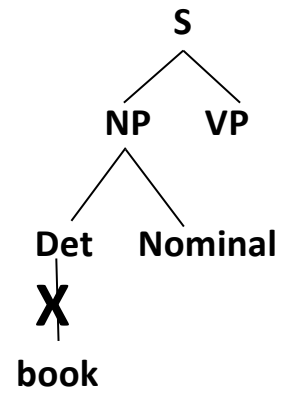
Top Down Parsing



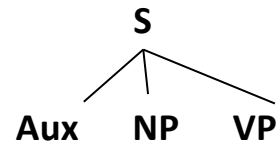
Top Down Parsing



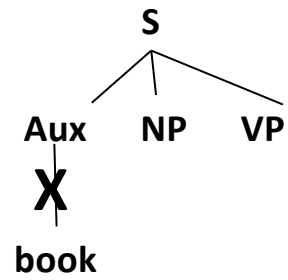
Top Down Parsing



Top Down Parsing



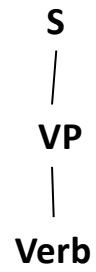
Top Down Parsing



Top Down Parsing

S
|
VP

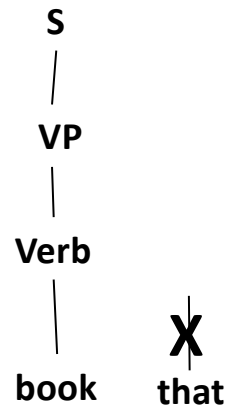
Top Down Parsing



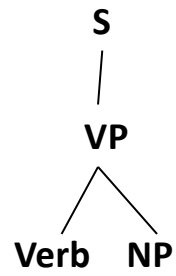
Top Down Parsing



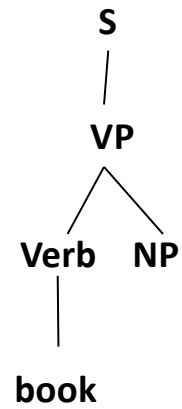
Top Down Parsing



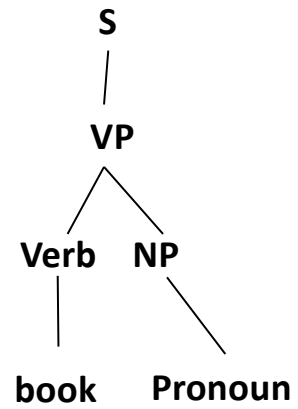
Top Down Parsing



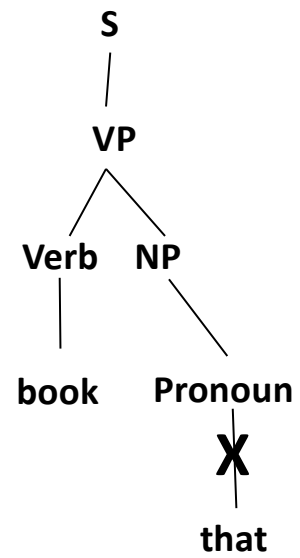
Top Down Parsing



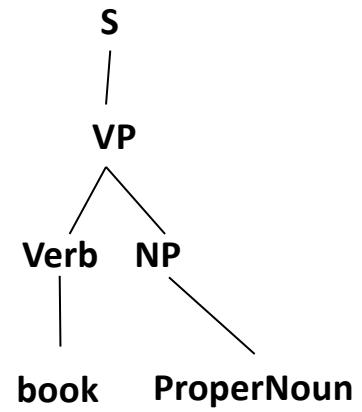
Top Down Parsing



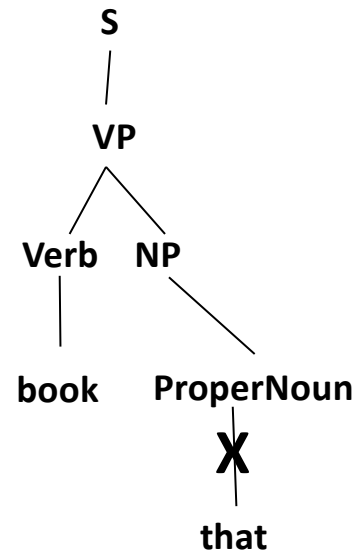
Top Down Parsing



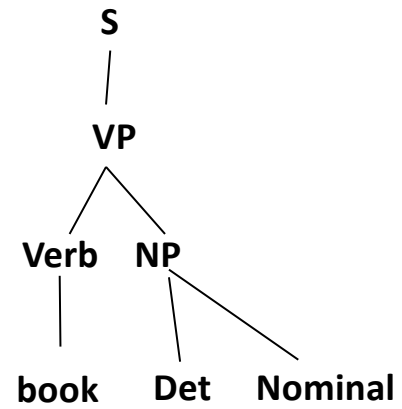
Top Down Parsing



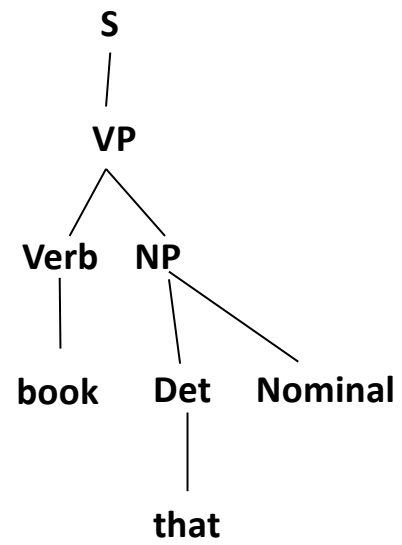
Top Down Parsing



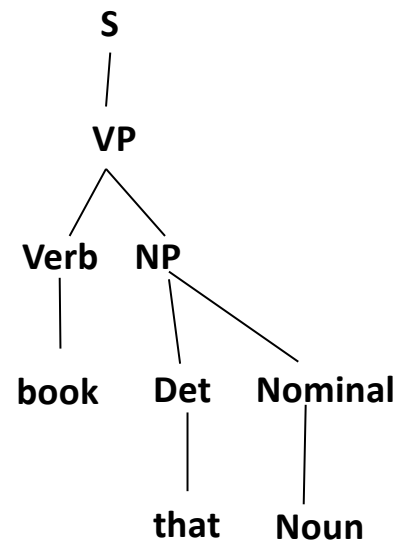
Top Down Parsing



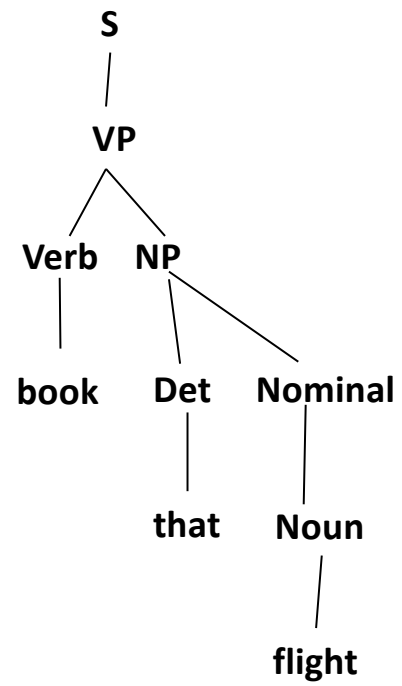
Top Down Parsing



Top Down Parsing



Top Down Parsing



Bottom Up Parsing

book that flight

Bottom Up Parsing

Noun
|
book **that** **flight**

Bottom Up Parsing

Nominal



Noun

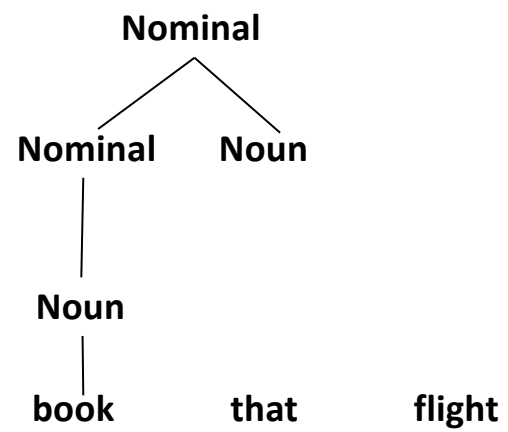


book

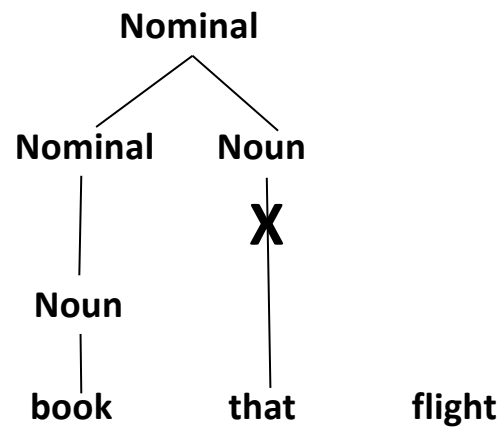
that

flight

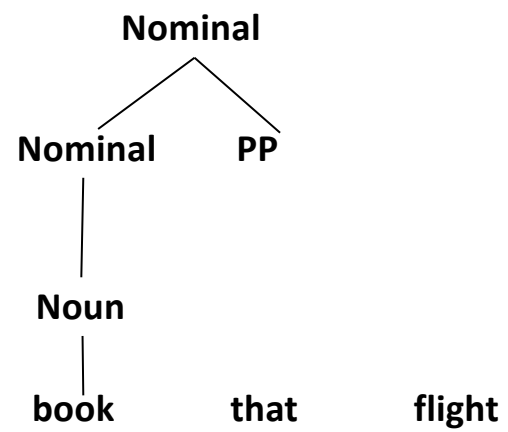
Bottom Up Parsing



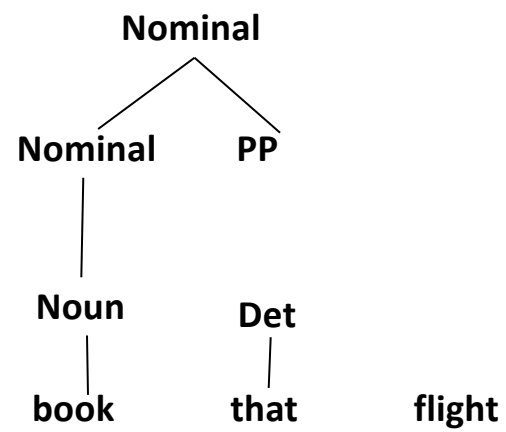
Bottom Up Parsing



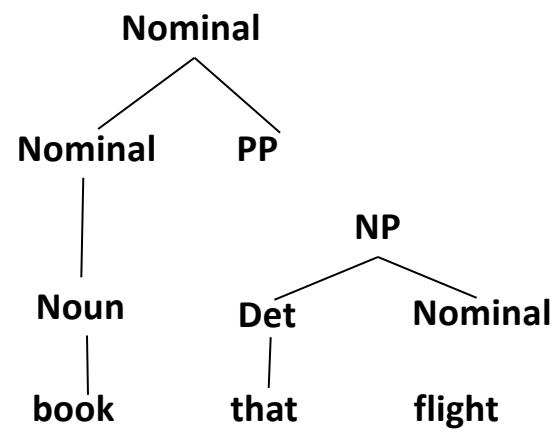
Bottom Up Parsing



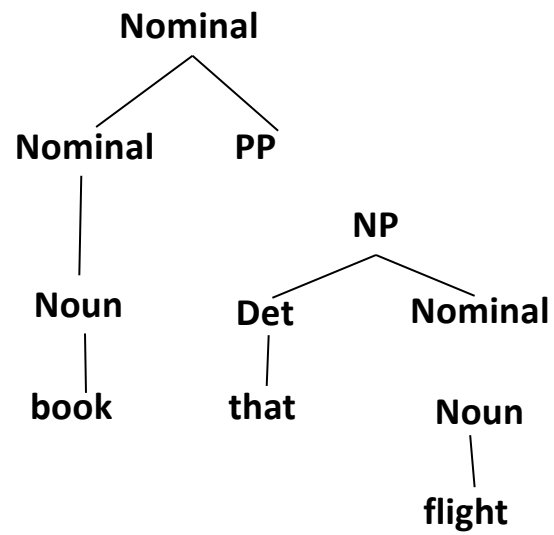
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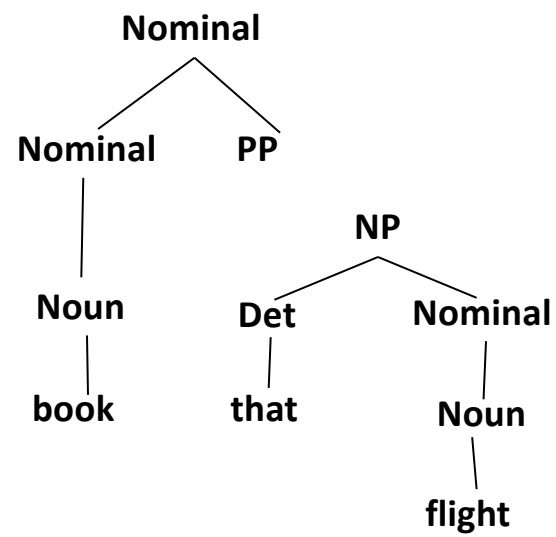
Bottom Up Parsing



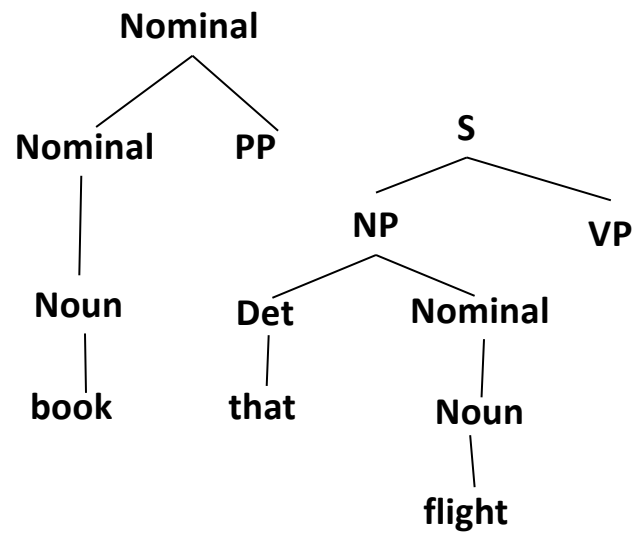
Bottom Up Parsing



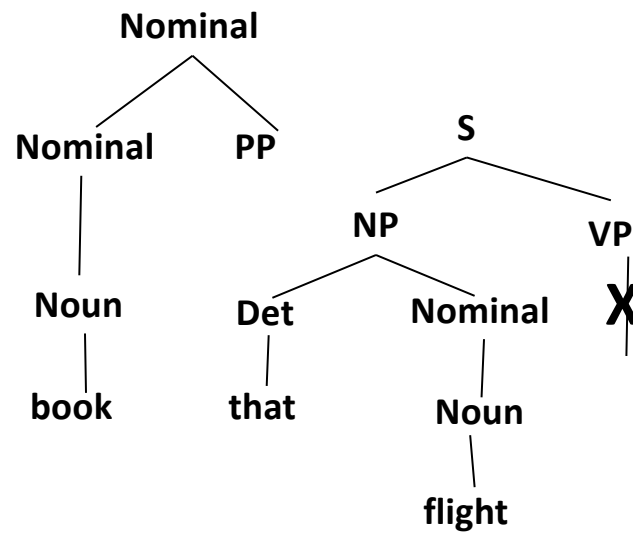
Bottom Up Parsing



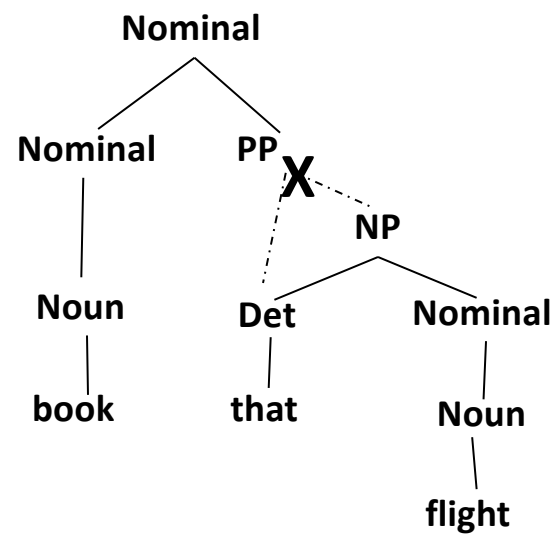
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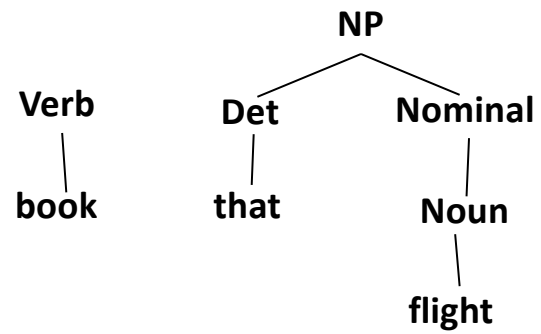
Bottom Up Parsing



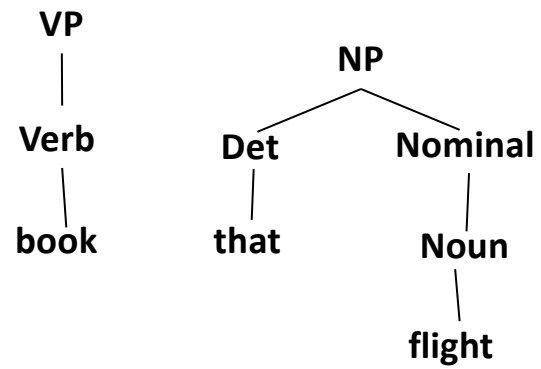
Bottom Up Parsing



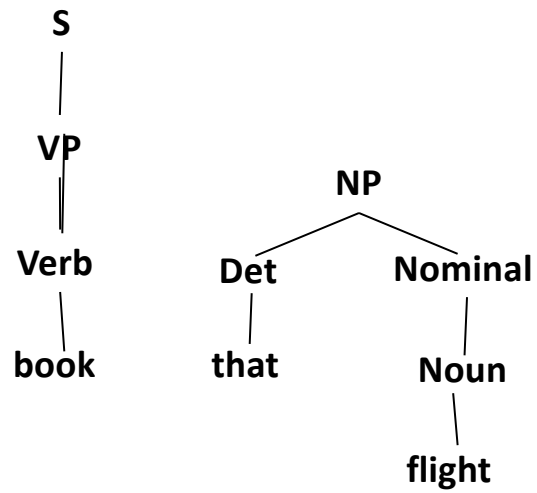
Bottom Up Parsing



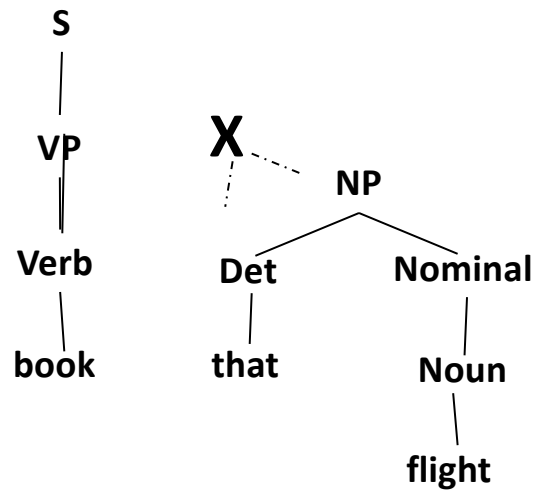
Bottom Up Parsing



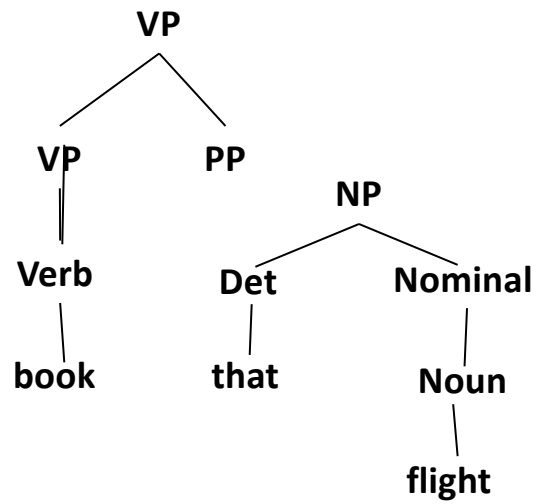
Bottom Up Parsing



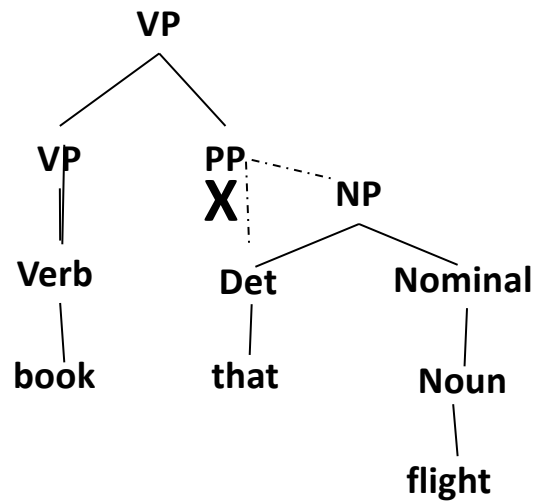
Bottom Up Parsing



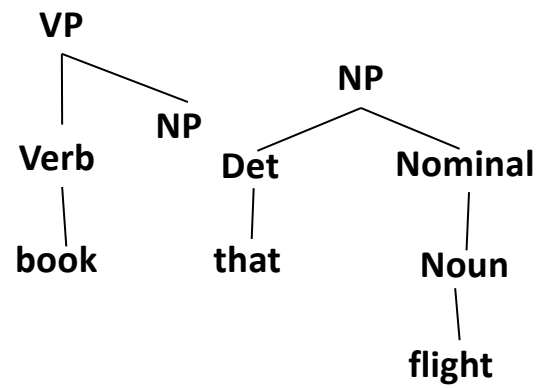
Bottom Up Parsing



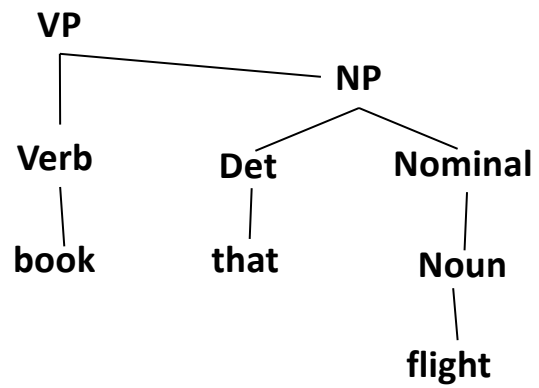
Bottom Up Parsing



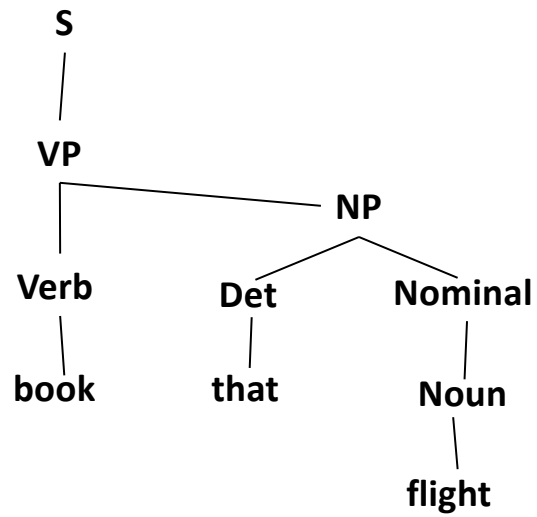
Bottom Up Parsing



Bottom Up Parsing



Bottom Up Parsing



Top Down vs. Bottom Up

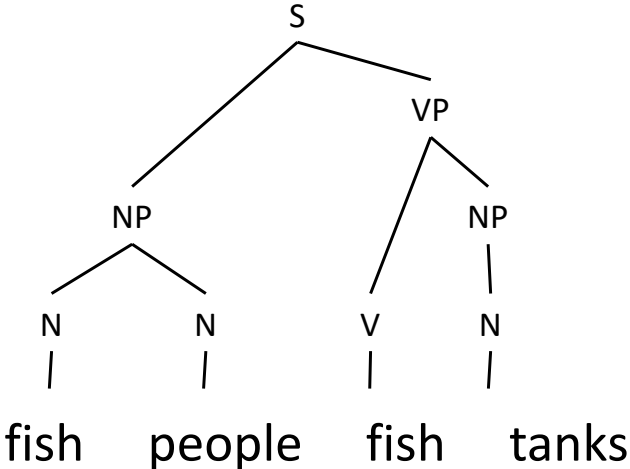
- Top down never explores options that will not lead to a full parse, but can explore many options that never connect to the actual sentence.
- Bottom up never explores options that do not connect to the actual sentence but can explore options that can never lead to a full parse.
- Relative amounts of wasted search depend on how much the grammar branches in each direction.

Dynamic Programming Parsing

- To avoid extensive repeated work, must cache intermediate results, i.e. completed phrases.
- Caching (memorizing) is critical to obtaining a polynomial time parsing (recognition) algorithm for CFGs.
- Dynamic programming algorithms based on both top-down and bottom-up search can achieve $O(n^3)$ time where n is the length of the input string.

(Probabilistic) CKY Parsing

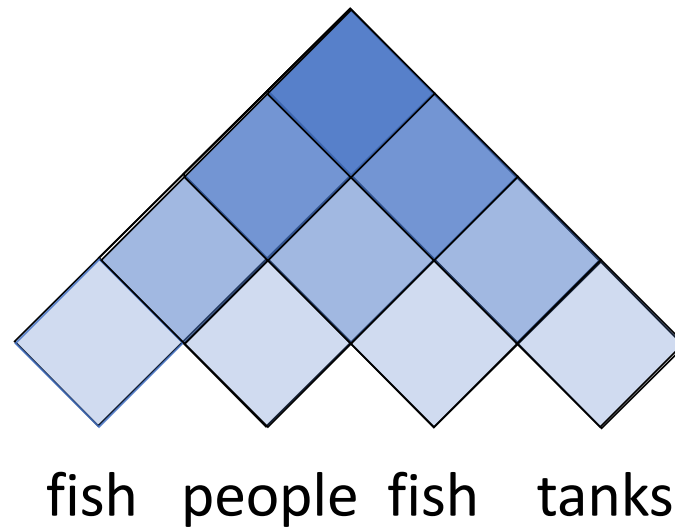
Constituency Parsing



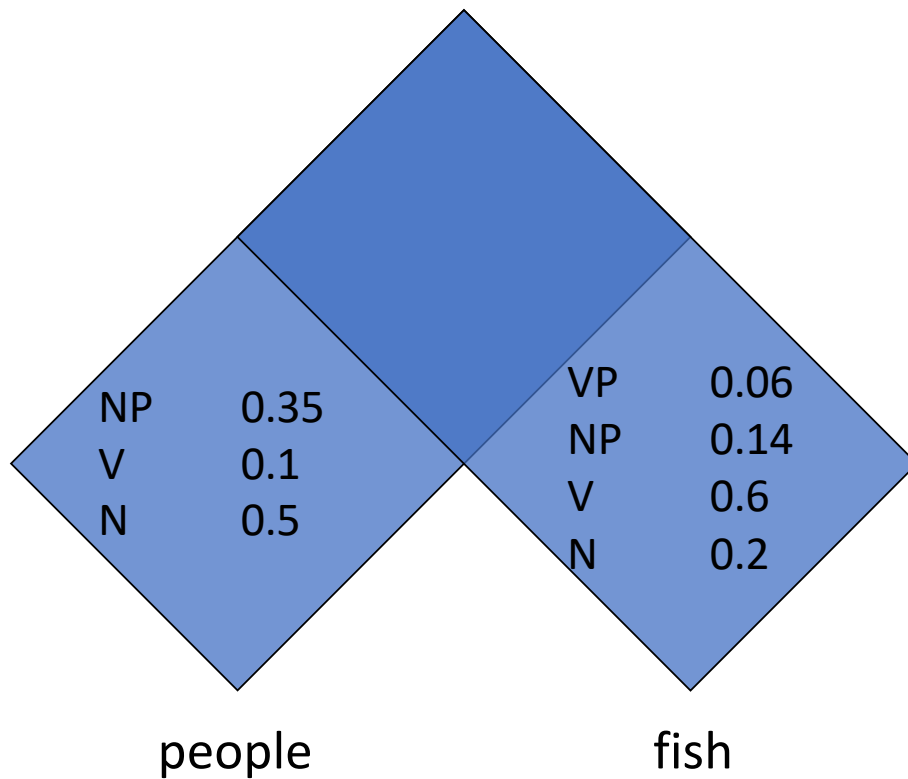
PCFG

Rule	Prob θ_i
$S \rightarrow NP VP$	θ_0
$NP \rightarrow NP NP$	θ_1
...	
$N \rightarrow fish$	θ_{42}
$N \rightarrow people$	θ_{43}
$V \rightarrow fish$	θ_{44}
...	

Cocke-Kasami-Younger (CKY) Constituency Parsing



Viterbi (Max) Scores



$S \rightarrow NP VP$	0.9
$S \rightarrow VP$	0.1
$VP \rightarrow V NP$	0.5
$VP \rightarrow V$	0.1
$VP \rightarrow V @VP_V$	0.3
$VP \rightarrow V PP$	0.1
$@VP_V \rightarrow NP PP$	1.0
$NP \rightarrow NP NP$	0.1
$NP \rightarrow NP PP$	0.2
$NP \rightarrow N$	0.7
$PP \rightarrow P NP$	1.0

Extended CKY parsing

- Unaries can be incorporated into the algorithm
 - Messy, but doesn't increase algorithmic complexity
- Empties can be incorporated
 - Doesn't increase complexity; essentially like unaries
- Binarization is *vital*
 - Without binarization, you don't get parsing cubic in the length of the sentence and in the number of nonterminals in the grammar

The CKY algorithm (1960/1965) ... extended to unaries

```
function CKY(words, grammar) returns [most_probable_parse, prob]
  score = new double[#(words)+1][#(words)+1][#(nonterms)]
  back = new Pair[#(words)+1][#(words)+1][#(nonterms)]
  for i=0; i<#(words); i++
    for A in nonterms
      if A -> words[i] in grammar
        score[i][i+1][A] = P(A -> words[i])
  //handle unaries
  boolean added = true
  while added
    added = false
    for A, B in nonterms
      if score[i][i+1][B] > 0 && A->B in grammar
        prob = P(A->B)*score[i][i+1][B]
        if prob > score[i][i+1][A]
          score[i][i+1][A] = prob
          back[i][i+1][A] = B
          added = true
```

The CKY algorithm (1960/1965)

... extended to unaries

```
for span = 2 to #(words)
  for begin = 0 to #(words)- span
    end = begin + span
    for split = begin+1 to end-1
      for A,B,C in nonterms
        prob=score[begin][split][B]*score[split][end][C]*P(A->BC)
        if prob > score[begin][end][A]
          score[begin][end][A] = prob
          back[begin][end][A] = new Triple(split,B,C)
      //handle unaries
      boolean added = true
      while added
        added = false
        for A, B in nonterms
          prob = P(A->B)*score[begin][end][B];
          if prob > score[begin][end][A]
            score[begin][end][A] = prob
            back[begin][end][A] = B
            added = true
    return buildTree(score, back)
```