Safe Autonomous Overtaking with Intention Estimation

Vishnu S. Chipade¹, Qiang Shen², Lixing Huang³, Necmiye Ozay⁴, Sze Zheng Yong², Dimitra Panagou¹,³

Abstract—This paper investigates the problem of overtaking a lead car by an autonomous ego car on a two-lane road in the presence of an oncoming car. We propose an intention-aware overtaking controller for the ego car. The intention of the lead car is estimated via a combination of active model discrimination and model selection algorithms. Then, a safe overtaking controller is designed based on vector fields that take into account the estimated intent, and ensure safety of the overtaking maneuver. Simulation results demonstrate the efficacy of the proposed approach.

I. INTRODUCTION

Autonomous cars have been a very active topic of research recently due to numerous potential benefits such as driver comfort, reduced road fatalities, improved mobility, etc. Various aspects of them such as perception, real-time decision making and motion planning have been extensively studied (see, e.g., the review papers [1]–[4] for more details). In particular, safely overtaking a slower car moving on a two-lane road is of great interest since this could be crucial in emergency situations. Thus, in this paper, we investigate intent-aware safe overtaking of a lead car by an autonomous vehicle (the ego car) in the presence of an oncoming car on the left lane.

Autonomous overtaking has been studied using various strategies in the literature. The authors in [5] use MPC for generating overtaking trajectories in the presence of an oncoming car, while a hierarchical planning approach including strategic-level and low-level trajectory optimization for lane changing is presented in [6]. Receding horizon control has also been used to deal with lane changing problems, where the surrounding vehicles are modeled as Markov Gaussian Processes in [7], and stochastic MPC is employed to account for the uncertainty in other vehicles’ motion. Similarly, the approach in [8] samples independent and identically distributed (iid) prediction trajectories of other vehicles from a generic model and build multi-level optimization problems based on these iid scenario samples. Other approaches use multi-policy decision making for high-level lane-changing behavior, where buffered Voronoi cells were used to compute a geometric partition and then, reducing the safety control design to ensuring that the vehicles avoid the partition boundaries [9]. However, these works do not consider the reaction of the other cars to the ego car’s overtaking maneuver.

Another set of relevant literature pertains to approaches for active model discrimination, which injects a small input signal that causes the behaviors of all models to be distinct, thus can be discriminated from each other [10], [11]. These approaches have been successfully adopted for intention estimation in [12], [13]. In [12], an active model discrimination approach was proposed by solving an mixed-integer linear program (MILP) and applied to the problem of intention identification of other autonomous vehicle or human drivers in scenarios of intersection crossing and lane changing, while in [13], an affine abstraction-based separating input design problem was studied for a set of uncertain nonlinear models and used in an intention estimation example of a highway lane changing scenario with Dubins vehicle models.

In this paper, we propose a safe, autonomous overtaking algorithm for an ego car that accounts for the intention of a lead car. The intention estimation algorithm consists of two phases: 1) an offline phase where an optimal control input sequence for the ego car over a finite time horizon is found to distinguish the intentions of the lead car, and 2) an online phase where the computed sequence is applied to actively distinguish and find out the intention of the lead car. This intention is then used to generate an overtaking trajectory for the ego car, based on vector field guidance. The major contributions of this paper are: (1) the generalization of the active model discrimination formulation to allow piece-wise state-dependent constraints on the controlled inputs, making it applicable to a more general class of affine models when compared to those in [12], [13], and (2) an intent-aware, finite-time tracking controller for overtaking the lead car, based on a novel vector field guidance approach that uses super-elliptic contours and safely guides the ego car around the lead car.

The rest of the paper is organized as follows: Section II provides the mathematical modeling. The intent estimation, and trajectory generation and control algorithms are discussed in Sections III and IV, respectively. Simulation results are provided in Section VI. Conclusions and
our thoughts on future work are provided in Section VII.

II. Modeling and Problem Statement

Notations: The set of positive integers up to $n$ is denoted by $\mathbb{Z}_n^+$, and the set of non-negative integers up to $n$ is denoted by $\mathbb{Z}_n$. Vectors are denoted in bold letters (e.g., $\mathbf{r}$). $\| \cdot \|$ is the 2-norm and $\| \cdot \|_{\infty}$ is the infinity vector norm.

A. Vehicle dynamics

We consider a two-lane road $\mathcal{R} \subseteq \mathbb{R}^2$ of lane width $y_{lane}$, and 3 cars: an ego car, $\mathcal{E}$, a lead car, $\mathcal{L}$, and an oncoming car, $\mathcal{O}$. All cars are identical in shape and are rectangular with length $l_e$ and width $w_e(< y_{lane})$. The cars are assumed to have the following dynamics:

$$
\begin{align*}
\dot{x}_j &= \left[ \begin{array}{c} x_j \\ y_j \end{array} \right] = \left[ \begin{array}{c} v_{xj} \\ v_{yj} \end{array} \right] = v_j, \\
\dot{v}_{xj} &= u_{xj} - C_d v_{xj},
\end{align*}
$$

(1)

for $j \in \{e, l, o\}$. $v_j = [x_j, y_j]^\top$, for $j \in \{e, l, o\}$, are the position vectors of $\mathcal{E}$, $\mathcal{L}$ and $\mathcal{O}$, respectively, in the X-Y plane with respect to (w.r.t.) a global inertial frame $\mathcal{F}_g(i, j, k)$ fixed on the outer edge of the rightmost lane as shown in Fig. 1; $v_{xj}$ are longitudinal velocities; $u_{xj}$ and $v_{yj}$ are longitudinal acceleration inputs and lateral velocity inputs, respectively, which are bounded as:

$$
|u_{xj}| \leq u_{xj}^{\text{max}}, \quad |v_{yj}| \leq v_{yj}^{\text{max}},
$$

(2)

for $j \in \{e, l, o\}$, and $C_d$ is the coefficient of drag. Since overtaking requires more control authority for $\mathcal{E}$, we assume a larger control bound on $\mathcal{E}$ while overtaking:

$$
|u_{xe}| \leq u_{e}^{\text{max,over}}.
$$

(3)

This can be interpreted as that $\mathcal{E}$ will not fully utilize its control authority in normal driving, but in overtaking, it will leverage that to accomplish the task.

![Fig. 1: Coordinate frame](image)

The cars are modeled as rectangles with their edges aligned with the axes of $\mathcal{F}_g$, defined as:

$$
\begin{align*}
\mathcal{E} &= \{ \mathbf{r} \in \mathbb{R}^2 | |x - x_e| \leq \frac{l_e}{2}, |y - y_e| \leq \frac{w_e}{2} \}, \\
\mathcal{L} &= \{ \mathbf{r} \in \mathbb{R}^2 | |x - x_l| \leq \frac{l_l}{2}, |y - y_l| \leq \frac{w_l}{2} \}, \\
\mathcal{O} &= \{ \mathbf{r} \in \mathbb{R}^2 | |x - x_o| \leq \frac{l_o}{2}, |y - y_o| \leq \frac{w_o}{2} \}.
\end{align*}
$$

(4)

For simplicity, we assume that $\mathcal{O}$ is moving with a constant speed $v_{xo}$ on the left lane in the opposite direction.

B. Intention models of the lead car $\mathcal{L}$

During the intention estimation phase, we assume that $\mathcal{E}$ is behind $\mathcal{L}$ in the same lane and the headway $h(k) = x_l(k) - x_e(k)$ between $\mathcal{L}$ and $\mathcal{E}$ satisfies $h(k) > h_{\text{min}} > 0$ to avoid collision and ensure safety. We also limit our intention estimation problem to the case where $\mathcal{L}$ has a constant lateral position and its longitudinal velocity under different driving behaviors does not saturate in the process of intention estimation. Specifically, we consider two driver intentions $i \in \{A, C\}$ for $\mathcal{L}$, corresponding to Annoying and Cautious drivers, which are modeled as:

$$
\begin{align*}
&u_{xl,i} = \begin{cases} u_{zl,0} + K_{l,1} \Delta y + K_{l,2} \Delta h_i + \delta_i, & h_{\text{min}} < h < h_{\text{max}}, \\
u_{zl,0}, & \text{otherwise},
\end{cases}
\end{align*}
$$

(5)

where $\Delta y = y_e - y_l$, $\Delta h_i = h_{\text{max}} - h$, $\Delta h_C = h$, $K_{l,1}$ and $K_{l,2}$ are constants and $\delta_i$ is an input uncertainty accounting for nonlinear non-deterministic driving behavior. $u_{zl,0} = -K_{l}(v_{zl} - v_{zl}^{\text{des}}) + C_d v_{zl}^{\text{des}}$ is a baseline controller that represents the default lead car $\mathcal{L}$ behavior to maintain a desired speed $v_{zl}^{\text{des}}$. We choose $K_{A,1} > 0$ and $K_{A,2} > 0$ in (5) such that the annoying driver drives aggressively and speeds up when $\mathcal{E}$ tries to overtake $\mathcal{L}$, while $K_{C,1} < 0$ and $K_{C,2} < 0$ for the cautious driver who slows down and makes it easier for $\mathcal{E}$ to overtake $\mathcal{L}$.

C. Problem formulation

The problem of autonomously overtaking a lead car $\mathcal{L}$ in the presence of an oncoming car $\mathcal{O}$ on the left lane is hard task when there is no knowledge on how $\mathcal{L}$ is going to behave. Since the knowledge of $\mathcal{L}$'s intention would be beneficial in motion planning, we propose to split the overall overtaking problem into two sequential sub-problems: 1) Intention estimation of $\mathcal{L}$ based on the ideal models (5), and 2) Overtaking control for $\mathcal{E}$ given the intention of $\mathcal{L}$. Formally, the sub-problems are:

**Problem 1:** Estimate the intention of $\mathcal{L}$ over a fixed time horizon $T$. This includes the following two parts:

- **Active model discrimination:** Find an optimal $\mathcal{L}$'s input sequence $\mathbf{u}_T = \{ \mathbf{u}_e^*(0), \ldots, \mathbf{u}_e^*(T - 1) \}$ ($\mathbf{u}_e = [u_{xe} v_{ye}]^\top$, with zero-order hold) over a finite horizon $T$ offline such that the observed trajectory of $\mathcal{L}$ is only consistent with one intention model regardless of any realization of uncertainties.

- **Model selection:** Implement the obtained optimal input sequence $\mathbf{u}_T^*$ alongside a model selection algorithm in real-time to identify the intention of $\mathcal{L}$ based on its observed output trajectories.

**Problem 2:** Find a control input $\mathbf{u}_e = [u_{xe} v_{ye}]^\top$ for the ego car $\mathcal{E}$ to overtake the lead car $\mathcal{L}$ safely in the presence of the oncoming car $\mathcal{O}$ based on the estimated intention from Problem 1.

III. Intention Estimation of the Lead Car

In this section, we design an optimal $\mathcal{E}$'s input sequence and an intention estimation algorithm to distinguish the two intentions of $\mathcal{L}$. The following time-discretized model for $\mathcal{L}$ and $\mathcal{E}$ is used in this section:

$$
\begin{align*}
v_{xe}(k + 1) &= (1 - C_d \Delta T) v_{xe}(k) + u_{xe}(k) \Delta T, \\
y_e(k + 1) &= y_e(k) + v_{ye}(k) \Delta T, \\
h(k + 1) &= h(k) - v_{xe}(k) \Delta T + v_{zl}(k) \Delta T, \\
v_{zl}(k + 1) &= (1 - C_d \Delta T) v_{zl}(k) + u_{zl}(k) \Delta T
\end{align*}
$$

(6a-6d)

where $\Delta T$ is the sampling time. The output of the discrete-time model is $\mathcal{L}$'s velocity, i.e., $z_m(k) = v_{zl}(k)$. Note that the separating input $\mathbf{u}_e = [u_{xe} v_{ye}]^\top$ is equal for both intention models.
A. Vehicle dynamics with different intentions

The discrete-time state-space models \( G_i, i \in \{A, C\} \), for both the annoying car and cautious car, are given by

\[
\begin{align*}
\bar{x}_i(k) &= A_i \bar{x}_i(k) + B_i u_i(k) + B_{s,i} \delta_i(k) + f_i, \\
z_i(k) &= C_i \bar{x}_i(k),
\end{align*}
\]

where \( \bar{x}_i(k) = [v_{xe,i}(k) v_{ye,i}(k) h_i(k) v_{xi,i}(k)]^T, z_i(k) = v_{xi,i}(k), \) and the system matrices are

\[
A_i = \begin{bmatrix}
1 - C_i \Delta_T & 0 & 0 & 0 \\
0 & 1 & 0 & \Delta_T \\
-\Delta_T & 0 & 1 & \Delta_T \\
K_{i,1} \Delta_T & \bar{a}_{i,1} \Delta_T & 1 - (K_0 + C_i \Delta_T)
\end{bmatrix}, \\
B_i = \begin{bmatrix}
\Delta_T & 0 \\
0 & \Delta_T \\
0 & 0 \\
(K_0 + C_i \Delta_T) c_{\text{def}}^i \Delta_T + \bar{f}_{i}
\end{bmatrix}, \\
C_i = \begin{bmatrix}
0 & 0 & 0 & 1
\end{bmatrix},
\]

where \( \bar{a}_{i} \) and \( \bar{f}_{i} \) are defined as

\[
\bar{a}_{i} = \begin{cases}
-1, & i = A \\
1, & i = C
\end{cases}, \quad \text{and} \quad \bar{f}_{i} = \begin{cases}
K_{A,2} h_{\text{max}} \Delta_T, & i = A \\
0, & i = C.
\end{cases}
\]

For both vehicle models \( G_i, i \in \{A, C\} \), we assume that the initial condition for model \( i \), denoted by \( \bar{x}_i^0 = \bar{x}_i(0) \), is constrained to a polyhedral set defined as:

\[
\bar{x}_i^0 \in X_0 = \{ \bar{x} \in \mathbb{R}^4 : P_0 \bar{x} \leq p_0 \}, \quad \forall i \in \{A, C\}.
\]

Further, the constraints on controlled input \( u_i \) in (2) are written using the following polyhedral set representation (for \( k \in \mathbb{Z}_B^0 \)):

\[
u_i^0 \in U = \{ u_i \in \mathbb{R}^2 : Q_u u_i \leq q_u \}.
\]

In addition, \( E \)'s lateral velocity input has to satisfy a piece-wise state-dependent constraint defined as

\[
\begin{align*}
v_{ye} &\in \begin{cases}
\{0\}, & \text{if } \beta_1 \leq \frac{v_{ye,i}}{v_{xe,i}} \leq \beta_2, \\
\{v_{ye} : \beta_1 \leq \frac{v_{ye,i}}{v_{xe,i}} \leq \beta_2\}, & \text{if } v_{xe,i} \in [v_{xe,i}^{\min}, v_{xe,i}^{\max}],
\end{cases} \\
v_{xe,i} &\in [v_{xe,i}^{\min}, v_{xe,i}^{\max}],
\end{align*}
\]

where \( v_{xe,i}^{\max} \) can be considered as a dead-zone, within which \( E \) does not have lateral motion, while \( \beta_1 \) and \( \beta_2 \) are slopes that mimic curvature constraints of real cars. The constraint in (11) implies that \( E \) is allowed to overtake \( L \) only when its longitudinal velocity is greater than \( v_{xe,i}^{\max} \).

An example of the piece-wise state-dependent constraint with \( v_{xe,i}^{\max} = 10 \), \( \beta_1 = -1 \) and \( \beta_2 = 1 \) is shown in Fig. 2.

![Fig. 2: Piece-wise state-dependent constraint in (11)](image)

Moreover, the uncertainty \( \delta_i \) is also constrained to a polyhedral set (for \( k \in \mathbb{Z}_B^0 \)) defined as

\[
\delta_i(k) \in D_i = \{ \delta \in \mathbb{R} : Q_g \delta \leq q_g \},
\]

The states \( \bar{x}_i(k) \) are divided into controlled state \( x_i(k) = [v_{xe,i}(k) v_{ye,i}(k) h_i(k) v_{xi,i}(k)]^T \), and uncontrolled state \( y_i(k) = v_{xi,i}(k) \in \mathbb{R} \). The controlled state \( x_i \) are constrained to the following polyhedral set (for \( k \in \mathbb{Z}_T^F \)):

\[
x_i(k) \in X_{x,i} = \{ x \in \mathbb{R}^3 : P_x x \leq p_{x,i} \}.
\]

Specifically, we require \( L \) and \( E \) to keep a minimum distance to avoid collision during the intention estimation process, and this safety constraint is given by

\[
h_i(k) \in H_i \in \{ h \in \mathbb{R} : h \geq h_{\text{min}} \},
\]

where \( h_{\text{min}} > 0 \) is a constant. We also constrain \( E \)'s longitudinal velocity to an interval with \( v_{xe,i} \in [v_{xe,i}^{\min}, v_{xe,i}^{\max}] \).

**Remark 1:** We assume that the intention models are well-posed, whose definition can be found in [12, Remark 1]. Vehicle dynamic models are impractical if they are not well-posed, since the responsibilities of the inputs will be impossible to be satisfied.

Now, the Problem 1 can be formally redefined as:

**Problem 3:** Given two intention models \( G_i, i \in \{A, C\} \), and state, input and uncertainty constraints, (9)-(11), find an optimal input \( u_T^* = \{u_T^*(0), \ldots, u_T^*(T-1)\} \) over a finite horizon \( T \) to minimize a given cost \( ||u_T||_\infty \) ensuring comfort with small maximum input amplitudes, so that for all initial states \( x(0) \) and uncertainty \( \delta_i(k) \), \( \forall k \in \mathbb{Z}_T^0 \), only one model is valid, i.e., the output trajectories of models \( G_i \) over a finite horizon \( T \) have to differ by a separation threshold \( \epsilon \) in at least one time instance. The optimization problem can be stated as:

\[
\min_{u_T} ||u_T||_\infty \quad \text{s.t.} \quad \forall k \in \mathbb{Z}_T^0 \text{ (10) holds, (14a)}
\]

\[
\forall i \in \{A, C\}, \forall k \in \mathbb{Z}_T^0, \forall x_{x,i}^0, y_i(k), \delta_i(k), (T),(9),(12) \text{ hold (11), (13) hold, (14b)}
\]

\[
\forall i, j \in \{A, C\}, i \neq j, \forall k \in \mathbb{Z}_T^0, \forall x_{x,i}^0, y_i(k), \delta_i(k), (7)-(8),(12)-(13) \text{ hold (11), (13) hold, (14c)}
\]

where \( x_{i,T} = \{x_i(0), \ldots, x_i(T)\} \) with \( i \in \{A, C\} \).

B. Intention estimation approach

To solve Problem 1, an optimization-based approach is proposed, consisting of an offline active model discrimination step and an online model selection step. For brevity, we only give the main results of the approach. Its proofs are omitted as they follow similar steps to [12].

**Proposition 1 (Active Model Discrimination):** Given any separation threshold \( \epsilon \), the active model discrimination problem in Problem 3 is equivalent to a bilevel optimization problem with the following outer problem:

\[
\min_{u_T} ||u_T||_\infty \quad \text{(POuter)}
\]

\[
\text{s.t.} \quad \forall k \in \mathbb{Z}_T^0 \text{ (10) holds, (15a)}
\]

\[
\forall i \in \{A, C\}, \forall k \in \mathbb{Z}_T^0, \forall x_{x,i}^0, y_i(k), \delta_i(k), (7),(9),(12) \text{ hold (11), (13) hold, (15b)}
\]

\[
\Delta^*(u_T) \geq \epsilon, \quad (15c)
\]
where $\Delta^*(u_T)$ is the solution to the inner problem:

$$
\Delta^*(u_T) = \min_{\Delta \in \mathbb{R}^{2,\delta,T}} \Delta \quad (P_{\text{inner}})
$$

\begin{align*}
\text{s.t. } & \forall i \in \{A,C\}, \forall k \in \mathbb{Z}^L_{T-1} : (7), (12) \text{ hold,} \\
& \forall i \in \{A,C\}, \forall k \in \mathbb{Z}^L_T : (8) \text{ holds,} \\
& \forall i \in \{A,C\} : (9) \text{ holds,}
\end{align*}

\begin{align*}
\forall i,j \in \{A,C\}, i \neq j, \forall k \in \mathbb{Z}^L_j : |z_i(k) - z_j(k)| & \leq \Delta, \tag{16d}
\end{align*}

where $\delta_{i,T} = \{\delta_i(0), \ldots, \delta_i(T)\}$ with $i \in \{A,C\}$.

Based on the bilevel problem proposed in Proposition 1, we can further leverage Karush-Kuhn-Tucker (KKT) conditions to convert the bi-level problem into a single level MILP problem, which can be solved by off-the-shelf optimization software, such as Gurobi [14] and CPLEX [15]. These details can be found in our previous paper [12, Theorem 1]. Comparing with [12], we consider additional piece-wise state-dependent constraints and responsibilities on the the controlled input in the outer problem of this paper, in order to make the intention estimation problem more realistic and practical.

In addition, to estimate the intention of $L$, the optimal separating input is applied in real-time and the following model selection problem is considered:

\textbf{Proposition 2 (Model Selection):} Given two vehicle models $G_i, i \in \{A,C\}$, and an input-output sequence $\{u_*(k), z_m(k)\}_{k=0}^\infty$, where $u_*(k)$ is obtained in Proposition 1, the model selection problem in Proposition 1 is equivalent to the following feasibility problem:

\begin{align*}
\text{s.t. } & \forall i \in \{A,C\}, \forall k \in \mathbb{Z}^L_{T-1} : z_m(k) - z_i(k) = 0, \\
& \forall k \in \mathbb{Z}^L_{T-1} : \Delta^*(\bar{x}(k) + 1) = A_i \bar{x}(k) + B_i u_*(k) + B_{\delta,i} \delta(k) + f_i, \\
& \forall k \in \mathbb{Z}^L_{T-1} : (10)-(12) \text{ hold,} \forall k \in \mathbb{Z}^L_T : (13) \text{ holds.}
\end{align*}

We can solve the above feasibility check problem by leveraging the model validation algorithm in [16] and identify the true intention, which is guaranteed since the separating input in Proposition 1 is applied.

\textbf{IV. Trajectory Generation and Control for the Ego Car}

In this section, we provide a solution to Problem 2, i.e., we design the control actions $u_{x_e}(t)$ and $v_{y_e}(t)$ of $L$ so that it safely overtakes $L$ at some finite time $T < \infty$.

To assess the safety of the cars, we define a weighted ∞-norm distance between two rectangular cars $i, j$ as:

$$
||r_i - r_j||_{\infty} = \max \left( \frac{x_i - x_j}{l_c}, \frac{y_i - y_j}{w_c} \right),
$$

where $l_c$ and $w_c$ are the dimensions of the rectangles. The distance is referred to as ∞-distance hereafter.

\textbf{Definition 1 (Safety):} Two cars $i$ and $j$ are safe with regards to each other if $||r_i(t) - r_j(t)||_{\infty} > 1, \forall t \geq t_0$.

To ensure the safety of the ego car $E$ from the lead car $L$, we inflate $L$ as $\hat{L} = \{r \in \mathbb{R}^2 \mid |x - x_l| \leq \frac{l_c}{2}, |y - y_l| \leq \frac{w}{2} \}$, where $l_c = l_c + 2(x_{safe}), w_c = w_c + 2(y_{safe})$, and $x_{safe} \geq \frac{l_c}{2}, y_{safe} \geq \frac{w}{2}$ are safety parameters. Further, let $\mathcal{R}_l = \{y \in \mathbb{R} \mid \frac{w}{2} \leq y \leq y_{ane} - \frac{w}{2} \}$.

\textbf{Definition 2 (Safe overtake):} A maneuver and the resulting trajectory $r_e(t; t_0, r_e(t_0))$ for $E$, where the initial position of $E$ is behind $L$ on the same lane (i.e., $x_e(t_0) < x_l(t_0)$ and $y_e(t_0), y_l(t_0) \in R_l$) and its final position is ahead of $L$ on the same lane (i.e., $x_e(t_f) > x_l(t_f)$ and $y_e(t_f), y_l(t_f) \in R_l$), is a safe overtake if $E$ remains safe with regards to $L$ and $O$ (i.e., $||r_e(t) - r_l(t)||_{\infty} > 1$ and $||r_e(t) - r_l(t)||_{\infty} > 1, \forall t \in [t_0, t_f]$).

To enable safe overtake, we design a finite-time tracking controller based on a safe vector field. First, we choose a desired point $r_d$ ahead of $L$ that is subject to vehicle dynamics corresponding to the estimated intent from the previous section. Next, we define a vector field $F$ that safely guides $E$ around $L$ to $r_d$, and a tracking controller such that $E$ tracks the vector field in finite-time.

The vector field $F$ is a combination of two vector fields: (1) Guide-away vector field ($F_1$), and (2) Guide-to vector field ($F_d$). The Guide-away vector field $F_1$ is defined to closely follow the rectangular shape of the cars using superquadric isopotential contours [17], called E-contours in this paper for brevity. The super-elliptic distance from $L$ is defined as:

$$
E_l(r) = \frac{(x - x_l)^{2n}}{a} + \frac{(y - y_l)^{2n}}{b} - 1, \tag{19}
$$

where $a = \frac{l_c}{2}(2)^{\frac{1}{n}}, b = \frac{w}{2}(2)^{\frac{1}{n}}, n > 1$, and is referred to as E-distance hereafter. For larger values of $n$, the contours corresponding to a constant value of E-distance $E_l$ tend to be of rectangular shape. Figure 3 shows three contours for $E_l = 0, E_l = E_l = 1.94$ and $E_l = E_l = 19.43$, with $n = 1.5$ and $L$ situated at $[30,1.85]^T$.

The inflated lead car $L$ can be approximated by a bounding smallest super-ellipse that contains $L$: $L^n = \{r \in \mathbb{R}^2 \mid E_l(r) \leq 0 \}$. Then, the slope of the tangent to E-contours at a point with position vector $r \in \mathbb{R}^2$ is:

$$
\tan(\hat{\beta}_l(r)) = \frac{b^{2n}(x - x_l)\{x - x_l\}^{2n-2}}{a^{2n}(y - y_l)\{y - y_l\}^{2n-2}}. \tag{20}
$$

Let the unit tangent vector at $r$ be $t_l(r) = \left[ \cos(\hat{\beta}_l(r)), \sin(\hat{\beta}_l(r)) \right]^T$.

\textbf{A. Vector fields for trajectory generation}

\begin{enumerate}
\item \textbf{Guide-away vector field:} The Guide-away vector field $F_1$ around the obstacle $L$ is defined as:

$$
F_1(r) = \left[ \cos(\hat{\beta}_l(r)), \sin(\hat{\beta}_l(r)) \right]^T, \tag{21}
$$

where $\hat{\beta}_l(r) = \left\{ \begin{array}{ll}
\hat{\beta}_l(r) - \pi, & (r - r_d) \cdot t_l(r) - \hat{\beta}_l(r) - \pi,
\hat{\beta}_l(r) - \pi, & \text{otherwise,}
\end{array} \right.$

with $\hat{\beta}_l = atan2\left( y - y_d, x - x_d \right)$. This way, $F_1$ takes the form shown in regions $A_l = \{r \in \mathbb{R}^2 \mid 0 < E_l(r) < \hat{\beta}_l, (r - r_d) \cdot t_l(r) - \hat{\beta}_l > 0 \}$ (see violet vectors in Fig. 3) and $B_l = \{r \in \mathbb{R}^2 \mid 0 < E_l(r) < E_l^b, (r - r_d) \cdot t_l(r) > 0 \}$ (see green vectors in Fig. 3).

\item \textbf{Guide-to vector field:} The Guide-to vector field $F_d$ is defined as a radially converging vector field to the desired location $r_d$:

$$
F_d(r) = \frac{r_d - r}{||r_d - r||}. \tag{22}
$$
\end{enumerate}
We set $\mathbf{F}_d(r_d) = 0$, so that $\mathbf{F}_d$ is defined everywhere.

3) Combining vector fields: For the resulting vector field to be continuously differentiable near $\mathcal{L}$, the Guide- to and Guide-away vector fields are combined using a blending function defined as:

$$
\sigma(E_i) = \begin{cases} 
1, & 0 \leq E_i \leq \tilde{E}_i, \\
0, & E_i^u < E_i, \\
\frac{AE_i^3 + BE_i^2 + CE_i + D}{E_i^u - E_i}, & E_i^u \leq E_i,
\end{cases} 
$$

where $\tilde{E}_i$, $E_i^u$ are the super-elliptic distances defining the inner and outer boundaries of the blending region $D_i = \{ r \in \mathbb{R}^2 \mid \tilde{E}_i < E_i(r) < E_i^u \}$, and the coefficients $A, B, C, D$ are chosen as:

$$
A = \frac{2}{(E_i^u - \tilde{E}_i)^3}, \quad B = -\frac{3(E_i^u + \tilde{E}_i)}{(E_i^u - \tilde{E}_i)^3}, \quad C = \frac{6E_i^3}{(E_i^u - \tilde{E}_i)^3}, \quad D = \frac{(E_i^u)^3 - 3E_i^3}{(E_i^u - \tilde{E}_i)^3},
$$

so that (23) is a $C^1$ function. We choose $E_i^u = \left( \frac{2\beta_{lane} - \frac{\bar{y}}{\bar{x}} - \frac{\bar{y}}{\bar{x}}}{\bar{x}} \right)^2 - 1$ such that $\mathbf{F}_i$ is active for $\frac{\bar{y}}{\bar{x}} \leq y_e \leq \frac{2\beta_{lane} - \frac{\bar{y}}{\bar{x}} - \frac{\bar{y}}{\bar{x}}}{\bar{x}}$. The value of $\tilde{E}_i$ is chosen such that $\tilde{E}_i < E_i^u$. The maximum distance $x_{\text{rep}}$ from $\mathcal{E}$ along $i$ at which the Guide-away vector field $\mathbf{F}_i$ is active is given as $x_{\text{rep}}^{\text{max}} = a \left( E_i^u + 1 \right)^{\frac{1}{a}}$. Then the Guide-to and Guide-away vector fields are blended as:

$$
\mathbf{F} = (1 - \sigma(E_i))\mathbf{F}_d + \sigma(E_i)\mathbf{F}_i = [F_x, F_y]^T.
$$

A vector field similar to $\mathbf{F}_i$ is considered around $\mathcal{L}$ when $\mathcal{E}$ attempts to overtake. However, the decision making and analysis is just based on the vector field around $\mathcal{L}$.

B. Control Design for the Ego Car

The desired position $r_d$ of $\mathcal{E}$ is chosen ahead of $\mathcal{L}$ (i.e., $x_d(t) > x_l(t)$), and is assumed to follow dynamics:

$$
\begin{aligned}
\dot{r}_d &= \frac{x_d - x_l(t)}{y_d} = v_{xd} y_{yd}, \\
v_{xd} &= u_{xd} - C_d v_{yd},
\end{aligned}
$$

where $v_{yd} = 0$, $u_{xd} = u_{zd,0} + \delta_{\text{min}}$ and $u_{zd,0} = u_{zd,i} = \delta_i$, $i = A, C, N$; $i = N$ stands for the case when $\mathcal{E}$ is not estimating the intention of $\mathcal{L}$, which we consider for comparison. In the latter case, $\mathcal{L}$ is assumed to be moving with constant average traffic speed ($v_{i,\text{avg}}$), with some uncertainty in its acceleration such that the corresponding input is $u_{zd,N} = C_d v_{i,\text{avg}} + \delta_N$, where $\delta_N \in [\delta_{\text{min}}, \delta_{\text{max}}]$. We obtain the dynamics of the motion of $\mathcal{E}$ and $\mathcal{L}$ relative to a coordinate frame attached on $r_d$. Define $\tilde{r}_e = r_e - r_d$, $\tilde{v}_e = v_e - v_d$ and $\tilde{\mathbf{F}} = \mathbf{F} - \mathbf{F}_d$. Then the dynamics of $\mathcal{E}$ and $\mathcal{L}$ expressed in the new frame are:

$$
\dot{\tilde{r}}_j = \begin{bmatrix} \tilde{x}_j - x_l(t) \\ \tilde{y}_j - y_l(t) \end{bmatrix} = \begin{bmatrix} v_{xd} - u_{xd} \\ v_{yd} - v_{yd} \end{bmatrix} = \tilde{v}_j, \\
\dot{\tilde{v}}_{xj} = \tilde{u}_{xj} - C_d \tilde{v}_{xj},
$$

for $j \in \{ e, l \}$, where $\tilde{u}_{xj} = u_{xe} - u_{xd}$ and $\tilde{u}_{xd} = u_{zd,i} - u_{xd} = \delta_i - \delta_{\text{min}}$. With this choice, we have that $\mathcal{L}$ is either stationary or moving towards the desired position $r_d$. In the worst case, the maximum value of $\tilde{u}_{xj}$ is $\tilde{u}_{xj}^{\text{max}} = \delta_i^{\text{max}} - \delta_i^{\text{min}}$. This results in a maximum velocity of $\mathcal{L}$ relative to $r_d$ of $\tilde{v}_{xj}^{\text{max}} = \frac{\tilde{u}_{xj}^{\text{max}}}{\bar{x}}$.

We design a desired velocity profile for $\mathcal{E}$ that is safe and convergent to the desired position $r_d$ along $\mathbf{F}$ as:

$$
\begin{aligned}
\tilde{v}_{xe}^{\text{des}} &= \tilde{v}_{xj}^{\text{des}} + k_e \tilde{v}_{xe} + \tilde{v}_{xe, \alpha}, \\
\tilde{v}_{ye}^{\text{des}} &= \tilde{v}_{yj}^{\text{des}} + k_e \tilde{v}_{ye} + \tilde{v}_{ye, \alpha}.
\end{aligned}
$$

where $\tilde{v}_{xe}^{\text{des}}$ is the desired relative velocity along the $x$-axis. The acceleration input $u_{xe}$ to track the desired longitudinal velocity $\tilde{v}_{xe}^{\text{des}}$ is designed as:

$$
\tilde{u}_{xe} = C_d \tilde{v}_{xe}^{\text{des}} + k_e \tilde{v}_{xe} + k_v \tilde{v}_{xe} \tilde{v}_{xe, \alpha},
$$

where $\tilde{v}_{xe} = \tilde{v}_{xe}^{\text{des}} - \tilde{v}_{xe}$ and $\alpha \in (0, 1)$ is a gain. In the global coordinate frame, the input $u_{xe}$ of $\mathcal{E}$ is:

$$
u_{xe} = \tilde{u}_{xe} + u_{xd}.
$$

Theorem 1: The relative velocity $\tilde{v}_{xe}$ converges to the desired relative velocity profile $\tilde{v}_{xe}^{\text{des}}$ in finite time under the control action $u_{xe}$ given by (29).

Proof: With $\tilde{u}_{xe}$ (Eq. (29)), the error dynamics is:

$$
\begin{aligned}
\tilde{v}_{xe}^{\text{e}} &= \frac{\hat{\nu}_{fix}}{\delta_i^{\text{max}}} \tilde{v}_{xe} + \tilde{v}_{xe, \alpha \text{e}} - 1.
\end{aligned}
$$

From [18, Lemma 1], we obtain that the equilibrium $\tilde{v}_{xe}^{\text{e}} = \tilde{v}_{xe}^{\text{e}} = 0$ of (31) is finite-time stable.

The safe initial distance $|\tilde{x}_l(t_0)|$ between $\mathcal{L}$ and $r_d$ at the start of the overtake ($t = t_0$) should be such that $\mathcal{L}$ does not come $x_{\text{rep}} + R_e$ close to $r_d$ when $\mathcal{E}$ converges to $r_d$. Since the time of convergence $T_f$ depends on $|\tilde{x}_l(t_0)|$, we use an iterative approach to find $|\tilde{x}_l(t_0)|$ as follows: Initialize $|\tilde{x}_l(t_0)|_0 = x_{\text{rep}} + R_e$, then $|\tilde{x}_l(t_0)|$ is iteratively updated using:

$$
|\tilde{x}_l(t_0)|_{m+1} = |\tilde{x}_l(t_0)|_m + |\tilde{v}_{xe}(0) + \Delta t)| \tilde{v}_{xe}^{\text{max}} + R_e.
$$

where $\tilde{v}_{xe}^{\text{max}}$ is the worst-case relative velocity, and $\Delta t = |\tilde{x}_l(t_0)|_{m+1} - x_{\text{rep}} + R_e$. The iterative approach is terminated when $\|\tilde{v}_{xe}(t_0 + \Delta t)\| < \frac{\bar{y}}{\bar{x}} - y_d(t_0)$, where $y_d(t_0) =$...
where the non-convexity and non-linearity of these problems, the blending region $\mathcal{F}$ is a 2-D square region capturing that $x_{e}(t_{0}) < x_{i}(t_{0}) - x_{e,\text{max}} - x_{c}$, where $x_{c}$ is the maximum bound on the distance that $\mathcal{E}$ would have traveled along $\mathbf{i}$ relative to $\mathbf{r}_{d}$ before it converges to $\bar{v}_{e,\text{converge}}$. Integrating (31) yields: $e_{v_{e}}(t) = \bar{v}_{e,\text{max}}(1 - \frac{1 - \bar{v}_{e,\text{max}}}{\bar{v}_{e,\text{converge}}})$, where $\bar{e}_{v_{e}}(0)$. The error $e_{v_{e}}(t)$ becomes 0 at $t = t_{c} = \frac{\bar{v}_{e,\text{max}}(1 - \bar{v}_{e,\text{converge}})}{\bar{v}_{e,\text{max}}}$ and remains zero for all $t > t_{c}$. Since $\bar{v}_{e,\text{max}} < \bar{v}_{e,\text{converge}}$, we have $x_{e} = \bar{v}_{e,\text{max}}$.

**Theorem 2:** The position $\mathbf{r}_{e}(t)$ under the relative dynamics $\dot{\mathbf{r}}_{e} = \mathbf{v}_{e,\text{des}}$, where $\mathbf{v}_{e,\text{des}}$ as in Eq. (27) is safe and convergent to $\mathbf{r}_{d}$ in some finite time $T_{f}$, if $\forall t < T_{f}$, $\mathbf{r}_{d}(t) \notin \mathcal{D}_{l}$, and $\min_{\mathbf{r}_{e} \in \mathcal{S}_{l}} |\mathbf{r}_{d}(t) - \mathbf{r}_{e}(t)| > R_{l}$, where $\mathcal{S}_{l} = \{\mathbf{r} \in \mathbb{R}^{2} \mid E_{l}(\mathbf{r}) = E_{l}^{0}\}$ is the boundary of $\mathcal{D}_{l}$.

**Proof:** By definition, $\mathbf{v}_{e,\text{des}}$ is always aligned with $\mathbf{F}$, then showing $\mathbf{F}$ is safe implies $\mathbf{v}_{e,\text{des}}$ is also safe. To show $\mathbf{F}$ is safe, we follow a similar analysis to [19, Lemma 1].

Consider $\mathcal{S}_{l}^{-} = \{\mathbf{r} \in \mathbb{R}^{2} \mid E_{l}(\mathbf{r}) = E_{l}^{0} + \epsilon_{E}\}$ and $\mathcal{S}_{l}^{-} = \{\mathbf{r} \in \mathbb{R}^{2} \mid E_{l}(\mathbf{r}) = E_{l}^{0} - \epsilon_{E}\}$, with $\epsilon_{E} > 0$ arbitrarily small. Then:

$$\nabla S_{l}^{-}(\mathbf{r}) = \nabla S_{l}^{-}(\mathbf{r})$$

From the definition of $\mathbf{F}$, we have: $D S_{l}^{-} \mathbf{F} = DS_{l}^{-} \mathbf{F}$, $\nabla S_{l}^{-} \mathbf{F} = D S_{l}^{-} \mathbf{F}$. For $D S_{l}^{-} \mathbf{F}$, consider following cases:

1) Let $\mathbf{r} \in S_{l}^{+} \mathbf{F} = D S_{l}^{-} \mathbf{F}$. This implies that the integral curves cross the surface $\mathcal{S}_{l}$. Let $\mathcal{V} S_{l}^{-} \mathbf{F} > 0$, this implies $\nabla S_{l}^{-} \mathbf{F} > 0$. This contradicts the fact that the integral curves cross $\mathcal{S}_{l}$. Then $\mathcal{V} S_{l}^{-} \mathbf{F} < 0$, which means that the integral curves approach the boundary $T_{l} = \{\mathbf{r} \in \mathbb{R}^{2} \mid E_{l}(\mathbf{r}) = E_{l}\}$ of $\mathcal{D}_{l}$. Let $T_{l}^{-} = \{\mathbf{r} \in \mathbb{R}^{2} \mid E_{l}(\mathbf{r}) = E_{l}^{-}\}$. We have $D T_{l}^{-} \mathbf{F} = D S_{l}^{-} \mathbf{F} < 0$ and $\nabla T_{l}^{-} \mathbf{F} = 0$ because on $T_{l}$ we have $\sigma(E_{l}) = 1$. This implies that the integral curves do not cross $T_{l}$ and keep sliding over $T_{l}$ until reaching $B_{l}$. Since, by definition, the vector field $\mathbf{F}$ in $B_{l}$ points toward $\mathbf{r}_{d}$ that is situated outside $B_{l}$, one can show using a similar analysis that the integral curves exit $B_{l}$.

2) Let $\mathbf{r} \notin S_{l}^{+} \mathbf{F} = D S_{l}^{-} \mathbf{F}$. By definition, the vector fields $\mathbf{F}_{l}$ and $\mathbf{F}_{d}$ both point towards the desired location, which implies $\mathbf{F} = \mathbf{F}_{d}$. Then, using a similar analysis as in the previous case, it can be shown that the integral curves exit the switching surface $\mathcal{S}_{l}$ in this region.

This proves that $\mathbf{F}$ is safe and so is $\mathbf{v}_{e,\text{des}}$. Now, since the blending region $\mathcal{D}_{l}$ is finite, the integral curves of $\mathbf{F}$ inside
$D_l$ are of finite length. Then, an object moving with non-zero speed along the vector field $F$ exits the blending region $D_l$ in finite time. Further, we have that outside $D_l$, the vector field $F$ is convergent to $r_d \notin D_l$ by definition. Thus, given a non-zero speed and by moving along $F$, there exists a finite time $T_1$ such that $|r_e| = R_l$. At this instance, $F = \frac{-F}{|F|}$ because $\sigma(E(r_e)) = 0$. This renders the relative position dynamics as: $\dot{r}_e = -k_e \|r_e\|^{\alpha-1}$. The equilibrium $r_e = r_d$ of this system is finite-time stable as shown in [18, Lemma 1]. Let $T_2$ be time for $r_e(t)$ to converge to $0$ with $\dot{r}_e(0) = R_l$. Then, $r_e$ converges to $r_d$ in finite time $T_f = T_1 + T_2$ with $\dot{v}_e = \frac{d}{dt}r_e$.

\section{Overtake Decision Making}

The ego car $E$ is safe with respect to the lead car $L$ as established in the previous section. The overtaking is performed only when it is deemed safe with respect to the oncoming car $O$. For the chosen $r_d(t_0) = [x_l(t_0) + \bar{\eta}_l(t_0) \; \; y_l(t_0)]^T$, we calculate the worst-case time and $x$-distance traveled by $E$ before it overtakes $L$, assuming maximum relative velocity of $L$ relative to $r_d$, i.e., $\bar{v}_2 = v_{x2,\max}$. Denote the worst-case time and $x$-distance by $\Delta t_W$ and $\Delta x_{e,W}$, respectively, see Fig. 4, and the corresponding actual values as $\Delta t$ and $\Delta x_e$.

For $E$ to be safe with respect to $O$, we require $|r_e(t_0) - r_d(t)|_{E_2} > 1$ for all $t \in [t_0, t_0 + \Delta t_W]$. Then, if $r_e(t) \notin Z_1 = \{r_o \in \mathbb{R} \mid x_e(t_0) < x_o(t) < x_e(t_0) + \Delta x_{e,W}\}$, we have $|r_e - r_o|_{E_2} > 1$, for all $t \in [t_0, t_0 + \Delta t_W]$. For this to hold, $O$ should start outside the region $Z_1 \cup Z_2$, shown in Fig. 4, so that $O$ does not enter $Z_1$ during the worst-case overtake maneuver of $E$, whose trajectory is denoted with the blue curve. This implies that $\langle x_o(t_0) - x_e(t_0) > \Delta x_{e,W} + \Delta t_W | v_o(t_0)| \rangle$ OR $(x_o(t_0) < x_e(t_0))$, i.e., $O$ requires at least $\Delta t_W$ seconds to enter the unsafe zone $Z_1$ if it starts with $x_e(t_0) < x_o(t_0)$ OR it has already crossed $Z_1$ and thereby renders the overtake by $E$ safe.

\begin{figure}[h]
  \centering
  \includegraphics[width=0.8\textwidth]{fig4.pdf}
  \caption{Initial conditions of $O$ for unsafe overtake}
\end{figure}

\section{Case Study and Simulation Results}

We apply our proposed intention estimation based approach to the overtaking scenario when $E$ is behind $L$ in the same lane, where the underlying goal is to detect the intention of $L$. Table I shows parameters of $L$’s intention, while Table II depicts the initial conditions and state and input bounds used in this intention estimation step. The computed optimal input from Proposition 1 is $u_c = \begin{bmatrix} 0 & 0 & 0 & 0 \\ 0.7919 & 0.7919 & 0 & 0 \end{bmatrix}$. Then, this optimal separating input is implemented in real-time while running the model selection algorithm in Proposition 2 to identify the intention of $L$.

\begin{table}[h]
  \centering
  \caption{Parameters in intentions (5)}
  \begin{tabular}{|c|c|c|c|c|}
    \hline
    Parameter & Value & Parameter & Value & Parameter & Value \\
    \hline
    $K_{\theta,1}$ & 0.1 & $K_{C,1}$ & -0.5 & $\delta_A$ & [-0.1,0.1] \\
    $K_{\theta,2}$ & 0.002 & $K_{C,2}$ & -0.04 & $\delta_C$ & [-0.1,0.1] \\
    $K_0$ & 0.1 & $h_{\min} [m]$ & 4 & $h_{\max} [m]$ & 32 \\
    \hline
  \end{tabular}
\end{table}

Next, we provide simulation results for 3 case studies that demonstrate the efficacy of the proposed intention-aware overtaking algorithm for $E$ in the presence of $O$:

Case 1: The intention of $L$ is not known (i.e., $i = N$). The control law for $E$ is $u_{xd} = u_{xL,0} + \delta_{N}$. Table IV shows $u_{xd}$ for the cases with the initial conditions for $E$, $L$, $O$ as given in Table III. It can be observed that, when there is no estimation of the intention of $L$, then it is deemed unsafe for $E$ to overtake for the given initial conditions. However, if $E$ estimates the intention as in Cases 2 and 3, then overtaking is deemed safe. Additionally, when the $L$’s driver is cautious, the $x$-distance that $E$ traveled to overtake $L$ and the control effort during the overtake $U$ is smaller than the corresponding values when the $L$’s driver is annoying. This is expected because the cautious driver slows down to ease out the overtaking maneuver of $E$. Intention estimation helps in effectively deciding whether to overtake or not, and also in guiding $E$ smoothly to overtake $L$ in the presence of $O$.

\begin{table}[h]
  \centering
  \caption{Initial conditions and parameters in intention estimation example}
  \begin{tabular}{|c|c|c|c|}
    \hline
    Parameter & Value & Parameter & Value \\
    \hline
    $v_{xL}(0) [\frac{m}{s}]$ & [22,20] & $v_{xe}([\frac{m}{s}] & [0.34] \\
    $y_{xL}(0) [m]$ & [1.85,2.15] & $y_{xe} [m]$ & [0.9,2.8] \\
    $h_0 (0) [m]$ & [10,20] & $v_{xL} [\frac{m}{s}]$ & [10,28] \\
    $\Delta t [s]$ & [20,23] & $y_{xe} [m]$ & [-4.2,4.2] \\
    $\Delta x_{e,W}$ & 0.05 & $\Delta x_{e,W}$ & [-2.5,2.5] \\
    $u_{xd} [\frac{m}{s}]$ & [-4,-2.4.2] & $u_{xd}'' [\frac{m}{s}]$ & 22 \\
    \hline
  \end{tabular}
\end{table}

Fig. 5(a)–(b) show the $\infty$-distances between $E$ and $L$, and between $E$ and $O$, respectively, for the Case 3 when $L$’s driver is annoying. As observed in Fig. 5(a)–(b), the $\infty$-distances are always greater than 1, demonstrating that there is no collision between $E$ and the other two cars. Figure 6(a) shows the 2-norm distance between $E$ and $r_d$, which goes to zero in finite time, and hence $E$ converges to the desired dynamics (25) in finite time. Moreover, Fig. 6(b) shows that control input $u_{xe}$ applied by $E$ is within the control bounds for all times. The discontinuities in $u_{xe}$ at some places are because the desired velocity profile is only continuous and not differentiable at those points. The corresponding simulation video can be found at: https://youtu.be/fVy3anBvc4.
TABLE III: Initial conditions and other parameters

<table>
<thead>
<tr>
<th>Case</th>
<th>Initial Conditions</th>
<th>Other Parameters</th>
</tr>
</thead>
<tbody>
<tr>
<td>1 (N)</td>
<td>( x_e(0) = 1335)</td>
<td>( R^I_{\text{max,over}} = 0.15 )</td>
</tr>
<tr>
<td>2 (C)</td>
<td>( 650.14 )</td>
<td>( 645.48 )</td>
</tr>
<tr>
<td>3 (A)</td>
<td>( 714.86 )</td>
<td>( 645.48 )</td>
</tr>
</tbody>
</table>

Fig. 5: Weighted \( \infty \)-norm distances between the cars

Fig. 6: Performance of the tracking controller

Fig. 7: Weighted \( \infty \)-norm distances between \( E \) and \( \mathcal{O} \)

(a) Weighted \( \infty \)-norm distance between \( E \) and \( \mathcal{L} \)

(b) Weighted \( \infty \)-norm distance between \( E \) and \( \mathcal{O} \)

VII. CONCLUSIONS AND FUTURE WORK

We developed an intention-aware overtaking algorithm using model discrimination and safe guidance techniques. The intention estimate enables the ego car to decide on whether it is safe to overtake a lead car. The guidance vector fields enable the safe overtake in the presence of an oncoming car. In the future, we would like to also include intention estimation for the oncoming car to further improve the overall proposed architecture.

REFERENCES


