

Signals: Voltages or currents that varies with time.

Examples: **Audio** signals include speech and music.

Musical notes (middle C is a 254 Hz sinusoid), octaves.

Periodic: $x(t)$ has *period* $T \leftrightarrow x(t) = x(t + T)$ repeats every T .

Examples: Musical tones; EKGs (heart); 60 Hz wall sockets.

Then: Periodic signals can be decomposed into sinusoids:

Periodic signal=sum of sinusoids at frequencies which are integer multiples of the *fundamental frequency*= $\frac{1}{T}$ Hz~*prism*.

Have **frequency content**. See Fourier series handout for details.

Circuits: Components connected together in a network.

Components: Resistors, inductors, capacitors, sources.

Examples: Op-amps modelled using dependent sources.

Systems: Use of a circuit to *process* signals to do something.

Filters: Circuits that affect the frequency content of a signal.

EX #1: Low-pass filters to reduce noise in sensor signals;

EX #2: Bass and treble controls or graphic equalizers;

EX #3: Dolby noise reduction; preemphasis and deemphasis.

Sinusoid: Signal having form $x(t) = A \cos(\omega t + \theta)$ where:

Amplitude: A =(usual) amplitude; $2A$ =*peak-to-peak* amplitude A_{pp} ;

Amplitude: $\frac{A}{\sqrt{2}} \approx 0.707A$ =*rms* amplitude A_{rms} ; $20 \log_{10} A_{rms}$ =*dBV*.

Why? A_{pp} easy to measure on scope; A_{rms} for AC power (see later).

$$A_{rms} = \sqrt{\frac{1}{T} \int_0^T A^2 \cos^2(\omega t + \theta) dt} = \frac{A}{\sqrt{2}} \text{ if } \omega \neq 0. \quad \omega = 0 \rightarrow \text{DC value.}$$

Frequency: ω =circular frequency in $\frac{\text{radians}}{\text{second}}$;

Frequency: $\omega = 2\pi f$ where f =frequency in Hertz ($\frac{\text{cycles}}{\text{second}}$).

Period: $T = \frac{1}{f} = \frac{2\pi}{\omega}$. Sinusoid repeats every T : $x(t) = x(t + T)$.

Phase: θ =phase (shift) in radians or degrees. 1 radian= $\frac{180}{\pi} \approx 57.3^\circ$.

Example: Voltage in wall socket: $v(t) = 170 \cos(377t + \theta)$ for some θ .

Amplitude: A_{usual} =170 volts; A_{pp} =340 volts; A_{rms} =120 volts.

Frequency: $T = \frac{1}{60}$ seconds; f =60 Hz; $\omega = 377 \frac{\text{radians}}{\text{second}}$.

where: Approximating $170 \approx 120\sqrt{2}$ and $377 \approx 2\pi 60$ (quite close).