EECS	451
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PROBLEM SET #6

ASSIGNED: Mar. 05, 2015. READ: Sects. 5.4-5.6. All of Chap. 7. DUE DATE: Mar. 12, 2015. TOPICS: Frequency response.

Please box your answers. Show your work. Turn in all Matlab plots and Matlab code.

[20] 1. We are given that $3+4\cos(\frac{\pi}{2}n+\frac{\pi}{4}) \to y[n]+y[n-1]=x[n]-x[n-1] \to y[n].$

[10] (a) Compute the frequency response $H(e^{j\omega})$. [10] (b) Compute the output y[n].

- [20] 2. Designing MA and ARMA filters for rejecting two interfering sinusoids:
- [10] (a) Design a filter $x[n] \rightarrow y[n] = x[n] + ax[n-1] + bx[n-2] + ax[n-3] + x[n-4] \rightarrow y[n]$ that rejects sinusoids of frequencies 100 and 500 Hertz in a DSP system at 1200 $\frac{\text{SAMPLE}}{\text{SECOND}}$.
- [10] (b) Use y[n]+cy[n-1]+dy[n-2]+ey[n-3]+fy[n-4]=x[n]+ax[n-1]+bx[n-2]+ax[n-3]+x[n-4].Design a more selective filter that rejects sinusoids of frequencies 100 and 500 Hz.

 $[20] \ 3. \ Given \ y[n] = 0.5 x[n] + 0.29 (x[n+1] + x[n-1]) - 0.042 (x[n+3] + x[n-3]) + 0.005 (x[n+5] + x[n-5]).$

- [10] (a) Compute an expression for $H(e^{j\omega})$. Express as a sum of 3 cosines and a constant.
- [05] (b) Plot the gain $|H(e^{j\omega})|$ at the points $\omega = \frac{2\pi k}{200}, 0 \le k \le 99$. Turn in this plot.
- [05] (c) Describe in words what this system does to a signal x[n].

[20] 4. Download p6.mat. In Matlab, type >>load p6.mat to get sampled signals X1,X2.

- [05] (a) Listen to X1 using sound(X1,24000). Describe it.
- [05] (b) Plot the spectrum of X1 using the Matlab command from problem set #1. Compare to the spectrum plot from problem set #1. Note the vertical scale.
- [10] (c) Design an ARMA notch filter that eliminates the sinusoidal interference. Give the Matlab command using filter that implements it.

[20] 5. Download p6.mat. In Matlab, type >>load p6.mat to get sampled signals X1,X2.

- [05] (a) Listen to X2 using sound(X2,24000). Describe it.
- [05] (b) Plot the spectrum of X2 using the Matlab command from problem set #1. Compare to the spectrum plot from problem set #1. Note the vertical scale.
- [10] (c) Design an ARMA comb filter that eliminates the periodic interference.This filter should actually be simpler than the ARMA notch filter used in #4.Give the Matlab command using filter that implements it.

"Football embodies the worst of America–violence punctuated by committee meetings"–George Will