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**DIGITAL SIGNAL PROCESSING: COMPLETE SYSTEM**


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$x(t)$  =Continuous-time (analog) signal.

**EX:** Audio (from microphone) signal.

**Goal:** *Digitally* filter this signal  $x(t)$ .

$\tilde{x}(t)$  =Lowpass-filtered version of  $x(t)$ .

**How?** Analog filter; use EECS 215 ideas.

**Why?** Remove frequencies  $> \frac{1}{2} \left( \frac{\text{SAMPLING}}{\text{FREQUENCY}} \right)$   
 → ensures there will be no aliasing.

$x[n]$  =Discrete-time (sampled) signal.

**How?**  $x[n] = \tilde{x}(t = n\Delta)$ ;  $\Delta = \frac{\text{SAMPLING}}{\text{INTERVAL}}$ .

**Why?** We can now use EECS 206 ideas.

**Note:** Can recover  $\tilde{x}(t)$  from  $x[n]$  exactly,  
 due to the anti-alias filter.

$\hat{x}[n]$  =Quantized version of  $x[n]$ .

**How?** Round  $x[n]$  to nearest of  $2^B$  levels.

B=#bits used to represent numbers.

**Why?** To send/store bits, not numbers.

**Note:** Can't recover  $x[n]$  from  $\hat{x}[n]$ , but  
 the error is usually negligible.

$y[n]$  =Filtered version of input  $\hat{x}[n]$ .

**How?**  $y[n] = h[n] * \hat{x}[n] = \sum_i h[i]\hat{x}[n - i]$ .

$h[n]$  =impulse response of digital filter.

**Why?** Lowpass filter→remove some noise.

Notch filter→remove 60 Hz “hum.”

$y(t)$  =Interpolated  $y[n]$ =analog output.

**How?** Use zero-order hold (constant interpolation)

OR: Linear interpolation (between samples  $y[n]$ )

OR: Exact formula (*Sampling* handout).

