## Model-based image reconstruction of chemiluminescence using a plenoptic 2.0 camera

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- Equipment support from Intel Corporation

Motivation: combustion in transparent engine cylinder


## Motivation

Tomographic reconstruction of 3D chemiluminescence patterns such as flame fronts using a plenoptic camera.

Previous work

- Tomo-PIV (particle image velocimetry) (4-6 cameras) [Elsinga et al., 2006]
- Plenoptic 1.0 camera for PIV [Fahringer et al., 2012]
- Single-camera stereo [Greene et al., 2013] [Chen et al., 2015]

Depth maps for translucent objects?


## Plenoptic camera

Plenoptic cameras use micro-lens arrays to capture 4-D light field information of a scene. The angular information enables:

- depth estimation (for object surfaces illuminated externally) e.g., via triangulation [Perwaß, SPIE, 2012]
- tomographic reconstruction (for luminescent objects) (cf., digital X-ray tomosynthesis - limited-angle tomography).

$\diamond$ Images courtesy of Raytrix GmbH and Lytro, Inc.


## Model-based image reconstruction (MBIR)

Overall goal: reconstruct 3D chemiluminescence pattern $\mathbf{x}$ from plenoptic camera measurement $\mathbf{y}$.

MBIR components:

- 3D object model (basis coefficients) x
- Image voxel, basis function, ...
- System model A (\# of sensor elements $\times \#$ of object voxels)
- Linearity, finite voxel size, finite pixel size, ...
- Data noise statistics $\mathrm{p}(\mathbf{y} \mid \mathbf{A x})$
- Additive Gaussian, Poisson, ...
- Cost function $\Psi(\mathbf{x})$
- Data fidelity, regularizer, physical constraints, ...
- Iterative algorithm (arg $\min _{x}$ )
- MART, FISTA, Newton's methods, ...
[Nuyts et al., Phys. Med. Biol., 2013]


## Model-based image reconstruction (continued)

We reconstructed objects by solving a regularized LS problem:

$$
\mathbf{x}^{\star} \in \arg \min _{\mathbf{x}}\left\{\Psi(\mathbf{x}) \triangleq \frac{1}{2}\|\mathbf{y}-\mathbf{A}\|_{2}^{2}+\mathrm{R}(\mathbf{x})\right\} \text { s.t. } \mathbf{x} \succeq \mathbf{0}
$$

where R denotes an edge-preserving corner-rounded TV regularizer.
We focused on $R$ defined as

$$
\mathrm{R}(\mathbf{x}) \triangleq \sum_{i=1} \beta_{i} \sum_{n} \varphi_{\text {Huber }}\left(\left[\mathbf{C}_{i} \mathbf{x}\right]_{n}\right)
$$

- $\mathbf{C}_{i}$ : finite difference matrix along ith direction
- $\beta_{i}$ : corresponding regularization parameter.
- $\varphi_{\text {Huber }}(t) \approx|t|$


## System model for a plenoptic camera


[Bishop \& Favaro, IEEE T-PAMI, 2012]

## System model for a plenoptic camera



Build (pre-compute) system matrix $\mathbf{A}$ one column at a time

## System model for a plenoptic camera


thin lens formula: $1 / z+1 / Z=1 / F$

## System model for a plenoptic camera



## System model for a plenoptic camera



## System model for a plenoptic camera



Use superposition to consider one microlens at a time

## System model for a plenoptic camera



If microlens had large diameter...

## System model for a plenoptic camera



If main lens had large diameter...

## System model for a plenoptic camera



Combined effect of main lens and microlens

## System model for a plenoptic camera



Combined effect of main lens and microlens

## System model - continued

Continuous-space PSF of the $i$ th micro-lens is:

$$
\beta_{i}(s, t ; x, y, z)=\underbrace{\beta_{i}^{\mathrm{ML}-\mu \mathrm{L}}(s, t ; x, y, z)}_{\alpha \operatorname{circ}\left(s, t ; c_{i}^{\mathrm{ML}-\mu \mathrm{L}}, B_{i}\right)} \cdot \underbrace{\beta_{i}^{\mu \mathrm{L}}(s, t ; x, y, z)}_{\alpha \operatorname{circ}\left(s, t ; c_{i}^{\mu \mathrm{L}}, b_{i}\right)},
$$

where

- $(s, t)$ denotes 2D sensor coordinates
- centers $\mathbf{c}_{i}^{\mathrm{ML}-\mu \mathrm{L}}, \mathbf{c}_{i}^{\mu \mathrm{L}}$, and radii $B_{i}$, and $b_{i}$ depend on the object point position $(x, y, z)$ and camera geometry.
- $\sum_{i} \beta_{i}(s, t ; x, y, z)$ sketched:

Continuous-space PSF


## Computational challenges

- Dense micro-lens array
- Highly shift-variant point spread function
- Non-separable aperture / PSF (cf., X-ray CT)
- Lens aberrations
- Finite sensor pixel size

The discrete PSF of a micro-lens consists of integrals of the circle-circle intersection over each sensor pixel, where the circle centers depend on the position of the "point source."
We approximate each finite-sized sensor pixel as $L \times L$ infinitesimal pixels, i.e., $L \times$-subsampling in each direction.

- Finite object voxel size


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- Finite object voxel size


## Finite-sized object voxel effects

One $(x, y)$ transaxial plane of a 3D object voxel


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One $(x, y)$ transaxial plane of a 3D object voxel


## Finite-sized object voxel: baseline approximation

We approximate each cubic voxel as $K \times K \times K$ equally spaced infinitesimal voxels, i.e., $K \times$-subsampling in each direction.

$\dagger$ We used $K=7$ here.

## Finite-sized object voxel: baseline approximation

We approximate each cubic voxel as $K \times K \times K$ equally spaced infinitesimal voxels, i.e., $K \times$-subsampling in each direction.

(infinitesimal)

## Why finite voxel size matters



##  <br> 븁 -

Infinitesimal voxels


Finite-sized voxels

$\dagger$ Using $0.5 \times 0.5 \times 0.5\left[\mathrm{~mm}^{3}\right]$ cubic voxels and $K=7$.

## Why finite voxel size matters (zoomed)

##  <br> - <br> -



Numerical experiments: imaging geometry


## Numerical experiments: object geometry

- $100 \times 100 \times 100$ voxel object
- $0.5 \times 0.5 \times 0.5\left[\mathrm{~mm}^{3}\right]$ voxels
- 50 [mm] field-of-view
- $7 \times$ sensor subsampling when precomputing $\mathbf{A}$
- 50 dB SNR (additive white Gaussian noise)

- To avoid an inverse crime when synthesizing plenoptic sensor pictures, we used a voxelized object having a $2 \times$ finer grid in 3D, with $11 \times$ subsampling per dimension.


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## Numerical experiments: plenoptic cameras

|  | Camera \#1 | Camera \#2 | Camera \#3 |  |
| :--- | ---: | ---: | ---: | :--- |
| $f_{\text {main }}$ | 80 | 80 | 80 | $[\mathrm{~mm}]$ |
| f-number | 1.4 | 2.8 | 1.4 |  |
| $d_{\text {main }}$ | 57.14 | 28.57 | 57.14 | $[\mathrm{~mm}]$ |
| $f_{\text {micro }}$ | 0.35 | 0.35 | 0.35 | $[\mathrm{~mm}]$ |
| $d_{\text {micro }}$ | 0.27 | 0.135 | 0.135 | $[\mathrm{~mm}]$ |
| type | larger | Bishop \& Favaro | overlaps |  |

- $9 \mu \mathrm{~m} \times 9 \mu \mathrm{~m}$ sensor pixel size
- $850 \times 850$ pixel sensor


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## Numerical experiments: simulated plenoptic pictures



Better angular resolution than Camera \#2, but worse spatial resolution

Numerical experiments: simulated plenoptic pictures


Bishop \& Favaro, 2012

## Numerical experiments: simulated plenoptic pictures



Overlapping (larger) subimages: demultiplexing needed, but (perhaps) more angular information than Camera \#2.

## Numerical experiments: image reconstruction

[Recap] Our image reconstruction problem is:

$$
\mathbf{x}^{\star} \in \arg \min _{\mathbf{x}}\left\{\Psi(\mathbf{x}) \triangleq \frac{1}{2}\|\mathbf{y}-\mathbf{A} \mathbf{x}\|_{2}^{2}+\mathrm{R}(\mathbf{x})\right\} \text { s.t. } \mathbf{x} \succeq \mathbf{0}
$$

- 500 iterations of FISTA with adaptive restart [Beck \& Teboulle, IEEE T-IP, 2009]
[O'Donoghue \& Candès, FCM, 2015]
- Precomputed / stored A (column-wise sparse)
- $7 \times$ object subsampling $(x, y, z)$
- $7 \times$ sensor subsampling $(s, t)$
- 320 secs/slice for camera \#1 ( 60 threads @ MATLAB)
- 26 3D neighbors used in the (smoothed) TV regularizer


## Numerical experiments: finite voxel size

Infinitesimal voxels
Camera \#1

Finite-sized voxels Camera \#1

Contours at isovalue $=20 \%$ of maximum intensity.

## Numerical experiments: aperture size

Large aperture/coarse MLA Camera \#1


Small aperture/dense MLA Camera \#2

Better lateral resolution of Camera 2 not helpful here.

## Numerical experiments: aperture size - slices

Prantom

Phantom



Camera \#1 [approx., SNR = 50 dB ]


Camera \#2 [approx., SNR = 50 dB ]
xy

## Numerical experiments: overlapping subimages

Non-overlapping subimages

Camera \#2


Overlapping subimages


Numerical experiments: overlapping subimages - slices

Prantom

Phantom



Camera \#2 [approx., SNR = 50 dB ]


Camera \#3 [approx., SNR = 50 dB ]


## Numerical experiments: object distance

$$
d_{\text {object }}=700[\mathrm{~mm}]
$$

Camera \#2


$$
d_{\text {object }}=550[\mathrm{~mm}]
$$



## Numerical experiments: object distance - slices

Prantom

Phantom
$x y$ az

Camera \#2 [approx., SNR = 50 dB ]


$$
d_{\text {object }}=700[\mathrm{~mm}]
$$

Camera \#2 [approx., SNR = 50 dB ]

$d_{\text {object }}=550[\mathrm{~mm}]$

## Numerical experiments: sharp vs smooth object

Sharp object edges

Camera \#3


Smooth object edges


Numerical experiments: sharp vs smooth object - slices

Sharp phantom


Smooth phantom


## Conclusions

- Model-based image reconstruction may be viable for 3D chemiluminescence from plenoptic camera data
- Voxel-size modeling is important
- Larger angular range of incident light improves z-resolution (but more severe lens aberration?)
- F-number matching can be relaxed (overlapping sub-images) to improve depth resolution in tomographic formulation
- Need fast on-the-fly forward/back-nrojections to solve real large-scale image reconstruction problems


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## Approximate box blur

In practice, $B_{i} \gg b_{i}$, so $\beta_{i}$ is usually a circle.
The continuous-space PSF of a voxel slice at depth $z$ is

$$
\begin{aligned}
& \int_{x-\frac{\Delta_{x}}{2}}^{x+\frac{\Delta_{x}}{2}} \int_{y-\frac{\Delta_{y}}{2}}^{y+\frac{\Delta_{y}}{2}} \beta_{i}(s, t ; \bar{x}, \bar{y}, z) d \bar{y} d \bar{x} \\
\approx & \int_{x-\frac{\Delta_{x}}{2}}^{x+\frac{\Delta_{x}}{2}} \int_{y-\frac{\Delta_{y}}{2}}^{y+\frac{\Delta_{y}}{2}} \operatorname{circ}\left(s, t ; \mathbf{c}_{i}^{\mu \mathrm{L}}(\bar{x}, \bar{y}), b_{i}\right) d \bar{y} d \bar{x} \\
= & \int_{-\frac{\Delta_{x}}{2}}^{\frac{\Delta_{x}}{2}} \int_{-\frac{\Delta_{y}}{2}}^{\frac{\Delta_{y}}{2}} \operatorname{circ}\left(s, t ; \mathbf{c}_{i}^{\mu \mathrm{L}}\left(x+\delta_{x}, y+\delta_{y}\right), b_{i}\right) d \delta_{y} d \delta_{x} \\
= & \iint \operatorname{circ}\left(s-\delta_{s}, t-\delta_{t} ; \mathbf{c}_{i}^{\mu \mathrm{L}}(x, y), b_{i}\right) \cdot \operatorname{rect}\left(\delta_{s}, \delta_{t} ; w_{s}, w_{t}\right) d \delta_{t} d \delta_{s} .
\end{aligned}
$$

## Infinitesimal vs finite-sized sensor pixel: point object




(For an infinitesimal voxel)

## Infinitesimal vs finite-sized sensor pixel: sphere object





point voxel point sensor

point voxel finite sensor

finite voxel finite sensor

