

$$\#1 = t$$

$$\#2 = t \frac{(1 + \sqrt{2})}{3}$$

$$\#3 = \frac{t\sqrt{5}}{3}$$

When I'm walking,
I worry a lot
about the efficiency
of my path.

Local Optimizations

One-Slide Summary

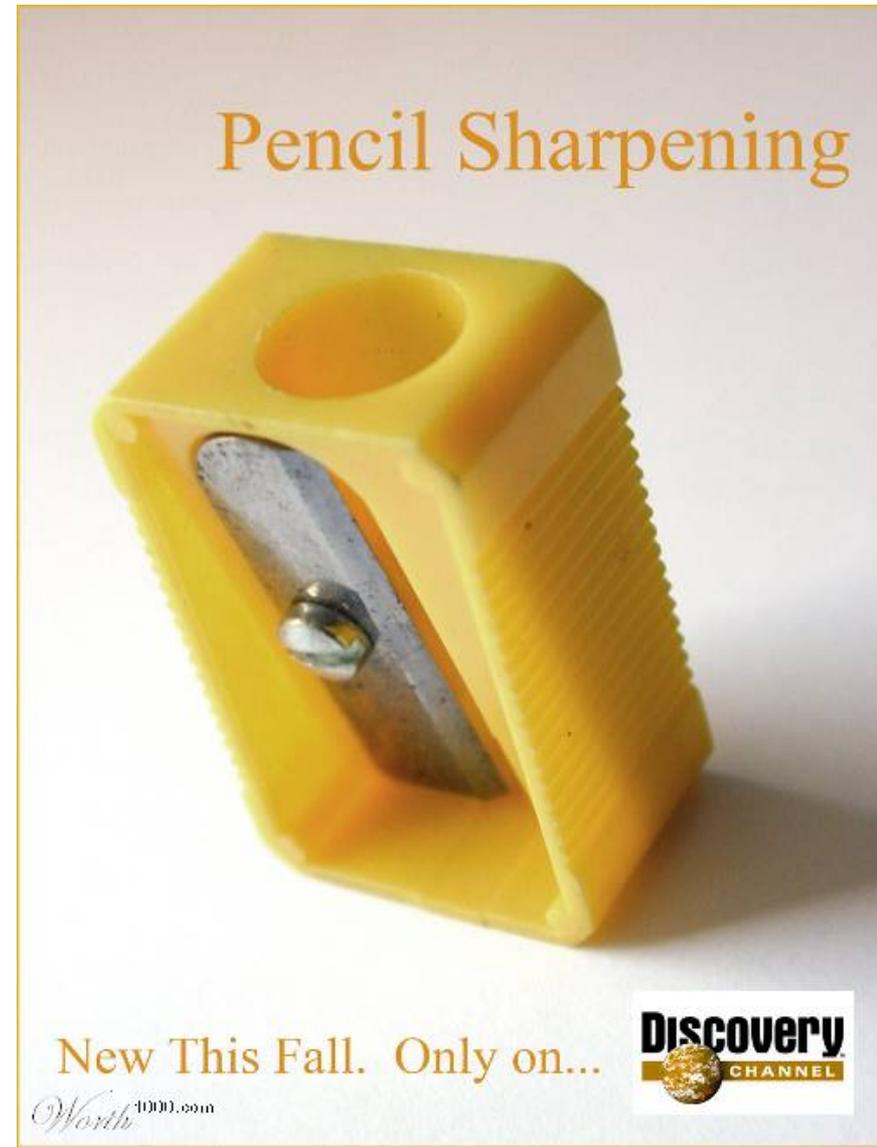
- An **optimization** changes a program so that it computes the **same answer** in **less time** (or using less of some other resource).
- We represent the program using a special **intermediate form**.
- Each method is viewed as a **control flow graph** where the nodes are **basic blocks** of instructions with **known entry** and **exit** points. The instructions have been changed so that a **single assignment** defines each variable.

Upcoming Events

- This Friday, 4pm, 228E/236D
 - “Halloween Fall Festival”. Prizes for best costumes, trick-or-treats provided, bring an artistic dish if you like, apple dunking, music?
- **Postponed!**
 - Barbara Liskov lectures, www.liskovatuva.com
- Wednesday Nov 18, evening
 - Fireside chat with Kim “Reality TV” Hazelwood and Wes “Romance Novel” Weimer
- ???
 - The final for this class. Vote.

Lecture Outline

- Intermediate code
- Local optimizations
- Next time: larger-scale program analyses



Why Optimize?

- What's the point?
- Do we care about this in real life?



When To Optimize?

- When to perform optimizations
 - On AST (just like type checking)
 - **Pro**: Machine independent
 - **Cons**: Too high level
 - On assembly language (compilers only)
 - **Pro**: Exposes optimization opportunities
 - **Cons**: Machine dependent
 - **Cons**: Must reimplement optimizations when retargetting
 - On an intermediate language
 - **Pro**: Machine independent
 - **Pro**: Exposes optimization opportunities
 - **Cons**: One more language to worry about

Intermediate Languages

- Each compiler uses its own **intermediate language**
 - IL design is still an active area of research
- Intermediate language = high-level assembly language
 - Uses register names, but has an unlimited number
 - Uses control structures like assembly language
 - Uses opcodes but some are higher level
 - e.g., **push** translates to several assembly instructions
 - Most opcodes correspond directly to assembly opcodes

Three-Address Intermediate Code

- Each instruction is of the form

$$x := y \text{ op } z$$

- y and z can be only registers, variables or constants
- Common form of intermediate code
- The AST expression $x + y * z$ is translated as

$$t_1 := y * z$$

$$t_2 := x + t_1$$

- Each **subexpression** lives in a temporary

Generating Intermediate Code

- $\text{igen}(e, t)$ function generates code to compute the value of e in register t

- Example:

$\text{igen}(e_1 + e_2, t) =$

$\text{igen}(e_1, t_1)$ *(t_1 is a fresh register)*

$\text{igen}(e_2, t_2)$ *(t_2 is a fresh register)*

$t := t_1 + t_2$

- Unlimited number of registers
 \Rightarrow simple code generation

An Intermediate Language

$P \rightarrow S P \mid \epsilon$

$S \rightarrow id := id \ op \ id$

| $id := op \ id$

| $id := id$

| $push \ id$

| $id := pop$

| $if \ id \ relop \ id \ goto \ L$

| $L:$

| $jump \ L$

- id 's are register names
- Constants can replace id 's
- Typical operators: +, -, *

Basic Blocks

- A **basic block** is a *maximal* sequence of instructions with:
 - no labels (except at the first instruction), and
 - no jumps (except in the last instruction)
- Idea:
 - Cannot jump into a basic block (*except* at beginning)
 - Cannot jump out of a basic block (*except* at end)
 - Each instruction in a basic block is executed after all the preceding instructions have been executed

Basic Block Example

- Consider the basic block
 1. L1:
 2. $t := 2 * x$
 3. $w := t + x$
 4. if $w > 0$ goto L2
- No way for (3) to be executed without (2) having been executed right before

Basic Block Example

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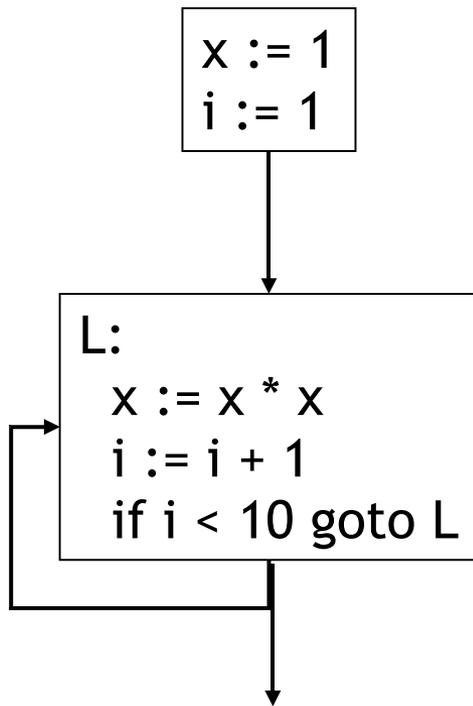
Basic Block Example

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 - We can change (3) to $w := 3 * x$
 - Can we eliminate (2) as well?

Control-Flow Graphs

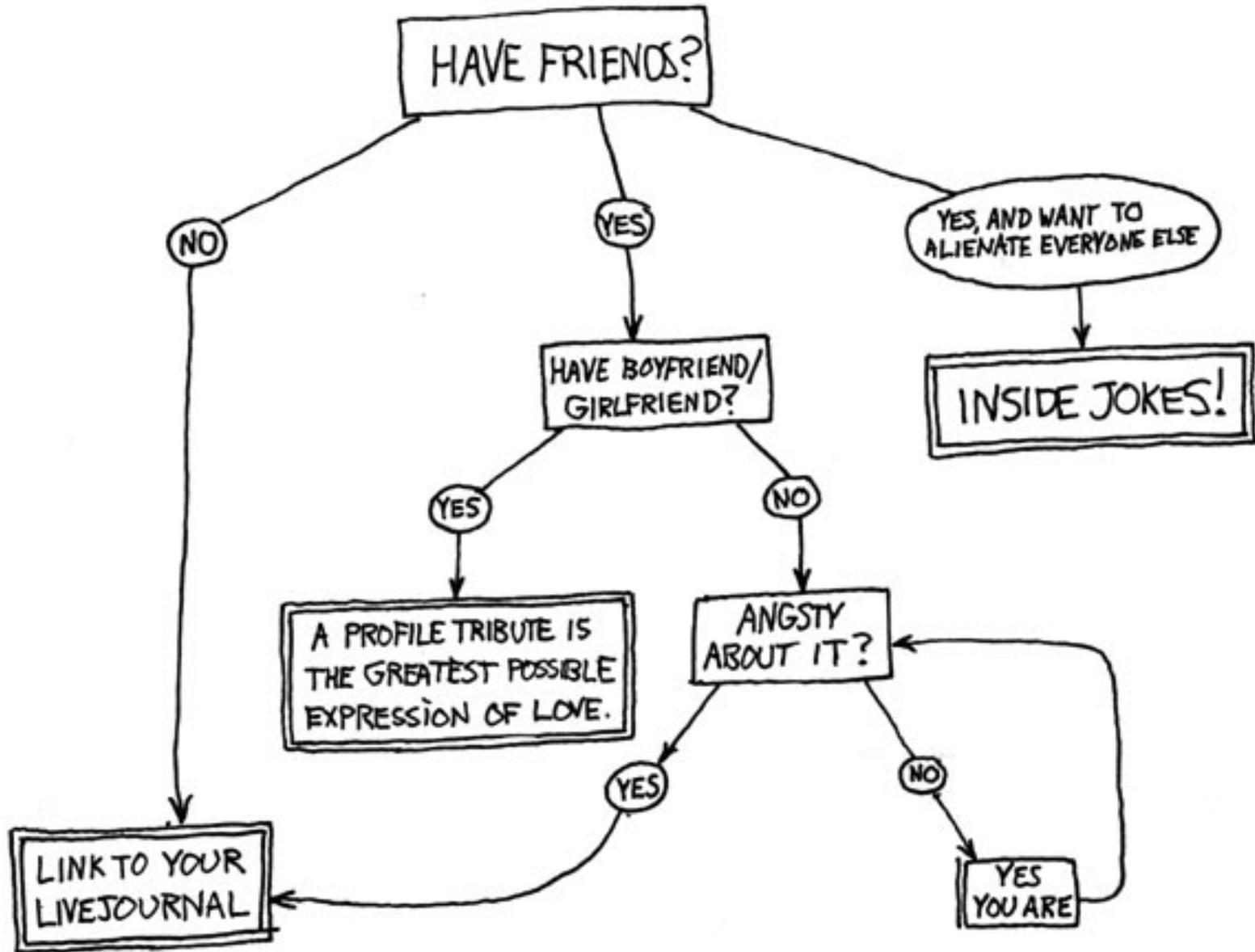
- A **control-flow graph** is a directed graph:
 - Basic blocks as **nodes**
 - An **edge** from block A to block B if the execution can flow from the last instruction in A to the first instruction in B
 - e.g., the last instruction in A is **jump L_B**
 - e.g., the execution can fall-through from block A to block B
- Frequently abbreviated as **CFG**

Control-Flow Graphs. Example.



- The body of a method (or procedure) can be represented as a control-flow graph
- There is one initial node
 - The “start node”
- All “return” nodes are terminal

CREATING AN AIM PROFILE:



CFG
≈
Flow
Chart

Optimization Overview

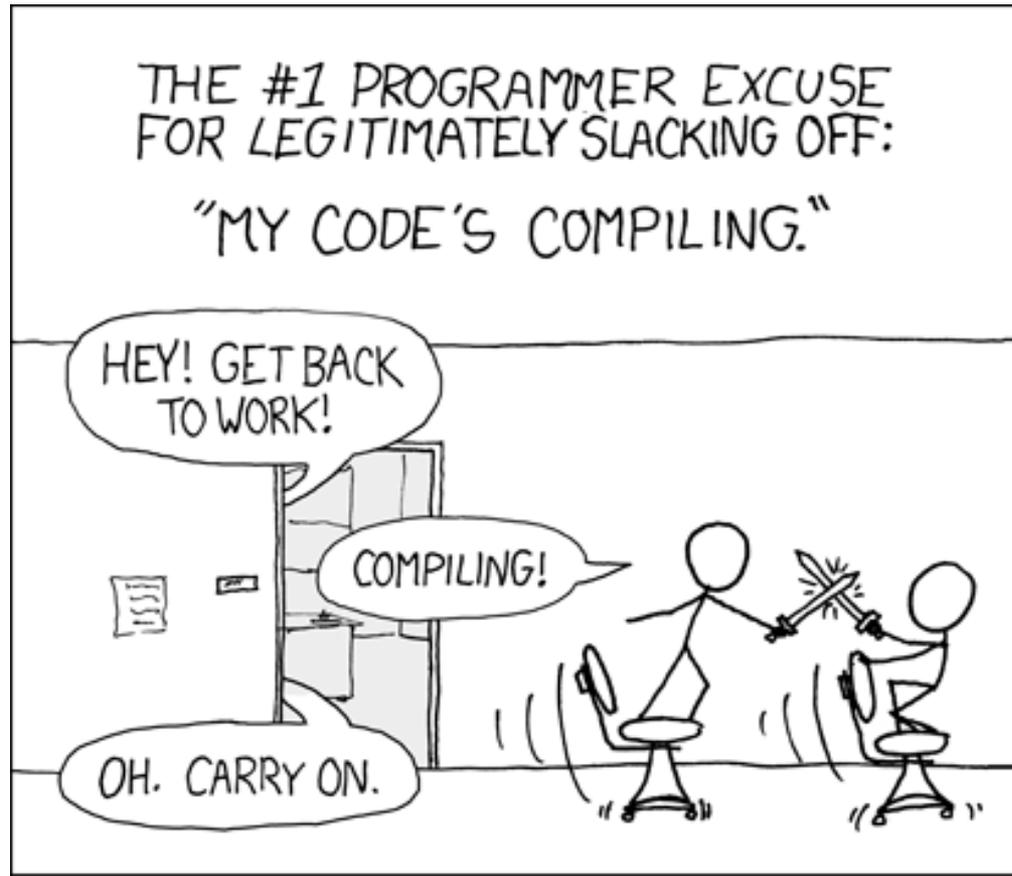
- **Optimization** seeks to improve a program's utilization of some resource
 - Execution time (most often)
 - Code size
 - Network messages sent
 - Battery power used, etc.
- Optimization should *not* alter what the program computes
 - The answer must still be the same
 - **First Rule of Optimization Club: Don't Break The Build**

A Classification of Optimizations

- For languages like C and Cool there are three granularities of optimizations
 1. **Local optimizations**
 - Apply to a basic block in isolation
 2. **Global optimizations**
 - Apply to a control-flow graph (method body) in isolation
 3. **Inter-procedural optimizations**
 - Apply across method boundaries
- Most **compilers** do (1), many do (2) and very few do (3)
- Some **interpreters** do (1), few do (2), basically none do (3)

Cost of Optimizations

- In practice, a conscious decision is made *not* to implement the fanciest optimization known
- Why?



Cost of Optimizations

- In practice, a conscious decision is made *not* to implement the fanciest optimization known
- Why?
 - Some optimizations are hard to implement
 - Some optimizations are costly in terms of compilation/interpretation time
 - The fancy optimizations are both hard and costly
- The goal: maximum improvement with minimum of cost

Q: Movies (363 / 842)

- This 1993 comedy film also starring Andie MacDowell "begins" with the following radio banter: *"Rise and shine, campers, and don't forget your booties 'cause it's coooooold out there today. / It's cold out there every day. What is this, Miami Beach? / Not hardly. So the big question on everybody's lips / -- On their chapped lips -- / their chapped lips is, does Phil feel lucky?"*

Q: Books (763 / 842)

- This 18th- and 19th-century English poet, painter and religious printmaker believed in racial and sexual equality and rejected imposed secular authority. Peter Marshall described him as, "a revolutionary anarchist, [...] anticipating modern anarchism and social ecology. With William Godwin, he stands as a great forerunner of British Anarchism". His poem **Night** includes: "*The sun descending in the west, / The evening star does shine; / The birds are silent in their nest. / And I must seek for mine.*"

Q: Cartoons (674 / 842)

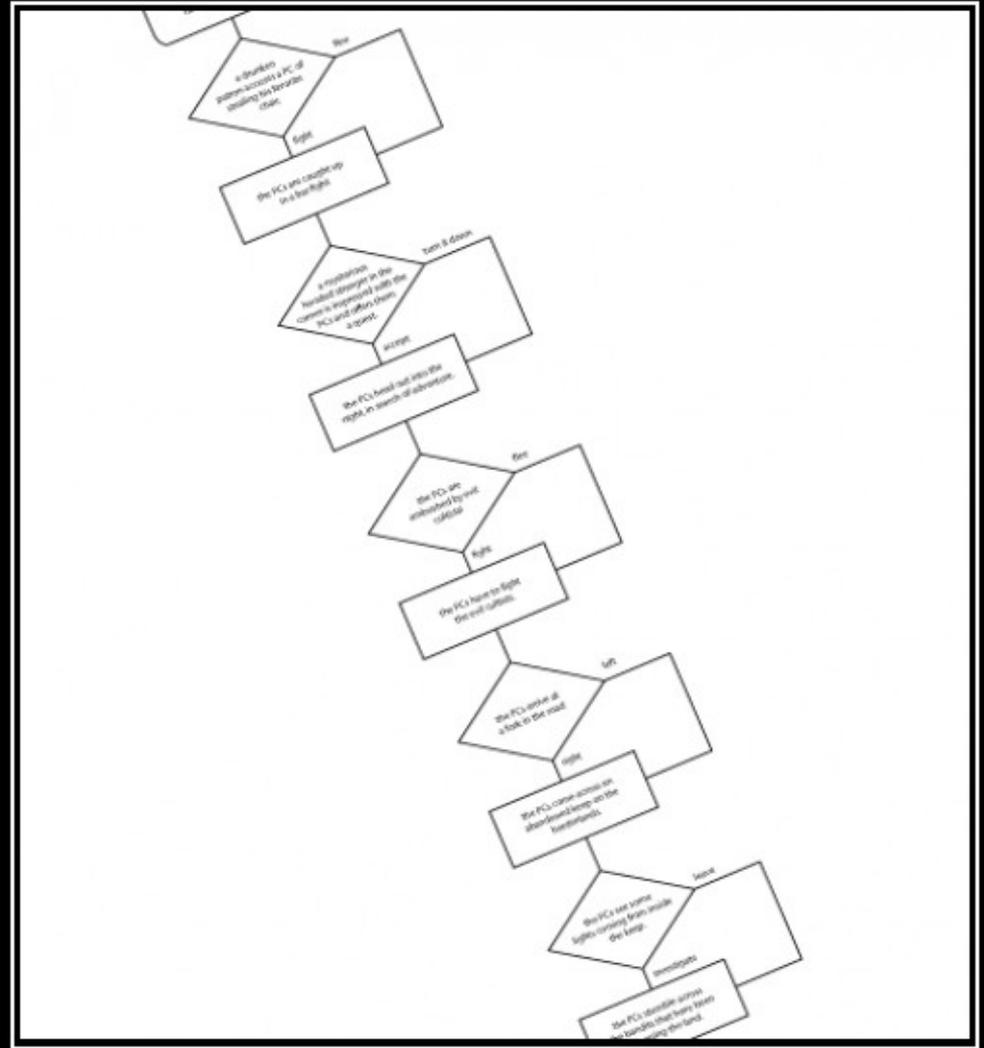
- This 1953 Warner Brothers' cartoon mouse is known for his cry of "*Arriba! Arriba! Andele!*"

Q: Books (764 / 842)

- Name the 1957 novel and the controlling protagonist associated with one of the following three companies: **Taggart Transcontinental, Rearden Steel and d'Anconia Copper.**

CFG

- This CFG stuff sounds complicated ...
- Can't we skip it for now?



ILLUSIONISM

Always give the players a choice as long as it's your choice.

Local Optimizations

- The simplest form of optimizations
- No need to analyze the whole procedure body
 - Just the basic block in question
- Example:
 - algebraic simplification
 - constant folding
 - Python 2.5+ does stuff like this if you say “-0”

Algebraic Simplification

- Some statements can be deleted

$x := x + 0$

$x := x * 1$

- Some statements can be simplified

$x := x * 0 \quad \Rightarrow \quad x := 0$

$y := y ** 2 \quad \Rightarrow \quad y := y * y$

$x := x * 8 \quad \Rightarrow \quad x := x \ll 3$

$x := x * 15 \quad \Rightarrow \quad t := x \ll 4; x := t - x$

(on some machines \ll is faster than $*$; but not on all!)

Constant Folding

- Operations on constants can be computed before the code executes
- In general, if there is a statement
$$x := y \text{ op } z$$
 - And y and z are **constants**
 - Then $y \text{ op } z$ can be computed early
- Example: $x := 2 + 2 \Rightarrow x := 4$
- Example: $\text{if } 2 < 0 \text{ jump } L$ can be deleted
- When might **constant folding** be dangerous?

Flow of Control Optimizations

- Eliminating **unreachable code**:
 - Code that is unreachable in the control-flow graph
 - Basic blocks that are not the target of any jump or “fall through” from a conditional
 - Such basic blocks can be eliminated
- Why would such basic blocks occur?
- Removing unreachable code makes the program smaller
 - And sometimes also faster
 - Due to memory cache effects (increased spatial locality)

Single Assignment Form

- Most optimizations are simplified if each assignment is to a temporary that *has not appeared already* in the basic block
- Intermediate code can be rewritten to be in **single assignment form**

$x := a + y$

$a := x$

$x := a * x$

$b := x + a$

\Rightarrow

$x := a + y$

$a_1 := x$

$x_1 := a_1 * x$

$b := x_1 + a_1$

(x_1 and a_1 are fresh temporaries)

Single Assignment vs. Functional Programming

- In **functional programming** variable values do not change
- Instead you make a new variable with a similar name
- Single assignment form is just like that!

$x := a + y$

$\text{let } x = a + y \text{ in}$

$a_1 := x$

\simeq

$\text{let } a_1 = x \text{ in}$

$x_1 := a_1 * x$

$\text{let } x_1 = a_1 * x \text{ in}$

$b := x_1 + a_1$

$\text{let } b = x_1 + a_1 \text{ in}$

Common Subexpression Elimination

- Assume:
 - Basic block is in single assignment form
- Then all assignments with same right-hand side compute the same value (*why?*)

- Example:

$x := y + z$

...

$w := y + z$

\Rightarrow

$x := y + z$

...

$w := x$

- Why is single assignment important here?

Copy Propagation

- If $w := x$ appears in a block, all subsequent uses of w can be replaced with uses of x

- Example:

$b := z + y$		$b := z + y$
$a := b$	\Rightarrow	$a := b$
$x := 2 * a$		$x := 2 * b$

- This does not make the program smaller or faster but might enable other optimizations
 - Constant folding
 - Dead code elimination (we'll see this in a bit!)
- Again, single assignment is important here.

Copy Propagation and Constant Folding

- Example:

a := 5

x := 2 * a

y := x + 6

t := x * y

⇒

a := 5

x := 10

y := 16

t := x << 4

Dead Code Elimination

If

$w := rhs$ appears in a basic block

w does not appear anywhere else in the program

Then

the statement $w := rhs$ is dead and can be eliminated

- **Dead** = does not contribute to the program's result

Example: (a is not used anywhere else)

$x := z + y$		$b := z + y$		$b := z + y$
$a := x$	\Rightarrow	$a := b$	\Rightarrow	$x := 2 * b$
$x := 2 * a$		$x := 2 * b$		

Applying Local Optimizations

- Each local optimization does very little by itself
- Typically optimizations *interact*
 - Performing one optimizations enables other opts
- Typical optimizing compilers repeatedly perform optimizations until no improvement is possible
- Interpreters and JITs must be fast!
 - The optimizer can also be stopped at any time to limit the compilation time

An Example

- Initial code:

a := x ** 2

b := 3

c := x

d := c * c

e := b * 2

f := a + d

g := e * f

An Example

- Algebraic optimization:

a := x ** 2

b := 3

c := x

d := c * c

e := b * 2

f := a + d

g := e * f

An Example

- Algebraic optimization:

a := x * x

b := 3

c := x

d := c * c

e := b + b

f := a + d

g := e * f

An Example

- Copy propagation:

a := x * x

b := 3

c := x

d := c * c

e := b + b

f := a + d

g := e * f

An Example

- Copy propagation:

a := x * x

b := 3

c := x

d := x * x

e := 3 + 3

f := a + d

g := e * f

An Example

- Constant folding:

a := x * x

b := 3

c := x

d := x * x

e := 3 + 3

f := a + d

g := e * f

An Example

- Constant folding:

a := x * x

b := 3

c := x

d := x * x

e := 6

f := a + d

g := e * f

An Example

- Common subexpression elimination:

a := x * x

b := 3

c := x

d := x * x

e := 6

f := a + d

g := e * f

An Example

- Common subexpression elimination:

a := x * x

b := 3

c := x

d := a

e := 6

f := a + d

g := e * f

An Example

- Copy propagation:

a := x * x

b := 3

c := x

d := a

e := 6

f := a + d

g := e * f

An Example

- Copy propagation:

a := x * x

b := 3

c := x

d := a

e := 6

f := a + a

g := 6 * f

An Example

- Dead code elimination:

a := x * x

b := 3

c := x

d := a

e := 6

f := a + a

g := 6 * f

An Example

- Dead code elimination:

$a := x * x$



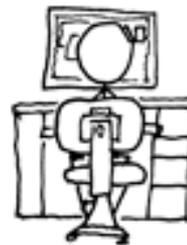
$f := a + a$

$g := 6 * f$

- This is the final form
 - Could we get to $g = 12 * a$?

Cool and Intermediate Form

- Cool does not have **goto**
- Cool does not have **break**
- Cool does not have **exceptions**
- How would you make basic blocks from a Cool AST?



Local Optimization Notes

- Intermediate code is helpful for many optimizations
 - Basic Blocks: known entry and exit
 - Single Assignment: one definition per variable
- “Program optimization” is grossly misnamed
 - Code produced by “optimizers” is not optimal in any reasonable sense
 - “Program improvement” is a more appropriate term
- Next: larger-scale program changes

Homework

- WA5 due today
- WA6 due next Thursday
- Start PA5!
- Reading for next time (basic blocks, etc.)
- **Midterm 2** - Tuesday Nov 24 (26 days)