

1. In #1a, referring to loops in circuit. In #1b, referring to nodes in circuit.

1a. **Left:** $36-36=0$ ; **Middle:** $36+18+(-54)=0$ ; **Right:** $-(-54)+30-84=0$ ; **Upper:** $48-30-18=0$ .

1b. **Left:**  $12+(-4)+8=16$ ; **Middle:**  $(-4)+(-10)+14=0$ ; **Right:**  $22-10=12$ .

1c. In alphabet order:  $(48)(12)+(-18)(-4)+(-30)(-10)+(-36)(16)+(-36)(8)+(-54)(14)+(-84)(22)=0$ .

All of these check out, so the circuit is valid. Note signs are for power *dissipated*.

2. KCL holds at lower left node; can't write KVL anywhere, so circuit is valid.

**Power supplied:100V:**  $-(100)(5)=-500W$  (so dissipated); **60V:**  $(60)(5)=300W$ .

$20A \parallel -25A = -5A$  consistent with other  $5A$ ;  $60-100=-40V$ . Get  $5A \downarrow \parallel -40V \_$ .

3b.  $v_g = (1.6A)(90\Omega) = 144V$ .  $v_{30\Omega} = (1.6A)(30\Omega) = 48V$ .  $v_{source} = 144 + 48 = 192V$ .

3a.  $i_a = 192V/80\Omega = 2.4A$ .  $i_g = i_a + 1.6A = 2.4 + 1.6 = 4A$ . In #3c, all powers in watts.

3c.  $P_{80\Omega} = (2.4)^2(80) = 460.8$ .  $P_{30\Omega} = (1.6)^2(30) = 76.8$ .  $P_{90\Omega} = (1.6)^2(90) = 230.4$ .

$P_{source} = (192V)(4A) = 768$  supplied.  $460.8 + 76.8 + 230.4 = 768$  checks.

4a,b. **Straightforward way:**  $50 - 4(i_a + i_b) - 20i_a = 0$  and  $50 - 4(i_a + i_b) - 80i_b = 0$ .

Solving 2 equations in 2 unknowns  $\rightarrow i_a = 2A, i_b = \frac{1}{2}A$ . **Clever but easier way:**

$20\Omega, 80\Omega$  same voltage  $\rightarrow i_a = 4i_b \rightarrow 50 - 4(5i_b) - 80i_b = 0 \rightarrow i_b = \frac{1}{2}A, i_a = 2A$ .

4c.  $v_o = (80\Omega)i_b = 40V$ . OR:  $v_o = 50V - (4\Omega)(i_a + i_b) = 50V - (4\Omega)(2A + \frac{1}{2}A) = 40V$ .

4d.  $P_{4\Omega} = (i_a + i_b)^2(4\Omega) = 25W$ .  $P_{20\Omega} = i_a^2(20\Omega) = 80W$ .  $P_{80\Omega} = i_b^2(80\Omega) = 20W$ .

4e.  $P_{50V} = (50V)(i_a + i_b) = 125W$  supplied.  $125 = 25 + 80 + 20$  checks.

5. Has to be current source  $i_s$  and resistor  $R$  in parallel (in series  $\rightarrow$  constant current).

$i_t = v_t/R - i_s$  (Norton equivalent circuit:  $i_s \uparrow \parallel R$ ).

From data:  $i_t = 0 \rightarrow 50 = Ri_s$  and  $3 = (65V)/R - i_s \rightarrow R = 5\Omega, i_s = 10A$ .

6a.  $R_{ab} = 2\Omega + 12\Omega \parallel 24\Omega + 6\Omega = 16\Omega$ . In #6b, everything is in  $k\Omega$ :

6b.  $20 \parallel 30 \parallel 24 : G_{eq} = 1/20 + 1/30 + 1/24 = (6 + 4 + 5)/120 = 1/8 \rightarrow R_{eq} = 8 + 7 = 15$ .

$R_{ab} = 15 \parallel 30 \parallel 15 : G_{ab} = 1/15 + 1/30 + 1/15 = (2 + 1 + 2)/30 = 1/6 \rightarrow R_{ab} = 6k\Omega$ .

7. Connect a  $1A$  current source as suggested.  $1A$  splits into 3 equal currents  $@\frac{1}{3}A$ , each of which in turn splits into 2 equal currents  $@\frac{1}{6}A$ , which then recombine similarly.

Using KVL, the voltage is  $(1\Omega)(\frac{1}{3}A) + (1\Omega)(\frac{1}{6}A) + (1\Omega)(\frac{1}{3}A) = \frac{5}{6}V \rightarrow \frac{5}{6}\Omega$ .