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# Multi-Job Production Systems 

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Introduction: MJP systems

## Problems

Solutions and results
Case study
Summary and future work

## Introduction

## Multi-Job Production (MJP) Systems

- Jobs are released one-by-one according to a product-mix and build schedule.
- Different job-types require different amount of work at some or all operations.
- Processing times are deterministic and job-dependent.
- The setup times are zero.
- In-process buffers are non-dedicated.
- Jobs are processed on a FIFO basis.
- The machines are unreliable and experience random breakdowns.


## MJP Systems illustration



## MJP Systems illustration



## Who uses MJP

- Auto industry
- Assembly plants
- Engine and transmission plants
- Battery plants
- Suppliers
- Household appliance industry
- Computer industry

Problems

## The Problem

- The relation between throughput, bottleneck and product-mix is not known.
- Performance losses of 10-20\% consistently observed in MJP plants
- No theory exists to address these losses


## MJP Theory

- MJP Theory addresses the following problems


## Performance analysis

Calculate performance characteristics of MJP systems (e.g., TP, WIP, probability of machine blockage and starvation) as functions of the product-mix.

## Continuous improvement

Determine MJP system bottlenecks, indicate a way to alleviate them, and quantify the resulting performance improvement as functions of the product-mix.

- MJP Toolbox

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MJP Toolbox
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Provide a software package to make the theory usable to industry and academia, via both real-time and off-line analysis capabilities.

## Different types of MJP systems

- Serial line



## Different types of MJP systems

- Hybrid serial line



## Different types of MJP systems

- Assembly system


MA main assembly line $\mathrm{SA}_{i}$ subassembly lines

## Solutions and results

## Work-based model

- Work-based model
- Machines produce work
- Work capacity of machine $i: W_{i}$
- Jobs require work
- Work-requirement of job $j$ at machine $i: w_{i j}$
- Different job-types require different amount of work.
- Processing time of job-type $j$ at machine $i: \tau_{i j}=w_{i j} / W_{i}$
- Suitable for analysis of MJP and Single-Job Production (SJP) systems


## Performance analysis for serial lines

- Three-step procedure


## Virtual SJP <br> system

## Performance estimation

## Conversion to MJP

## Performance analysis for serial lines

- Three-step procedure


## Virtual SJP system

## Performance estimation

## Conversion to MJP

For the given product-mix, create a virtual SJP system processing a virtual job whose work-requirements are weighted (by product mix) average of jobs' work requirements ( $w_{i, v}=\sum_{j} r_{j} w_{i j}$ )

## Performance analysis for serial lines

- Three-step procedure


## Virtual SJP system

## Performance estimation

## Conversion to MJP

Performance of the virtual system is estimated using the methods available in the literature. We used aggregation method from Li and Meerkov (2007).

## Performance analysis for serial lines

- Three-step procedure


## Virtual SJP system

## Performance estimation

## Conversion to MJP

Estimate the performance metrics of the original MJP line from the virtual SJP system.

## Accuracy

- Accuracy of the conversion from MJP to virtual SJP is very high
- Less than 0.2\% error in TP for 10-machine lines
- Accuracy of step 2 depends on the method used
- We used aggregation method by Li and Meerkov, 2009
- Around $4 \%$ error in TP for 10-machine lines
- Conversion from SJP back to MJP does not introduce additional errors.


## Classification of MJP systems

- Two distinct behaviors of TP as function of product-mix
- Definition. Two job-types are non-conflicting if $B N_{J 1}=B N_{J 2}$
- Otherwise, they are conflicting.

For illustration purposes, systems with 2 job-types are presented in the rest of the presentation.
Product-mix is denoted as $r_{1}=r, r_{2}=1-r$

## Non-conflicting jobs

- Theorem. If J1 and J2 are non-conflicting with common bottleneck $m_{k}$, and all buffers are of zero or infinite capacity
- $m_{k}$ is BN for any $r$
- $T P_{v}(r)$ is given by
- $T P_{v}(r)=\frac{1}{\frac{r}{T P_{J 1}}+\frac{1-r}{T P_{J 2}}}$
- $T P_{v}(r)$ is
- Strictly monotonically increasing if $T P_{J 1}>T P_{J 2}$
- Strictly monotonically decreasing if $T P_{J 1}<T P_{J 2}$
- Constant if $T P_{J 1}=T P_{J 2}$
- Numerical fact. The above results hold true for lines with any buffers. Analyzing 25000 lines:
- $B N$ remaining the same machine in $99.2 \%$ of cases

- $T P$ is monotonic in $92.8 \%$ of cases
- Accuracy of (b) is above $99 \%$ in $95.8 \%$ of cases


## Non-conflicting jobs

- Intuitive behavior
- Not linear
- No BN switches
- Easily expandable to more than two job-types



## Conflicting jobs

- Theorem. Consider an $M$-machine line producing conflicting jobs J1 and J2, i.e., $B N_{J 1} \neq B N_{J 2}$. If buffers are $N=0$ or $N=\infty$, then
- BN has at most $M-1$ switches in the interval of $r$
- If there are $K$ BN switches, then $T P(r)$ has $K+1$ intervals of continuous differentiability.
- If $w_{B N_{J 1,1}}>w_{B N_{J 1}, 2}$ and $w_{B N_{J 2}, 1}<w_{B N_{J 2}, 2}$, then there is an interval $R \subset[0,1]$, at which $T P(r) \stackrel{>}{>} T P_{J j}$





## Conflicting jobs

- Why TP(r) acts non-monotonically?





$$
T P=\frac{8}{12}=0.66
$$

$33 \%$ more production

## Performance portrait

- Graphically presents throughput and bottlenecks as functions of the productmix
- Works with systems with more than two job-types by introducing additional degrees of freedom.


Primary job-type: © J1 ○ J2 ○ J3
Mix of non-primary job-types:

## Case study

The data presented in the following slides are modified due to confidentiality purposes

## Production System

- Automotive assembly plant > Body shop > Underbody
- Two job-types
- Study period: 14 weeks



## Current system

- Body shop target TP: 55 JPH
- Body shop current TP: 49 JPH
- Typical range of product-mix of job 1 - $r_{1} \in[25 \%, 50 \%]$
- Bottleneck OP7



## Continuous improvement project

- Improve OP7
- Prioritize maintenance
- Prioritize delivery
- Improve manual loading
- Result



## Continuous improvement project

- Improve OP1
- Look into Front comp. line for J1
- Model Front comp. line
- Find BNs
- Design improvement plan
- Result



## Continuous improvement project




## Summary

## Summary

- MJP systems are widely used in the industries
- $15 \%-20 \%$ of their capacity is wasted
- MJP theory helps recover these losses
- Performance portraits are quick and easy way to understand system behavior and plan continuous improvement projects


## Future work

- Develop the theory for the assembly systems
- Improve overall MJP accuracy by improving the accuracy of current methods for SJP systems analyses
- Integrating MJP tools especially performance portrait into plants' production management dashboard

Thank you

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## Continuous improvement

- Bottleneck identification
- Bottleneck: machine whose capacity affects throughput the most
- $m_{i}$ is bottleneck iff $w_{i, v}(r) \frac{\partial T P}{\partial W_{i}}>\frac{\partial T P}{\partial W_{k}} w_{k, v}(r)$, for all machine $k \neq i$
- Alternate approach: arrow method
- Use blockage and starvation data
- Compare $B L_{i}$ with $S T_{i+1}$ and draw an arrow toward the smaller
- The machine(s) with no emanating arrows is the bottleneck


## Work-based model

- WBM characterizes the production system components
- Machines (Operations)
- Work capacity
- Reliability characteristics (MTBF/MTTR/...)
- Starvation/blockage measurement policy
- Buffers
- Non-dedicated vs. dedicated
- Jobs
- Work requirement at each operation
- Release
- According to product-mix or build-schedule


## Accuracy

- Step one has high accuracy
- Less than $0.6 \%$ discrepancy in BN identification of 5-machine lines
- Step two
- Lower accuracy; 10\% discrepancy in BN identification of 5-machine lines
- Step three
- No additional errors are introduced


## Performance analysis for serial lines

- Three-step procedure
- For any product-mix, create the corresponding virtual SJP system
- Calculate (estimate) performance of the virtual system using the methods available in the literature
- Convert the results back to original MJP system coordinates


