

# Cryptanalysis of Two Lightweight RFID Authentication Schemes

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## Outline

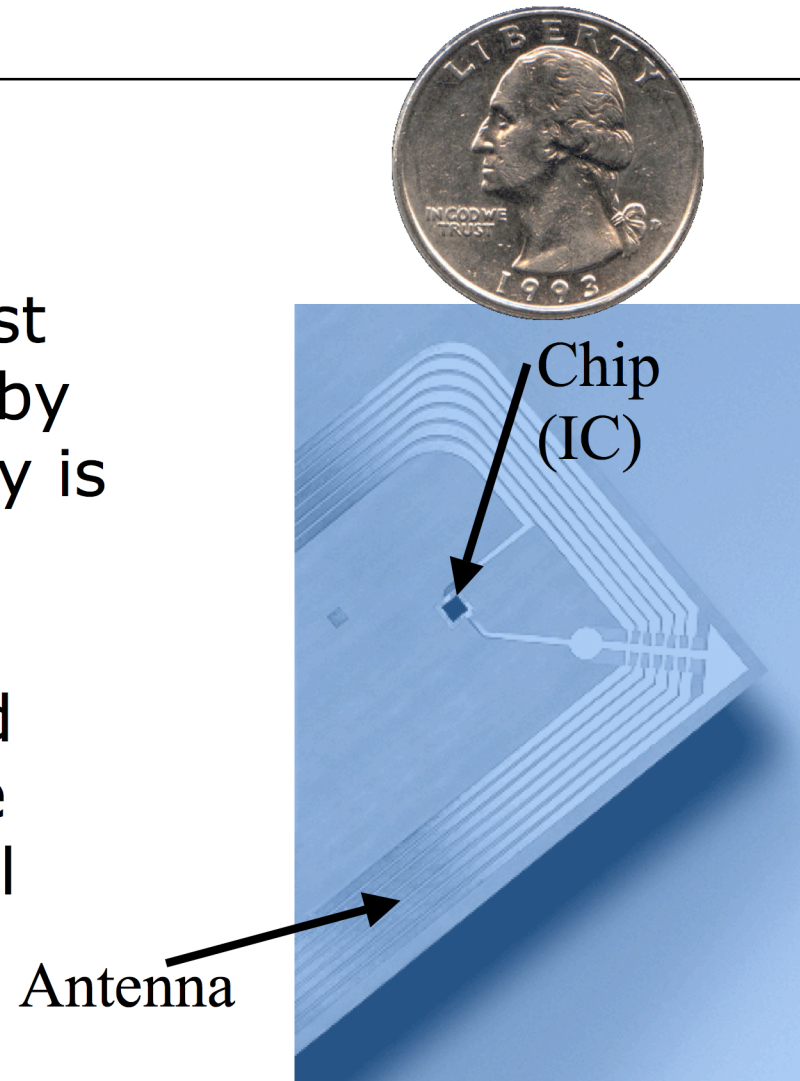
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- Introduction to RFID
- Original low-cost RFID authentication protocol
- Implementation Results
- Repeated Keys Attack
- Nibble Attack
- Suggestions for future protocols



## Introduction to RFID

- Radio Frequency Identification
- A radio signal is broadcast by a reader, interpreted by a transponder and a reply is returned to the reader.
- Tags are either active (possess a self-contained power source) or passive (powered solely by signal received from reader)



## Applications for RFID Tags

- Person Identification
  - Hospitals
  - Homes
  - Businesses
- Livestock Management
- Inventory Control
- Building Access Control



## Why Authentication for RFID Tags?

- Prevention of unauthorized communication
- Authorization of a tag by a reader
  - Detection of cloned/spoofed tags
  - Person identification
  - Theft prevention
  - Inventory control



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## Low Cost vs. Higher Cost

	Low Cost	Higher Cost
<b>Storage</b>	Few 100 bits	Few kB
<b>Computational Capabilities</b>	XOR, simple operations	RSA, AES, Triple DES
<b>Cost</b>	Few cents	Few dollars





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## Vajda and Buttyán Protocol 1

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- Challenge/Response Protocol
- Uses XOR operations -> lightweight
- Reader and Tag share secret
- Session key computed by “evolving” previous key

“Lightweight Authentication Protocols for Low-Cost RFID Tags” by I. Vajda and L. Buttyan. In UBICOMP, 2003.”

# Vajda and Buttyán Protocol 1

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# Vajda and Buttyán Protocol 1

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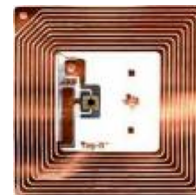
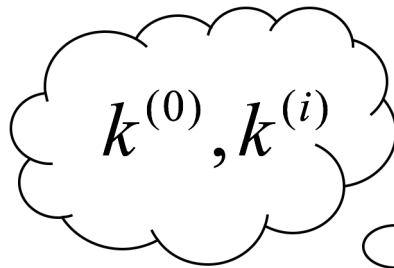
# Vajda and Buttyán Protocol 1

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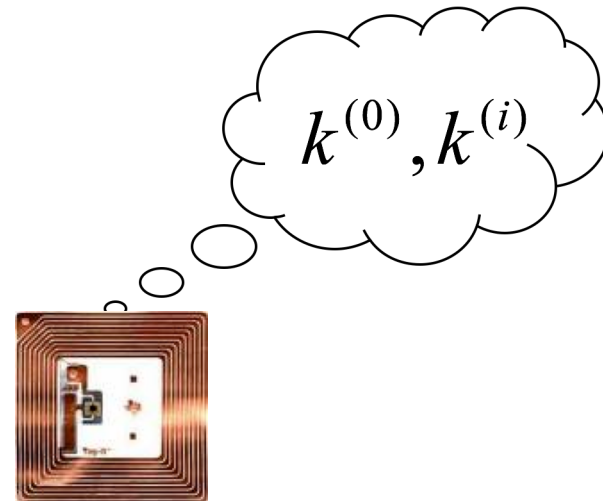
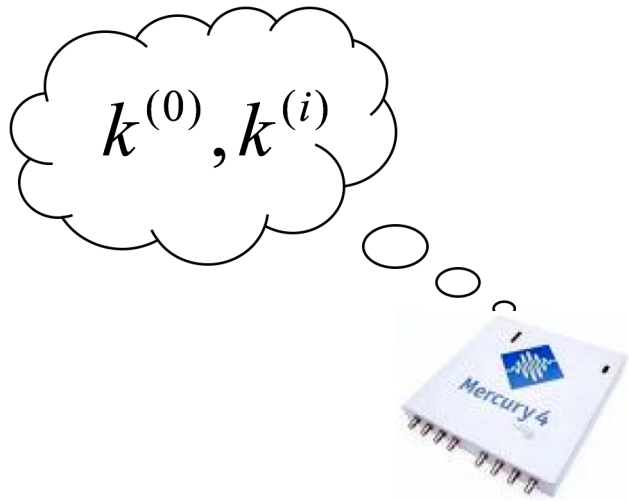
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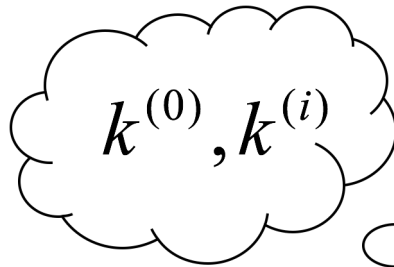
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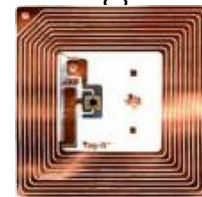
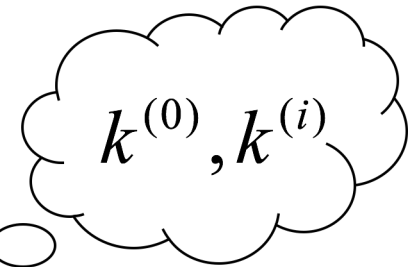
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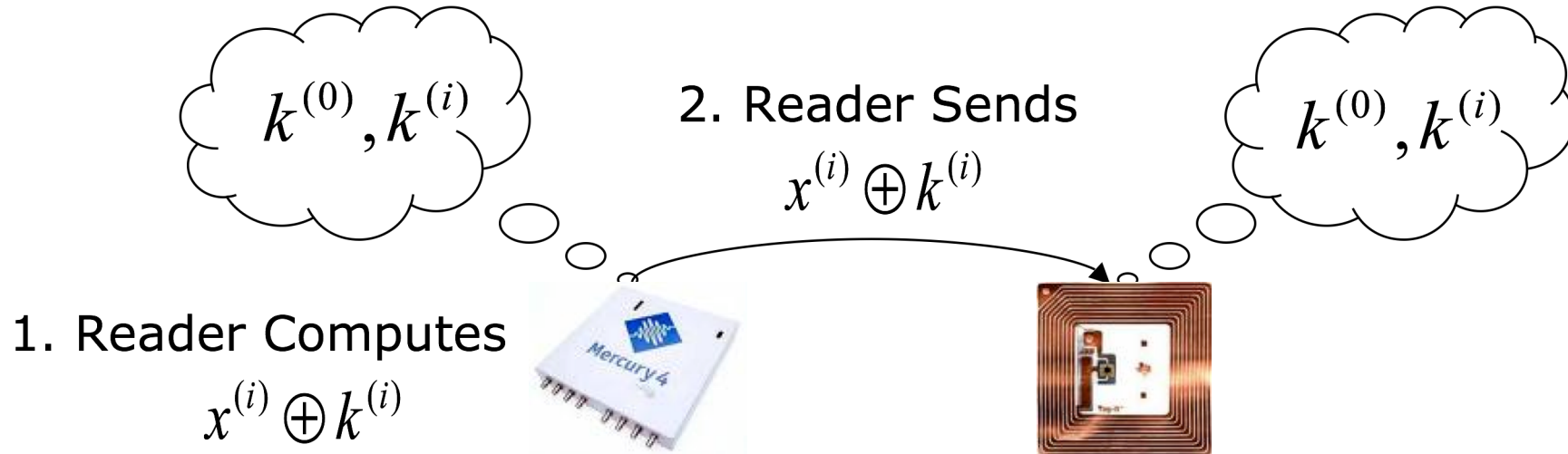


1. Reader Computes

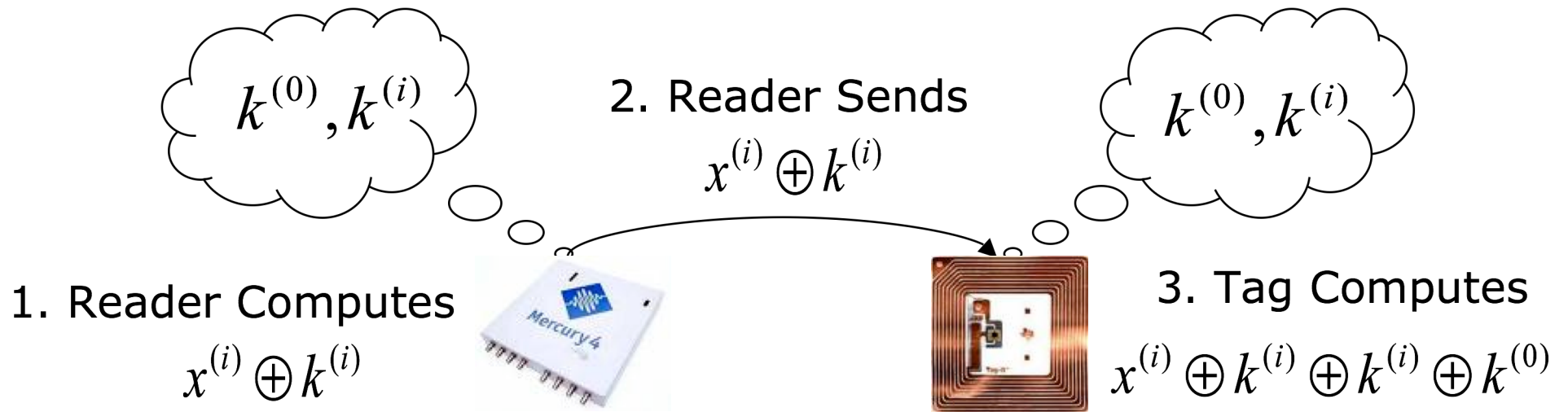
$$x^{(i)} \oplus k^{(i)}$$



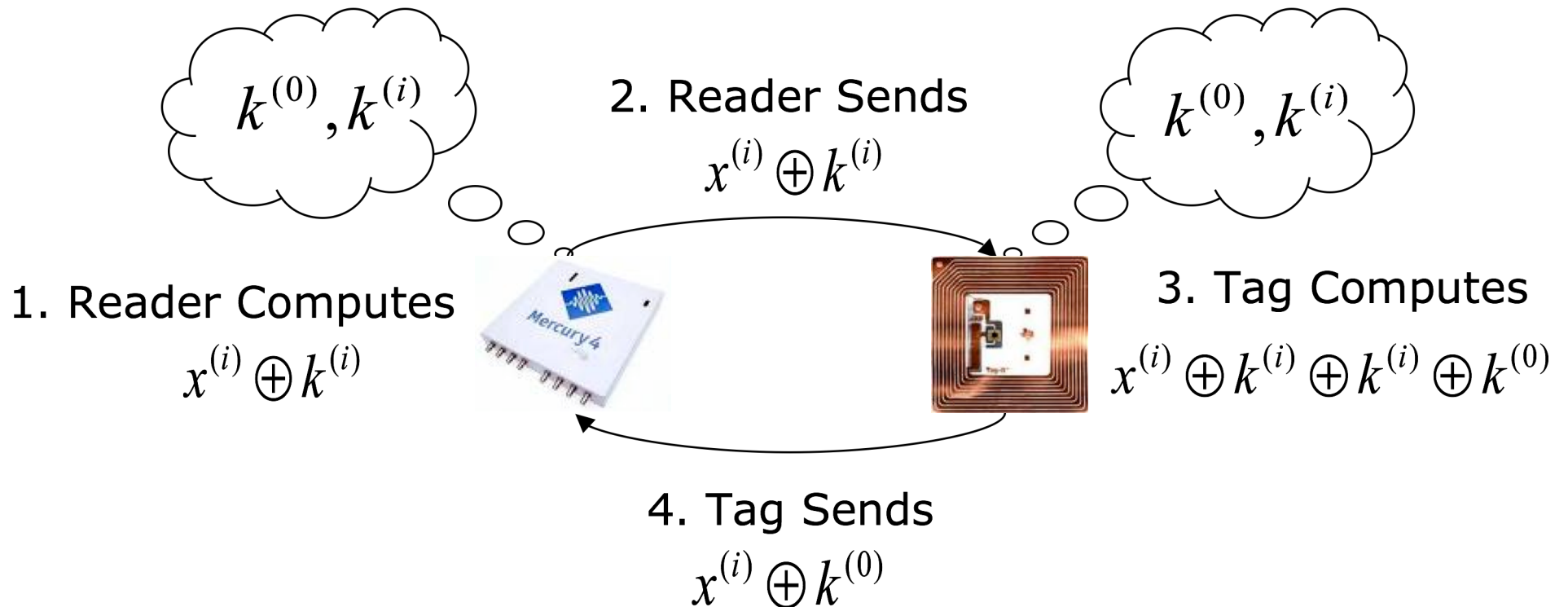
## Vajda and Buttyán Protocol 1



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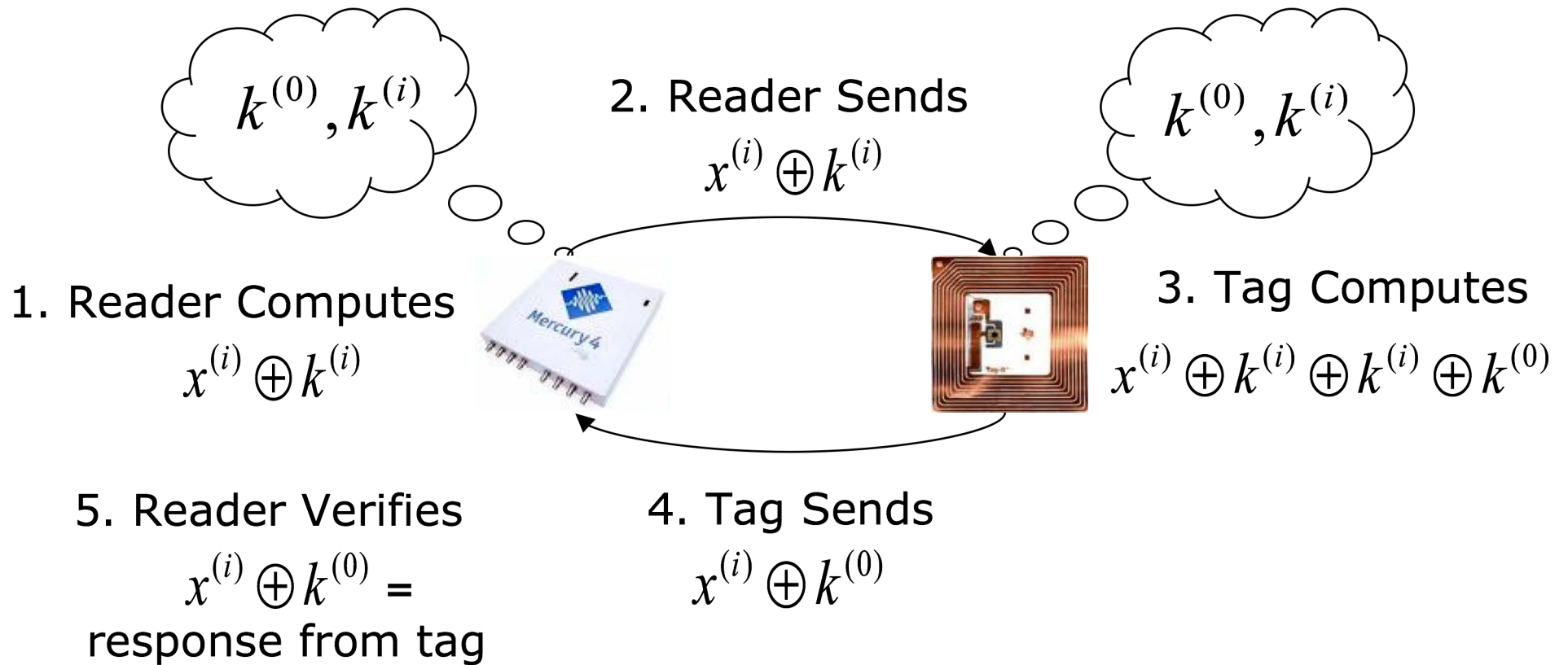


# Vajda and Buttyán Protocol 1





# Vajda and Buttyán Protocol 1



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- Introduction to RFID
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- **Implementation Results**
- Repeated Keys Attack
- Nibble Attack
- Suggestions for future protocols

## Implementation Results

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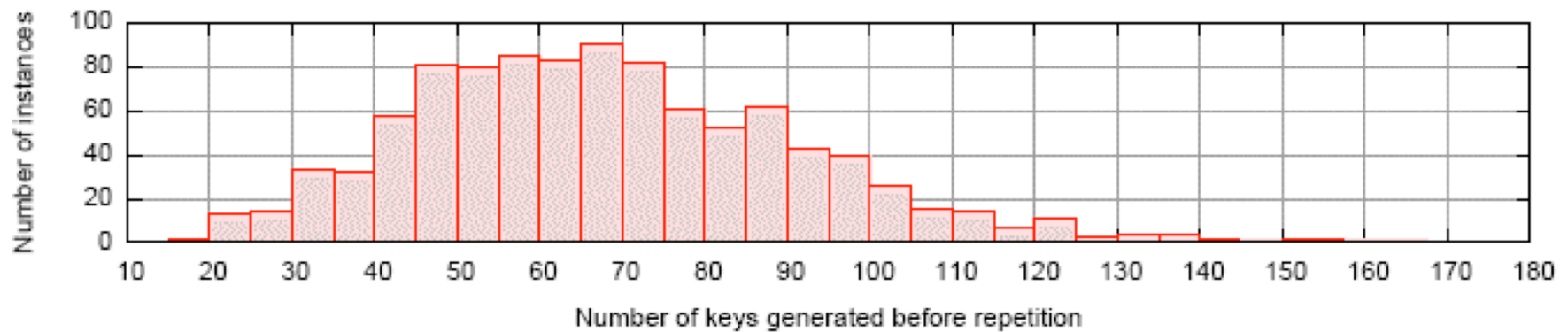
- 128-bit key length
- 1,000 trials with 10,000 sessions/trial
- After an average of 68 keys, the session key repeats
  - Average: 68.7%, cycle period = 2, i.e.  $k^{(i)} = k^{(i-2)}$
  - Minimum: 31.9%, cycle period = 1
  - Maximum: 0.1%, cycle period = 36

$$k^{(68)} = k^{(70)} \quad k^{(69)} = k^{(71)}$$

*ρ*

$$k^{(0)}$$

## Key Repetition



- 1,000 trials with random  $k^{(0)}$ 's execute until a key repeats
- Average is 68 transactions before keys repeat
- When keys repeat, they repeat (cycle) every 2 keys on average

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## Repeated Keys Attack

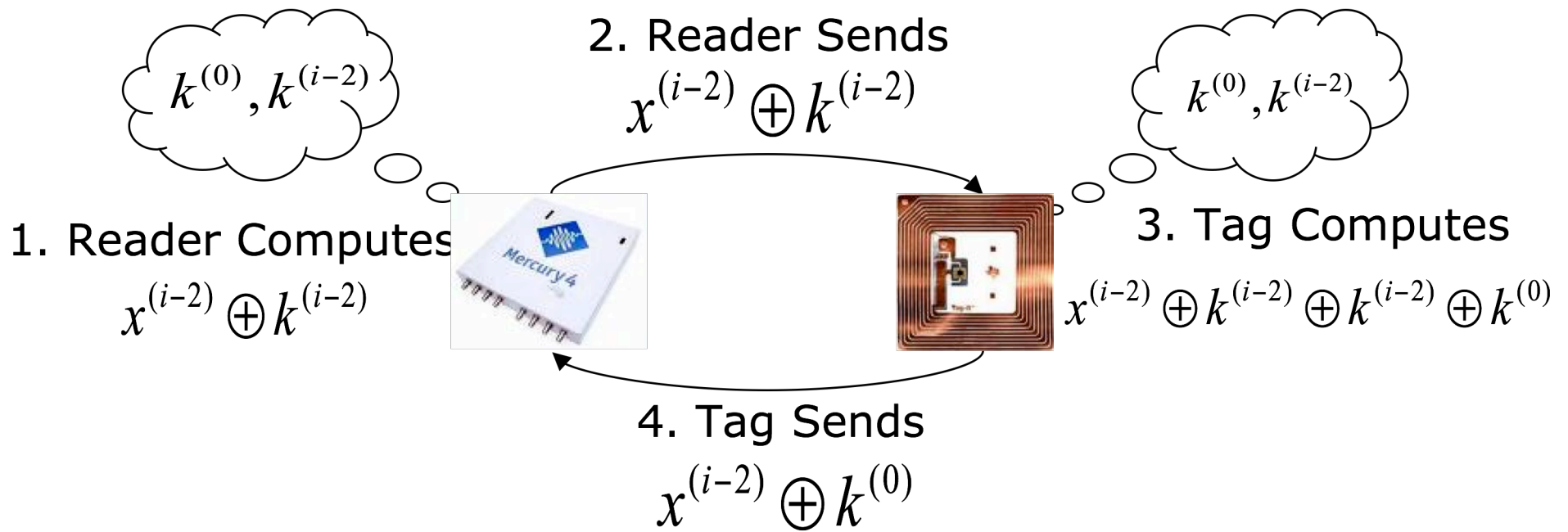
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- Can impersonate a tag
- Information is leaked by each transaction
- A passive eavesdropper can impersonate the tag in as few as 3 transactions, on average

# Repeated Keys Attack, Transaction $i-2$ $k^{(i)} = k^{(i-2)}$

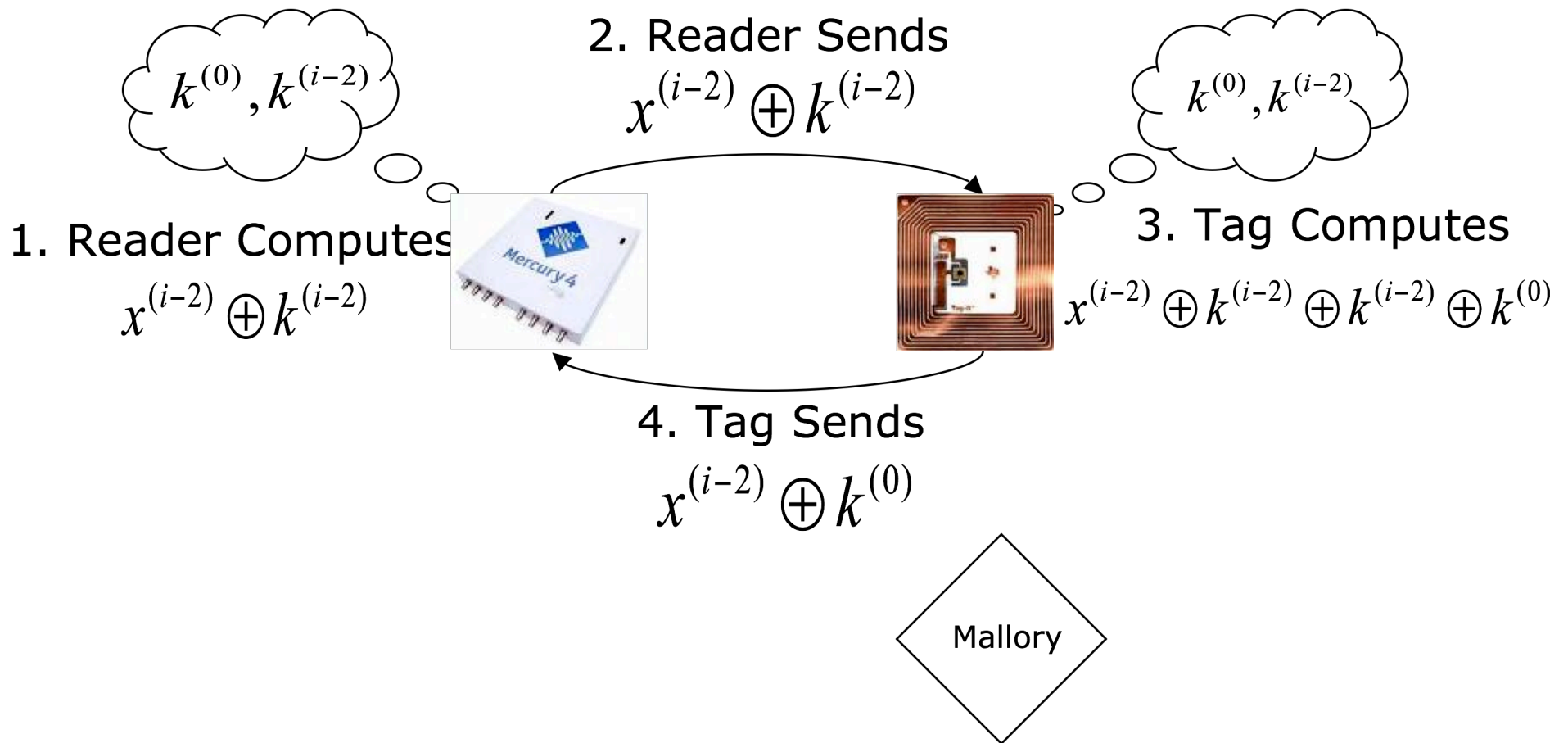
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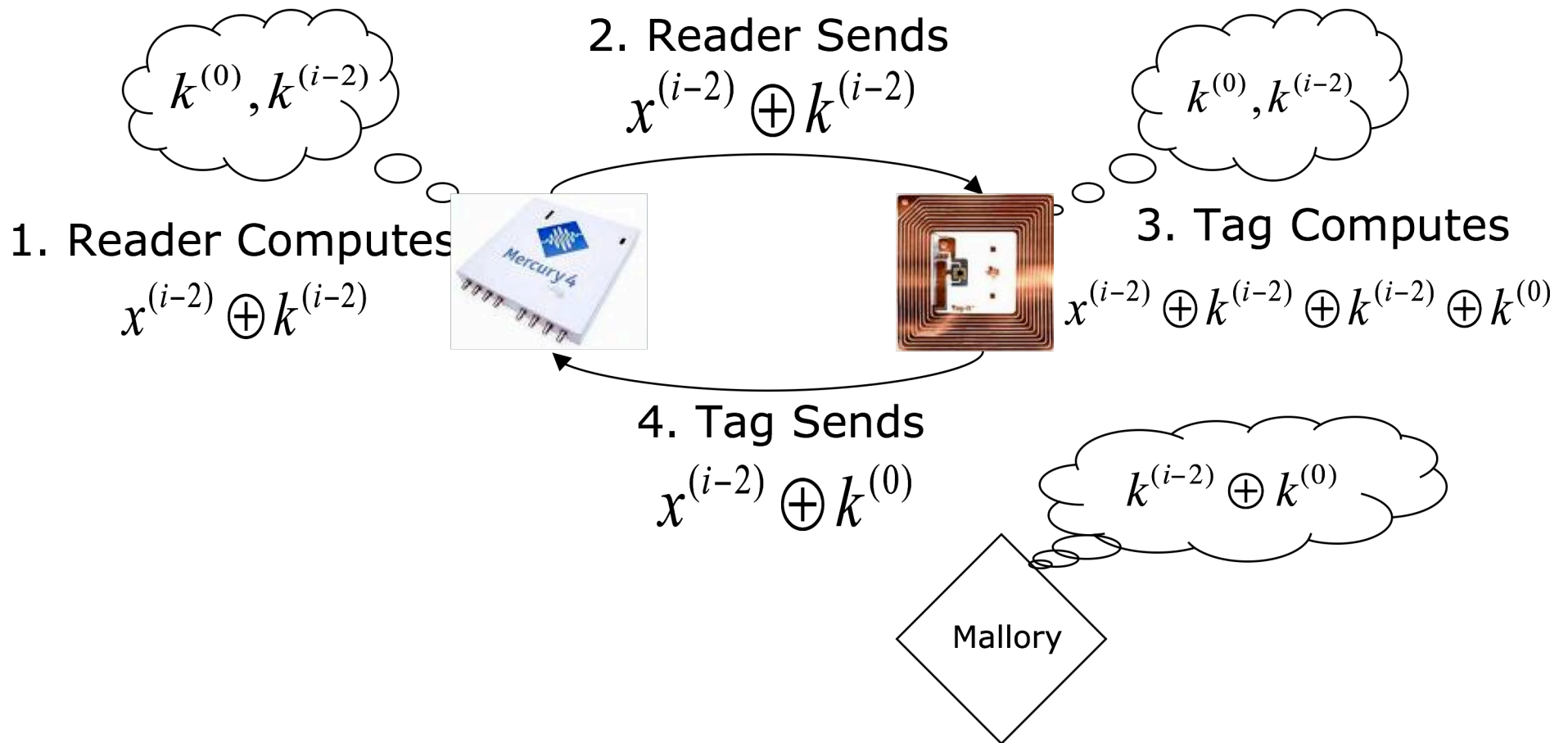




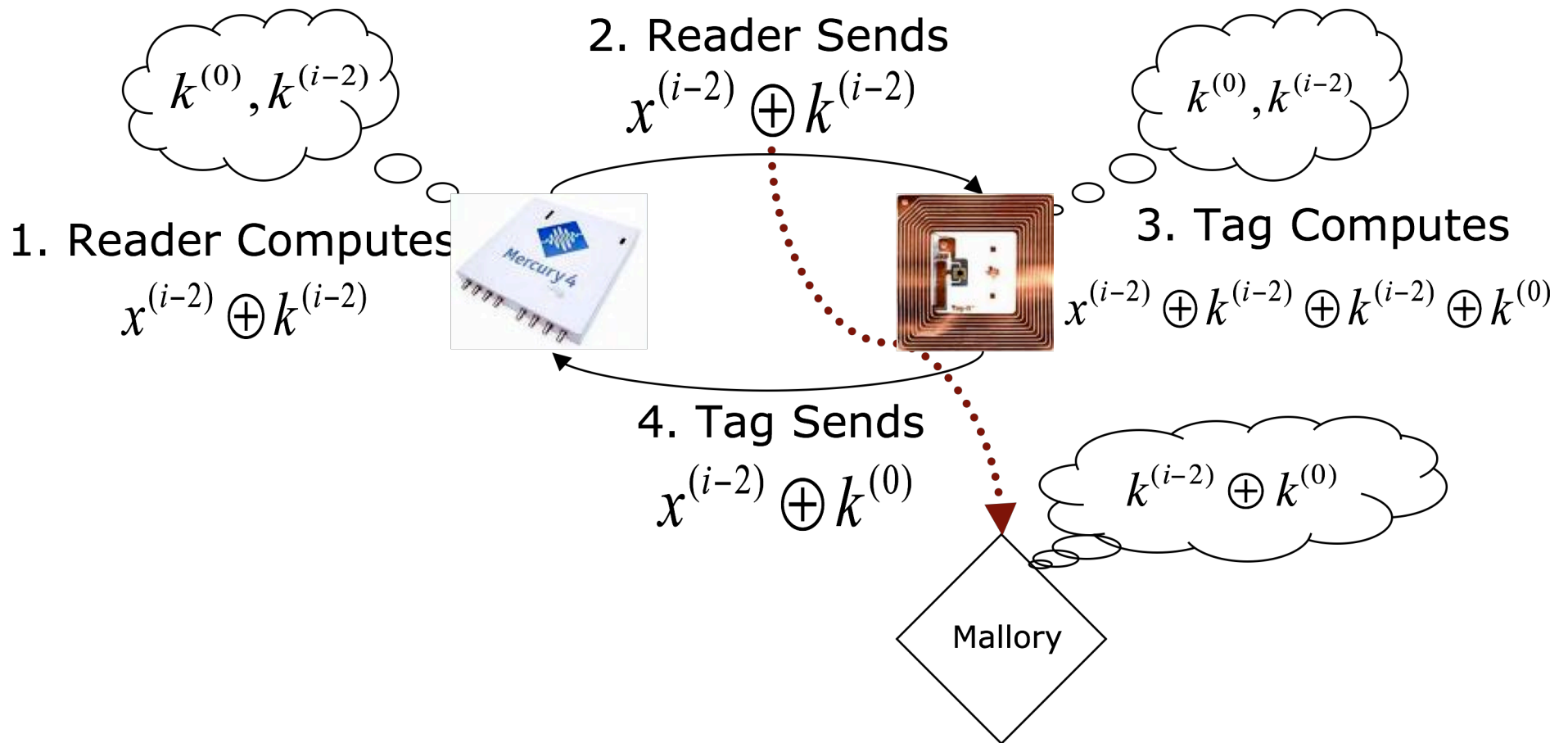
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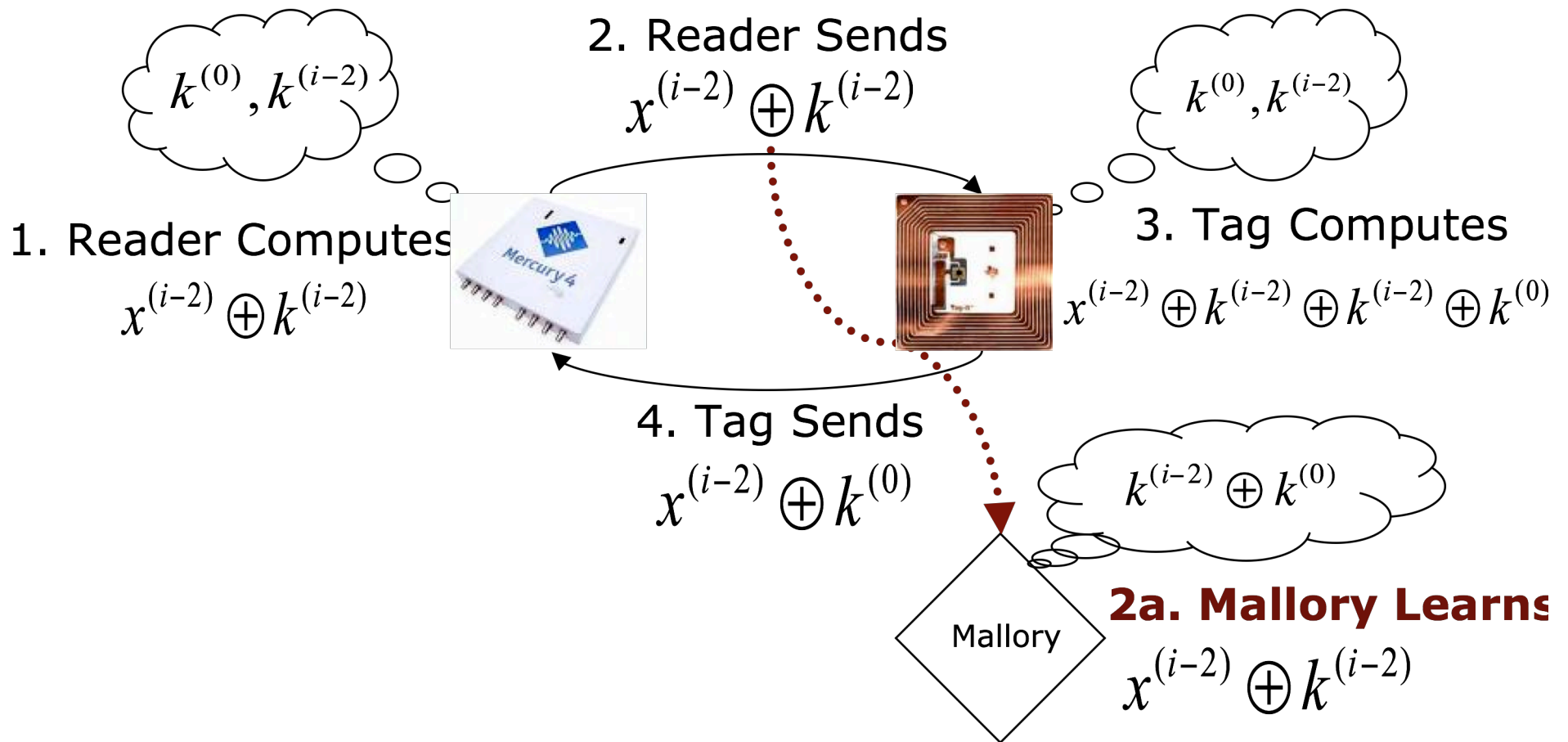
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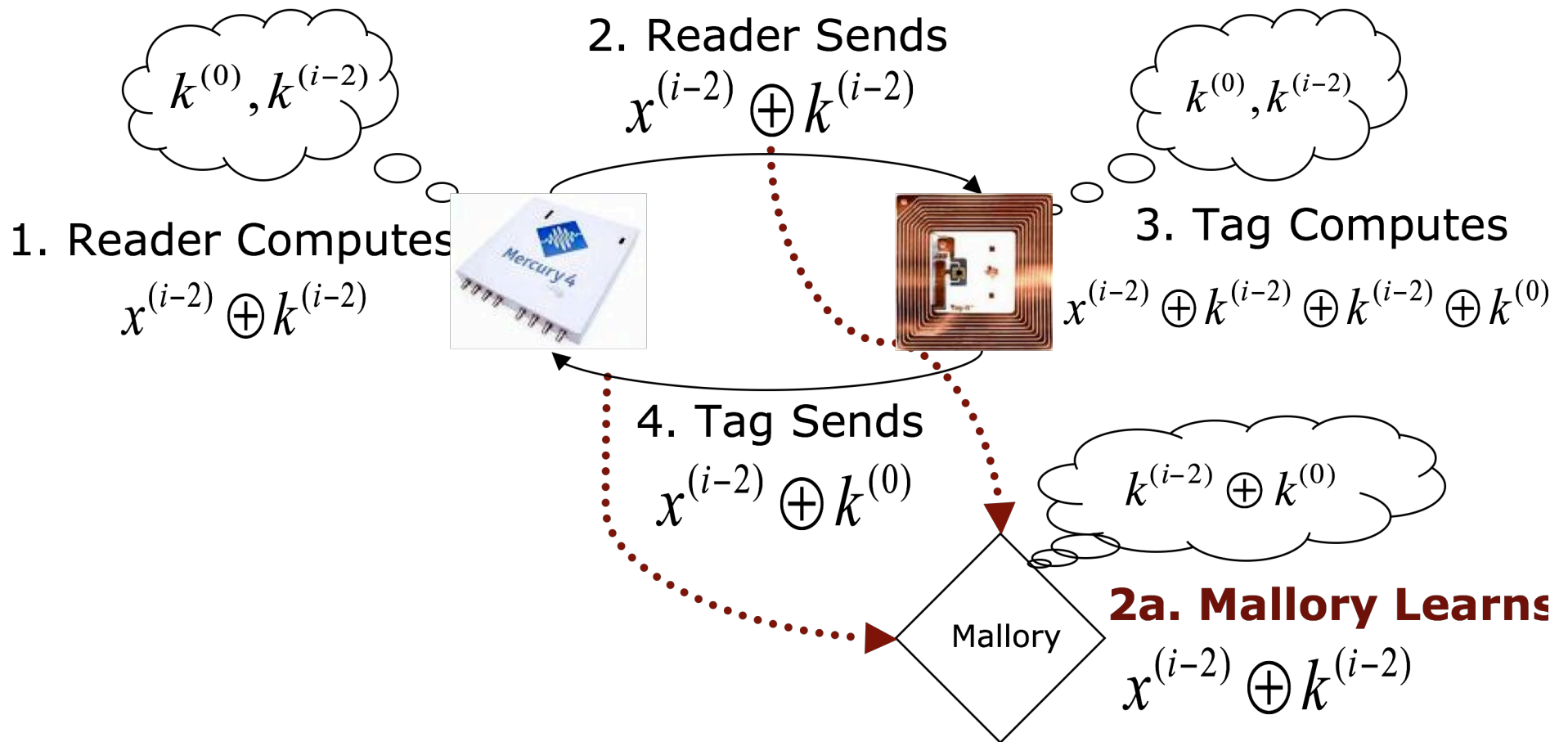
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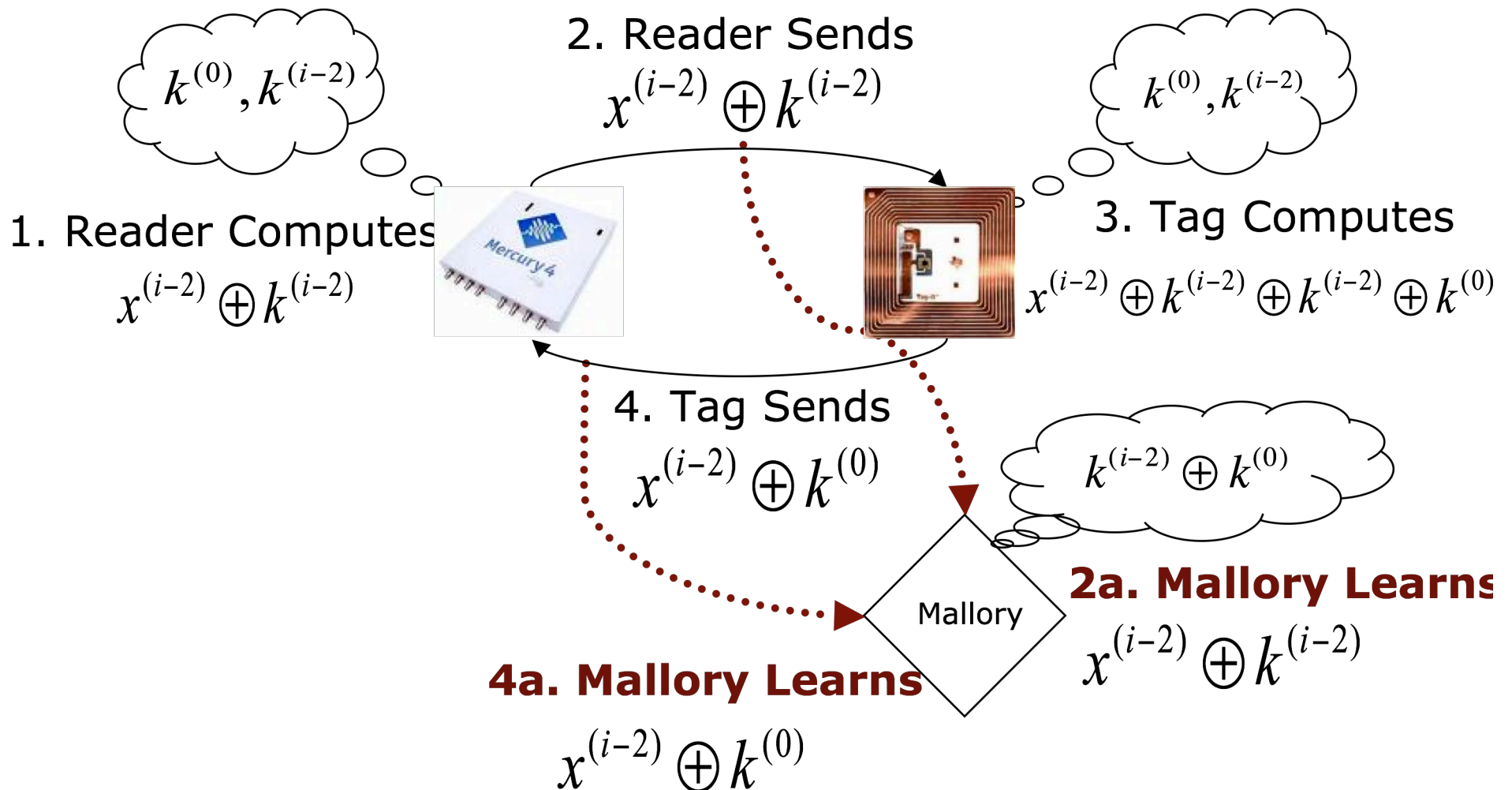
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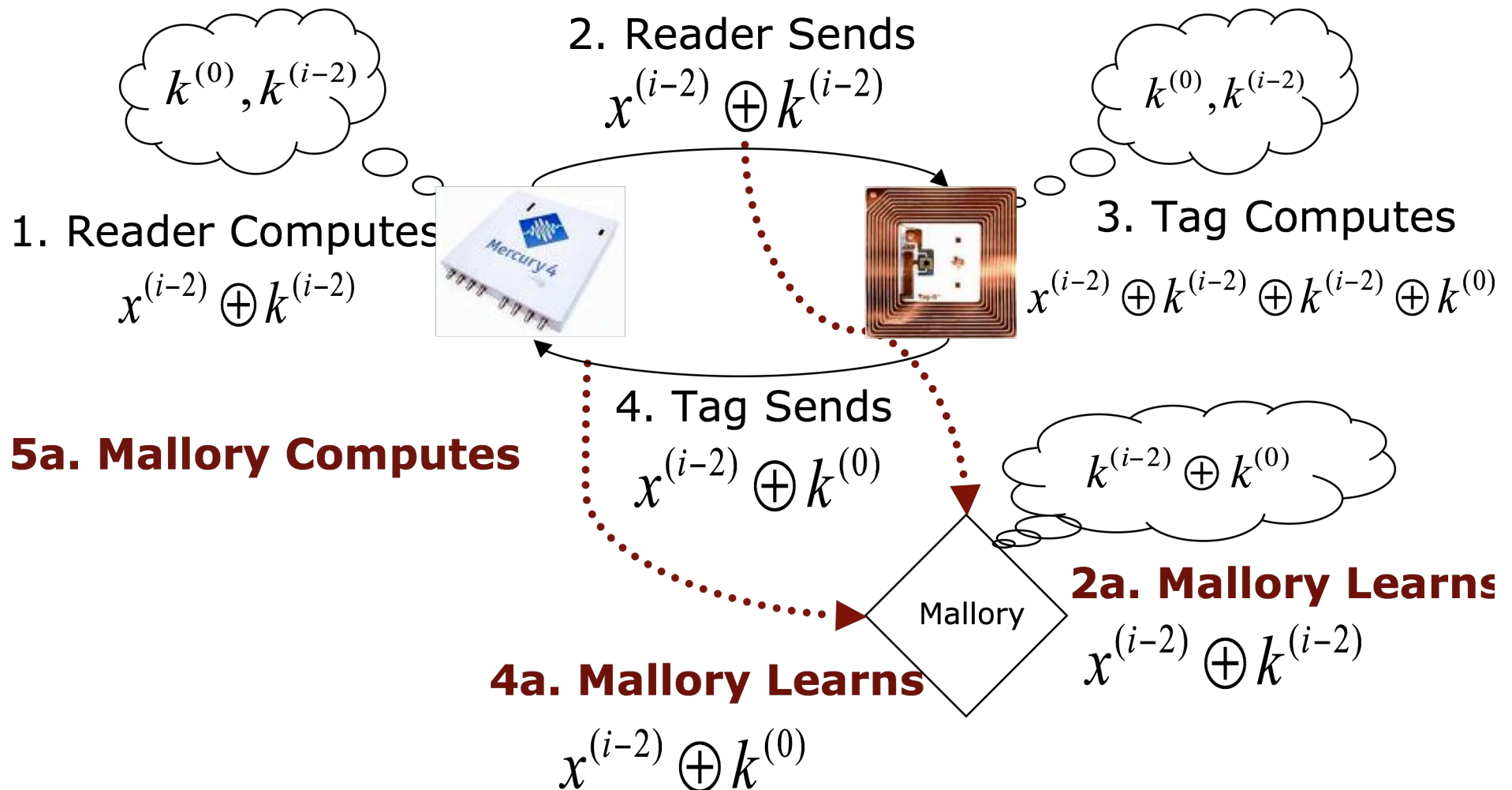
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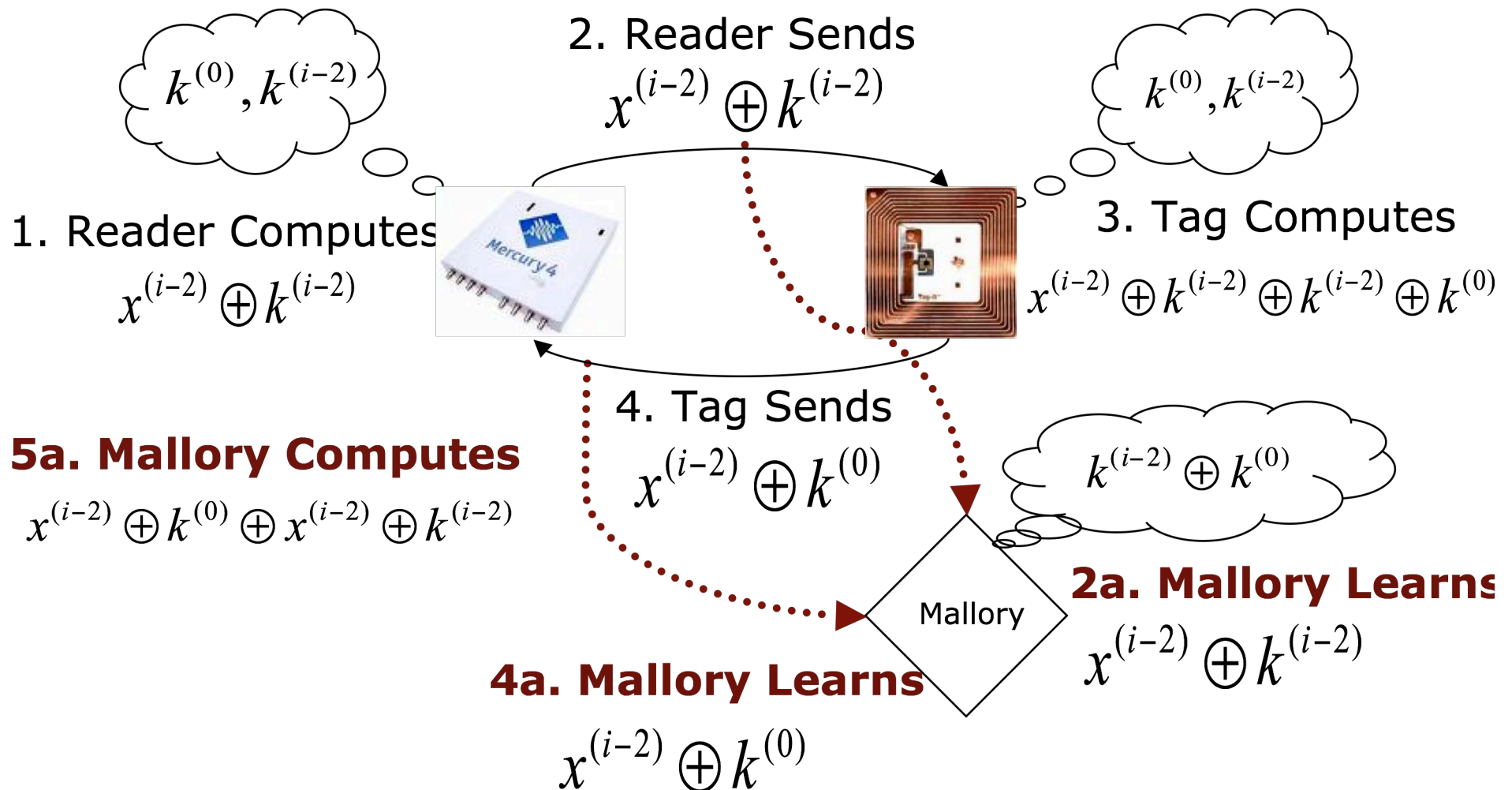
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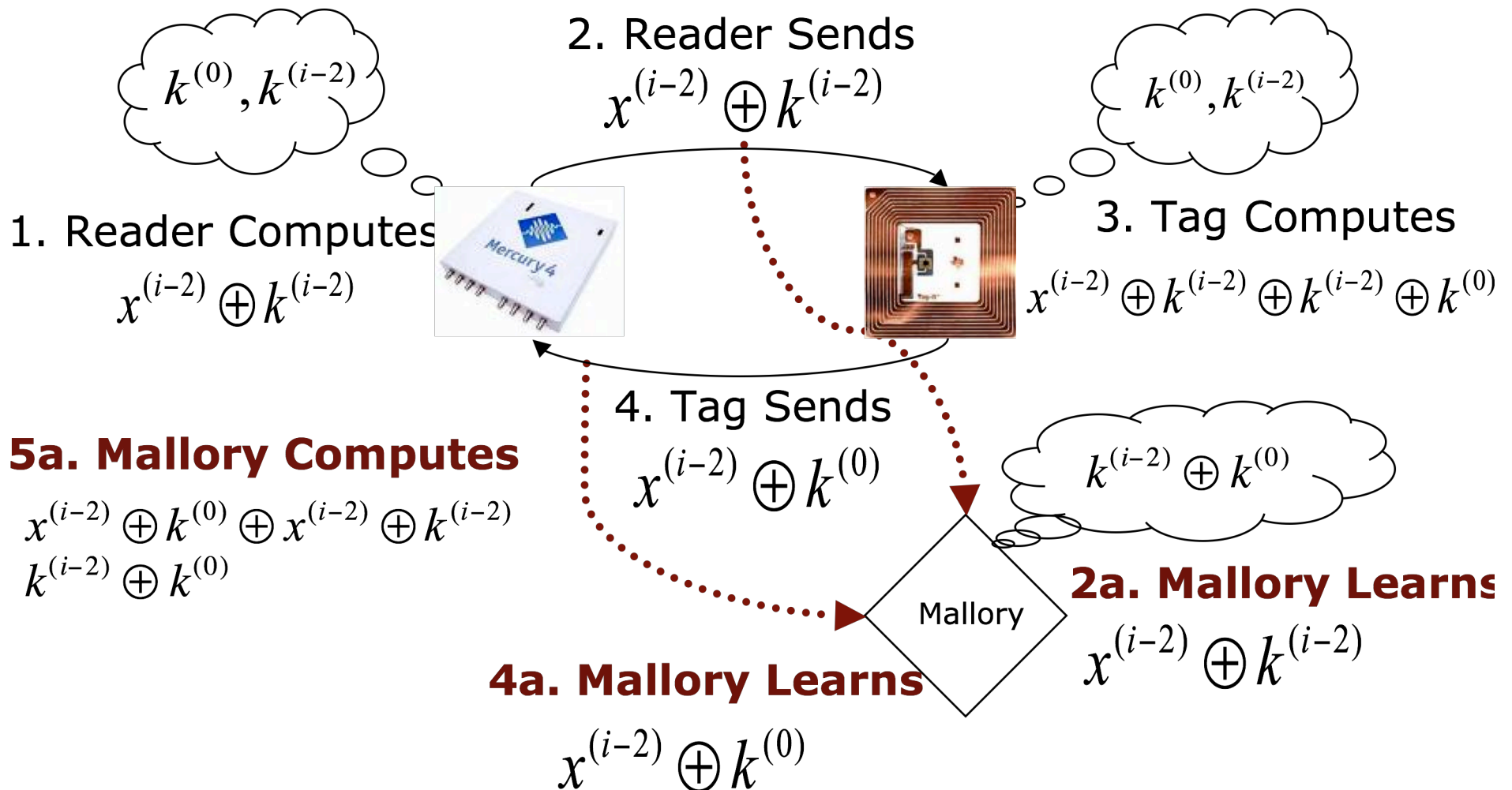


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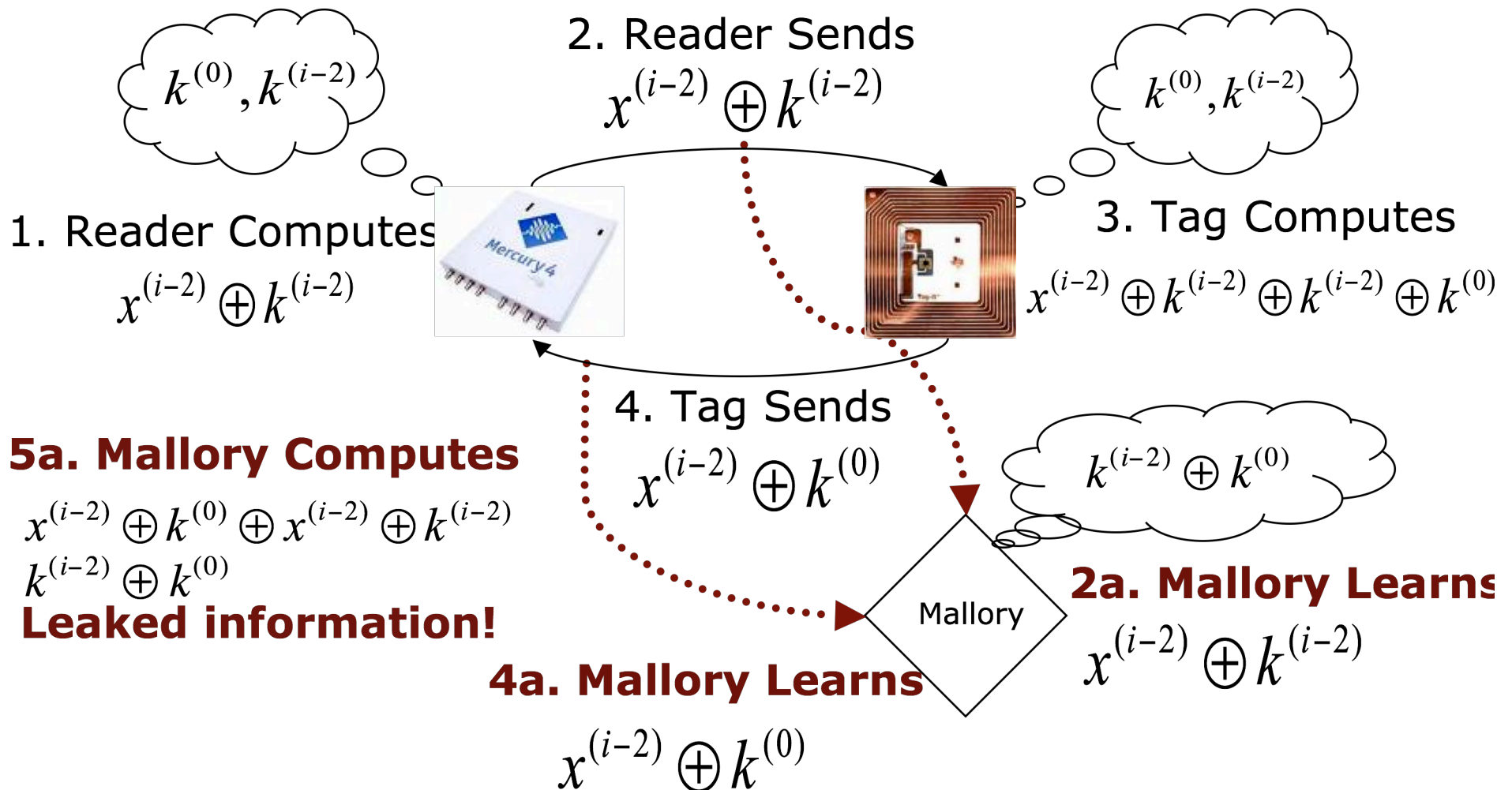




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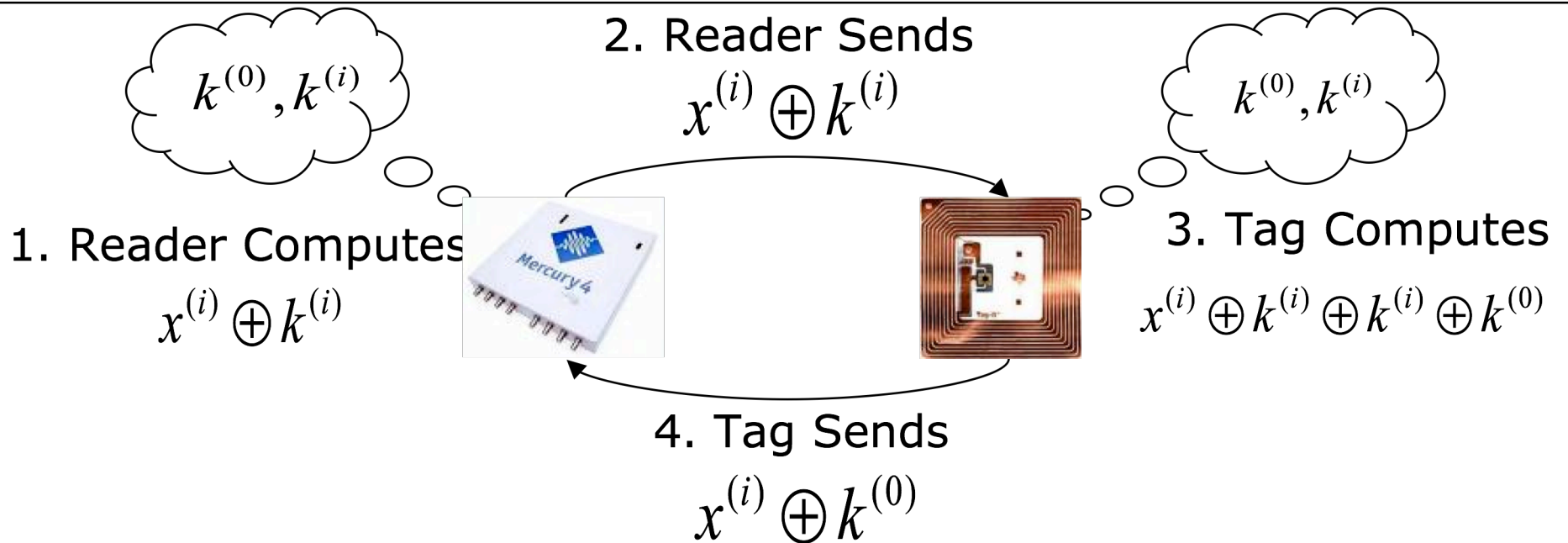
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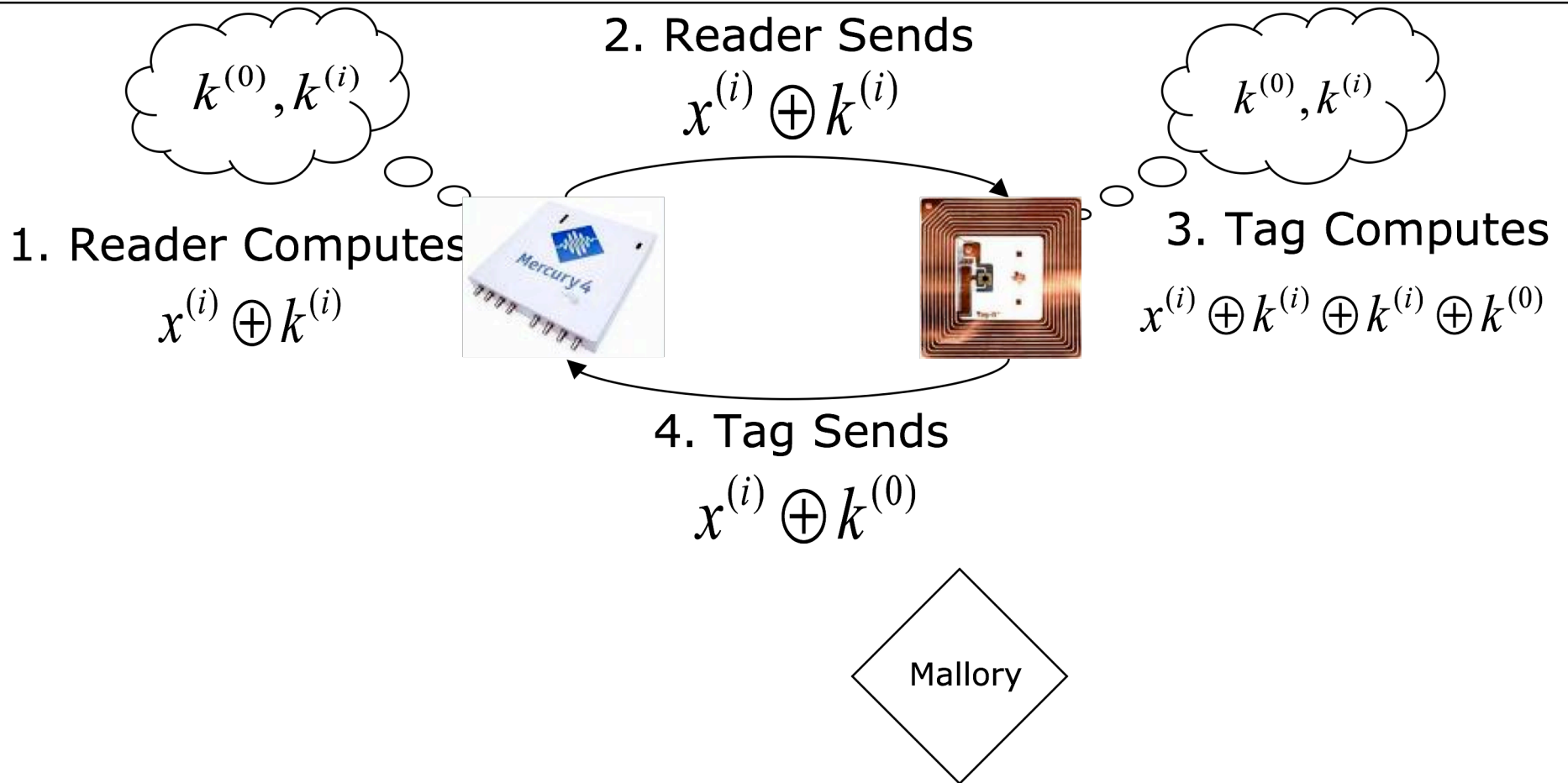
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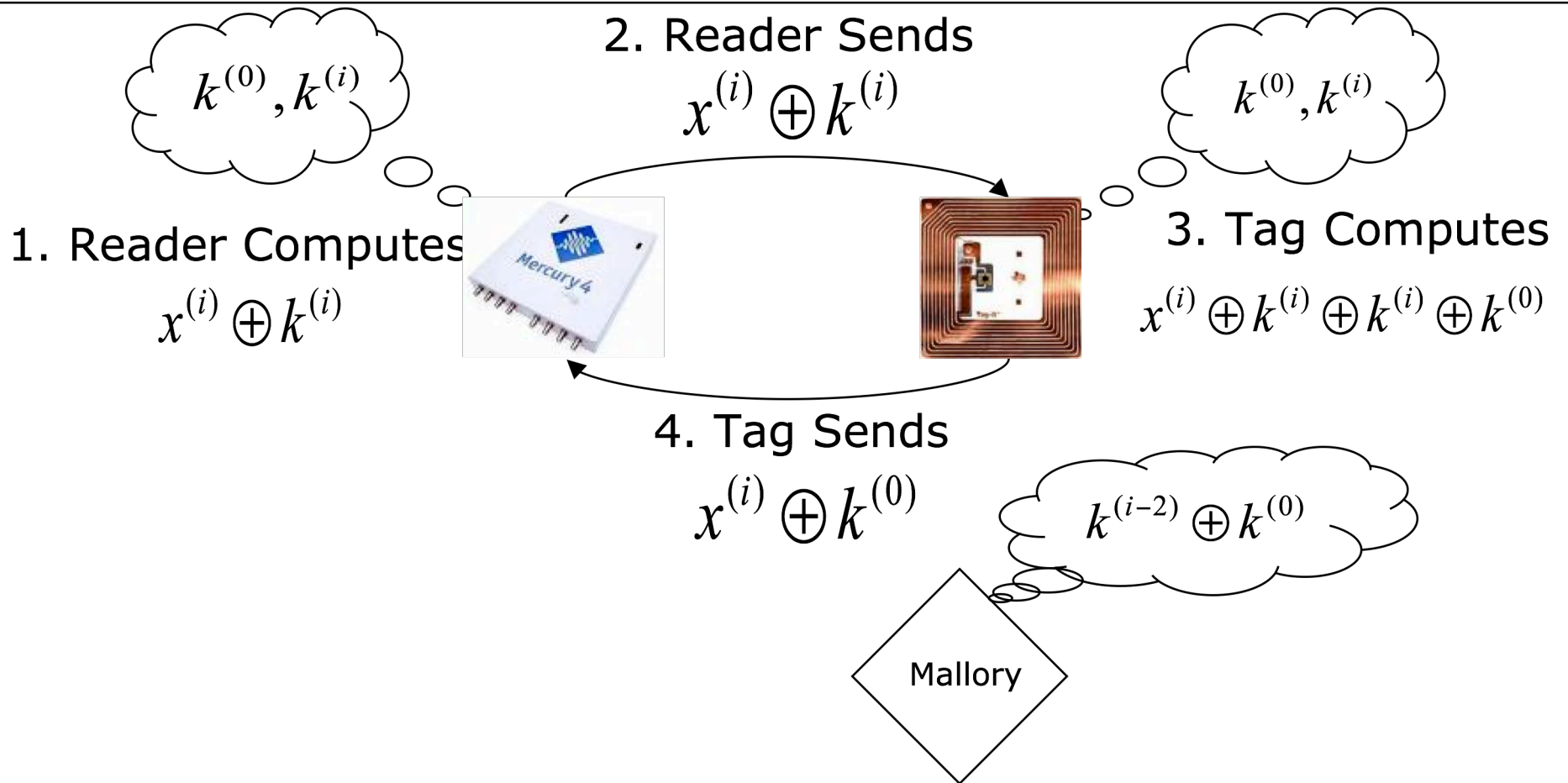
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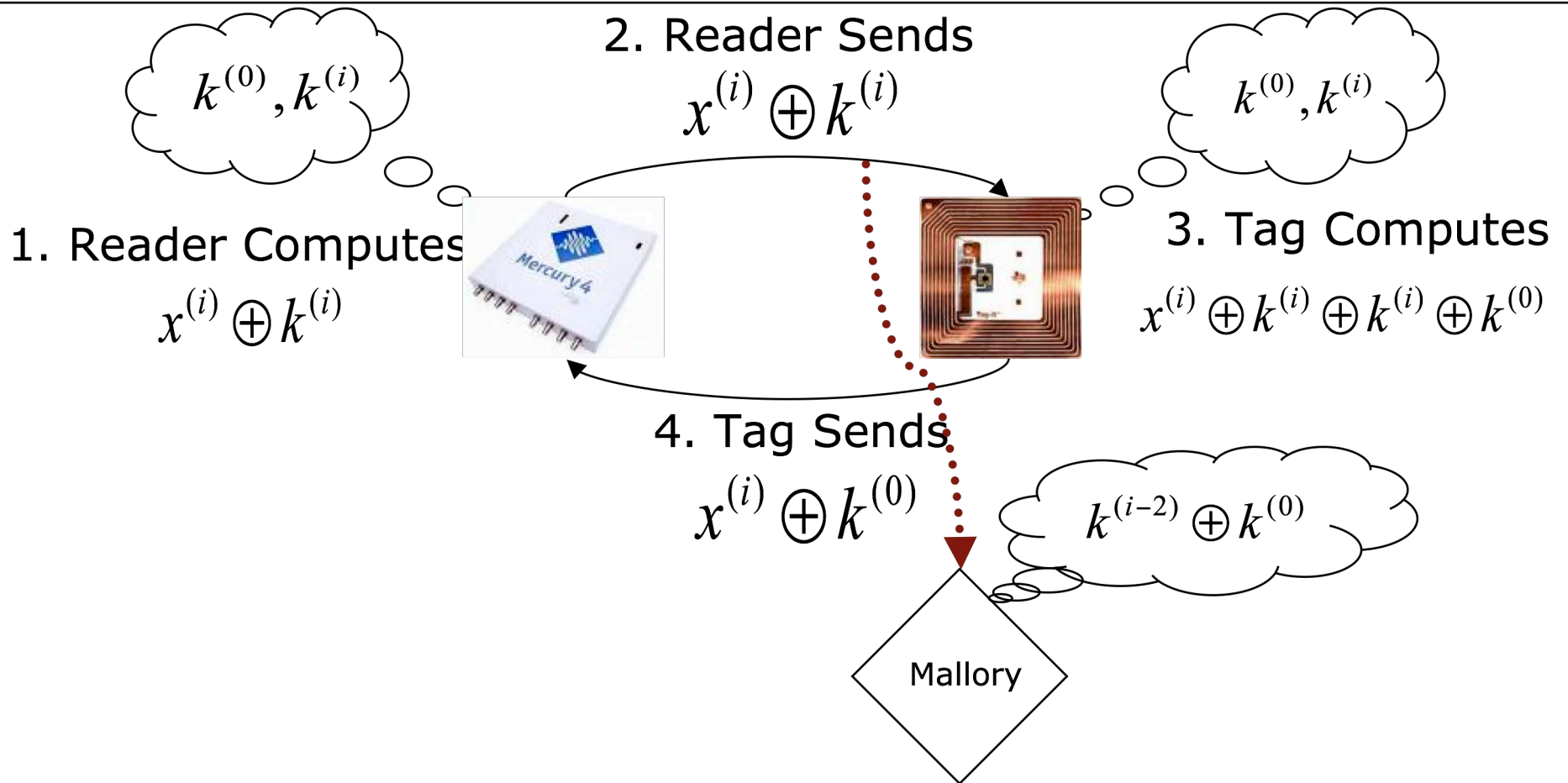
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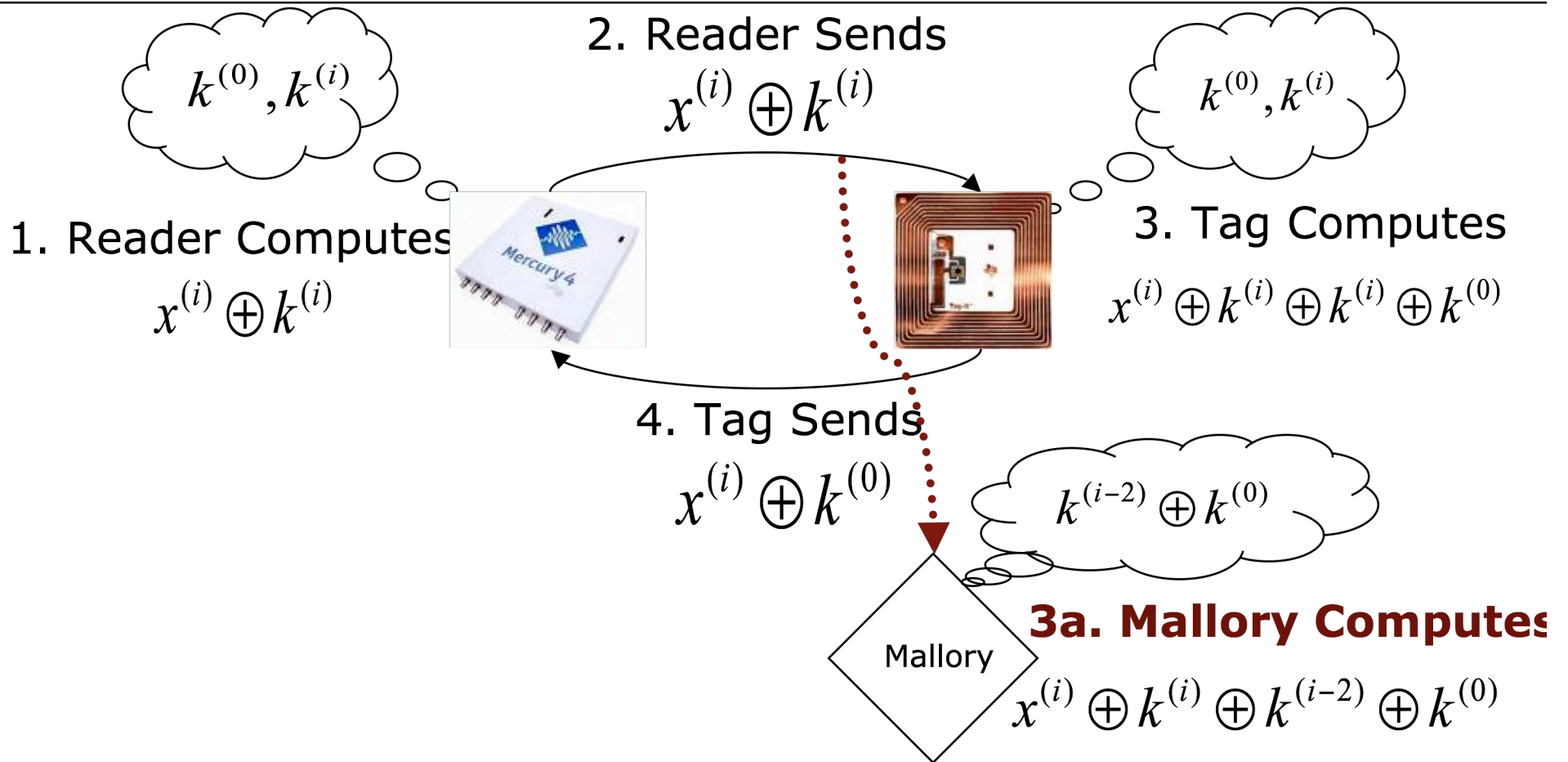
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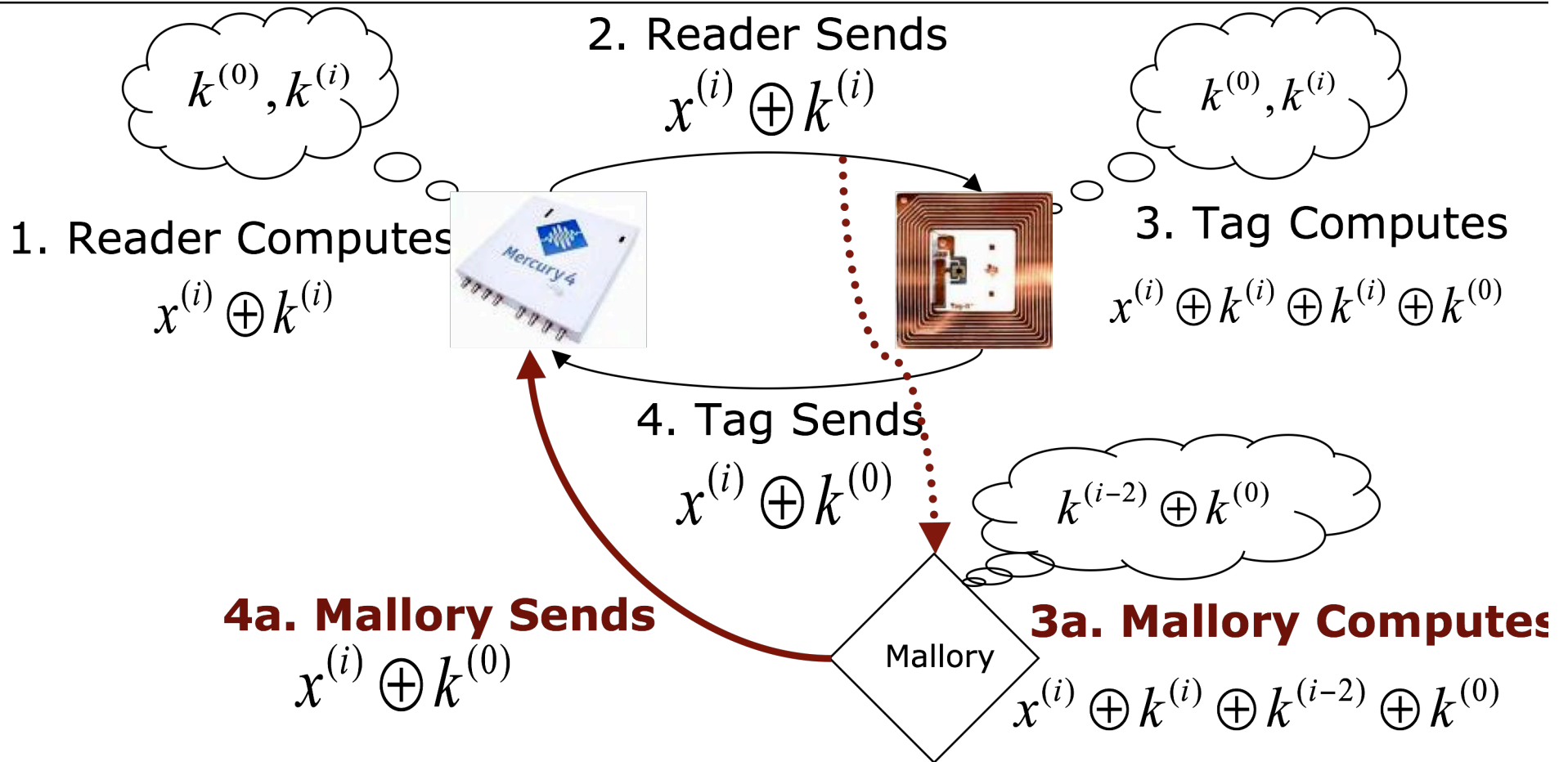


# Repeated Keys Attack, Transaction $i$ $k^{(i)} = k^{(i-2)}$





## Repeated Keys Attack, Transaction $i$ $k^{(i)} = k^{(i-2)}$



## Repeated Keys Attack

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- Mallory knows information leaked from an earlier transaction
- XOR's this information with current challenge to get valid response
- Does *not* know the session key or shared secret
- Does *not* brute force

## Implications of Repeated Keys Attack

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- A passive eavesdropper can impersonate the tag after an average of:
  - 70 transactions if listening from start
  - 3 transactions if listening after 68th transaction
- Vajda and Buttyán gave a theoretical maximum of  $16! \times 2 = 4.18455798 \times 10^{13}$  transactions

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## Nibble Attack

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- Exploits properties of the session key function
- Consider 128-bit key length example
- Attacker can learn shared secret after observing an expected 1,092 transactions

## Session Key $k^{(i)}$

$$k^{(i)} = \begin{array}{|c|c|c|c|c|c|c|c|c|} \hline 1010 & 0100 & 1000 & 0110 & \dots & 0001 & 1100 & 0111 & 0010 \\ \hline \end{array}$$

$$\begin{array}{cccccccc} k_{0,L}^{(i)} & k_{0,R}^{(i)} & k_{1,L}^{(i)} & k_{1,R}^{(i)} & & k_{14,L}^{(i)} & k_{14,R}^{(i)} & k_{15,L}^{(i)} & k_{15,R}^{(i)} \end{array}$$

$$k_L^{(i)} = \{k_{0,L}^{(i)}, k_{1,L}^{(i)}, \dots, k_{15,L}^{(i)}\} = \begin{array}{|c|c|c|c|c|} \hline 1010 & 1000 & \dots & 0001 & 0111 \\ \hline \end{array}$$

$$k_R^{(i)} = \{k_{0,R}^{(i)}, k_{1,R}^{(i)}, \dots, k_{15,R}^{(i)}\} = \begin{array}{|c|c|c|c|c|} \hline 0100 & 0110 & \dots & 1100 & 0010 \\ \hline \end{array}$$

## Session Key Function $k^{(i+1)} = F(k^{(i)})$

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- $k^{(i+1)}$  is formed by moving nibbles of the left and right vectors of  $k^{(i)}$
- $k_L^{(i+1)}$  is formed in a similar way using elements of  $k_R^{(i)}$  to swap elements of  $k_L^{(i)}$
- $k^{(i+1)}$  is formed by interleaving  $k_L^{(i+1)}$  and  $k_R^{(i+1)}$

## Session Key Example, Original Protocol

$$k_R^{(i)} = \{k_{0,R}^{(i)}, k_{1,R}^{(i)}, k_{2,R}^{(i)}, k_{3,R}^{(i)}\} = \begin{array}{|c|c|c|c|} \hline 2 & 1 & 3 & 0 \\ \hline \end{array}$$

$$k_L^{(i)} = \{k_{0,L}^{(i)}, k_{1,L}^{(i)}, k_{2,L}^{(i)}, k_{3,L}^{(i)}\} = \begin{array}{|c|c|c|c|} \hline 1 & 3 & 0 & 2 \\ \hline \end{array}$$

$$k^{(i)} = \begin{array}{|c|c|c|c|c|c|c|c|} \hline 1 & 2 & 3 & 1 & 0 & 3 & 2 & 0 \\ \hline \end{array}$$

$$\begin{array}{cccccccc} k_{0,L}^{(i)} & k_{0,R}^{(i)} & k_{1,L}^{(i)} & k_{1,R}^{(i)} & k_{2,L}^{(i)} & k_{2,R}^{(i)} & k_{3,L}^{(i)} & k_{3,R}^{(i)} \end{array}$$



## Session Key Example, Original Protocol

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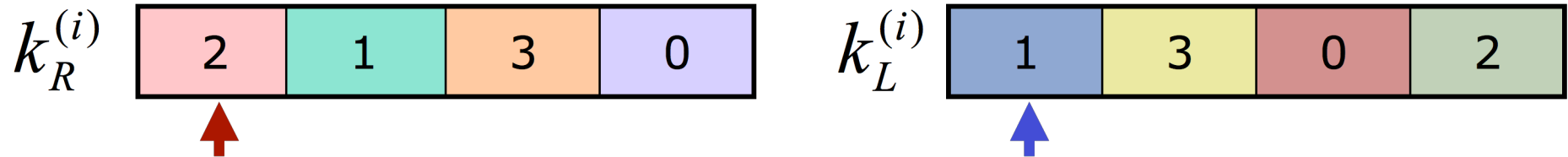
 $k_R^{(i)}$ 

2	1	3	0
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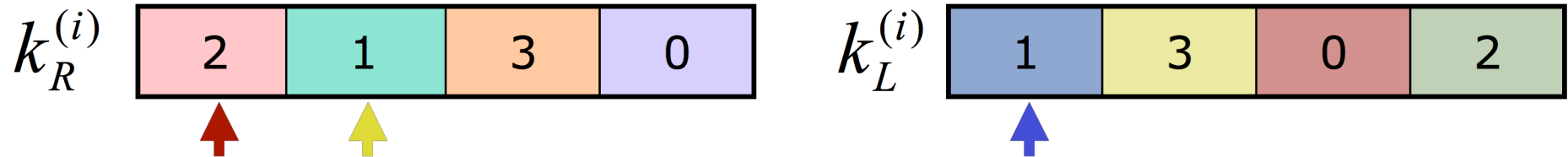
 $k_L^{(i)}$ 

1	3	0	2
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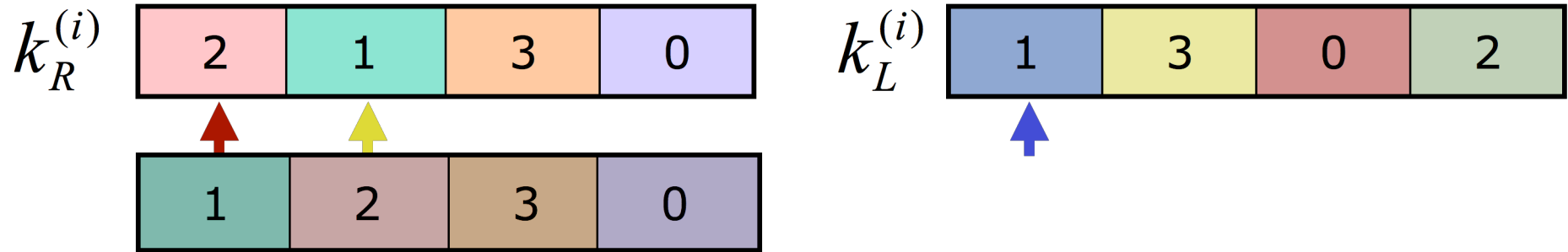
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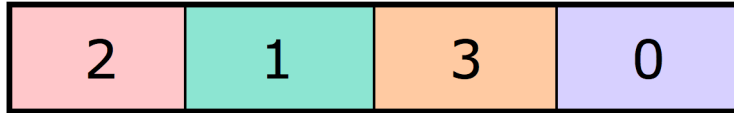
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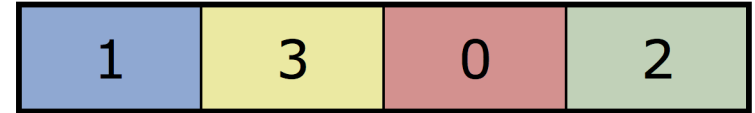
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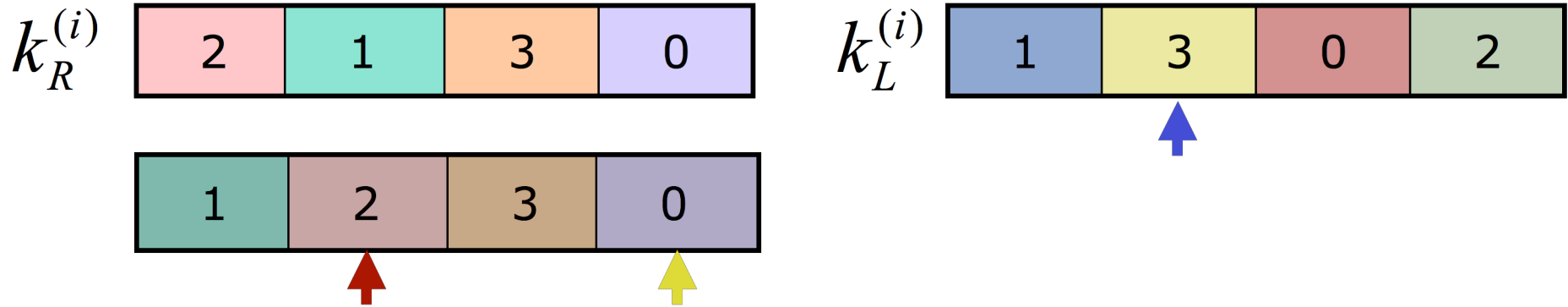
$k_R^{(i)}$



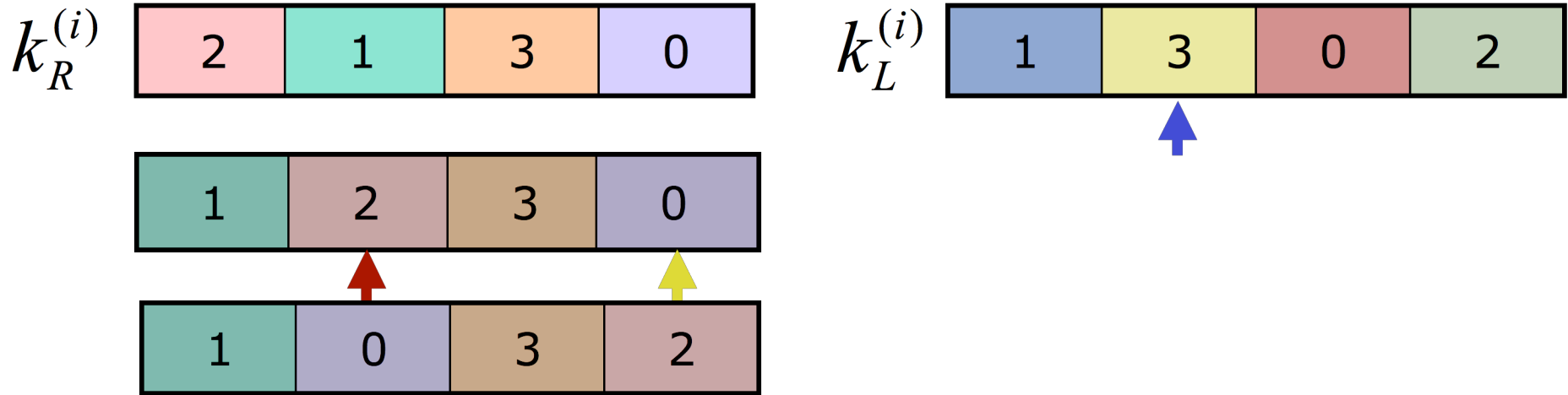
$k_L^{(i)}$



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$k_R^{(i)}$

2	1	3	0
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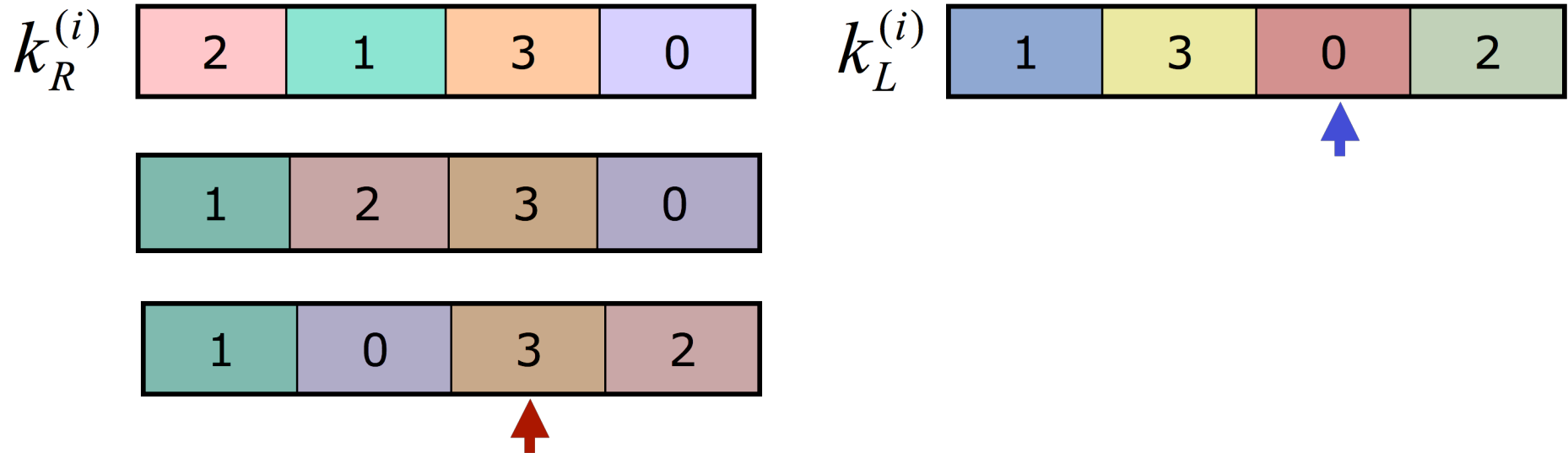
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1	3	0	2
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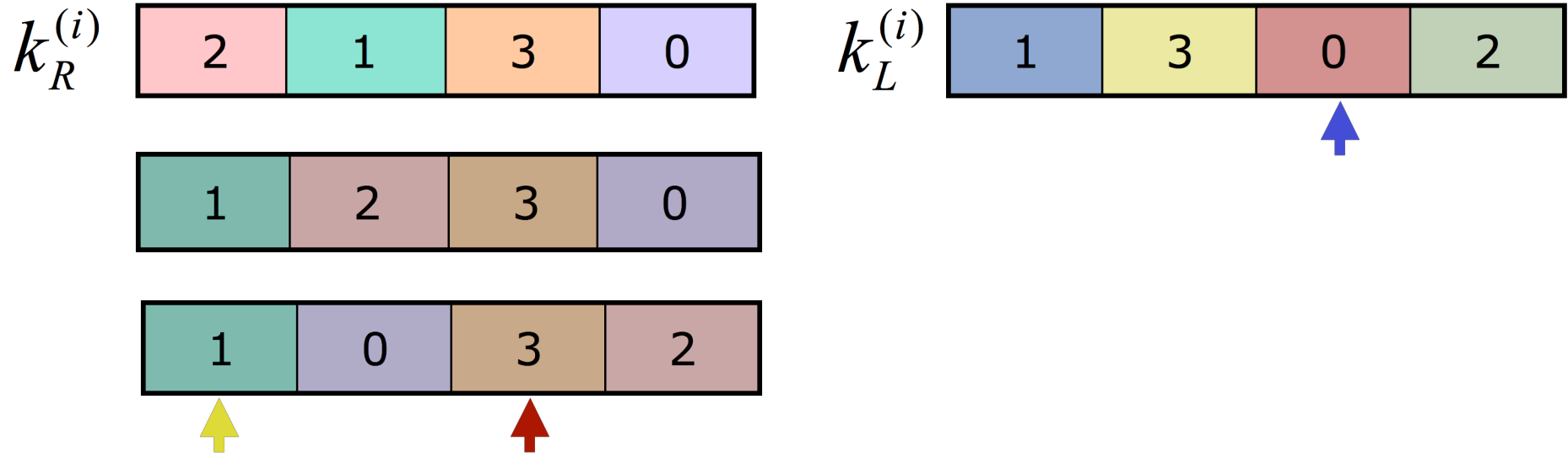
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1	0	3	2
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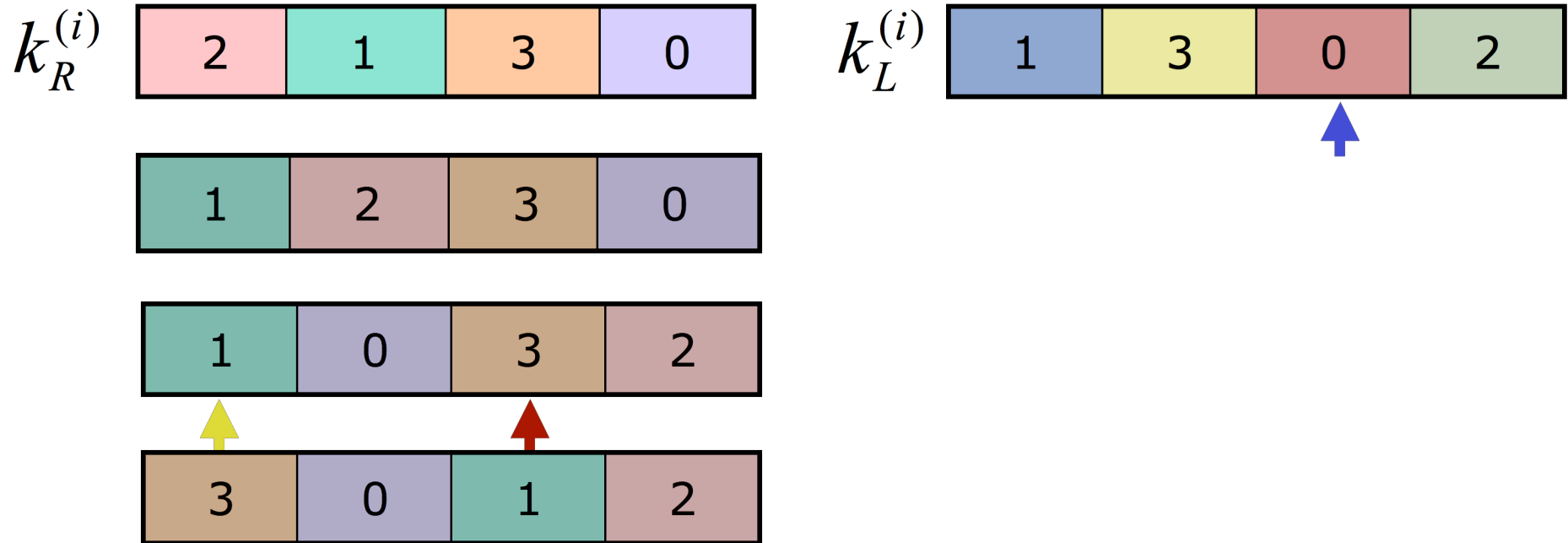
## Session Key Example, Original Protocol



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# Session Key Example, Original Protocol

 $k_R^{(i)}$ 

2	1	3	0
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1	2	3	0
---	---	---	---

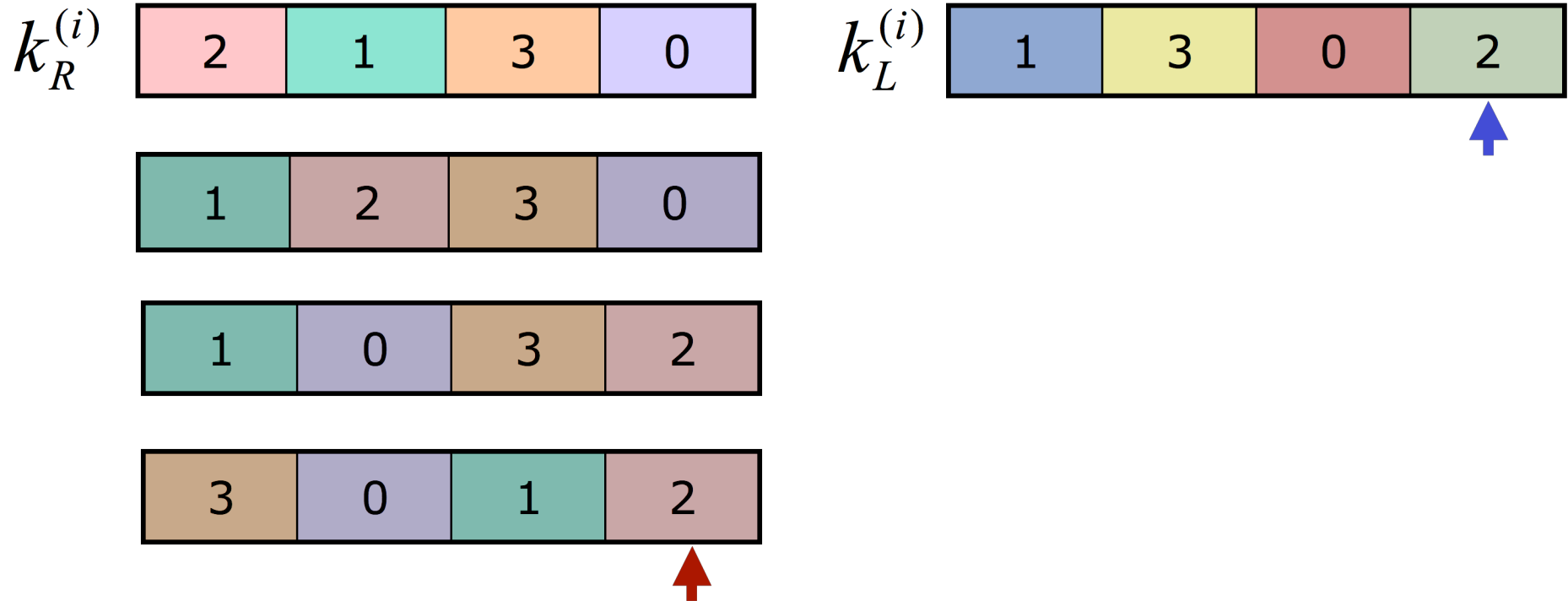
1	0	3	2
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3	0	1	2
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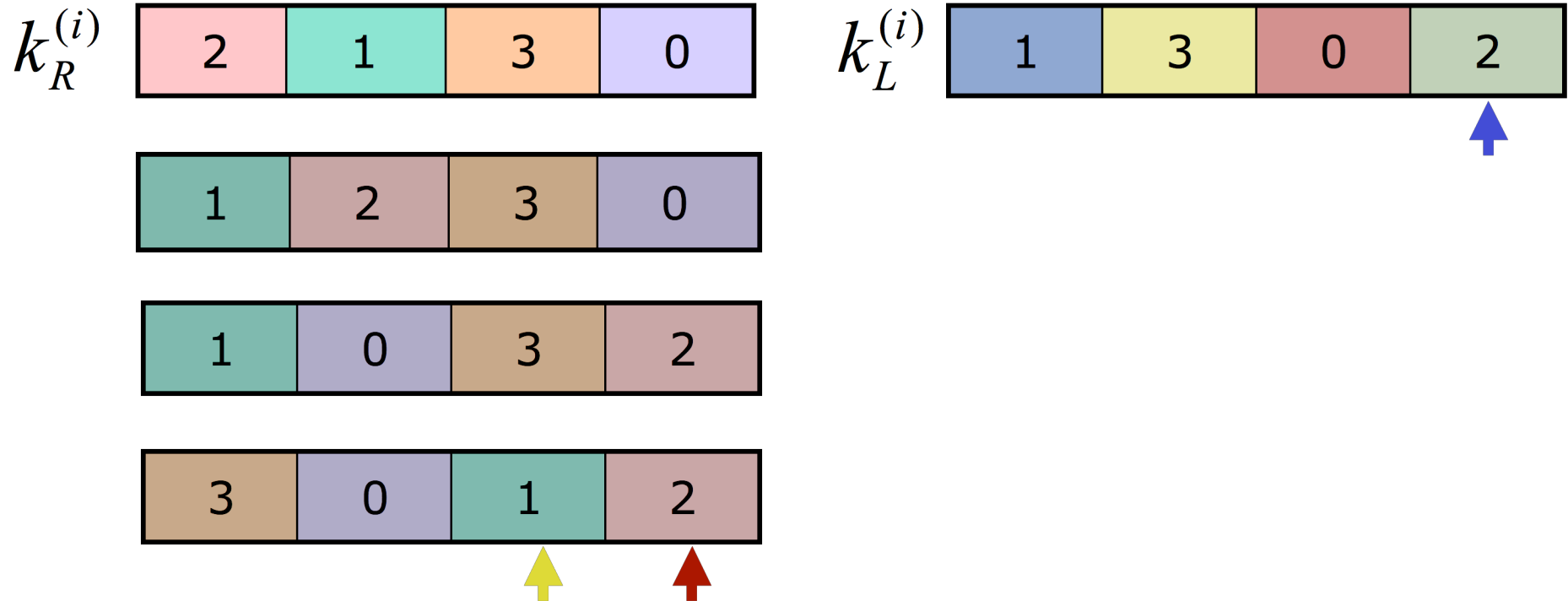
 $k_L^{(i)}$ 

1	3	0	2
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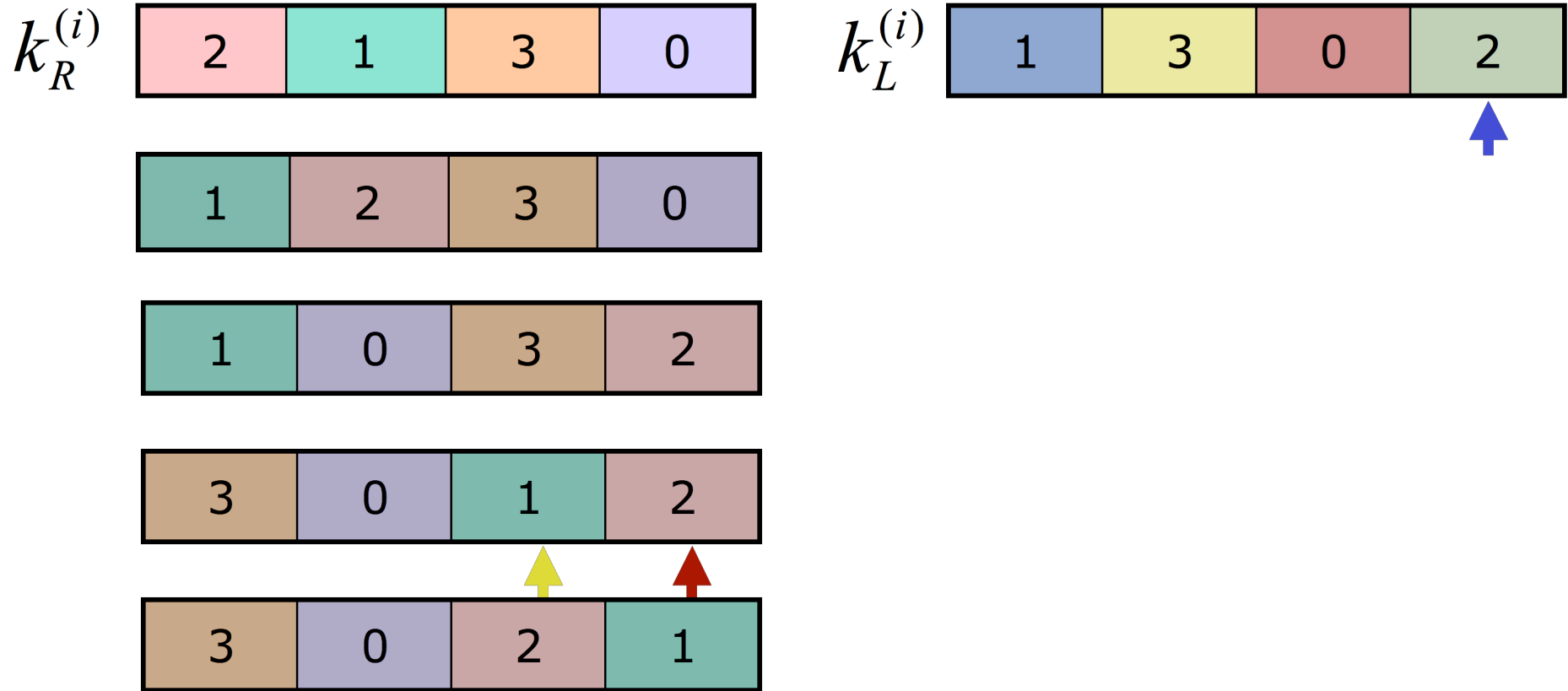
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## Session Key Example, Original Protocol

$k_R^{(i)}$

2	1	3	0
---	---	---	---

1	2	3	0
---	---	---	---

1	0	3	2
---	---	---	---

3	0	1	2
---	---	---	---

3	0	2	1
---	---	---	---

$k_L^{(i)}$

1	3	0	2
---	---	---	---

## Session Key Example, Original Protocol

 $k_R^{(i)}$ 

2	1	3	0
---	---	---	---

 $k_L^{(i)}$ 

1	3	0	2
---	---	---	---

1	2	3	0
---	---	---	---

1	0	3	2
---	---	---	---

3	0	1	2
---	---	---	---

 $k_R^{(i+1)}$ 

3	0	2	1
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## Session Key Example, Original Protocol

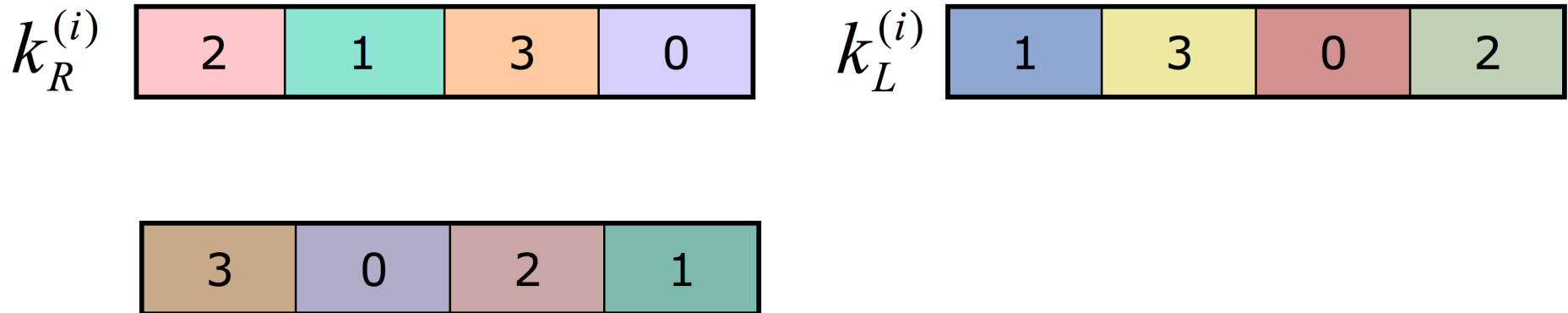
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- Observe that sometimes a nibble “does not move”



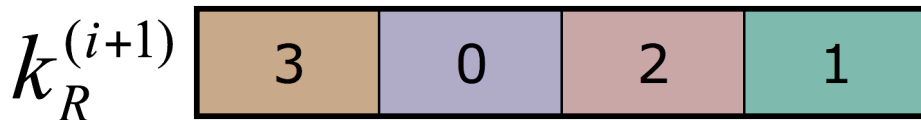
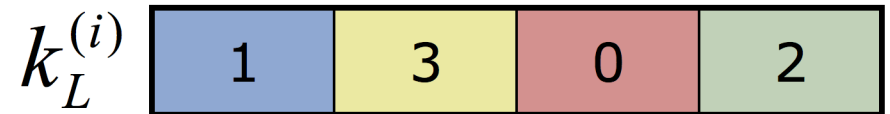
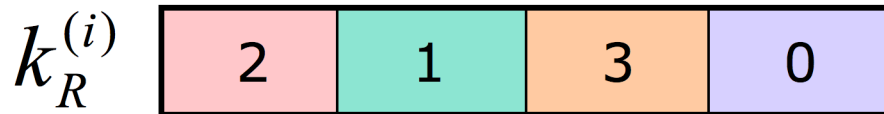
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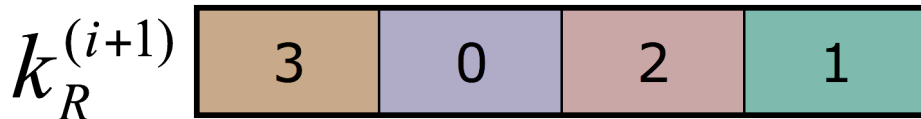
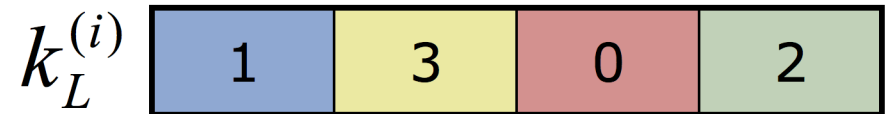
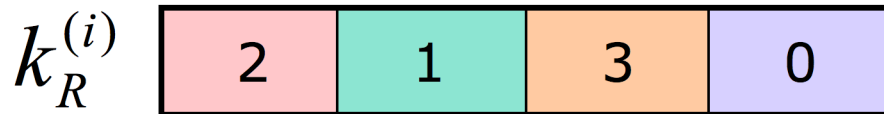
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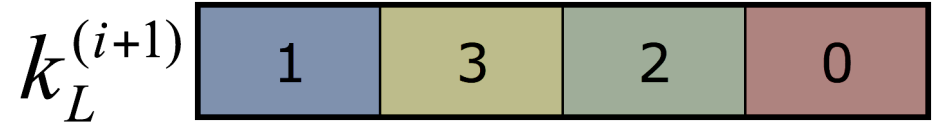
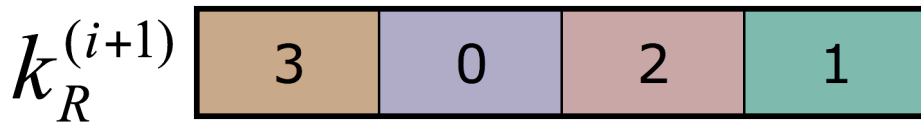
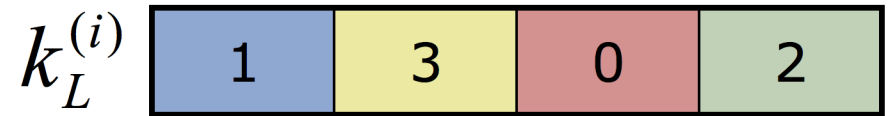
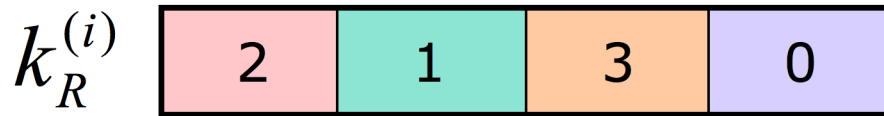
## Session Key Example, Original Protocol

- Observe that sometimes a nibble “does not move”



## Session Key Example, Original Protocol

- Observe that sometimes a nibble “does not move”



## Nibble Attack

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- Exploits deficiencies of session key function
  - Determine which nibbles “don’t move”
  - Construct table of observed values
  - Can determine one nibble of shared secret
- Can determine full shared secret with high probability after expected 1,092 transactions
- Active or passive attack



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## Conclusions & Suggestions for future protocols

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- Reader *cannot prevent or detect* the attacks
  - Attack 1: impersonate a tag after an average of 70 transactions
  - Attack 2: learn shared secret after an average of 1,092 transactions
- Adversary *never* needs to brute force the key
- Suggestions
  - Importance of implementation
  - Statistical measurements

## Questions?

`defend@cs.umass.edu`

`http://www.cs.umass.edu/~defend`

`http://www.rfid-cusp.org/`

## Session Key Function $k^{(i+1)} = F(k^{(i)})$

---

- $k^{(i+1)}$  is formed by moving nibbles of the left and right vectors of  $k^{(i)}$

- To form  $k_R^{(i+1)}$ :

$k_{0,R}^{(i+1)} = \text{swap } 0^{th} \text{ and } k_{0,L}^{(i)th} \text{ elements of } k_R^{(i)}$

$k_{1,R}^{(i+1)} = \text{swap } 1^{st} \text{ and } k_{1,L}^{(i)th} \text{ elements of } k_R^{(i)}$

$\vdots$

$k_{15,R}^{(i+1)} = \text{swap } 15^{th} \text{ and } k_{15,L}^{(i)th} \text{ elements of } k_R^{(i)}$

## Session Key Example

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 $k_R^{(i)}$ 

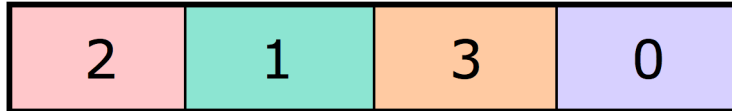
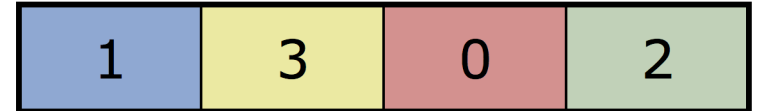
2	1	3	0
---	---	---	---

 $k_L^{(i)}$ 

1	3	0	2
---	---	---	---

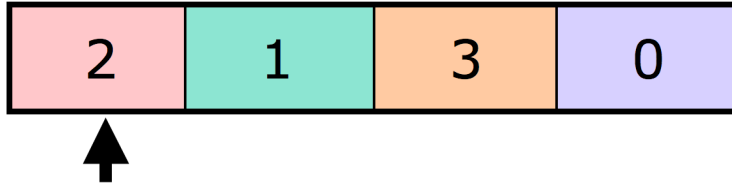
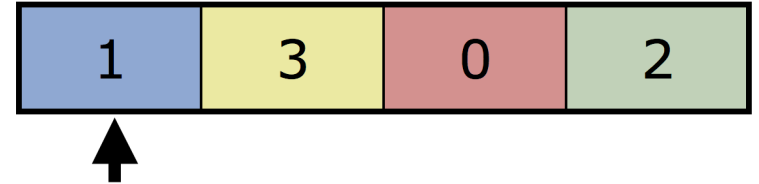
## Session Key Example

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 $k_R^{(i)}$  $k_L^{(i)}$ 

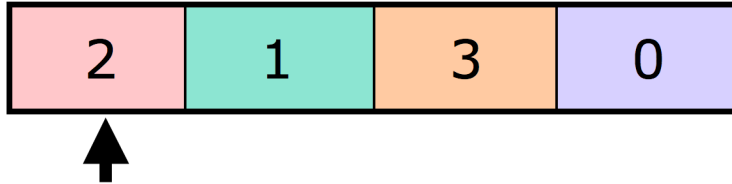
## Session Key Example

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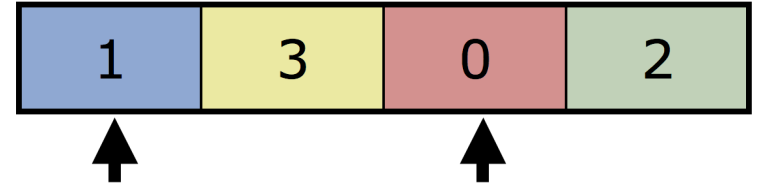
 $k_R^{(i)}$  $k_L^{(i)}$ 

## Session Key Example

$k_R^{(i)}$



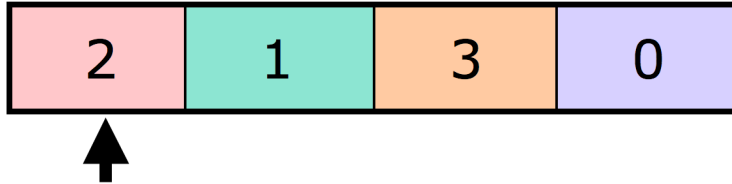
$k_L^{(i)}$



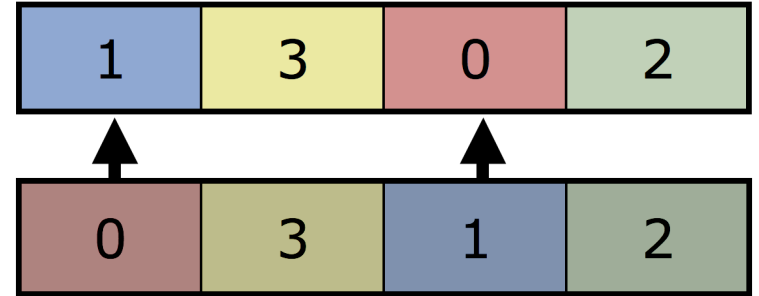


## Session Key Example

$k_R^{(i)}$



$k_L^{(i)}$



## Session Key Example

---

 $k_R^{(i)}$ 

2	1	3	0
---	---	---	---

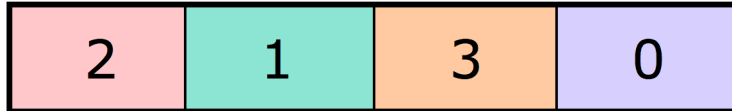
 $k_L^{(i)}$ 

1	3	0	2
---	---	---	---

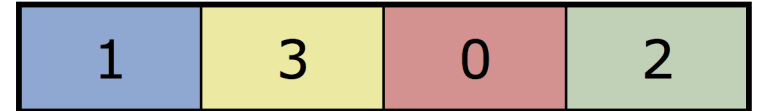
0	3	1	2
---	---	---	---

## Session Key Example

$k_R^{(i)}$

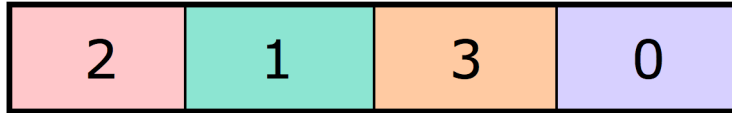


$k_L^{(i)}$

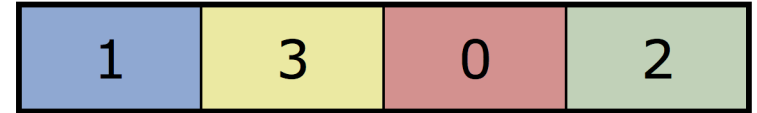


## Session Key Example

$k_R^{(i)}$

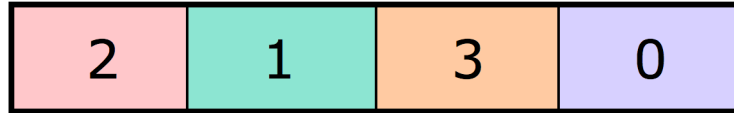


$k_L^{(i)}$

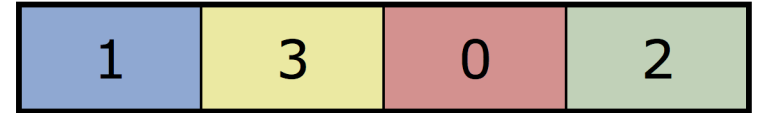


## Session Key Example

$k_R^{(i)}$



$k_L^{(i)}$



## Session Key Example

---

 $k_R^{(i)}$ 

2	1	3	0
---	---	---	---

 $k_L^{(i)}$ 

1	3	0	2
---	---	---	---

0	3	1	2
---	---	---	---

0	3	1	2
---	---	---	---

## Session Key Example

 $k_R^{(i)}$ 

2	1	3	0
---	---	---	---

 $k_L^{(i)}$ 

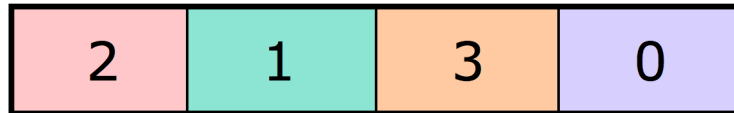
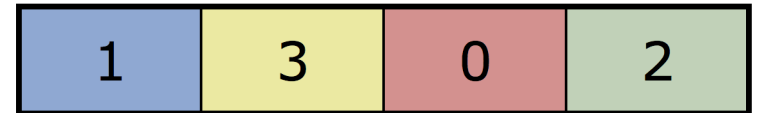
1	3	0	2
---	---	---	---

0	3	1	2
---	---	---	---

0	3	1	2
---	---	---	---



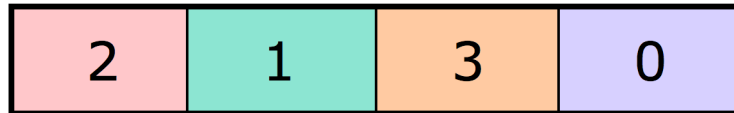
## Session Key Example

 $k_R^{(i)}$ 

 $k_L^{(i)}$ 


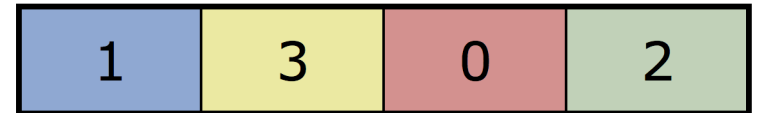


## Session Key Example

$k_R^{(i)}$

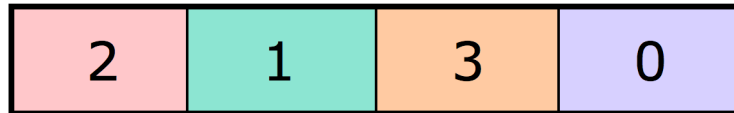


$k_L^{(i)}$

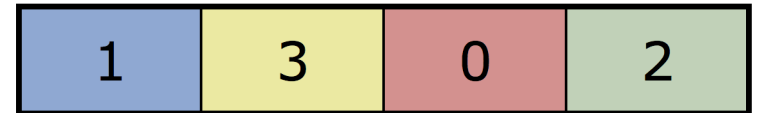


## Session Key Example

$k_R^{(i)}$



$k_L^{(i)}$



## Session Key Example

 $k_R^{(i)}$ 

2	1	3	0
---	---	---	---

 $k_L^{(i)}$ 

1	3	0	2
---	---	---	---

0	3	1	2
---	---	---	---

0	3	1	2
---	---	---	---

0	3	2	1
---	---	---	---

## Session Key Example

 $k_R^{(i)}$ 

2	1	3	0
---	---	---	---

 $k_L^{(i)}$ 

1	3	0	2
---	---	---	---

0	3	1	2
---	---	---	---

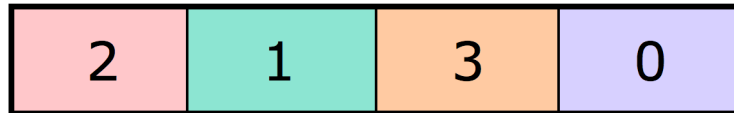
0	3	1	2
---	---	---	---

0	3	2	1
---	---	---	---

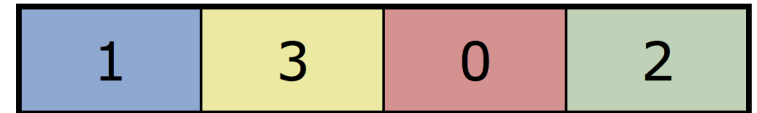


## Session Key Example

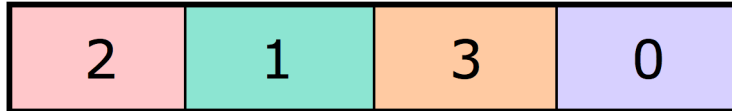
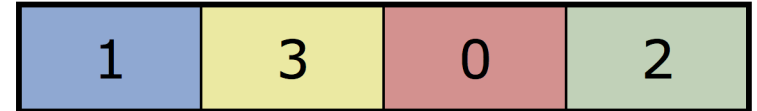
$k_R^{(i)}$



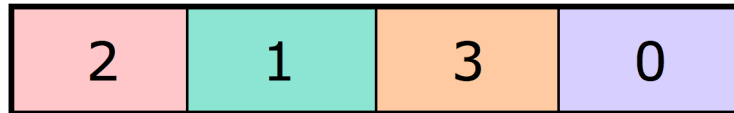
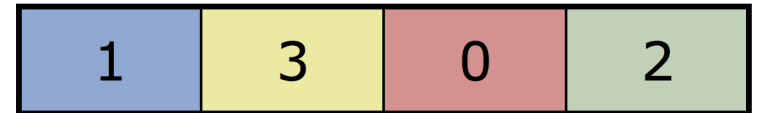
$k_L^{(i)}$



## Session Key Example

 $k_R^{(i)}$ 

 $k_L^{(i)}$ 


## Session Key Example

 $k_R^{(i)}$ 

 $k_L^{(i)}$ 


## Session Key Example

