## Homework #6

Due: 12/5/06

- 1. A region of the body has a 10cm thickness of muscle with 2cm of bone imbedded as shown in Figure 1. The densities ( $\rho$ ) of muscle and bone are 1.0 and 1.75 g/cm<sup>3</sup>, respectively.
  - a. Calculate the x-ray transmission along paths through muscle alone and through muscle and bone for photon energies of 30 and 100 keV using Figure 2. Assume mono-energetic beams of photons.
  - b. Determine the contrast between the background (muscle only) and muscle + bone. Which energy has the best contrast? ( $C = \Delta N / \overline{N}_{background}$ )
  - c. Assuming that number of photons in  $I_0$  is inversely proportional to the photon energy and that  $I_0$  is fixed (e.g. the total energy transmitted is the same), which energy has the best contrast to noise ratio?  $(C = \Delta N / \overline{N}_{background})$

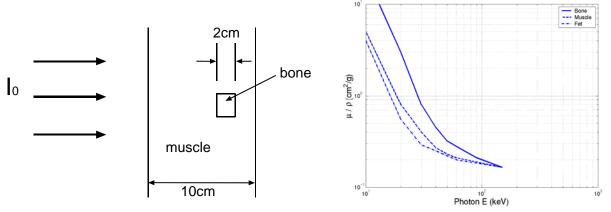
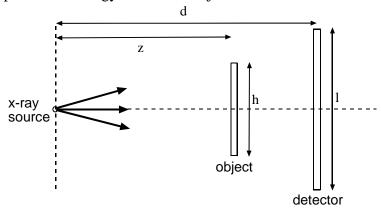


Figure 1. Object to be imaged

Figure 2. Mass attenuation coefficient of several tissues.

2. A source emits photons at energy E to a thin object as shown below.



- a. Fine the minimum energy of a Compton-scattered photon reaching the x-ray detector assuming single scattering events.
- b. What is this energy given E = 100 keV, z = d/2, h = d/4, l = d/4.

- 3. Projection properties:
  - a. If the area of a function is  $A = \iint f(x, y) dx dy$ , find an expression for A in terms of  $g_{\theta}(R)$ .
  - b. Suppose the project function is separable, e.g.  $g_{\theta}(R) = h_{R}(R)h_{\theta}(\theta)$ , show that this is not a valid project unless  $h_{\theta}(\theta)$  is a constant.
- 4. Suppose we have a CT system with a parallel ray source. Let's assume that the detector system contains a scintillator that disperses light to the photodetectors in roughly a Gaussian pattern. That is, we can assume that the projection detected by the computer is the ideal project convolved with a Gaussian in the form  $h(R) = \exp(-\pi R^2/W^2)$ . Find the reconstructed image  $\hat{f}(x, y)$  in terms of the true image f(x, y).