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1. **B.** $f = \frac{0.56\pi}{2\pi} = 0.28 = \frac{7}{25} \rightarrow \text{period}=25$. **NOTE: Discrete time!**

 2. **B.** $\sin(40\pi \frac{n}{100}) + 2 \sin(160\pi \frac{n}{100}) = \sin(0.4\pi n) + 2 \sin(1.6\pi n) = -\sin(0.4\pi n)$. **Miss "2"?**

 3. **B.** $\{1, 2\} * \{3, 4, 5\} = \{1 \cdot 3, 2 \cdot 3 + 1 \cdot 4, 2 \cdot 4 + 1 \cdot 5, 2 \cdot 5\} = \{3, 10, 13, 10\}$.

 4. **C.** $H(z) = \mathcal{Z}\{y[n]\} / \mathcal{Z}\{x[n]\} = [\frac{2z^2-3z}{z^2-3z+2}] / [\frac{z}{z-2}] = \frac{2z-3}{z-1}$.

 5. **D.** $H(z) = \mathcal{Z}\{y[n]\} / \mathcal{Z}\{x[n]\} = \frac{4+5z^{-1}+6z^{-2}}{1+2z^{-1}+3z^{-2}} = \frac{4z^2+5z+6}{z^2+2z+3}$.

 6. **C.** $\frac{z}{z-2} \frac{z+4}{z+4} + \frac{z}{z+4} \frac{z-2}{z-2} = \frac{2z^2+2z}{z^2+2z-8}$. **For #7: Use initial value theorem to check.**

 7. **E.** $\frac{H(z)}{z} = \frac{2}{z^2+1} = \frac{j}{z+j} - \frac{j}{z-j} \rightarrow h[n] = j(-j)^n u[n] - j(j)^n u[n] = 2 \sin(\frac{\pi}{2}n) u[n]$.

 8. **C.** $H(z) = \frac{z^2-5z+6}{z^2(z-1)} = (1-5z^{-1}+6z^{-2}) \frac{z}{z-1} z^{-1} \rightarrow h[n] = \{1, -5, 6\} * u[n-1]$.

 9. **D.** $H(z) = 1 / [\frac{z}{z-2} \frac{z-4}{z-4} + \frac{z}{z-4} \frac{z-2}{z-2}] = \frac{z^2-6z+8}{2z(z-3)}$. $h[n] = \frac{1}{2} \{1, -6, 8\} (3)^n u[n] = C(3)^n$ for $n > 3$.

 10. **A. 1-sided:** $Y^+(z) - 2z^{-1}Y^+(z) - 2y(-1) = 0 \rightarrow Y^+(z) = \frac{2z}{z-2} \rightarrow y[n] = 2(2)^n u(n)$.

 11. **C.** Poles are **denominator**=0 roots; zeros are **numerator**=0 roots.

 12. **B.** $\frac{Y(z)}{X(z)} = \frac{z}{z^2-3z+2} \frac{z^{-2}}{z^{-2}} = \frac{z^{-1}}{1-3z^{-1}+2z^{-2}}$. Cross-multiply and take inverse z-transform.

 13. **C.** $\frac{H(z)}{z} = \frac{1}{(z-1)(z-2)} = \frac{1}{z-2} - \frac{1}{z-1} \rightarrow H(z) = \frac{z}{z-2} - \frac{z}{z-1} \rightarrow h[n] = 2^n u[n] - u[n]$.

 14. **E.** $Y(z) = H(z)X(z) = \frac{z}{z^2-3z+2} \frac{2z^2-6z+4}{z^2} = \frac{2}{z} \rightarrow y[n] = 2\delta[n-1]$. **Watch z power!**

 15. **C.** $Y(z) = H(z)X(z) = \frac{z}{(z-1)(z-2)} \frac{z-1}{z} = \frac{1}{z-2} \rightarrow y[n] = 2^{n-1} u[n-1]$.

 16.

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|--|--------------|----------------------------------|-------------------------|-------------------|-----------------|
| | <i>(i)</i> | $(0.2)^n u[n] + 2^n u[n]$ | $\{z : z > 2\}$ | causal | unstable |
| | <i>(ii)</i> | $(0.2)^n u[n] - 2^n u[-n-1]$ | $\{z : 0.2 < z < 2\}$ | noncausal | stable |
| | <i>(iii)</i> | $-(0.2)^n u[-n-1] - 2^n u[-n-1]$ | $\{z : z < 0.2\}$ | anticausal | unstable |

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|--------|------|-----|----|----|----|----|----|----|
| SCORE | Mean | 100 | 95 | 90 | 85 | 80 | 75 | 70 |
| NUMBER | 89.4 | 15 | 09 | 12 | 03 | 05 | 02 | 06 |

A few scores between these ranges were rounded up or down.
 Undergraduates and graduates (only 5) are lumped together.
 Two taking the exam late are not listed above.
 OK, it was too easy. Exam #2 will be harder!
