Optimizing Non-Cartesian Sampling Patterns via Gradient Methods

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Target Audience: researchers interested in fast imaging and efficient sampling

Purpose: Efficient sampling trajectories are important for fast imaging. This abstract presents a method named SNOPY (**S**tochastic Optimization of **No**n-Cartesian Sampling Trajectory). SNOPY proposes a gradient method for optimizing non-Cartesian sampling patterns, enabled by an efficient NUFFT's Jacobian approximation approach [1]. SNOPY has several optimization objectives, including reconstructed image quality, compliance to hardware constraints (maximum slew rate and gradient strength), reduction of peripheral nerve stimulation (PNS), and parameter-weighted contrast. SNOPY is versatile for different applications, such as optimizing gradient waveforms or optimizing rotation angles of radial/spiral trajectories. SNOPY uses several computational strategies to relieve the high computation demand brought by this non-convex and large-scale

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Methods: SNOPY uses stochastic gradient descent (or its variants) to learn sampling trajectories and other reconstruction parameters. The method utilizes differentiable programming to compute the gradient w.r.t. the sampling trajectories. The training loss includes several terms. The image quality loss calculates the distance between images reconstructed from undersampled k-space signals and the reference

image. By minimizing this loss, the trajectory (and possibly the reconstruction method) learns to generate high-quality images. The optimization also includes physical constraints, including gradient strength, slew rate, and peripheral nerve stimulation (PNS) effect. We formulated such constraints as soft penalty terms. To maintain certain parameter-weighted contrasts, SNOPY may also include a penalty on the echo time (TE). One may optimize existing trajectory parameters, such as rotation angles or (continuous) phase-encoding locations. It is also possible to directly optimize gradient waveforms. Additionally, SNOPY allows multiscale optimization to avoid sub-optimal local minima and further improve optimization results. SNOPY proposes several techniques for more accurate and efficient optimization. See [2] for more details.



Discussion: SNOPY tailors sampling trajectories to specific training datasets and reconstruction algorithms, which may raise concerns about overfitting. In experiment 2, the training set used an MP-RAGE sequence, while the prospective sequence was an RF-spoiled GRE. In a 2D experiment [5], we found that trajectories learned with one anatomy (brain), contrast (T1w), and vendor (Siemens) still improved the image quality of other anatomies (like the knee), contrasts (T2w), and vendors (GE). These empirical studies indicate that trajectory optimization is robust to a moderate distribution shift between training and inference.

Conclusion: SNOPY presents a novel yet intuitive approach to optimizing non-Cartesian sampling trajectories. Various applications and in-vivo experiments showed the applicability and robustness of SNOPY.

References: [1] Wang G & Fessler JA. arXiv:2111.02912, 2021. [2] Wang G, et al. arXiv:2209.11030, 2-22. [3] Aggarwal HK, et al. arXiv:1712.02862, 2017. [4] Rettenmeier CA, Maziero D & Stenger VA. MRM, 2020. [5] Wang G, et al. IEEE T-MI, 2022. [6] Zhou Z, et al. MRM, 2017.









Figure 3. Prospective results of the second experiment, optimizing the rotation angles of the stack-of-stars (6× acceleration). 'Best empirical' uses the design from a previous study [6].



Figure 4. The subjective score of the PNS effect.