

- 1a. **YES** is LTI. This is a constant-coefficient MA difference equation.
- 1b. **NO** not causal since $y[n]$ depends on future inputs $\{x[n+1], x[n+2], \dots\}$
- 1c. Read off impulse response $h[n] = \{\dots, \frac{1}{3}, -\frac{1}{2}, 1, \underline{0}, -1, \frac{1}{2}, -\frac{1}{3}, \dots\}$
- 1d. **NOT** BIBO stable since $\sum |h[n]| = 2(1 + \frac{1}{2} + \frac{1}{3} + \dots)$ diverges. Note $\sum h[n] = 0$.
- 1e. $x[n] = -(-1)^n \text{sgn}[n] = \text{sgn}(h[-n])$ makes $y[0] = \sum |h[n]|$ which diverges.
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- 2a. $\{(3)(6), (3)(7)+(4)(6), (3)(8)+(4)(7)+(5)(6), (4)(8)+(5)(7), (5)(8)\} = \{\underline{18}, 45, 82, 67, 40\}$.
- 2b. $u[n] + 2u[n-1] - 3u[n-2] = \{\underline{1}, 3\}$ since $1+2=3$ ($n=1$) and $1+2-3=0$ ($n \geq 2$).
- 2c. $u[n] - u[n-3] = \{\underline{1}, 1, 1\}$ so get $\{3, 3+4, 3+4+5, 4+5, 5\} = \{\underline{3}, 7, 12, 9, 5\}$.
- 2d. Convolution by delayed impulse delays signal so get $\{\underline{0}, 0, 2, 4, 8\}$.
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- 3a. Suppose IS time-invariant. Then it is LTI. Write the 1st input in terms of the 2nd:
 $\{\underline{1}, 2, 3\} = \delta[n] + 2\delta[n-1] + 3\delta[n-2]$. Then since the system is LTI:
 $\{\underline{1}, 2, 3\} = \delta[n] + 2\delta[n-1] + 3\delta[n-2] \rightarrow \{\underline{1}, 3\} + \{0, 2, 6\} + \{0, 0, 3, 9\} = \{\underline{1}, 5, 9, 9\}$.
 But this contradicts $\{\underline{1}, 2, 3\} \rightarrow \{\underline{1}, 4, 7, 6\}$. So the system is not time-invariant.
- 3b. $\{\underline{1}, 2, 3\} * \{h[0], h[1]\} = \{\underline{1}, 4, 7, 6\}$ since durations of each sequence are $3+2-1=4$.
 $1h[0]=1$; $2h[0]+1h[1]=4$; $3h[0]+2h[1]=7$; $3h[1]=6$ are all satisfied by $h[n] = \{\underline{1}, 2\}$.
 If there were no consistent solution, $h[n]$ must have infinite duration.

- 4a. **n=0**: $y[0] - y[-1] - y[-2] = x[0] \rightarrow y[0] - 0 - 0 = 1 \rightarrow y[0] = 1$.
n=1: $y[1] - y[0] - y[-1] = x[1] \rightarrow y[1] - 1 - 0 = 0 \rightarrow y[1] = 1$.
n=2: $y[2] - y[1] - y[0] = x[2] \rightarrow y[2] - 1 - 1 = 0 \rightarrow y[2] = 2$.
n=3: $y[3] - y[2] - y[1] = x[3] \rightarrow y[3] - 2 - 1 = 0 \rightarrow y[3] = 3$.
n=4: $y[4] - y[3] - y[2] = x[4] \rightarrow y[4] - 3 - 2 = 0 \rightarrow y[4] = 5$.
n=5: $y[5] - y[4] - y[3] = x[5] \rightarrow y[5] - 5 - 3 = 0 \rightarrow y[5] = 8$.
n=6: $y[6] - y[5] - y[4] = x[6] \rightarrow y[6] - 8 - 5 = 0 \rightarrow y[6] = 13$.
- 4b. `Y=filter([1],[1 -1 -1],[1 zeros(1,6)]);Y(1:7)` gives 1 1 2 3 5 8 13

- 5a. The voice saying "Matlab-Breakfast of Champions" with high-frequency noise added.
- 5b. The spectrum (below left) has high-frequency noise in a band above 8000 Hertz.
- 5c. Most of the noise, but not all, has been eliminated. The voice is much clearer.
- 5d. The spectrum (below right) still has a much-smaller band of high-frequency noise.
 The convolution with this small lowpass filter eliminated much (not all) of the noise.

