

Preliminary Studies on the Feasibility of Addition of Vertex View to Conventional Brain SPECT¹

C.Y. Ng^{2,3}, N.H. Clinthorne², J.A. Fessler⁴, A.O. Hero⁴, Y. Zhang⁵ and W.L. Rogers^{2,3}

²Division of Nuclear Medicine, The University of Michigan, MI48109-0552

³Dept. of Biomedical Engineering, The University of Michigan, MI48109-2125

⁴Dept. of Electrical Engineering, The University of Michigan, MI48109-2122

⁵Dept. of Radiology, The University of Michigan, MI48109-0326

Abstract

We have investigated the improvement in resolution and sensitivity for brain imaging which would result by the addition of a single stationary vertex view to the tomographic data. This method has the practical advantage of being relatively inexpensive and easy to implement. The uniform Cramer Rao bound is a plot of the minimum achievable standard deviation for estimating the pixel intensity as a function of the bias gradient length. Uniform CR bound analysis indicated an improvement in performance when the vertex detector is added, especially for centrally located pixels for which improvement is seen over the useful depth for brain imaging. Simulation experiments were done with a simple six slice phantom and with the Hoffman brain phantom. Visual inspection of the reconstructed images showed improved resolution and noise characteristics over reconstructed images without the vertex data. Quantitatively, substantial reduction in mean square error was observed for a plane close to the vertex detector. Improvement reduced as distance from the vertex detector is increased. Background activities inside the field of view of the vertex detector but not the tomograph were represented by several blobs of activity on a plane lying outside the reconstruction volume. This activity was estimated by 3D spline fitting jointly with the image reconstruction process. Adding the vertex view to conventional brain SPECT should lead to improved cortical imaging, and to moderate improvement for deep structures.

I. INTRODUCTION

The predominant noise in SPECT imaging is Poisson which arises from the random nature of radionuclide decay and limited detection sensitivity of collimated imaging systems. In these systems there is always a compromise between sensitivity and spatial resolution. SPECT system sensitivity can be increased by improving the collimator geometric efficiency which decreases spatial resolution. Cone beam collimation used with conventional rotating Anger cameras is able to increase both resolution and sensitivity by reducing the field of view, but it has the drawback of

incomplete sampling which degrades the image quality [1]. Another approach to increase both resolution and sensitivity is to increase the amount of active detector surface that simultaneously views the organ of interest.

Addition of the vertex view data to the conventional tomographic data set is motivated by the desire to increase both the resolution and sensitivity for SPECT brain imaging, and it has the advantage of being relatively inexpensive and easy to implement. Existing systems can be modified to include the vertex detector without major alternations in hardware and image acquisition software. Substantial improvement in sensitivity for a given resolution can be achieved by positioning the vertex collimator in contact with the head. As the vertical dimension of the head is less than its diameter, the brain on average will be closer to the vertex detector. Hence the vertex data set will have higher resolution and reduced self attenuation when compared to the tomographic data set. Also, since fewer brain pixels are to be estimated along a vertex view projection element, these projections will have higher information content. And finally, since the tomographic data set is complete without the vertex view, portions of the vertex view can be disregarded to eliminate focal areas of uptake which are outside the reconstruction volume without introducing artifacts.

However, there are also challenges that are unique to this imaging geometry. First is the need for a 3-dimensional image reconstruction method. Conventional filtered backprojection (FBP) algorithm cannot incorporate the vertex data set as this sampling geometry does not fulfill the sampling requirement of 3D-FBP. We have adopted a penalized weighted least squares (PWLS) objective in conjunction with the iterative coordinate descent (ICD) algorithm as the image reconstruction method [2]. This algorithm converges rapidly to a global minimum of the objective function, readily incorporates a nonnegativity constraint and local roughness penalty, and easily accommodates the non-standard imaging geometry. Second there is a problem introduced by background activity arising from organs outside the brain (such as salivary glands, lung, heart and the thyroid) that are in the field of view of the vertex detector but not the ring tomograph. This background activity must be estimated as a part of the image reconstruction process, and the system model must be modified to incorporate it.

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for the pixel of interest in the six planes is shown in Fig. 4. The pixels of interest for planes 1, 2 and 3 are the small hot pixel of size 1 at the edge, while for plane 6, it is one of the pixels from the group of four hot pixels at the edge. The hot edge pixel of planes 1, 2 and 3 are at distances 12.7, 12.1 and 10.5 pixels from the center respectively and they have different bias and variance tradeoff characteristics even for tomograph only data. Pixels that are further away from the center have higher resolution as they are closer to the detector ring and have more favorable bias and variance tradeoff characteristics as demonstrated by the bias and variance curves.

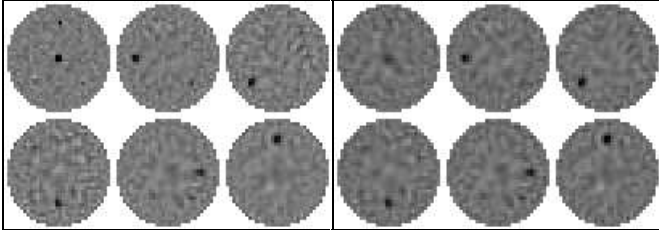


Figure 3: Left: 30 iterations of PWLS reconstruction for ring+vertex data, β set to match ratio of geometric resolution. Right: 30 iterations of PWLS reconstruction for ring only data.

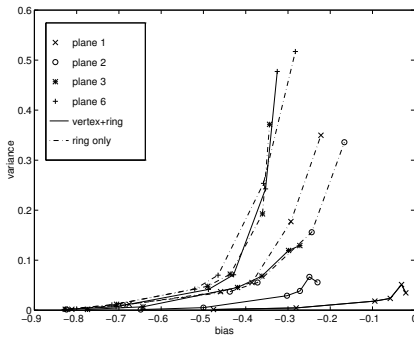


Figure 4: Bias and standard deviation tradeoff characteristics of reconstructed image with and without vertex data.

2). Background

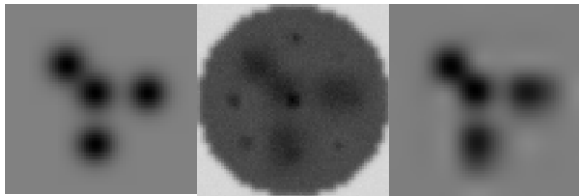


Figure 5: Left: Simulated background plane. Middle: Vertex detector projection data. Right: Reconstructed background plane.

Fig. 5 shows the background plane, the projection data of the vertex detector and the reconstructed background plane by spline method. Fig. 6 Left is the reconstructed image with the background plane modeled, Fig. 6 Right is the reconstructed image when the reconstruction algorithm does not model the background plane. The background plane shows up as hot spots on plane 1 of the image, and there are

ring artifacts at the edge of the slice indicating mismatch of system model.

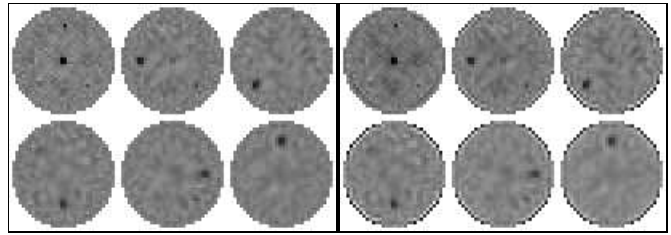


Figure 6: Left: Reconstructed image with background plane modeled. Right: Reconstructed image when reconstruction algorithm does not model background plane.

3) Hoffman Brain Phantom

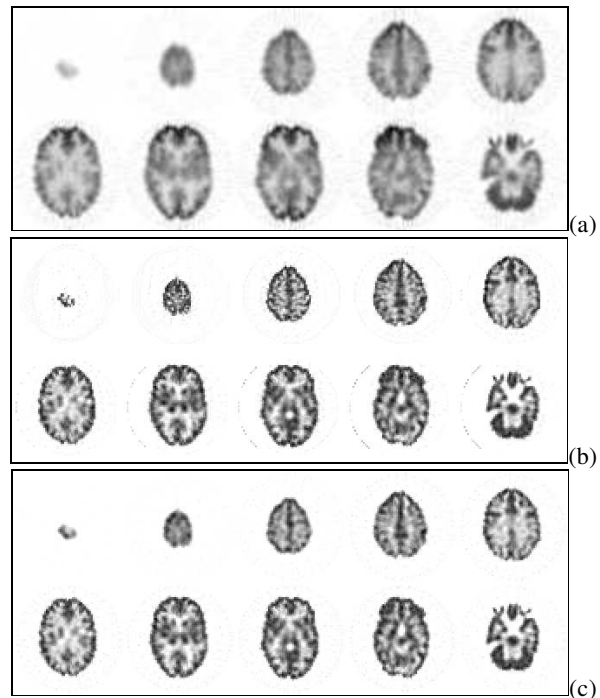


Figure 7(a): Filtered back projection reconstructed image of the digital Hoffman brain phantom. Top row is slices 1 through 5, starting from the left; and bottom row is slices 6 through 10. 7(b): 15 iterations of PWLS reconstruction for ring+vertex data, initialized with the FBP image. 7(c): 15 iterations of PWLS for ring only data. $\beta=2e-8$ for both reconstructions.

Reconstructed images of 10 slices of the digital Hoffman brain phantom, having 64x64 pixels on each slice, are shown in Fig. 7. For these images an average of 1 million counts are detected per slice of the ring detector. The FBP reconstructed image in Fig. 7(a) was reconstructed with ramp filter only. The images showed streak artifacts typical of FBP algorithm and poor image resolution. Reconstructed image with vertex data showed improved image resolution up to plane 6 which is at a distance of 7 cm from the surface of the vertex detector.

B. Uniform CR Bound Experiments

Part I: Fig. 8 shows the bounds on standard deviation for a center hot pixel of plane 1 and plane 6. C was chosen to be the inverse of the regularization matrix in bound computations. Substantial improvement in performance was obtained when vertex data was added for plane 1. At bias gradient length of 0.6, the bound was reduced from 3.125 for the ring only case to 0.104 when vertex data is added. The improvement is less prominent for the edge pixels of plane 6. For bias gradient length greater than 0.55, there is no difference in performance between the two systems.

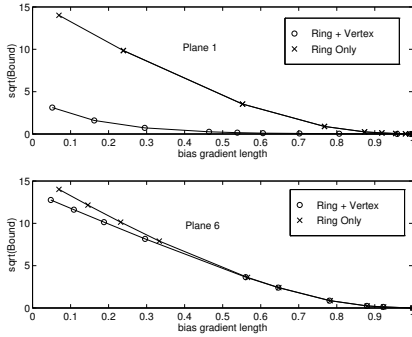


Figure 8: Uniform CR bound for of plane 1 hot center pixel and plane 6 hot edge pixel. C is inverse of regularization matrix.

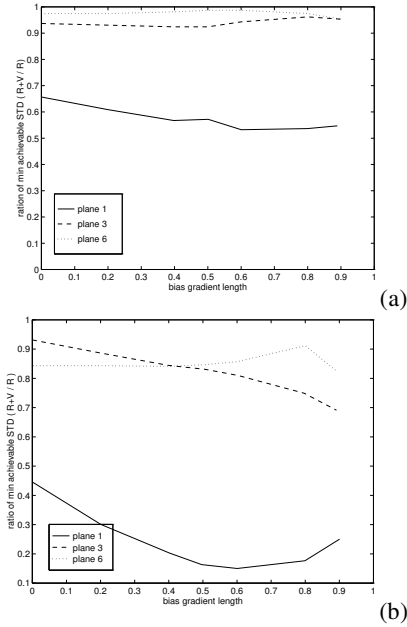


Figure 9(a): Ratio of sqrt(bound) for a peripheral hot pixel of Ring+vertex to Ring only for planes 1, 3 and 6. 9(b) Ratio of sqrt(bound) for a central hot pixel of Ring+vertex to Ring only for planes 1, 3 and 6. C is inverse of regularization matrix.

Part II: For *Part II* of the bound experiments, for the phantom with hot spots at the periphery, addition of the vertex data set resulted in considerable improvement for estimation of regions of interest at plane 1 only. The ratio of the minimum achievable STD for the two cases is less than 0.65, which is equivalent to a sensitivity increase of 2.8 times. However, the rest of the planes only show marginal

improvement when the vertex data set is added (Fig. 9(a)). The ratio of min. achievable STD is very close to 1 for plane 3 and 6. For the phantom with hot spots close to the center, the bound on STD for all the planes is lower for the ring+vertex case when compared to the ring only case. Even at plane 6, the ratio of the minimum achievable STD for the two cases is approximately 0.84, which is equivalent to a 40% increase in sensitivity.

IV. CONCLUSIONS

Using simulation experiments, we have shown that by adding the vertex data set to tomographic data set, the bias and variance trade-off characteristics are superior to standard tomographic data up to distances that are beyond 10 cm from the vertex detector where the advantage of the vertex view is offset by attenuation effect and decreased vertex resolution. The visual quality of the reconstructed images is also improved for the ring+vertex situation.

Cramer-Rao bound type analysis has been applied very successfully in parameter estimation problems for comparing the optimality of various estimators. In this work, we exploited the application of this type of analysis for performance comparison of medical imaging systems. The introduction of uniform Cramer-Rao bound allows the study of bias-variance and resolution-sensitivity trade-offs for biased image reconstruction algorithms. With this mathematical tool, we are able to examine the intrinsic benefits of these two data acquisition regimes relative to reconstruction accuracy as the data acquisition process is decoupled from the reconstruction algorithm.

It is of interest to note that the vertex view provide the largest benefit to centrally located pixels that are the most poorly measured by the tomograph only. this is probably because peripheral pixels have reduced attenuation and are closer to the aperture for 25% to 30% of the projections so that vertex view yields only a marginal increase in information.

V. BIBLIOGRAPHIC REFERENCES

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