

# Mining Spectrum Usage Data: a Large-scale Spectrum Measurement Study

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## ABSTRACT

Dynamic spectrum access has been a subject of extensive study in recent years. The increasing volume of literature calls for a deeper understanding of the characteristics of current spectrum utilization. In this paper we present a detailed spectrum measurement study, with data collected in the 20MHz to 3GHz spectrum band and at four locations concurrently in Guangdong province of China. We examine the first and second order statistics of the collected data, including channel occupancy/vacancy statistics, channel utilization within each individual wireless service, and the temporal, spectral, and spatial correlation of these measures. Main findings include that the channel vacancy durations follow an exponential-like distribution, but are not independently distributed over time, and that significant spectral and spatial correlations are found between channels of the same service. We then exploit such spectrum correlation to develop a 2-dimensional frequent pattern mining algorithm that can accurately predict channel availability based on past observations.

## Categories and Subject Descriptors

H.m [Information Systems]: Miscellaneous; K.m [Computing Milieux]: Miscellaneous

## General Terms

Measurement

## Keywords

Spectrum Measurement, Channel Vacancy Duration, Ser-

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vice Congestion Rate, Spectrum Usage Prediction, Frequent Pattern Mining, FPM-2D, Temporal Correlation, Spectral Correlation, Spatial Correlation

## 1. INTRODUCTION

Recent advances in software defined radio (SDR) [9] and cognitive radio (CR) [5, 16] combined with ever-increasing demand for wireless spectrum have led to the notion of dynamic spectrum access; wireless devices with the ability to detect spectrum availability and the flexibility to adjust operating frequencies can opportunistically access underutilized spectrum. This type of access is expected to significantly improve spectrum efficiency in light of evidence that abundant spectrum availability exists [10, 11] in the current allocation. This has also led to the notion of open access, whereby unlicensed users/devices are given access to licensed spectrum bands to encourage use of unexploited spectrum opportunity<sup>1</sup>.

These concepts have motivated extensive studies on both technical and policy issues related to dynamic spectrum access. With this comes the need for better and quantitative understanding of current spectrum utilization, beyond the qualitative knowledge of the existence of ample spectrum opportunity. Such understanding can help (1) validate spectrum/channel models often used in analysis without questioning, (2) provide grounds for more realistic channel models with better predictive power, and ultimately, (3) allow devices to make more effective dynamic spectrum access decisions.

To achieve these goals, we recently conducted a comprehensive spectrum measurement study in the 20MHz to 3GHz spectrum band in Guangdong province, China. This paper reports our methodology and findings from this study. There has been a number of spectrum measurement studies published in recent years, like [11, 10] conducted in the US, one in Singapore [7], one in New Zealand [1], and one in Germany [15]. A common finding among these studies is that spectrum is indeed heavily underutilized at the moment.

<sup>1</sup>For instance, the FCC on November 4, 2008 approved unlicensed wireless devices that operate in the empty white space between TV channels, after four years of effort.

Compared to the prior work, the salient features of the data sets we collected are:

- Our measurements are carried out in four locations concurrently;
- Our measurement locations are specifically selected (2 urban and 2 suburban locations) in order to study the potential spatial correlation of spectrum usage between similar and different types of locations.

There are two parts to this study. In the first part, we examine the first and second order statistics of the collected data. These include (1) channel occupancy/vacancy statistics (precisely defined later), over time, across channels, and for different wireless services (that occupy multiple channels), (2) service congestion rate that reveals how well channels assigned to a particular wireless service are utilized, and (3) temporal, spectral, and spatial correlation of spectrum usage. In the second part of the study we exploit such spectrum correlations to develop a 2-dimensional frequent pattern mining algorithm that can accurately predict channel availability based on past observations.

The key findings and contributions of this study are summarized as follows:

1. The channel vacancy duration (*CVD*) distribution is shown to have an exponential tail (but not exactly an exponential distribution; this is empirically obtained but with very high statistical significance), in all channels and locations we studied. This evidence to a certain degree supports some widely used channel models (e.g., the 0-1 Gilbert-Eliot model) under which such durations are exponentially distributed. On the other hand, our data reveals that these occupancy and vacancy durations are *not* independently distributed over time, as is commonly assumed. This finding suggests that spectrum usage is inherently more predictable than current models imply, and that better and more sophisticated models may allow us to exploit such predictability.
2. The service congestion rate (*SCR*), the spectrum utilization within a specific wireless service, appears to be highly cyclical with a period of a day and have significant temporal correlation. This is to be expected: it simply reflects the persistence of user habit within a particular service from day to day.
3. Spectral correlation of spectrum utilization is significant between channels belonging to the same service, and quite insignificant otherwise. This reflects the difference in the nature of these services, and the resulting different usage patterns.
4. There is very significant spatial correlation between the *SCRs* of the same service (e.g. GSM900 uplink) at different locations. The spatial correlation is even higher when the two locations are of the same type (both in urban or both in suburban areas). This suggests that usage patterns are heavily influenced by the nature/type of the wireless service, rather than the location. There is a population element (high vs. low density), but overall similarities in collective usage pattern of the same service are significant in different regions.

**Table 1: Location Overview**

Location	Type	Coordinate
1.Trade Center, Guangzhou	Downtown	E 113°15'25" N 23°08'01"
2.Canadian Garden, Guangzhou	Downtown	E 113°21'45" N 23°08'20"
3.Jiangmen	Suburban	E 113°7'59.9" N 22°22'46.9"
4.Zhongshan	Suburban	E 113°27'24.8" N 22°25'32.5"

5. Motivated by the strong correlation in temporal, spectral, and spatial dimensions, we propose an effective 2D frequent pattern mining algorithm, which can predict spectrum usage with the accuracy exceeding 95%.

We hope that these findings will lead to more discussions on how to better model current spectrum utilization, i.e., the behavior of primary users. This in turn can help us design better and more efficient spectrum sensing and access schemes for secondary users.

The remainder of the paper is organized as follows. Section II presents how our data is collected and processed. We then analysis the *CVD*, *SCR*, and the spectrum correlation (temporal, spectral and spatial) in Sections III, IV, and V, respectively. We present in detail a 2D frequent pattern mining technique in Section VI to predict spectrum usage. We discuss how these results can help in spectrum sensing and access in Section VII. Related work is presented in Section VIII, and Section IX concludes the paper.

## 2. DATA COLLECTION AND PREPROCESS

### 2.1 Data Collection

The results presented in this paper are based on the analysis of 4 sets of measurement data, which were collected at four different locations in Guangdong province, China, from 15:00 Feb 16, 2009 to 15:00 Feb 23, 2009. Locations 1 and 2 are in the downtown area of Guangzhou, the main metropolis of Guangdong province (roughly 10 kilometers apart), while Locations 3 and 4 are in suburban areas of two under-developed cities (roughly 45 kilometers apart). These locations are listed in Table 1.

We are primarily interested in spectrum usage of the frequency band between 20MHz and 3GHz. Within this range, the list of wireless services along with their spectrum assignment in the local region are provided in Table 2.

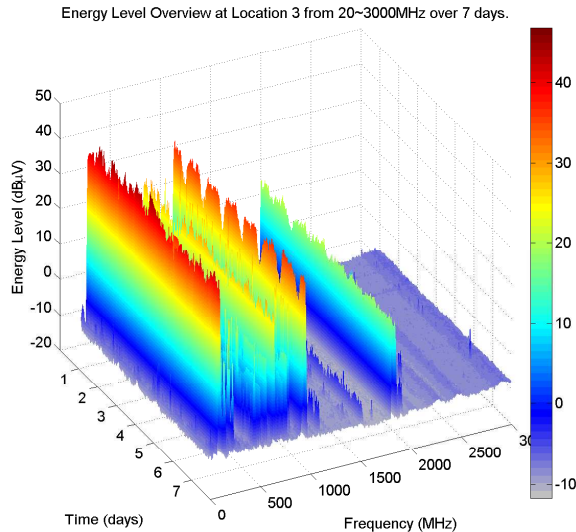
The measurement equipment we used is an R&S EM550 VHF / UHF Digital Wideband Receiver. EM550 is a superheterodyne receiver that covers a wide frequency range, from 20 MHz to 3.6 GHz. The measurement resolution is one per 0.2MHz, resulting in a total of 14,900 frequency readings per time slot (or sweep time, roughly 75 seconds). There are 8,058 (7 days/ 75s) time slots. As a result, there are 14,900×8,058 data points in the data set (roughly 2GB in size) per location.

Here we would like to briefly compare our data sets with those reported on the Shared Spectrum Company (SSC) website<sup>2</sup>. Judging by the published reports, our data sets

<sup>2</sup><http://www.sharespectrum.com/measurements>, one taken in Maine, one in Chicago, and one in Ireland.

**Table 2: Spectrum Allocation of Popular Services**

Services	Band
CDMA uplink	825MHz - 835MHz
CDMA downlink	870MHz - 880MHz
GSM900 uplink	885MHz - 915MHz
GSM900 downlink	925MHz - 960MHz
GSM1800 uplink	1710.0MHz - 1785.0MHz
GSM1800 downlink	1805.0MHz - 1880.0MHz
Broadcasting TV1	48.5 - 92MHz
Broadcasting TV2	167 - 233MHz
Broadcasting TV3	470MHz - 566MHz
Broadcasting TV4	606 - 870MHz
ISM	2400 - 2500MHz



**Figure 1: 3-D view of the energy level over all bands.**

are of a similar nature and have been collected in a similar way, e.g., the antennas are placed outdoor on the roof of a building while the receivers are placed indoor.

For illustration purpose, Figure 1 shows a 3-D depiction of the set of data at Location 3. The color coding (energy level from low to high on a scale from blue to bright red) on the figure is an attempt to make the figure easier to visualize, but does not provide extra information, as the vertical dimension already shows the energy reading (in  $\text{dB}\mu\text{V}$ ).

These data sets provide us with a fairly rich set of measurements, based on which spectrum utilization and patterns can be identified and analyzed as we show in subsequent sections.

## 2.2 Preprocessing

To conduct the sequence of analysis presented in later sections, we will first convert the above measurement data (in absolute energy reading) into a binary sequence of 0s and 1s, through a thresholding process, with 0 denoting a channel being unused, idle or available, and 1 denoting the opposite (i.e., used, busy or unavailable).

We begin by defining the following terms.

- *Channel*: a channel is an interval of radio frequency of

bandwidth 200KHz. Channels are indexed sequentially; Channel  $X$  is the frequency interval  $[(20+0.2(X-1))\text{MHz}, (20+0.2X)\text{MHz}]$ ,  $X > 0$ . Since 200KHz is the resolution of our measurement devices, a channel is the smallest unit at which we can distinguish energy.

- *Service*: a service is a set of channels that have been assigned to the same application/service, as listed in Table 2. Without ambiguity we will use this term to mean both the service and the set of channels assigned to the service.
- *Channel state information (CSI)*: this is a function of time and channel.  $CSI(t, c) = 0$  indicates that Channel  $c$  is idle at time slot  $t$ , and  $CSI(t, c) = 1$  otherwise.
- *Channel vacancy*: this is the period in which a channel remains idle. In the  $CSI$  time series of a channel, a channel vacancy is an interval of continuous 0's.

Converting energy level to  $CSI$  data (0 or 1) is essentially a binary hypothesis testing process, but done in a more simplistic way here through a simple thresholding procedure: for channel  $c$ , a threshold is set to be 3dB higher than the minimum value seen in this channel over the entire duration of the trace collected. At time slot  $t$  if the energy level is lower than this threshold, then  $CSI(t, c) = 0$ ; otherwise  $CSI(t, c) = 1$ . The reason for this thresholding scheme is the following. Figure 2 shows the maximum, minimum and average energy level of some noise channels (those higher than 2GHz but below the ISM band) at Location 2. They are called noise channels because they are currently assigned to satellite-to-satellite communications (the signal does not reach the ground and thus the only energy present on the ground is due to noise). We see that for these channels, the maximum and minimum power levels are all within a 3dB range. Assuming that noise behaves similarly across channels (which is not exactly true, but probably close), anything more than 3dB above the minimum power level suggests the presence of signal, hence the above thresholding rule. Decreasing this threshold will improve signal detection probability, but will also increase false alarms; the reverse is also true.<sup>3</sup> Calibrating the error in such a process is out of the scope of the present paper, though it is an important subject.

The end result of this process is a sequence of  $CSIs$  (0s and 1s) for each spectrum channel of 200KHz wide, representing its availability over a time resolution of approximately 75 seconds. This is shown in Figure 3 where black dots indicate busy channels. In subsequent sections we will try to uncover the properties inherent in these sequences.

## 3. CHANNEL VACANCY DURATION (CVD) DISTRIBUTION

In this section we present statistics on the channel vacancy durations ( $CVD$ ). They are shown to be exponential-like, but not independently distributed, in all channels we studied.

As defined earlier, in the  $CSI$  time series of a given channel, a channel vacancy is a complete interval of consecutive

<sup>3</sup>We did try increasing this threshold from 3dB to 4.5 dB and found the resulting 0-1 sequence to be nearly the same. The same thresholding process was used in a measurement study conducted in Aachen, Germany [15].

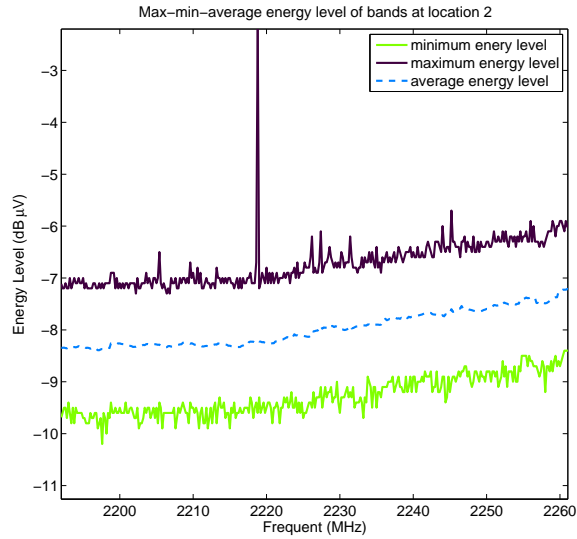


Figure 2: The maximum, minimum and average energy levels of noise channels at Location 2.

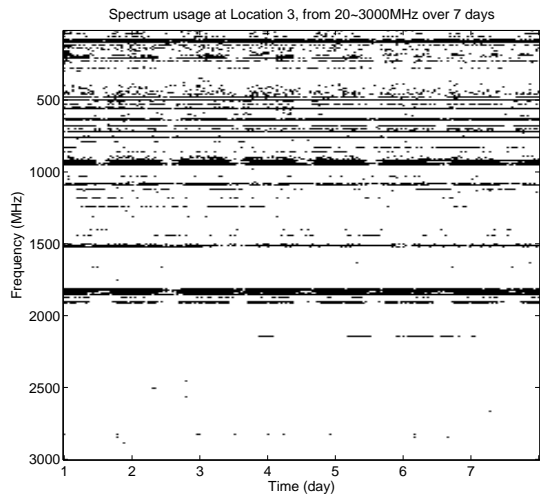


Figure 3: CSI map at Location 3

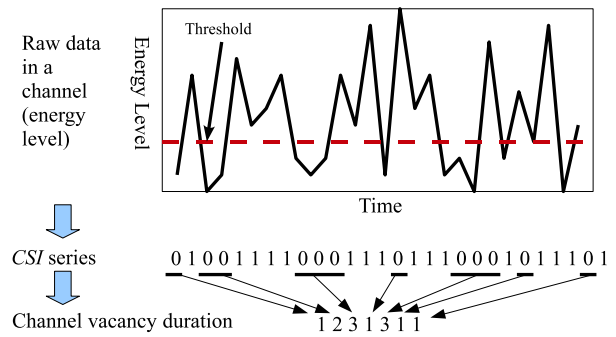


Figure 4: Extract channel vacancy durations from raw data.

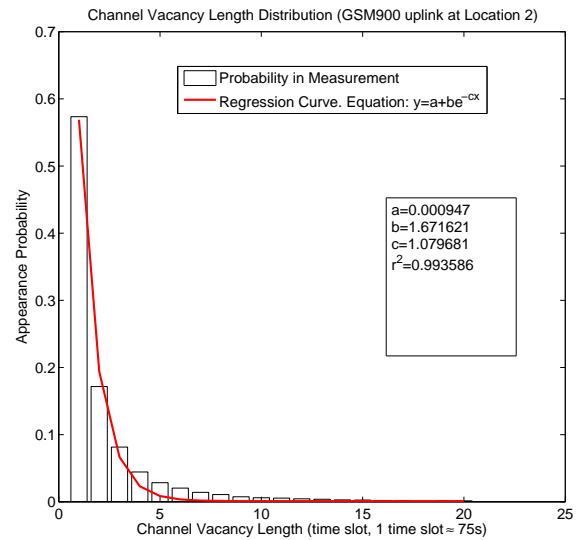


Figure 5: Channel Vacancy Duration (*CVD*) distribution (discrete) at Location 2.

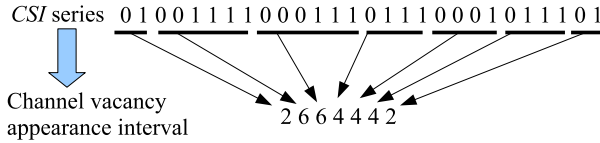
0's. We collect the duration of each such interval, a process (following the thresholding) illustrated in Figure 4.

On average each channel *CSI* time sequence (more than 8000 time slots) contains on the order of hundreds of channel vacancies. This sample size turns out to be too small to derive the *CVD* distribution. To increase this sample size we collect *CVD*s across all channels within the same service. This is done based on the observation that spectrum usages of channels within the same service are statistically very similar (shown in Section V.B). For example, spectrum usages in channels within GSM900 uplink service (885-915MHz) are nearly the same in terms of occupancy, periodicity, average energy level, etc. This gives us enough samples to obtain the empirical distribution of channel vacancies.

Figure 5 shows the probability distribution (histogram) of the *CVD* in GSM900 uplink service at Location 2. We then apply the least-square regression analysis to this data, as shown by the curve. The significance of the regression is measured by the coefficient of determination  $r^2$ , defined as:  $r^2 \equiv 1 - \frac{\sum_i (y_i - \bar{y})^2}{\sum_i (y_i - f_i)^2}$ , where  $y_i$  is the sample value with mean  $\bar{y}$  and  $f_i$  is the modelled/fitted value.

**Table 3: Channel vacancy duration distribution regression results at Location 2. Regression equation:  $y = a + be^{-cx}$**

Service	$a$	$b$	$c$	$r^2$
GSM900 uplink	0.001887	1.740828	1.086233	0.993586
GSM900 downlink	0.000883	1.203442	0.911078	0.987065
GSM1800 uplink	0.00046	1.044305	0.873491	0.981235
GSM1800 downlink	0.000289	2.239406	1.307285	0.993754
CDMA uplink	0.000937	0.355216	0.424722	0.947483
CDMA downlink	0.003895	2.197034	1.305444	0.991024
ISM	0.000187	1.001091	0.748866	0.995018
TV1	0.000577	1.014972	0.849229	0.982828
TV2	0.00056	0.776721	0.732062	0.977416
TV3	0.000263	1.040206	0.882333	0.976712
TV4	0.000187	1.213682	0.982802	0.977935



**Figure 6: Extract CVAI from CSI series.**

As shown the  $CVD$  distribution is very well approximated ( $r^2 > 0.99$ ) by an exponential-like distribution  $y = a + be^{-cx}$ . We repeated this exercise in all the services (GSM900 / 1800 uplink / downlink, broadcasting TV, CDMA, ISM) at all 4 locations and obtained similar results. The regression results at Location 2 are showed in Table 3, where  $y$  denotes  $\Pr[CVD = x]$  and  $x = 1, 2, 3, \dots$  time slot(s).

We also analyzed the following two similarly defined quantities. The first is the distribution of the channel occupancy durations ( $COD$ ), a channel occupancy being a complete interval of consecutive 1's in a  $CSI$  series. The second is the distribution of the channel vacancy appearance interval ( $CVAI$ ), which is the time interval from the start time of a channel vacancy to the start time of the next channel vacancy. This is illustrated in Figure 6. As can be seen,  $CVAI$  is a measure of how often a channel vacancy occurs. It turns out that both  $COD$  and  $CVAI$  are well approximated (with  $r^2 > 0.9$ ) by the same exponential-like distribution shown for  $CVD$ .

It should be noted that  $y = a + be^{-cx}$  has an exponential tail, but is *not* an exponential distribution. A direct consequence of this is that it does not have the memoryless property, i.e., how long a channel is going to remain in a certain state is a function of its history, rather than being independent of it. This latter independence assumption has been commonly used in channel access studies, see for example [14, 17, 13]. More precisely, these studies assume a two-state Markov chain model for the channel (i.e., an Eliot-Gilbert model). This channel model implies that the duration of consecutive 0's or 1's are geometrically distributed

(the discrete equivalent of an exponential distribution), and that these durations are independently distributed. Our results here indicate that such an assumption is inaccurate, and there is significantly more memory in the channel state information.

Specifically, the two-state Markov chain model implies that

$$\Pr[CSI(t+1, c)|CSI(t, c)] = \Pr[CSI(t+1, c)|CSI(t, c), CSI(t-1, c), CSI(t-2, c), \dots]$$

However, our data suggests for example in the GSM1800 uplink band at Location 2, that

$$\Pr[CSI(t+1, c) = 0|CSI(t, c) = 0] = 0.918953, \text{ but} \\ \Pr[CSI(t+1, c) = 0|CSI(t, c) = 0, CSI(t-1, c) = 1] = 0.55454.$$

This shows that the  $CSI$  is highly history dependent, a feature that cannot be captured by this type of 1st order Markov model. We tried using higher order Markov models, by defining a higher-dimensional state space (a higher-dimension state consists of a sequence of channel states, which results in an increase in the number states), without much success. This indicates that the channel state information possess some far richer properties. Technically, any discrete system can be modeled as a Markov chain provided we embed sufficient memory into the state, but the resulting expansion in the state space is in general computationally prohibitive. In Section VI we use a frequent pattern mining technique to get around this problem. This technique exploits the temporal and spectral correlation in  $CSIs$  and provides accurate prediction.

## 4. SERVICE CONGESTION RATE

$CVD$  provides long-term average information for a single channel. On the other hand, we often also need a real-time measure that tracks the time-varying channel availability. For example, suppose that a secondary user needs to choose one service from GSM900 uplink and TV2 for dynamic accessing for the next several time slots. It knows that the overall occupancy of these two services over one day is both 70% and the  $CVD$  distributions of these two services are nearly identical. Under such average measures, there is no difference between these two choices. However, if the user is able to track the short-term availability, then one may have a clear instantaneous advantage over the other. Below we define such a measure referred to as the service congestion rate ( $SCR$ ).

$SCR(t, S) = (\text{number of busy channels in } S \text{ at time } t) / (\text{total number of channels in } S)$ . Equivalently,  $SCR(t, S) = \sum_{c \in S} CSI(t, c) / n$ , where  $n$  is number of channels in the service  $S$ .

$SCR$  is thus a measure of the level of congestion in a service.  $SCR$  is a value ranging from 0 to 1. The larger the  $SCR$  of a service is, the fewer idle channels there are, and the more busy channels there are.

$SCR$  provides us with real-time information on spectrum occupancy status to make decisions on dynamic access adaptively. Figure 7 shows the  $SCR$  series of service GSM1800 uplink and GSM900 uplink at Location 2. We can see that the  $SCR$  series is cyclic in its outline with a period of one day. What's more interesting is that the  $SCR$  series of the two services are highly correlated: the rises and drops are very much in synchrony. We will give a more quantitative analysis in the next section.

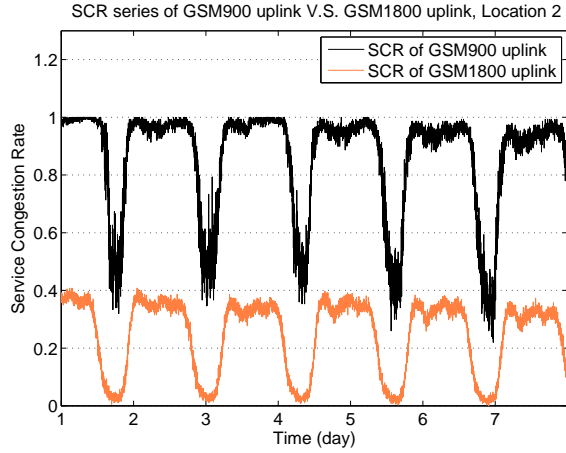


Figure 7: *SCR* series at Location 2. GSM1800 uplink vs. GSM900 uplink.

## 5. SPECTRUM CORRELATION ANALYSIS

The more we know about spectrum usage characteristics (of the primary users), the better predictions we can make about the spectrum opportunity, and the better we can make dynamic spectrum sensing and access decisions. Much of this predictive power lies in the temporal, spectral, and (sometimes) spatial dependence of spectrum usage. For instance, if everything is independently distributed, then knowing the past does not offer more information for the future. On the other hand, Figure 7 shown in the previous section suggests that measuring/sensing channels in GSM900 uplink provides ample information about channel availability in GSM1800 uplink. We thus set out to take a more in-depth look at the dependence characteristics of our data sets in this section. Specifically, we will analyze the temporal, spectral, and spatial correlation of the *CSI* series and the *SCR* series, respectively.

We will use the following two measures of correlation, the first one defined for two random variables and the second one defined for two 0-1 random sequences. The correlation coefficient  $\rho_{X,Y}$  between two random variables  $X$  and  $Y$  with sample mean  $\mu_X$  and  $\mu_Y$  and sample standard deviations  $\sigma_X$  and  $\sigma_Y$  is defined as:

$$\rho_{X,Y} = \frac{\text{cov}(X,Y)}{\sigma_X \sigma_Y} = \frac{E((X - \mu_X)(Y - \mu_Y))}{\sigma_X \sigma_Y} \quad (1)$$

where *cov* is the covariance operator. This coefficient ranges between -1 and 1, extreme values indicating  $X$  and  $Y$  are (inversely) fully correlated. In general correlation is considered high (i.e., one random variable proving a lot of information about the other) when the absolute value of the coefficient is closed to 1.

The correlation between two discrete-time 0-1 series  $X(t)$  and  $Y(t)$  are defined as follows:

$$\text{Corr}_{X(t),Y(t)} = \frac{\sum_t I\{X(t) = Y(t)\} - \sum_t I\{X(t) \neq Y(t)\}}{\sum_t I\{X(t) = Y(t)\} + \sum_t I\{X(t) \neq Y(t)\}} \quad (2)$$

where  $I\{A\}$  is the indicator function:  $I\{A\} = 1$  if  $A$  is true and 0 otherwise. The two summations in the above equation are the total number of positions that the two sequences

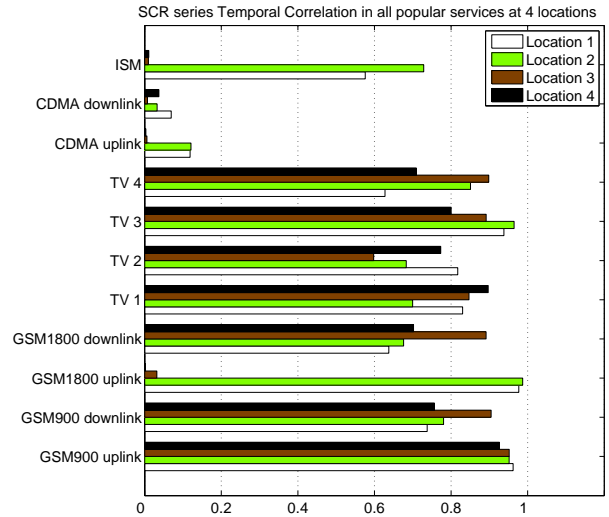


Figure 8: Temporal correlation at all locations.

coincide and differ, respectively. This is commonly used for evaluating the correlation between two binary sequences.

### 5.1 Temporal Correlation

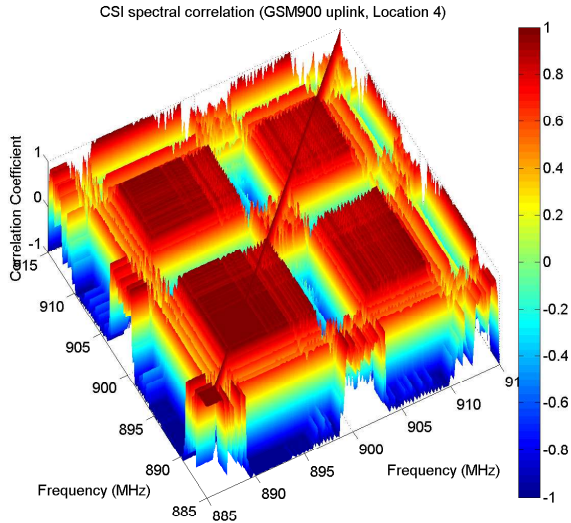
To study the temporal correlation within *CSI* and *SCR* series, we first divide an entire (over 7 days) *CSI* or *SCR* series evenly into 7 subsequences, one per day. The *SCR* subsequences are real-numbered. Treating each subsequence as a collection of samples of the same random variable, we can cross correlate any two subsequences using Eqn (1). This results in 21 ( $C_7^2$ ) temporal correlation coefficients and the final result is the average of these values. The *CSI* subsequences are 0-1 valued, and we cross correlate any two using Eqn (2). Again this results in 21 coefficients and the final result is the average.

Figure 8 shows that for most services at all locations, the temporal correlation of *SCR* within a service is significant (on average  $> 0.7$ ), especially for popular services like GSM and TV broadcast. This is easily explained by noting that the collective utilization of a certain service follows a clear daily pattern, thus the correlation between any two days is quite high.

There are a few exceptions to this:

1. The temporal correlation within CDMA service is rather low. This is due to the unique characteristics of CDMA signals: their presence adds relatively little energy to the noise floor, and therefore our simple thresholding technique is not very effective in this case. There are well-documented approaches to detect CDMA signals (see e.g., [3]), but were not used in this study due to complexity issues.

2. The temporal correlation in GSM1800 uplink and ISM is quite low at Locations 3 and 4. This is because these two locations have fewer cell phone users and GSM900 is sufficient for cellphone communication (thus GSM1800 uplink is not used), and there is virtually no WiFi presence. As a result GSM1800 uplink and ISM channels contain mostly noise at these locations. By contrast, the GSM1800 downlink is actually utilized at these locations, e.g. used for synchronization.



**Figure 9: Spectral Correlation Coefficients of *CSI* series within GSM900 uplink at Location 4.**

In contrast to the generally high temporal correlation between the *SCR* series, our results are less conclusive about the *CSI* series. The temporal correlation coefficients for the *CSI* series do not seem to follow a clear pattern (which is why no figure is shown here for the *CSI* series). Our explanation is that while the spectrum utilization within a service follows clear daily patterns due to collective consumer behavior, the individual channel's short-term (in time slots) states fluctuates.

This perhaps highlights the difference between the macroscopic behavior (*SCR*) and the microscopic behavior (*CSI*) of spectrum utilization, where a pattern emerges when the system is viewed as a whole, but not necessarily so at a microscopic level.

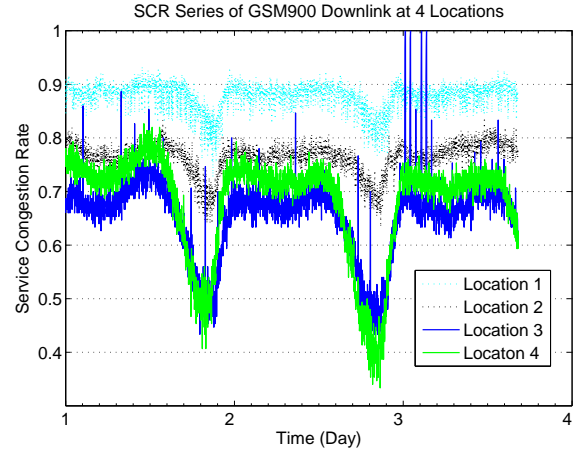
## 5.2 Spectral Correlation

We next take the *SCR* and *CSI* series and cross correlate them with their counterparts from a different service and different channel within the same service, using Eqn (1) and Eqn (2), respectively.

Figure 9 shows the *CSI* correlation coefficients between every two channels in the GSM900 uplink at Location 4. We see that these coefficients are extremely high for almost every two channels within the same service. This is because in most cases the channels are either all busy or all idle. There are also cases where the spectral correlation coefficients are closed to -1. This is because some channels are always idle while some others are always busy. For instance, there are channels in GSM that are kept idle to avoid inter-channel interference. These results are representative of what we found in other services.

Table 4 shows the spectral correlation coefficients between two *SCR* series at Location 1; these results are also representative of what we found at the other locations.

From the results shown in Table 4, we see that there is significant correlation among these services, for none of the coefficients falls below 0.55, even when between a broadcasting TV service and a GSM service. In addition, services of



**Figure 10: *SCR* Series of GSM900 Downlink at 4 Locations.**

the same type are particularly correlated, as high as 0.952 in the case between GSM900 uplink and GSM1800 uplink.

## 5.3 Spatial Correlation

Figure 10 shows 4 *SCR* series of the same service (GSM900 downlink) at all four locations. At a high level, these series appear all correlated with each other; they share common changes in value. In particular, Locations 1 and 2 are very similar, up to a constant shift, and Locations 3 and 4 are very similar, also up to a constant shift. This suggests spatial correlation across different locations. We thus cross correlate *SCR* / *CSI* series from the same service / channel at different locations.

Table 5 shows the spatial correlation coefficients of the *SCR* series in GSM900 downlink service among four locations. These are very high and none of the values falls below 0.8. It appears that within the same service, the spectrum utilization is highly correlated across different locations and different types of locations.

For other services the results are quite similar and are thus not presented separately. For instance between Locations 1 and 2, the spatial correlation coefficient of *SCR* series is as high as 0.962.

The reason for such high correlation is because for the same service, such as GSM voice calls, subscribers at different locations share common behavioral pattern (e.g., same peak calling hours of the day), even though the actual *SCR* values are different.

As in the temporal correlation case, the *CSI* series do not appear to have a clear spatial correlation pattern, for the same reason mentioned in Section 5.1.

## 5.4 Summary

To summarize this section, we have found high correlation along temporal / spectral / spatial dimensions for the *SCR* series, as well as high spectral correlation between *CSI* series within the same service. These results provide motivation and ground for building algorithms and models that exploit such correlation relationship and can better predict spectrum opportunity. We present such a methodology in the next section.

**Table 4: Spectral Correlation Coefficients of SCR at Location 1**

	GSM900UP	GSM900DN	GSM1800UP	GSM1800DN	TV1	TV2	TV3	TV4
GSM900UP	1.000							
GSM900DN	0.873	1.000						
GSM1800UP	0.952	0.832	1.000					
GSM1800DN	0.855	0.747	0.827	1.000				
TV1	0.674	0.616	0.713	0.636	1.000			
TV2	0.730	0.669	0.700	0.690	0.634	1.000		
TV3	0.789	0.742	0.809	0.710	0.833	0.711	1.000	
TV4	0.588	0.581	0.557	0.566	0.655	0.567	0.721	1.000

## 6. PREDICTION USING FREQUENT PATTERN MINING (FPM)

The correlation structure presented in the previous section suggests that it can be exploited to help us better predict channel state or spectrum opportunity based on measurements made in the past, in adjacent channels, or at similar locations. More precisely, we are interested in the question of whether one could accurately predict the value of  $CSI(t, c)$  based on the knowledge of  $CSI(t - k, c')$ ,  $k > 0$ , and if so how many past observations (what values of  $k$ ) and over what set of channels (what values of  $c'$ ) are needed.

There are different approaches one could take to model such correlation. For instance, as pointed out in Section III, the memory in channel state information could conceptually be captured by a sufficiently high-ordered Markov chain (and one can use measurement data to collect statistics on the transition probabilities of this chain), but with significant technical difficulty due to the exponential increase in the state space.

To overcome this difficulty, in this section we present a technique based on frequent pattern mining (FPM) ([2, 12] and a survey [4]) through an efficient pattern identification process over the spectrum data. This technique generates predictions of future channel state based on a collection of past observation in a set of channels. A unique feature of this approach is that it automatically adjusts the algorithm to the appropriate size of past observations (both in time and in channels) based on the data set. This method along with our experimental results are detailed in the remainder of this section.

### 6.1 FPM and Prediction

We begin by illustrating how FPM can be used for spectrum usage prediction and the challenges in doing so. Suppose we know the  $CSIs$  of Channels  $c, c+1$  of previous 8000 time slots (from time slot  $t - 7999$  to  $t$ ) and we would like to predict the  $CSI$  of the next time slot of Channel  $c$  and  $c+1$  (i.e.,  $CSI(t+1, c)$  and  $CSI(t+1, c+1)$ ). The known  $CSIs$  can be written into a single matrix shown below:

$$\begin{bmatrix} a_{t-7999,c} & a_{t-7998,c} & \dots & a_{t,c} \\ a_{t-7999,c+1} & a_{t-7998,c+1} & \dots & a_{t,c+1} \end{bmatrix},$$

where  $a_{i,j} = CSI(i, j)$ .

Define a submatrix as a pattern if it appears no less than 200 times throughout the  $CSI$  series of these channels. For instance, if the submatrix  $\begin{bmatrix} 1 & 0 & 1 \\ 1 & 1 & 0 \end{bmatrix}$  appears 1000 times, it's considered a pattern. We may find another pattern  $\begin{bmatrix} 1 & 0 & 1 & 1 \\ 1 & 1 & 0 & 0 \end{bmatrix}$  which appears 990 times. Comparing these

**Table 5: SCR spatial correlation coefficients for GSM900 downlink among 4 locations**

	Loc 1	Loc 2	Loc 3	Loc 4
Loc 1	1.000			
Loc 2	0.833	1.000		
Loc 3	0.858	0.846	1.000	
Loc 4	0.854	0.880	0.909	1.000

two patterns we can predict that  $CSI(t+1, c) = 1$  and  $CSI(t+1, c+1) = 0$  with probability 99% (990/1000) if  $CSI(t-2, c) = 1, CSI(t-1, c) = 0, CSI(t, c) = 1, CSI(t-2, c+1) = 1, CSI(t-1, c+1) = 1$ , and  $CSI(t, c+1) = 0$ .

Clearly this prediction method needs to successfully handle two issues: the first is to find frequent patterns, referred to as frequent pattern mining. The second issue is to find associations among these patterns, referred to as pattern association rules mining.

In our setting the dimension (number of rows and columns) of the patterns of interest are not fixed in advance, i.e., we do not know in advance how much history and how many neighboring channels are needed in order to have accurate prediction. Rather, this has to be learned during the mining process. This 2-D (of patterns) learning element is a unique challenge in our mining process, compared to existing FPM literature, e.g., [2, 12, 4]. In addition, in all these studies the patterns are 1-D and can be written in a row, although the data sets can be in multiple rows. In our problem, the patterns are in 2-D, which is another unique challenge. To summarize, both the width and the height of the patterns are variable, and their appropriate sizes need to be automatically identified in this process.

In the following we will refer to our problem as a FPM-2D problem.

### 6.2 FPM-2D Problem Definition

The goal of the FPM-2D problem is to find all relevant 2D patterns. Once this is achieved, it is fairly easy to compute the probabilities of future channel state (spectrum prediction). Table 6 contains a list of terminologies used in FPM-2D.

Formally, the FPM-2D problem is stated as follows: Given the input set  $\mathbb{M}$ ,  $min\_area$ , and  $min\_rep$ , find all valid block patterns and the corresponding match numbers.

### 6.3 Proposed Algorithm

We start by scanning the input matrix  $\mathbb{M}$  from left to right, top to bottom to find all the blocks with size  $x \times y$ . This is done for all  $x$  and  $y$  such that  $x \times y \geq min\_area$ .



**Table 6: Notations / concepts in FPM-2D**

Notation / Concept	Definition
$\Gamma$	The literals set. $\Gamma = \{0, 1\}$
$M$	An input matrix $M_{m \times n} = \begin{bmatrix} a_{1,1} & a_{1,2} & \dots & a_{1,n} \\ a_{2,1} & a_{2,2} & \dots & a_{2,n} \\ \dots & \dots & \dots & \dots \\ a_{m,1} & a_{m,2} & \dots & a_{m,n} \end{bmatrix}$ where $a_{i,j} \in \Gamma$ , $m$ : the number of adjacent channels, $n$ : the number of consecutive time slots
<i>block</i>	a submatrix of $M$
<i>subblock</i>	a submatrix of a block
<i>block area</i>	the number of elements in a block
<i>block pattern</i>	a block whose area $\geq \text{min\_area}$ . “pattern” and “block pattern” are used interchangeably.
<i>subpattern</i>	submatrix of a pattern
<i>matches (supports)</i>	If a pattern $P$ and a block $A$ are identical, we say $A$ is a match (support) of $P$ , or $A$ matches (supports) $P$
<i>match number</i>	the number of ALL matches of a pattern
<i>valid</i>	a pattern is valid if its match number is no less than $\text{min\_rep}$

We use a hash table to store the blocks for efficiently search, since it takes  $O(1)$  time to search an item in a hash table. A potential problem is the number of blocks might be too large; it is  $2^{x \times y}$  in the worst case. This problem is addressed by the following simple property.

Consider a block  $A_{x \times y}$ . We say block  $B$  is  $A_{x \times y}$ 's *parent block* if: a)  $B$  is  $A_{x \times y}$ 's subblock, b)  $B$ 's size is  $(x-1) \times y$  or  $x \times (y-1)$ , and c)  $B$ 's area is not less than  $\text{min\_area}$ . A simple yet key property concerning a valid pattern is that for any block  $A_{x \times y}$ , it has at most 4 parent blocks and it is a valid pattern only if all its parent blocks are valid patterns.

Thus, if any block has a parent block that is not valid, then we can simply skip this block because itself cannot be valid. By checking parent blocks, a large number of blocks can be ignored, which significantly reduces the memory consumption and improves the performance.

The pseudo code of the proposed algorithm is given in Algorithm 1. In Algorithm 1,  $T_{x,y}$  is the hash table to store patterns with size  $x \times y$ .

After all valid patterns have been identified, the prediction rules are extracted as follows. A prediction rule is defined as  $P_1 \rightarrow P_2$ , where  $P_1$  and  $P_2$  are all valid patterns.  $P_2$  has the form  $[P_1 \mathbf{V}]$ , where  $\mathbf{V}$  is a column vector  $(v_1, v_2, v_3, \dots, v_k)^T, v_i \in \Gamma$ . Thus  $P_1$  is one of the parent blocks of  $P_2$ . Let  $M(P_1)$  denote the match number of  $P_1$ , then the *transferring rate*  $R(P_1 \rightarrow P_2) = M(P_2)/M(P_1)$ . What this rule says is that if the current *CSI* appears to match  $P_1$ , then the *CSI* in the next time slot will match  $\mathbf{V}$  with probability  $R(P_1 \rightarrow P_2)$ . Clearly, a similar procedure can be used to predict the *CSI* over multiple future slots, by simply considering  $\mathbf{V}$  as multiple column vectors.

## 6.4 Experiment Result

To test our algorithm we split the measurement data into

---

### Algorithm 1 FPM-2D

---

```

for  $N=2$  to  $\infty$ :
    flag  $\leftarrow false$ 
    for each  $(x, y)$  s.t.  $(x + y = N, x \times y \geq \text{min\_area})$ :
         $T_{x,y} \leftarrow$  new empty hash table
        if  $T_{x-1,y}$  and  $T_{x,y-1}$  are both empty:
            continue;
        for each block  $B_{x \times y}$  in  $M$ :
            if one of  $B_{x \times y}$ 's parent blocks
            is not a valid pattern:
                continue
            if  $B_{x \times y}$  is in  $T_{x,y}$ :
                 $T_{x,y}[B_{x \times y}] \leftarrow T_{x,y}[B_{x \times y}] + 1$ 
            else:
                 $T_{x,y}[B_{x \times y}] \leftarrow 1$ 
        for each block  $P_{x \times y}$  in  $T_{x,y}$ :
            if  $T_{x,y}[P_{x \times y}] < \text{min\_rep}$ :
                remove  $P_{x \times y}$  from  $T_{x,y}$ 
        if  $T_{x,y}$  is not empty:
            flag  $\leftarrow true$ 
            output the valid patterns in  $T_{x,y}$  and
            the corresponding match numbers
        if flag ==  $false$ :
            break

```

---

two part, one as a training set on which we run Algorithm 1 and find the prediction rules, while the other as the testing set on which we apply the prediction rules and perform spectrum usage prediction. We set  $\text{min\_rep} = 200, \text{min\_area} = 4$ .

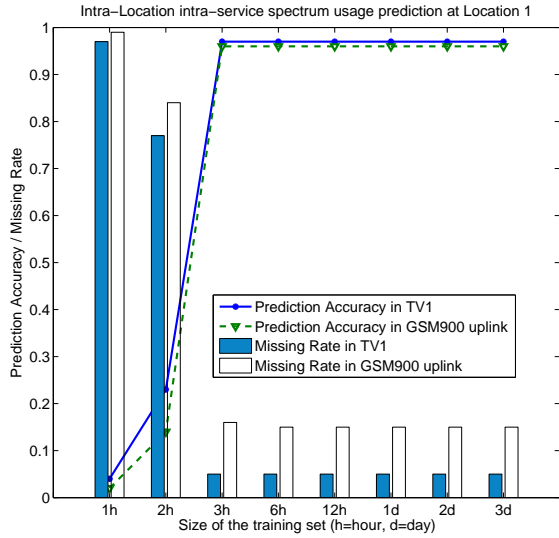
In our experiment we adopted the following prediction methods: a) We only consider those rules whose transferring rates are larger than 0.9. b) If the current *CSIs* appears to match the pattern  $P_1$  in a rule  $P_1 \rightarrow P_2$ , we predict the *CSIs* matches  $P_2$  in the next time slot. c) If the current *CSIs* do not match any patterns, we do not predict and count it as a miss.

We are interested in answering the following questions:

1. what is the prediction accuracy if the training set and corresponding testing set are from the same service (self-service prediction)?
2. what is the missing rate of the prediction?
3. can the mining result in one service be used to predict the *CSIs* in another service (cross-service prediction)?
4. can the mining result in a service at one location be used to predict the *CSIs* in the same service at a different location (cross-location prediction)?
5. how large the training set needs to be for accurate prediction?

We define prediction accuracy to be the ratio between the number of correctly predicted *CSIs* and the total number of predicted *CSIs*, and define missing rate as the ratio between the number of *CSIs* that cannot be predicted and the total number of *CSIs*.

We first study the case where the training set and the corresponding testing set are from the same service at Location 1, i.e., both from TV1 or both from GSM900 uplink. The training sets are *CSI* series over durations from 1 hour to



**Figure 11: The experiment results of intra-location intra-service spectrum usage prediction at Location 1. The prediction accuracy is larger than 0.95 if the training set size is no less than 3 hours.**

3 days. The testing sets are *CSIs* of the last 4 days. The results are shown in Figure 11. We observe that:

- The prediction accuracy is larger than 0.95, a very encouraging sign.
- The missing rate is around 5% for TV1 service, which is very low. It is higher, around 15% for GSM900 uplink. The reason why the missing rate on GSM900 uplink is higher than TV1 is that TV service is a pure broadcast service, while GSM service is an interactive service whose patterns are more complicated to match.
- The training set cannot be less than 2 hours. Otherwise FPM-2D cannot find sufficient prediction rules.
- A 3-hour training set appears sufficient and the performance of the algorithm saturates at this level. Beyond this threshold, more training data does not seem to help improve the prediction accuracy or reduce the missing rate.

For other services of Location 1, the results are similar except for the missing rate, which is listed in Table 7. We see that the prediction accuracy is consistently high but the missing rate varies from 4% up to 25%. We also give the overall occupancy of the services as a reference. If the overall occupancy is  $a$ , then the prediction does not help if its accuracy is lower than  $\max\{a, 1 - a\}$ . This is because we can always achieve this accuracy simply by guessing.

For comparison, we have also shown the prediction accuracy using the 1st-order Markov Chain model (1st MC), which is one of the most commonly used models in the existing papers [14, 17, 13]. We could see that the prediction accuracy of the 1st MC is only around 80%, which is much lower than that of FPM-2D, except for those services whose occupancy is high, in which case the prediction accuracy can be naturally high even by guessing.

**Table 7: The spectrum usage prediction results at Location 1. The training / testing sets are from the same service.**

Service	occupancy	1-st order Markov Prediction Accuracy	Miss rate	FPM-2D Prediction Accuracy
GSM900 downlink	85.1%	85.2%	11.8%	96.9%
GSM1800 uplink	60.3%	77.4%	24.8%	95.1%
GSM1800 downlink	30.2%	83.7%	16.2%	96.6%
TV2	92.1%	92.6%	5.4%	96.9%
TV3	44.5%	75.0%	4.2%	97.8%
TV4	41.9%	74.5%	6.3%	97.7%

**Table 8: The spectrum usage prediction results at Location 1. The training / testing sets are from different services.**

Training Set	Testing Set	Miss Rate	Prediction Accuracy
GSM900 downlink	TV1	66.1%	79.2%
TV1	GSM900 uplink	75.3%	80.4%
GSM900 uplink	GSM900 downlink	35.2%	86.4%
GSM900 downlink	GSM900 uplink	31.8%	87.4%

The results of the other locations are similar, and thus not repeated.

We next study the case where the training set (*CSIs* of 3 days) and the testing set (*CSIs* of 4 days) are from different services. The results are shown in Table 8.

We see that the accuracy of cross-service prediction is much lower than that of self-service prediction, and the missing rate is quite high. This is because the patterns in different services collide, i.e. patterns and prediction rules found in one service might lead to wrong prediction results in other services. This is another manifestation of the conclusion drawn earlier that the spectral correlation is high for channels within the same service but low across different services.

Consistent with earlier correlation result, we also observe that the prediction accuracy is high if we use the prediction rules at one location to predict the *CSIs* of the same service at another location, due to the high spatial correlation of

**Table 9: The cross-location spectrum usage prediction results.**

Service	Training Set	Testing Set	Miss Rate	Prediction Accuracy
TV1	Location 1	Location 2	5.7%	95.3%
TV1	Location 3	Location 4	7.3%	97.4%
TV1	Location 1	Location 3	6.5%	96.7%
TV1	Location 3	Location 1	7.7%	95.8%

channels within the same service. Table 9 Shows the experiment results of this cross-location self-service prediction.

To summarize this section, we conclude that:

1. The self-service self-location spectrum usage prediction accuracy is higher than 95%, which is significantly larger than that of the commonly used 1st-order Markov model.
2. The missing rate varies from 4% to 25%, an overall acceptable range.
3. The cross-service prediction accuracy ranges from 60% to 80%, much lower than the self-service prediction. The corresponding missing rate is above 30%, sometimes over 70%, which is too high.
4. The accuracy and missing rate of cross-location self-service prediction are nearly as high as that of self-location self-service prediction.
5. *CSIs* of 3 hours appear sufficient for training purpose.

## 7. DISCUSSIONS

In this section we briefly summarize how findings and results presented in previous sections may be used toward both the theory and practice in spectrum sensing and access within the context of cognitive radio networks.

Broadly speaking, these results contribute to two aspects of dynamic spectrum access: (1) the construction of better channel models (as a way of describing the spectrum usage of the primary users), that may be more generally applicable in other environments, and (2) the prediction of channel availability in a similar wireless spectrum environment.

Channel models are an essential component in an array of spectrum access studies, especially theoretical analysis. Our study has shown certain weaknesses of existing channel models (e.g., insufficient capture of history-dependence, inability to describe spectral and spatial dependence). Our results here can help build better channel models that more accurately reflect the primary users' activity. In particular, the statistics we collected on channel occupancy/vacancy, its rich dependency property, as well as the statistics on the *CSI* series may motivate the construction of certain type of discrete event models (e.g., a Petri net) to describe the channel behavior. This may allow us to model the memory structure as well as the spatial and spectral correlation while avoiding a large state space.

The frequent pattern mining technique introduced here can be a very powerful tool in analyzing spectrum usage data. For specific wireless environments where such data are available for training, we have shown that using this technique can generate very accurate predictions on channel availability (especially in the TV broadcast channels in our study). This allows a secondary user to make far better channel sensing and access decisions, and exploit much more effectively under-utilized spectrum opportunity.

## 8. RELATED WORKS

The Shared Spectrum Company (SSC) performed extensive spectrum measurements at 7 locations in the US and one outside the US between 2004 to 2007 [11, 10]. These measurements are all wide-band and over long periods of time. For instance, the measurement in Chicago scanned the energy level from 30MHz to 2900MHz and lasted 46

hours. The goal of these measurements is to gain a better understanding of the actual utilization of spectrum in rural and urban environments. To achieve this, the authors set two fixed thresholds for channels in higher and lower frequency bands, respectively, and considered a channel busy if the power level is above the corresponding threshold, and idle otherwise. According to their reports, among those 7 locations in the US, the lowest average occupancy is 1% at Greenbank, West Virginia while the highest is 17.4% at Chicago, Illinois.

In addition to SSC, there have been a few similar measurement studies recently. In 2008, Institute for Infocomm Research (I<sup>2</sup>R) published their spectrum measurement results in Singapore [7]. They scanned from 80MHz to 5850MHz for 12 weekdays. They found the average occupancy to be 4.54% and most of the allocated frequencies were heavily underutilized except the TV broadcast channels and cell phone channels. Similar results were reported from Auckland, New Zealand according to [1].

The above cited work primarily focused on collecting statistics on the average utilization of wireless spectrum, and they all confirmed that it is indeed heavily underutilized. Correlations in the temporal, spectral and spatial dimensions were not a focus in these studies.

There has also been work in exploring correlations. A spectrum measurement was carried out during the 2006 Football World Cup in Germany, in the cities of Kaiserslautern and Dortmund [6]. They found that the change of spectrum usage (energy level) was clearly related to specific events (football match). Moreover they investigated the autocorrelation structure of changes in energy levels. Later in 2007 another measurement was conducted in the US on the public safety band (around 800MHz) [8]. The authors collected data concurrently at two locations, with a total of 5 pairs of locations with distance ranging from 5 meters to a few kilometers. They investigated the adjacent channel interference and spatial correlation. They revealed that very different energy detection results were obtained at closely located detection stations (5 meters apart); this was attributed to the difference in sensitivity in the sensing devices used.

Compared to this set of studies, our analysis also explored spectral correlation, both within the same service and across services. The service congestion rate (SCR) is a unique notion that allows us to examine spectrum usage service by service. In addition, our measurement involves the most concurrent locations (4), is over a fairly long duration (7 days), and scans from 20MHz to 3GHz. This allowed us to conduct a very detailed analysis on both the first and second order statistics of these data sets.

## 9. CONCLUSIONS

In this paper we carried out a set of spectrum measurements in the 20MHz to 3GHz spectrum band at 4 locations concurrently in Guangdong province of China. Using these data sets we conducted a set of detailed analysis of the first and second order statistics of the collected data, including channel occupancy / vacancy statistics, channel utilization within each individual wireless service, and the temporal, spectral, and spatial correlation of these measures. Moreover, we also utilized such spectrum correlation to develop a 2-dimensional frequent pattern mining algorithm that can accurately predict channel availability based on past observations.

We believe our findings will spur more discussions on how to better model current spectrum utilization and help us design more efficient spectrum sensing and accessing schemes for secondary users.

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