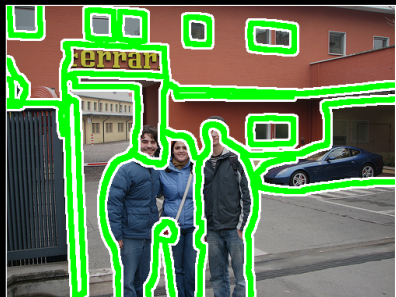


Object Detection and Segmentation from Joint Embedding of Parts and Pixels

Michael Maire¹, Stella X. Yu², Pietro Perona¹

¹California Institute of Technology - Pasadena, CA 91125

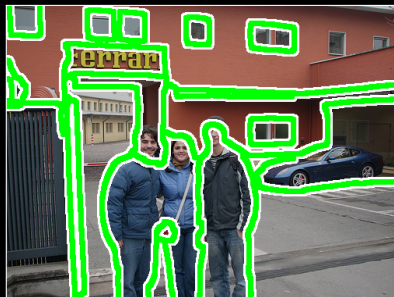
²Boston College - Chestnut Hill, MA 02467



Segmentation



Detection



Segmentation



Detection

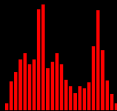
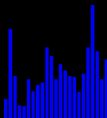
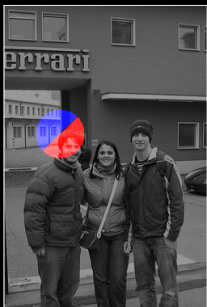
Perceptual Grouping Framework

Ingredients

Plug in state-of-the-art components:

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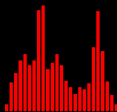
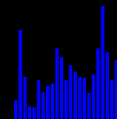
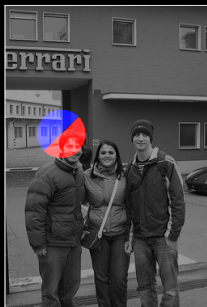


low-level cues:
color, texture, edges

[Arbeláez, Maire, Fowlkes, Malik, PAMI 2011]

Ingredients

Plug in state-of-the-art components:



low-level cues:
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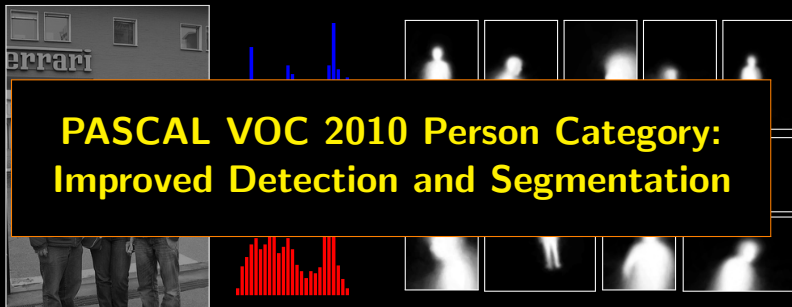
top-down parts:
poselets for person detection

[Arbeláez, Maire, Fowlkes, Malik, PAMI 2011]

[Bourdev, Maji, Brox, Malik, ECCV 2010]

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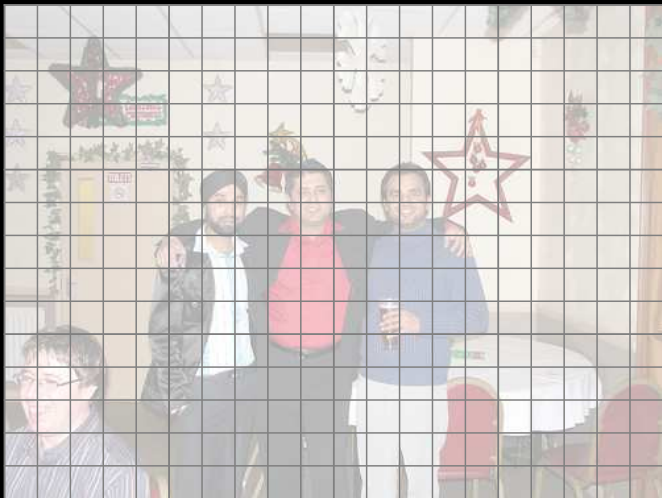
[Bourdev, Maji, Brox, Malik, ECCV 2010]

Grouping Relationships

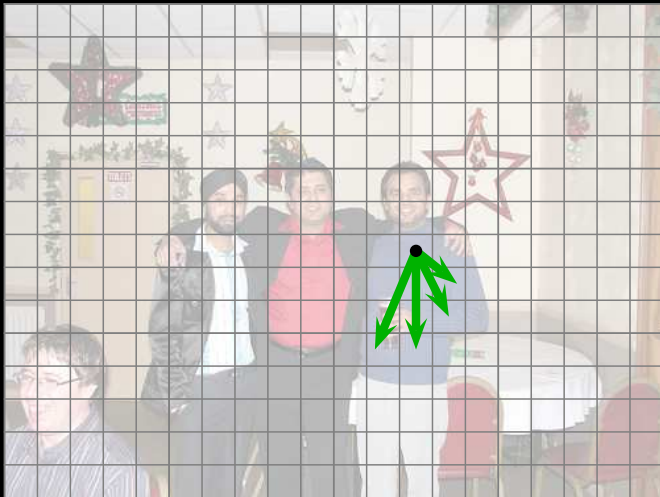
Grouping Relationships



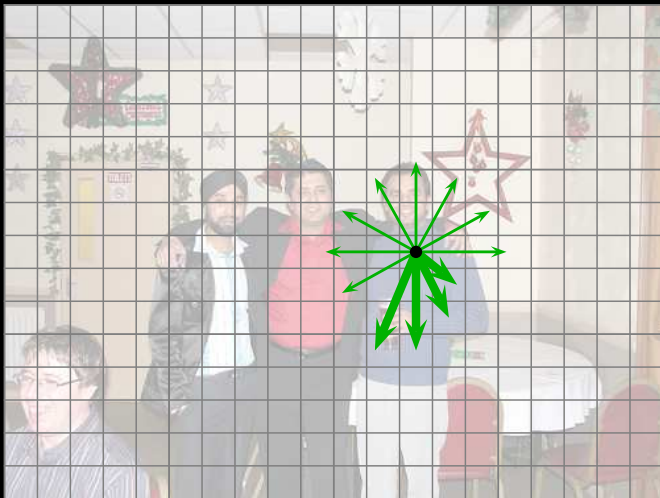
Pixel Affinity: Color, Texture Similarity



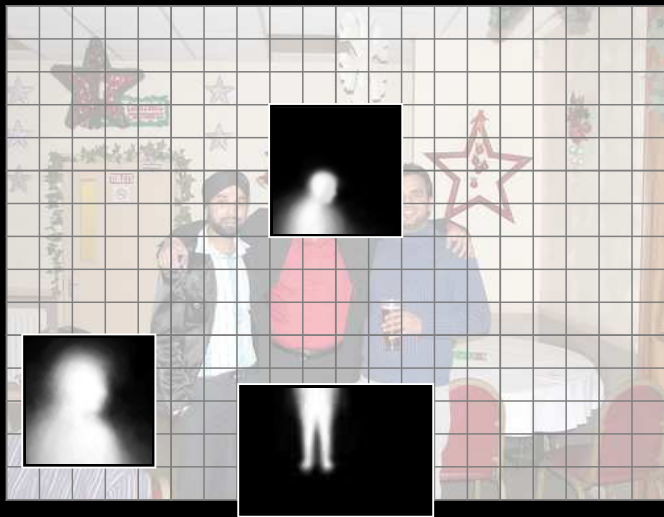
Pixel Affinity: Color, Texture Similarity



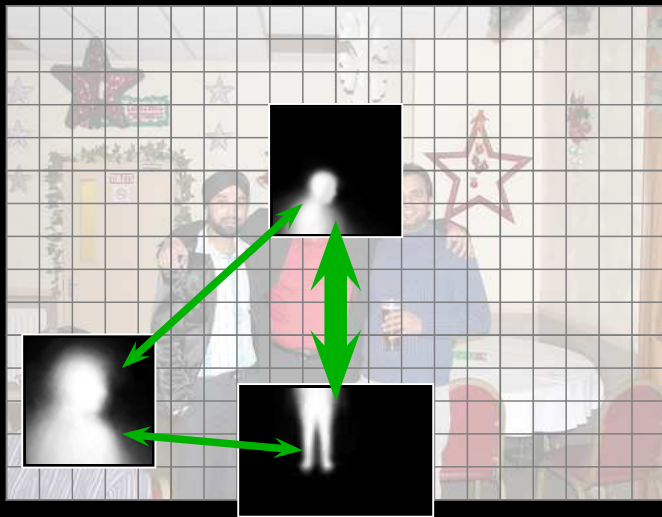
Pixel Affinity: Color, Texture Similarity



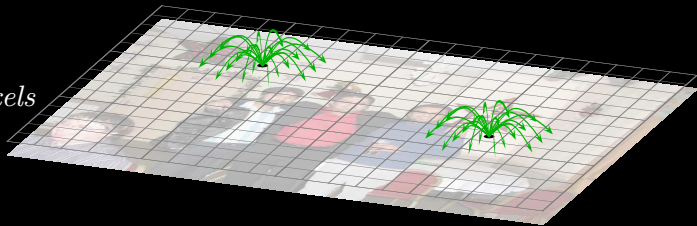
Part Affinity: Geometric Compatibility

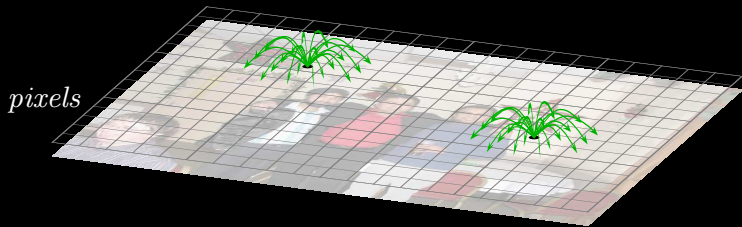
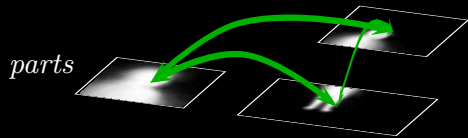


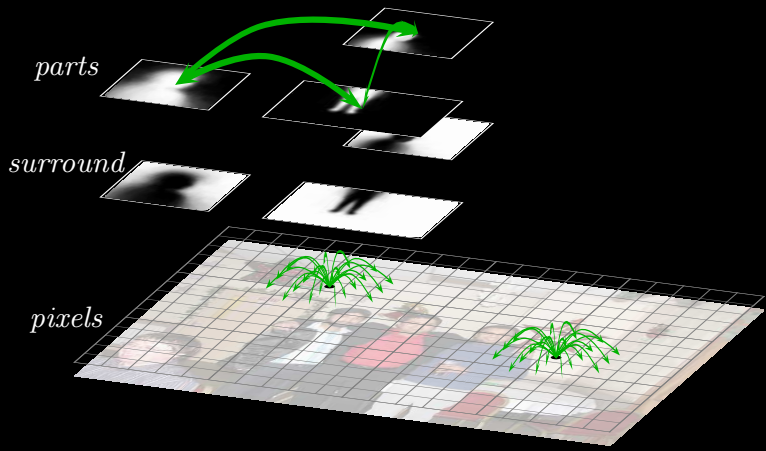
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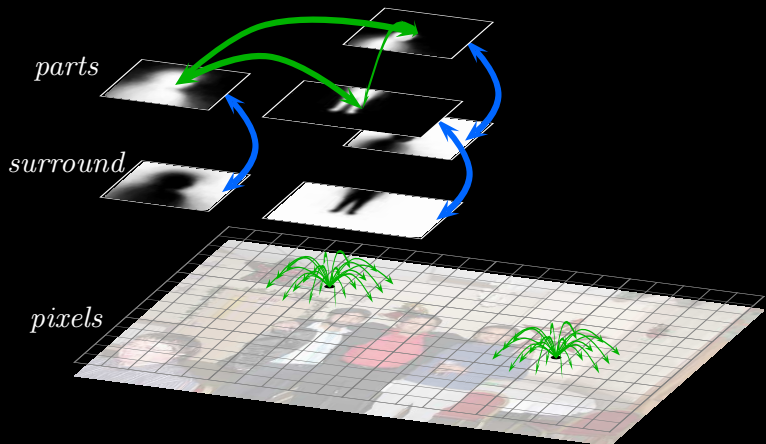


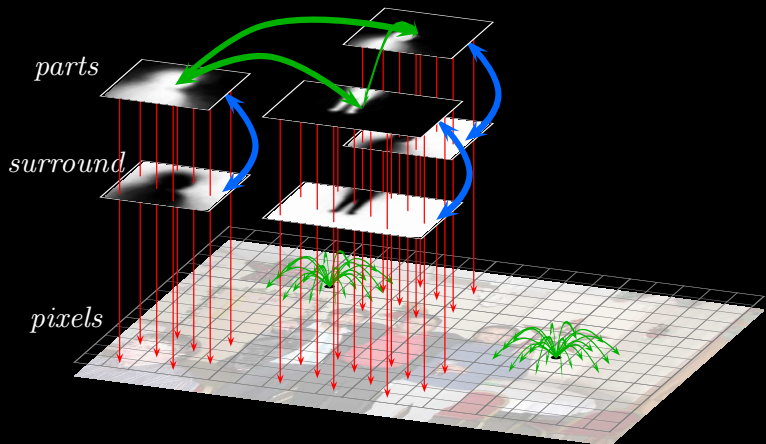
pixels

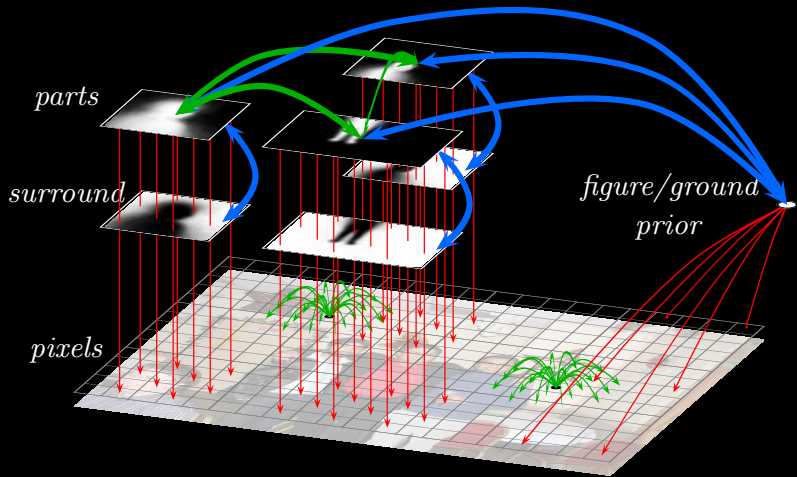


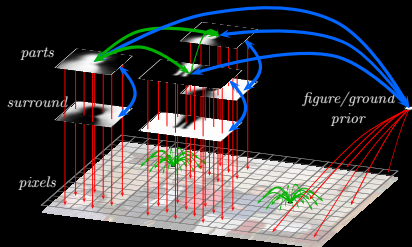




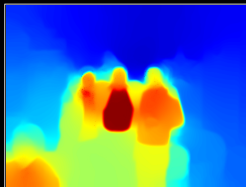
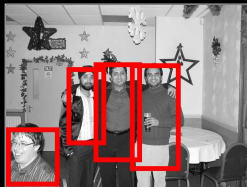








Angular Embedding



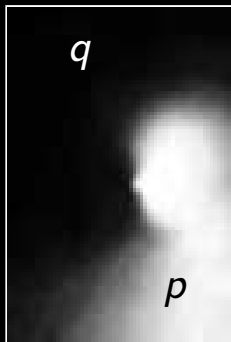
objects

figure/ground

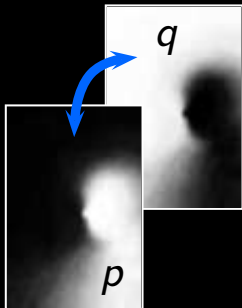
segmentation

Angular Embedding

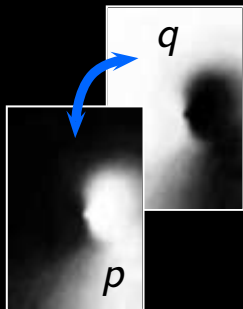
Angular Embedding



Angular Embedding



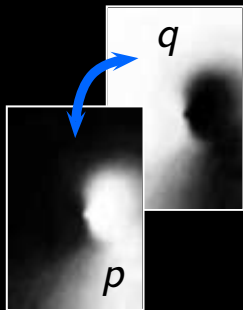
Angular Embedding



Given:

- ▶ Relative ordering $\Theta(\cdot, \cdot)$
- ▶ Confidence on relationships $C(\cdot, \cdot)$

Angular Embedding



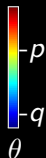
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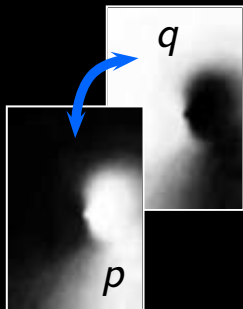
Compute:

- ▶ Global ordering $\theta(\cdot)$
- ▶ Embed into unit circle:

$$p \rightarrow z(p) = e^{i\theta(p)}$$



Angular Embedding



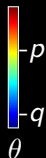
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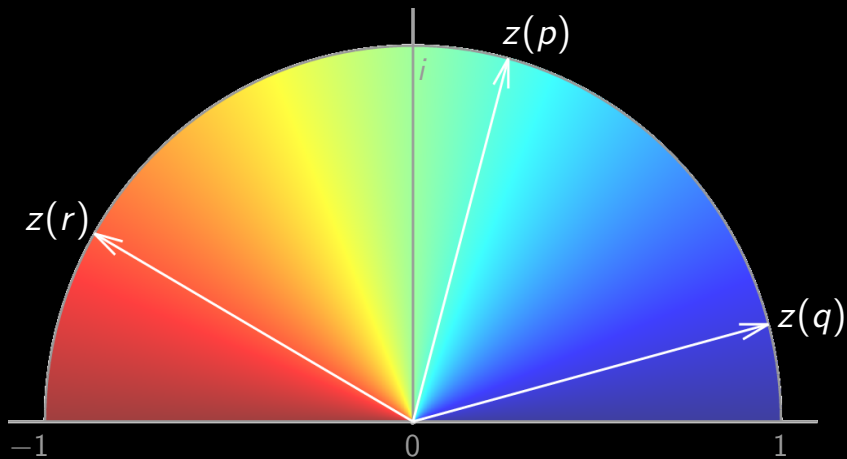
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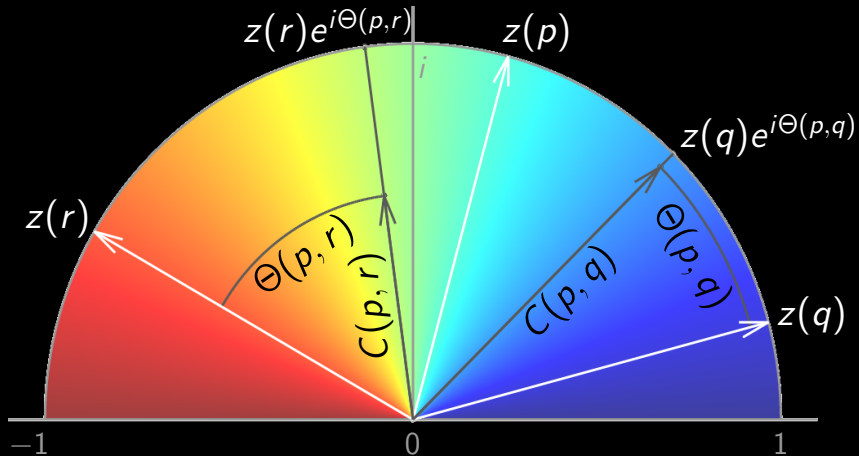
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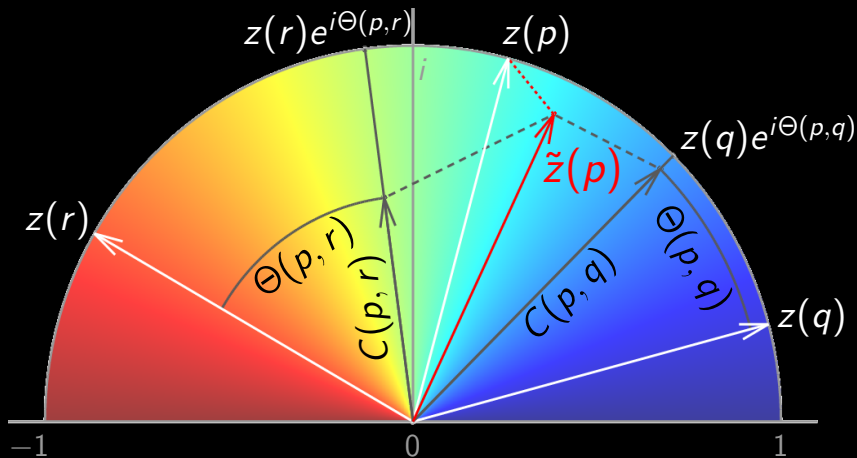


Subject to:

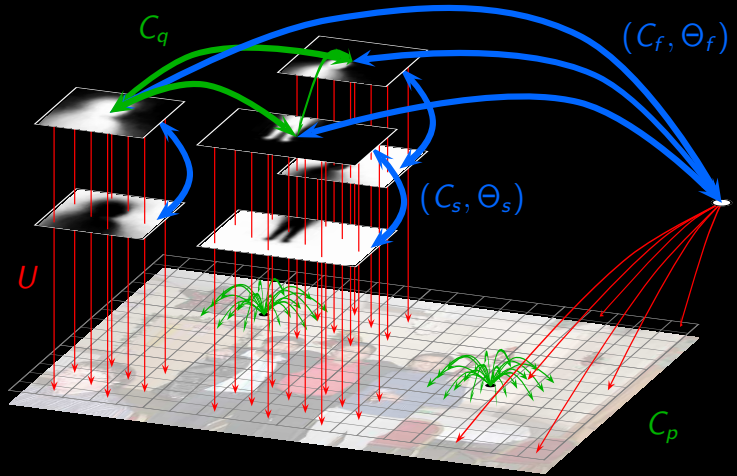
- ▶ Linear constraints on embedding solution in columns of U







$$\text{minimize: } \varepsilon = \sum_p \frac{\sum_q C(p,q)}{\sum_{p,q} C(p,q)} \cdot |z(p) - \tilde{z}(p)|^2$$



$$\begin{array}{cccc}
 & \underbrace{\text{pixels}} & \underbrace{\text{parts}} & \underbrace{\text{surround}} & \underbrace{\text{prior}} \\
 \mathbf{C} = & \begin{bmatrix} \mathbf{C}_p & 0 & 0 & 0 \\ 0 & \alpha \cdot \mathbf{C}_q & \beta \cdot \mathbf{C}_s & \gamma \cdot \mathbf{C}_f \\ 0 & \beta \cdot \mathbf{C}_s^T & 0 & 0 \\ 0 & \gamma \cdot \mathbf{C}_f^T & 0 & 0 \end{bmatrix}
 \end{array}$$

$$\Theta = \Sigma^{-1} \begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & \Theta_s & \Theta_f \\ 0 & -\Theta_s^T & 0 & 0 \\ 0 & -\Theta_f^T & 0 & 0 \end{bmatrix}$$

Angular Embedding

Relax to generalized eigenproblem $QPQz = \lambda z$:

$$P = D^{-1}W$$

$$Q = I - D^{-1}U(U^T D^{-1}U)^{-1}U^T$$

with D and W defined as:

$$D = \text{Diag}(C1_n)$$

$$W = C \bullet e^{i\Theta}$$

Eigenvectors $\{z_0, z_1, \dots, z_{m-1}\}$ embed pixels and parts into \mathbb{C}^m

Angular Embedding

$\angle z_0$ encodes global ordering

z_1, z_2, \dots, z_{m-1} encode grouping

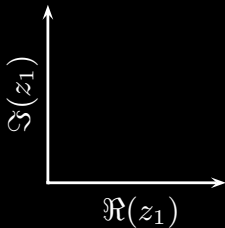
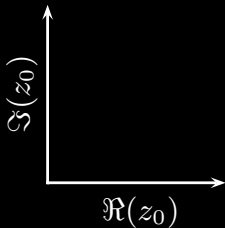
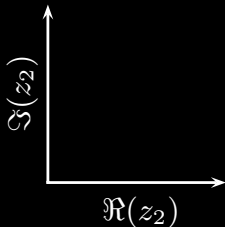
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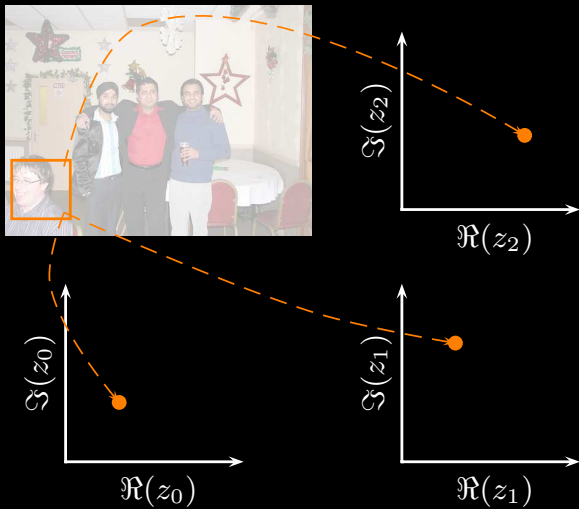
z_1, z_2, \dots, z_{m-1} encode grouping

if $\Theta = 0 \Rightarrow$ **Normalized Cuts**
(grouping without ordering)

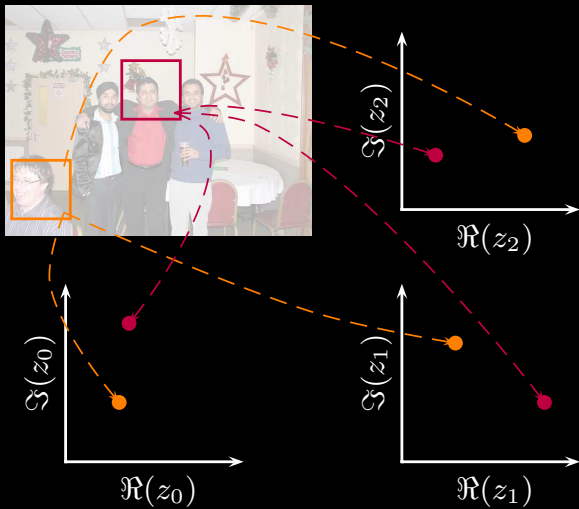
Decoding Eigenvectors: Object Detection



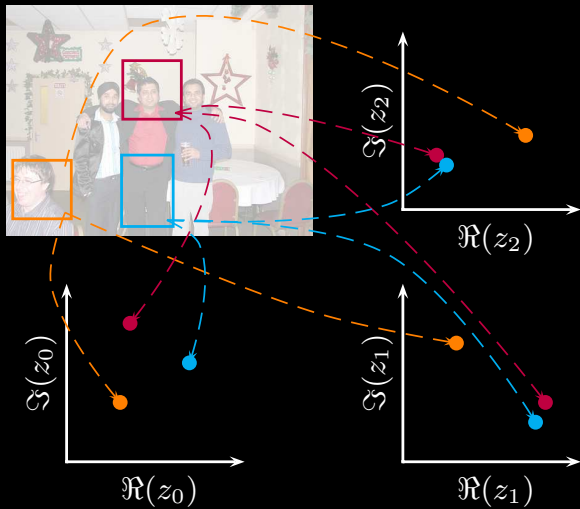
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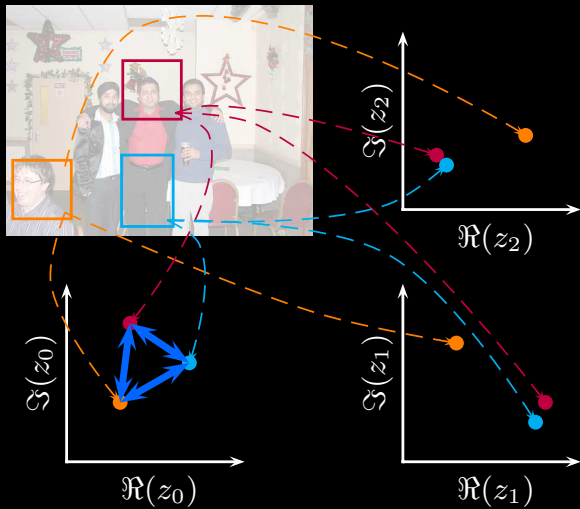
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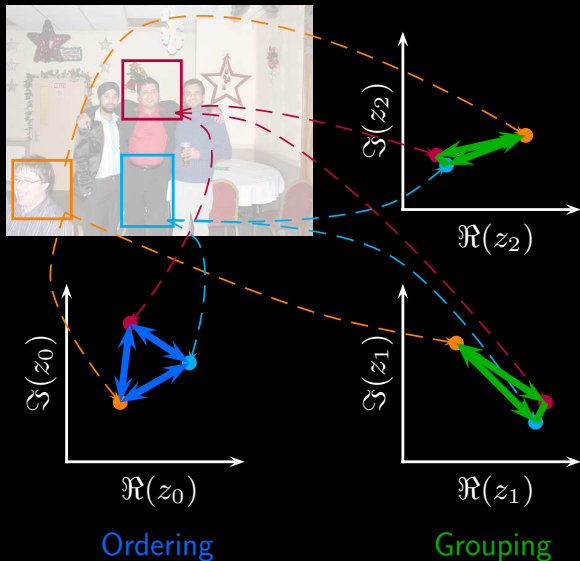


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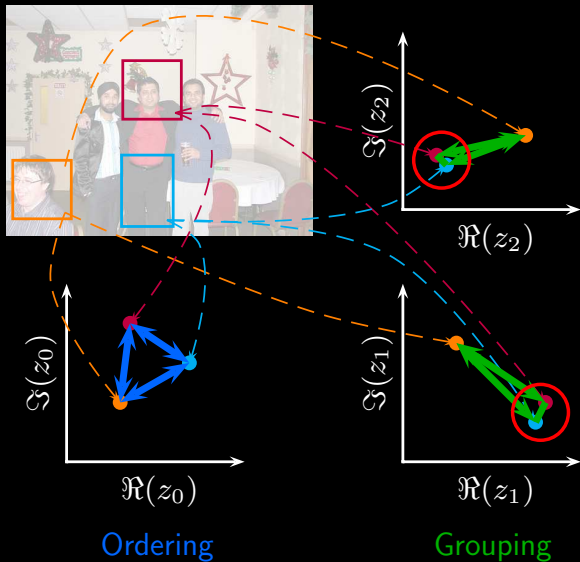


Ordering

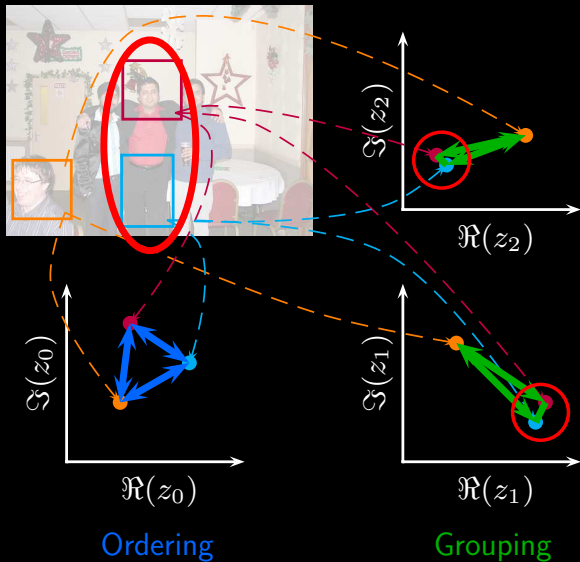
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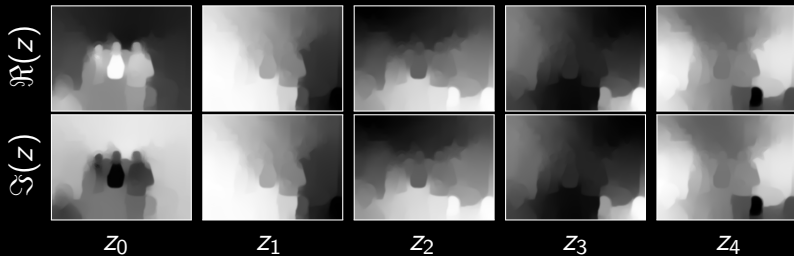
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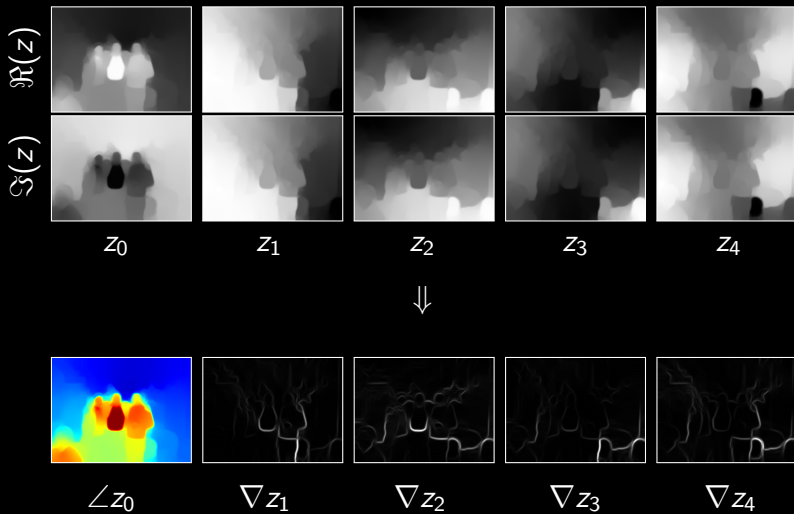
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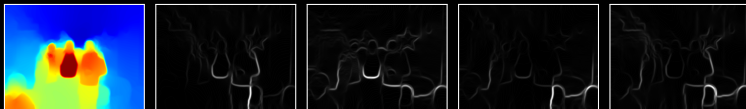
Decoding Eigenvectors: Figure/Ground



Decoding Eigenvectors: Figure/Ground



Decoding Eigenvectors: Segmentation



z_0

z_1

z_2

z_3

z_4

Figure/Ground

Hierarchical Segmentation

[Arbeláez, Maire, Fowlkes, Malik, PAMI 2011]



Decoding Eigenvectors: Object Segmentation

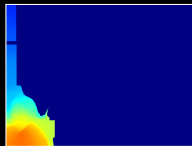
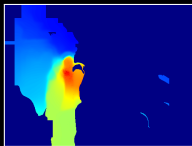
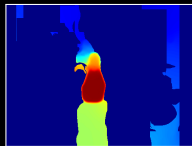
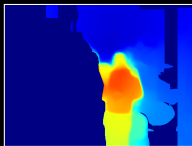
Assign pixels p_k to objects Q_i via parts q_j :

$$p_k \rightarrow \operatorname{argmin}_{Q_i} \left\{ \min_{q_j \in Q_i} \{ \operatorname{Dist}(p_k, q_j) \} \right\}$$

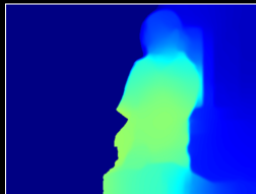
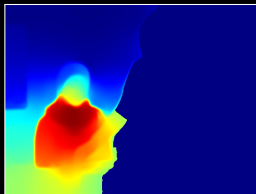
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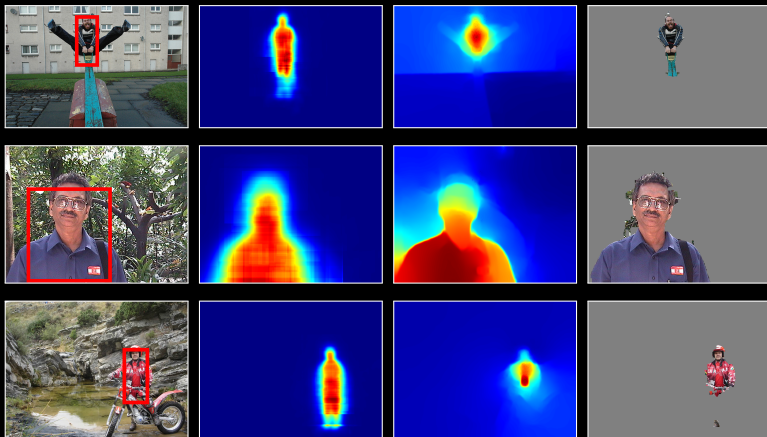
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Decoding Eigenvectors



Results: PASCAL 2010 Person Category



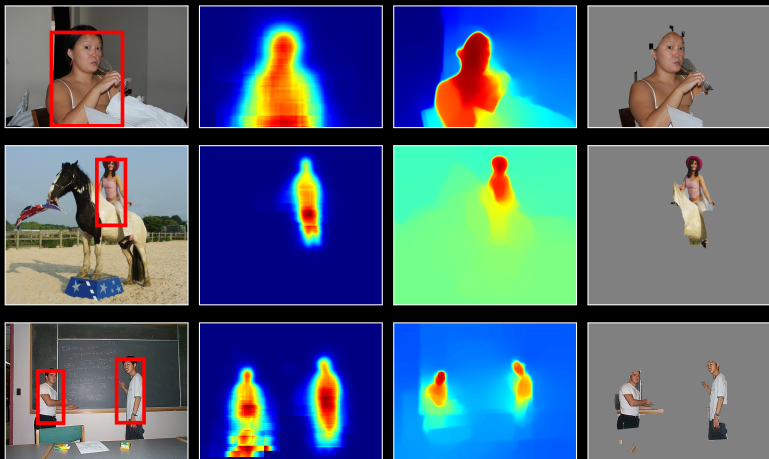
Detections

Poselet Mask

F/G Mask

Segmentation

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Detections

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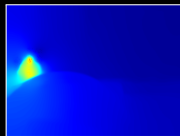
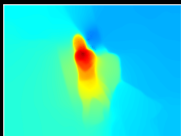
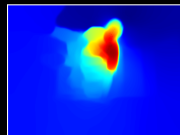
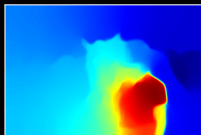
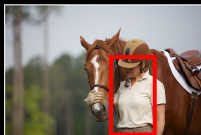
Segmentation

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- ▶ Segmentation task score: 41.1 (35.5 for poselet baseline)

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- ▶ 11% relative improvement due to better detection



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