

**PRINT YOUR NAME HERE:**

*HONOR CODE PLEDGE:* "I have neither given nor received aid on this exam, nor have I concealed any violations of the honor code." Closed book; 2 sides of 8.5×11 "cheat sheet."

**SIGN YOUR NAME HERE:****CIRCLE ONE:**

Undergraduate

Graduate

Write your answer to each question in the answer space to the right of that question. Problems #1-15 are multiple choice (here same as fill-in-the-blank) worth 5 points each.

1. The **period** of  $x[n] = 3 \cos(2\pi 0.075n + 1)$  for **integer**  $n$  is:  
 (a) 1 (b) 1/0.075 (c) 40 (d) 75 (e) not periodic

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2.  $\sin(32\pi t) + \sin(48\pi t)$  is sampled at 40 Hz, then *ideally* interpolated. The result is:  
 (a) 0 (b)  $\sin(16\pi t)$  (c)  $2 \sin(16\pi t)$  (d)  $\sin(32\pi t)$  (e)  $2 \sin(32\pi t)$

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3. The convolution  $\{1, 2, 3\} * \{4, 5, 6\} =$ : (a)  $\{7, 8, 9\}$  (b)  $\{4, 13, 27, 18\}$   
 (c)  $\{4, 13, 28, 27, 18\}$  (d)  $\{4, 14, 32, 28, 18\}$  (e)  $\{5, 11, 20, 23, 9\}$

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4. The system (transfer) function of a LTI system described by the difference equation  $y[n] + 2y[n-1] + 3y[n-2] = 4x[n] + 5x[n-1] + 6x[n-2]$  is:  
 (a)  $\frac{z^2+2z+3}{4z^2+5z+6}$  (b)  $\frac{3z^2+2z+1}{6z^2+5z+4}$  (c)  $\frac{4z^2+5z+6}{z^2+2z+3}$  (d)  $\frac{6z^2+5z+4}{3z^2+2z+1}$  (e)  $z^2 + z + 1$

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5. The system function of a LTI system with impulse response  $h[n] = u[n] + 2^n u[n]$  is:  
 (a)  $\frac{z+2}{z}$  (b)  $\frac{z+2}{z-1}$  (c)  $\frac{z+2}{z^2-3z+2}$  (d)  $\frac{z^2-3z}{z^2-3z+2}$  (e)  $\frac{2z^2-3z}{z^2-3z+2}$

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6.  $\mathcal{Z}\{2^n u[n] + 3^n u[n]\} =$ : (a)  $\frac{z^2-5z+6}{1}$  (b)  $\frac{1}{z^2+5z+6}$  (c)  $\frac{5}{z^2+5z+6}$  (d)  $\frac{2z-5}{z^2-5z+6}$  (e)  $\frac{2z^2-5z}{z^2-5z+6}$

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7. If  $H(z) = 6/[(z+1)(z-2)]$ , then  $h[n] = \mathcal{Z}^{-1}\{H(z)\} =$ :  
 (a)  $2^n u[n] + (-1)^n u[n]$  (b)  $2^n u[n] - (-1)^n u[n]$  (c)  $2(2^n)u[n] + 2(-1)^n u[n]$   
 (d)  $2(2^n)u[n] - 2(-1)^n u[n]$  (e)  $2^n u[n] + 2(-1)^n u[n] - 3\delta[n]$ .

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8. The z-transform of  $\{1, -3, 2\} * u[n]$  is:  
 (a)  $\frac{z-2}{z}$  (b)  $\frac{2z^3-4z^2+5z-2}{z^3-z^2}$  (c)  $1 + 3z^{-1} + 2z^{-2} + \frac{z}{z-1}$  (d)  $1 - 2z$  (e)  $z - 2$

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9. The impulse response if  $\delta[n] + 2^n u[n] \rightarrow \overline{LTI} \rightarrow \{2, -2\}$  is: (a)  $\delta[n] - 2^n u[n]$   
 (b)  $(\frac{1}{2})^n u[n]$  (c)  $2(\frac{1}{2})^n u[n] - 2(\frac{1}{2})^{n-1} u[n-1]$  (d)  $\{1, -2\}$  (e)  $2\delta[n] - 2(2^{n-1})u[n-1]$

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10. The zero-input response for  $y(n)-2y(n-1)=x(n)+x(n-1)$  with  $y(-1)=1$  is:  
 (a)  $2^{n+1}u(n)$  (b)  $2^n u(n)$  (c)  $2^{n-1}u(n-1)$  (d)  $2^n u(n)+2^{n-1}u(n-1)$  (e) 0

For problems #11-15: An LTI system has transfer function  $H(z) = \frac{(z-1)(z-6)}{(z-2)(z-3)}$ .

11. The zeros, poles, and BIBO stability of the system are: **(a)**  $\{1, 6\}; \{2, 3\}$ ;stable  
**(b)**  $\{1, 6\}; \{2, 3\}$ ;unstable **(c)**  $\{2, 3\}; \{1, 6\}$ ;stable **(d)**  $\{2, 3\}; \{1, 6\}$ ;unstable

12. The difference equation for the system is:

- (a)**  $y[n] - 7y[n-1] + 6y[n-2] = x[n] - 5x[n-1] + 6x[n-2]$   
**(b)**  $6y[n] - 7y[n-1] + y[n-2] = 6x[n] - 5x[n-1] + x[n-2]$   
**(c)**  $y[n] - 5y[n-1] + 6y[n-2] = x[n] - 7x[n-1] + 6x[n-2]$   
**(d)**  $6y[n] - 5y[n-1] + y[n-2] = 6x[n] - 7x[n-1] + x[n-2]$

13. The response of the system to  $x[n] = \{1, -5, 6\}$  is  $y[n] =$ :

- (a)**  $\{1, -7, 6\}$  **(b)**  $(2)^{n+1}u[n] - 2(3)^n u[n]$  **(c)**  $\{6, -7, 1\}$  **(d)**  $\delta[n] + (2)^{n+1}u[n] - 2(3)^n u[n]$

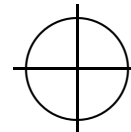
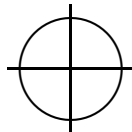
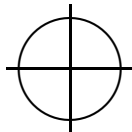
14. The response of the system to  $x[n] = 7$  for all  $n$  is  $y[n] =$ :

- (a)** 0 **(b)**  $\frac{7}{6} \cos(\pi n)$  **(c)**  $\infty$  **(d)**  $1.22 \cos(\pi n - 0.165)$  **(e)**  $1.22 \cos(\pi n + 0.165)$

15. The impulse response of the system is  $h[n] =$ :

- (a)**  $\{1, -7, 6\}$  **(b)**  $(2)^{n+1}u[n] - 2(3)^n u[n]$  **(c)**  $\{6, -7, 1\}$  **(d)**  $\delta[n] + (2)^{n+1}u[n] - 2(3)^n u[n]$

- [24] 16.  $X(z) = \frac{1}{z-0.5} - \frac{1}{z-3}$  has 3 different inverse z-transforms. For each one, compute:  
**[3@3]** **(a)**  $x[n]$  **[3@3]** **(b)** ROCs **[3@1]** **(c)** if stable **[3@1]** **(d)** if causal. Write below.






STABLE

CAUSAL

STABLE

CAUSAL

STABLE

CAUSAL

- [1] 17. Did you: (a) PRINT your name; (b) SIGN your name; (c) CIRCLE grad or undergrad?