



<ul> <li>Hierarchies</li> <li>Designing a class hierarchy is a tricky task</li> <li>More on it in later CS courses (e.g., 205)</li> </ul>	Quiz Wednesday <ul> <li>Short Reading Quiz In Class</li> </ul>
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Liberal Arts Trivia: Physics	Liberal Arts Trivia: Chemistry
<ul> <li>Name the vector quantity in physics measured in radians per second. The direction of the vector is perpendicular to the plane of rotation and is usually specified by the "right hand rule".</li> <li>PATING A RECORD? 11L SHOW YOU SOMETIME EDGE. THEY WE A COMPARE A POINT ON THE RECORDS OUTRE EDGE. THEY WHEN AN OWNER A COMPARE A POINT ON THE RECORDS OUTRE EDGE. THEY WHEN AN OWNER A COMPARE TO THE RECORDS OUTRE EDGE. THEY WHEN A COMPARE TO THE RECORDS OUTRE EDGE. THEY WHEN A COMPARE TO THE RECORDS OUTRE EDGE. THEY WHEN A COMPARE TO THE RECORDS OUTRE EDGE. THEY WHEN A COMPARE TO THE RECORDS OUTRE EDGE. THEY WHEN A COMPARE TO THE RECORDS OUT THE SAME MOUNT ON THE RECORDS OUT THE SAME MOUNT ON THE RECORDS OUT THEY BOTH MAKE A COMPARE TO SPECE. THEY WHEN A COMPARE TO THE RECORDS OUT THEY BOTH MAKE A COMPARE TO THE RECORDS OUT THE RECORDS OUT THE RECORDS OUT THEY BOTH MAKE A COMPARE TO THE RECORDS OUT THEY BOTH MAKE A COMPARE TO SPECE. THEY WHEN A COMPARE TO THE RECORDS OUT THE RECORDS OUT THE RECORDS OUT THEY BOTH MAKE A COMPARE TO THE RECORDS OUT THEY BOTH MAKE A COMPARE TO THE RECORDS OUT THE RECORDS OUT THE RECORDS OUT THEY BOTH MAKE A COMPARE TO THE RECORDS OUT THEY BOTH MAKE A COMPARE TO SPECE. THEY WHEN THE SAME RECOUNT ON THE RECORDS OUT THEY BOTH MAKE A COMPARE TO THE RECORDS OUT THEY BOTH MAKE A COMPARE TO SPECE. THEY WHEN THE SAME RECOUNT ON THE RECORDS OUT THEY BOTH MAKE A COMPARE TO THE RECORDS OUT THEY BOTH MAKE A COMPARE TO SPECE. THEY WHEN THE SAME RECOUNT ON THE RECORDS OUT THEY BOTH MAKE A COMPARE TO THE RECORDS OUT THEY BOTH MAKE A COMPARE TO SPECE. THEY WHEN THE SAME RECOUNT ON THE RECORDS OUT THEY BOTH MAKE A COMPARE TO SPECE. THEY WHEN THE SAME RECOUNT ON THE RECORDS OUT THEY BOTH MAKE A COMPARE TO SPECE. THEY WHEN THE RECORDS OUT THEY BOTH MAKE A COMPARE TO SPECE. THEY WHEN THE RECOUNT THEY BOTH MAKE A COMPARE TO SPECE. THEY WHEN THE RECORDS OUT THEY BOTH MAKE A COMPARE TO SPECE. THEY WHEN THE RECOUNT O</li></ul>	<ul> <li>Give the common name for hydragyrum, a heavy metal element. It is the only element that is liquid at standard temperature and pressure and is often used in the construction of sphygmomanometers. In the 18<sup>th</sup> to 19<sup>th</sup> centuries it was used to make felt hats, and the psychological symptoms associated with its poisoning are sometimes used to explain the phrase "mad as a hatter".</li> <li>Bonus: What does a sphygmomanometer measure?</li> </ul>
<ul> <li>Story So Far</li> <li>Much of the course so far: <ul> <li>Getting comfortable with recursive definitions</li> <li>Learning to write a program to do (almost) anything (PS1-4)</li> <li>Learning more elegant ways of programming (PS5-6)</li> </ul> </li> </ul>	<ul> <li>Computer Science / Mathematics</li> <li>Computer Science (Imperative Knowledge)</li> <li>Are there (well-defined) problems that cannot be solved by any procedure?</li> </ul>
<ul> <li>This Week:</li> <li>Getting <i>un</i>-comfortable with recursive definitions</li> <li>Understanding why there are some things no program can do!</li> </ul>	<ul> <li>Mathematics (Declarative Knowledge)</li> <li>Are there true conjectures that cannot be the shown using <i>any</i> proof?</li> </ul>





Russell's Resolution?	Epimenides Paradox
$\operatorname{Set} ::= \operatorname{Set}_n$	Epimenides (a Cretan): "All Cretans are liars."
$\operatorname{Set}_0 ::= \{ x \mid x \text{ is an } Object \}$	
$\operatorname{Set}_n ::= \{ x \mid x \text{ is an } Object \text{ or a } Set_{\underline{n-1}} \}$	Equivalently: "This statement is false."
<ul> <li>S: Set<sub>n</sub></li> <li>Is S a member of itself?</li> <li>No, it is a Set<sub>n</sub> so, it can't be a member of a Set<sub>n</sub></li> </ul>	Russell's types can help with the set paradox, but not with these.
Liberal Arts Trivia: English Literature and Drama • Name the tragedy by Shakespeare parodied below by Tatsuya Ishida. • Bonus points: the <i>blank</i> of animals.	<ul> <li>Liberal Arts Trivia: Woodworking</li> <li>This woodworking joinery technique is noted for its tensile strength (resistance to being pulled apart). A series of <i>pins</i> are cut from the end of one board and interlock with a</li> </ul>
TATSUBAR UNDER WORK IS A MAN! WORK IS A MAN! WORK IS A MAN! WHAT IS THIS ACTION HOW LIKE AN ADDEL IN APPRETENSION HOW LIKE A GOD! WORK IS A MAN! WHAT IS THIS OF DUST! MAN DELIGHTS NOT ME	series of <i>tails</i> cut into the end of another. Once glued it requires no fasteners.
Gödel's Solution	Kurt Gödel
All consistent axiomatic formulations of number theory include <i>undecidable</i> propositions. (GEB, p. 17) <i>undecidable</i> - cannot be proven either true or false inside the system.	<ul> <li>Born 1906 in Brno (now Czech Republic, then Austria-Hungary)</li> <li>1931: publishes Über formal unentscheidbare Sätze der Principia Mathematica und verwandter Systeme (On Formally Undecidable Propositions of Principia Mathematica and Related Systems)</li> </ul>
#35	#36

<ul> <li>1939: flees Vienna</li> <li>Institute for Advanced Study, Princeton</li> <li>Died in 1978 – convinced everything was poisoned and refused to eat</li> </ul>	Gödel's Theorem In the Principia Mathematica system, there are statements that cannot be proven either true or false.
Gödel's Theorem In any interesting rigid system, there are statements that cannot be proven either true or false.	Gödel's Theorem All logical systems of any complexity are <b>incomplete</b> : there are statements that are <i>true</i> that cannot be proven within the system.
Proof - General Idea • Theorem: In the Principia Mathematica system, there are statements that cannot be proven either true or false. • Proof: Find such a statement!	Gödel's Statement G: This statement does not have any proof in the system of Principia Mathematica. G is unprovable, but true! Why?

Gödel's Proof Idea G: This statement does not have any proof in the system of <i>PM</i> .	Homework • Read Chapter 11 • Short In-Class Quiz Wednesday • PS6 Due Mon Mar 23
If G is provable, PM would be inconsistent. If G is unprovable, PM would be incomplete.	
Thus, <b>PM cannot be complete and consistent!</b>	
#43	#44